Rheological control on the dynamics of explosive activity in the 2000 summit eruption of Mt. Etna

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Abstract

In the period from January to June 2000 Mt. Etna exhibited an exceptional explosive activity characterised by a succession of 64 Strombolian and fire-fountaining episodes from the summit South-East crater. Textural analysis of the eruptive products reveals that the magma associated with the Strombolian phases had a much larger crystal content ($>$55 vol%) with respect to the magma discharged during the fire-fountain phases ($\sim$35 vol%). Rheological modelling shows that the crystal-rich magma falls in a region beyond a critical crystal content where the small addition of solid particles causes an exponential increase of the effective magma viscosity. When implemented into the modelling of steady magma ascent dynamics, the large crystal content of the Strombolian eruption phases results in a one order of magnitude decrease of mass flow-rate, and in the onset of conditions where small heterogeneities in the solid fraction carried by the magma translate into highly unsteady eruption dynamics. Therefore, we argue that crystallization on top of the magmatic column during the intermediate phases when magma was not discharged caused the conditions to shift from fire-fountain to Strombolian activity. The numerical simulations also provide a consistent interpretation of the association between fire-fountain activity and emergence of lava flows from the crater flanks.

1 Introduction

Persistently active basal magmatic volcanoes, such as Mt. Etna, Italy, display different styles of volcanic activity including effusion of lava, fire-fountaining and Strombolian explosions. Plinian-like explosive eruptions are rarer events, but they have also been documented (e.g., Coltelli et al., 2000; Branca and Del Carlo, 2004). Because of its hazard implications, basaltic explosive activity is increasingly better monitored (as an example, see the Istituto Nazionale di Geofisica e Vulcanologia, sezione di Catania, website at www.ct.ingv.it) and studied (among the others, AL) by the international scientific
community. At Mt. Etna, the most common explosive activity spans from mild to moderate Strombolian explosions to violent fire-fountain episodes consisting of vigorous, continuously sustained jets of magma and gas, often accompanied by ash emissions. A spectacular example of this type of activity is represented by the 64 fire-fountain episodes which occurred at the Southeast crater (SEC) on the summit of Mt. Etna between January and June 2000 (Alparone et al., 2003) (Fig. 1). Characterisation of selected products erupted from this paroxysmal activity demonstrated substantial textural and compositional variations relating to the dominant style (either Strombolian- or fire-fountain) of the eruption (Polacci et al., 2006).

Despite compositions and textures that are known to control the rheological behaviour of magmas (e.g., Giordano et al., 2009; Pinkerton and Stevenson, 1996; Lejeune and Richet, 1995), a few studies have investigated the rheological properties of specific basaltic liquids (Giordano and Dingwell, 2003) and basaltic magmas at subliquidus conditions (Shaw, 1969; Ryerson, 1988; Pinkerton and Norton, 1995; Ishibashi and Sato, 2007; Sato, 2005; Ishibashi, 2009). However, none of the previous studies allows tracking of the rheological variation associated with crystallization, vesiculation, cooling and straining of a basaltic magma during its rise to the surface. Only recently, the accessibility of modern high temperature, high pressure deformational facilities has allowed Earth scientists to build numerical and experimental predictive models accounting for the evolution of the rheological properties of magmas as they change in the volcanic conduit during magma rise to the surface.

In order to quantify the effect of rheology on Mt. Etna’s eruptive style, in this study we combine two empirical models that allow us to account for the variation of silicate melt viscosity in the T (Temperature)-X (composition)-H$_2$O space (Giordano et al., 2008) and for the non-Newtonian rheological effects due to the presence of crystals in strained magmas (Costa et al., 2009). These models are applied to calculate the viscosity of volcanic products discharged during selected eruptive episodes of the January–June 2000 Mt. Etna explosive activity. In the following, we show that non-Newtonian effects due to straining of crystal-bearing magmas result in substantial dif-
ferences in the apparent viscosities for the magmas erupted during the Strombolian and fire-fountain phases. The textural and compositional changes observed in scoria clasts erupted during the two different eruptive phases (i.e. Strombolian or fire-fountain) of the 2000 eruption are related to pronounced and relatively sharp changes in rheology. Such changes were initiated by a difference in the crystal content of the erupted magmas and coincided with a change of the style of eruptions and a shift from Strombolian to fire-fountain activity. A better understanding of the rheology of Etnan magmas, and its correlation with the eruptive style, provides constraints to models of the dynamics of explosive activity in this volcano, including sudden shifts between eruptive styles that are common at basaltic volcanoes. Ultimately, a thorough comprehension of the rheological properties of magma systems is a valuable tool for improving monitoring and hazard forecasting of active volcanoes.

2 The January–June 2000 Mt. Etna eruption: summary of activity and features of the erupted products

In this study, we investigate the evolution of the rheological properties characterising volcanic products erupted at Mt. Etna during the first semester of 2000. We chose to study this period of activity for the following reasons: first, it represents the most remarkable cyclic explosive activity over a short period of time in the known history of the volcano; second, it allows us to constrain the transition from Strombolian to fire-fountain activity by a rheological point of view; and third, an accurate description of this activity exists in terms of geophysical and geochemical signals (Alparone et al., 2003; Allard et al., 2005), offering a substantial dataset to our rheological modelling.

2.1 Eruption chronology and styles of activity

The eruptive period considered in this study started on 26 January 2000, ended on 24 June of the same year and focussed at SEC, generating 64 paroxysms each consist-
ing of an initial Strombolian phase that was gradually replaced by a phase of sustained fire-fountain activity. The former activity, usually lasting from a few minutes to tens of minutes, consisted of mild to moderate to increasingly stronger explosions of gas and fragmented magma particles (ash, lapilli and bombs); the latter, so called paroxysmal phase, which also coincided with the peak of the tremor signal, lasted from tens of minutes to a few hours and consisted of continuous, violent, hundreds-of-metres-high jets of magma and gas and in the formation of ash plumes up to a height of 6 km above the crater. All paroxysmal episodes were preceded and accompanied by lava flows from the flanks of the SEC cone whose peak in volume coincided with the climax of the fire-fountain phase. A detailed description of the eruptive activity is contained in Alparone et al. (2003) and Behncke et al. (2006) and in the papers referenced therein.

2.2 Features of erupted products

Scoria clasts erupted during Strombolian and fire-fountain activity: present, distinct, compositional and textural characteristics which are respectively summarized in Tables 1 and 2. As a general observation, products erupted from both styles of activity are porphyritic rocks (Table 2) that exhibit two vesicle populations: small (<200 µm), generally isolated, rounded to sub-rounded vesicles, and larger (from hundreds of microns to >1 cm but mostly >0.5 mm), well connected vesicles (Fig. 2). Large vesicles that range from sub-rounded to mostly complex, irregularly-shaped in Strombolian scoriae (Fig. 2a) are more deformed in products from fire-fountains and may exhibit ellipsoidal to variably elongated shapes (Fig. 2b).

Scoriae from fire-fountains display a less crystallized groundmass (vesicle-free microlite content <∼20 vol%) (Table 2 and Fig. 2c, d), and are more vesicular (crystal-free vesicularity 0.7–0.8, Table 2) in comparison to products erupted during Strombolian activity (microlite cristallinity in the range 30–40 vol%, vesicularity ∼0.65). Fire-fountain scoriae also contain a higher number density of small, isolated vesicles (such vesicles ranging 2–8 mm$^{-2}$ in Strombolian scoriae and 11–23 mm$^{-2}$ in fire-fountain scoriae) and, in terms of glass chemistry, are less compositionally evolved than Strombolian
scoria clasts. Finally, eruptive temperatures calculated via the glass geothermometer of Pompilio et al. (1998) are up to 30 °C higher for the fire-fountain than for the Strombolian products (Table 1).

3 Rheological model and applications

3.1 The models

As mentioned above, the mixture viscosity is calculated by using two recently published models that account for the continuous description of the Newtonian liquid viscosity in the T – composition – H$_2$O space (Giordano et al., 2008), and for the non-Newtonian effects of crystals and applied rate of strain (Costa et al., 2009).

The model of Giordano et al. (2008) calculates the Newtonian shear viscosity ($\eta_m$) of silicate melts as a function of temperature, 10 major oxides, and volatile content (e.g., H$_2$O and F). The model is calibrated on ~1800 viscosity measurements on dry and hydrous multi-component melts, and accounts for non-Arrhenian temperature dependence. Since a significant dataset used to calibrate the model refers to basaltic compositions (e.g., Giordano and Dingwell, 2003; Sato, 2005; Giordano et al., 2006; Ishibashi and Sato, 2006), this model is particularly suited for calculating magma viscosity of undersaturated basaltic products. The ability of the model accurately predicting the viscosity of basaltic melts can be appreciated in Fig. 3.

The non-Newtonian rheology of crystal suspensions are accounted for by the Costa et al. (2009) model. This model computes the relative viscosity $\eta_r$ (viscosity of a crystal-melt mixture divided by the viscosity of the melt phase). Compared to previous models (e.g., Einstein-Roscoe, 1952; Costa, 2005; Caricchi et al., 2007), the Costa et al. (2009) model takes into account the strain-rate dependent rheology of liquid+crystal mixtures up to a higher crystal fraction of 0.80, ensuring consistency with calculations done via the Einstein-Roscoe equation (Roscoe, 1952) for low to vanishing crystal contents.
Major element glass composition, inferred temperatures and measured crystal contents were implemented in the above rheological modelling to estimate magma viscosity during the Strombolian and fire-fountain phases of the 2000 eruption at Mount Etna (Table 1). Temperature ranges of 1080–1103 °C and of 1106–1129 °C were respectively taken as representative of the Strombolian and fire-fountain phases of the eruption. These estimates (Table 1) are calculated via a glass geothermometer calibrated on Etnean rocks samples (Pompilio et al., 1998).

3.2 Viscosity calculations

Average crystal contents of 0.57 for the Strombolian phase and 0.37 for the fire-fountain phase, both referred to a bubble-free magma, were adopted in most calculations (see Table 2). Figure 4 shows the strain-rate dependence of the relative viscosity at varying crystal volume fractions. As shown in Fig. 4a, the relative viscosity of two-phase mixture increases following a sigmoid curve with an exponential increase above a critical solid fraction. Variations of the crystal content cause orders of magnitude changes in viscosity. The critical crystal volume fraction depends on the crystal shape, size distribution and crystal orientation, decreasing with randomness in object orientation and particle shape anisotropy (i.e., equant vs. elongated) and increasing with dispersion in object size (Chong, 1971; Lejeune and Richet, 1995; Saar, 2001; Caricchi et al., 2007; Caricchi et al., 2008; Costa et al., 2009).

As a first order approximation, calculations with the model of Costa et al. (2009) are shown for the simple case of equally sized, mono-distributed spheres. A huge effect on the magmatic mixture viscosity is observed when moving from a crystal volume fraction of 0.37 to 0.57 (Fig. 4b), representative of the two magma types erupted during the fire-fountain and Strombolian phases, respectively, of the 2000 Mt. Etna activity. This effect is maximum at low strain rates (<10^{-5} s^{-1}) where the rheology is approximately Newtonian, and it is reduced at higher strain-rates where non-Newtonian behaviour becomes substantial for large crystal contents.
Figure 5 shows calculations at constant H$_2$O contents of 0.3 wt% and 0.7 wt%, corresponding to the residual water content in the magma discharged during the Strombolian and fire-fountain phases, respectively (Metrich et al., 2004; Spilliaert et al., 2006). The calculations are shown for two different low and high rates of strain. To consider the effect of crystals on the viscosity of the erupted magmas, the relative viscosity of the Strombolian and fire-fountain products were first calculated using the Costa et al. (2009) model with crystal contents reported above and representative of those in Table 2. Relative viscosities were then multiplied by melt viscosities calculated through the Giordano et al. (2008) model. The plots in Fig. 5 clearly show that the viscosities of the two different crystal-rich and crystal-poor magmas plot in two well distinct fields, with the magma from the Strombolian activity displaying values >2 to 4 orders of magnitude higher.

3.3 Application to conduit flow dynamics

The rheological models described above have been implemented in the Conduit4 code for the 1-D steady multiphase dynamics of conduit flow (Papale, 2001). With this update, the code embodies the non-Newtonian rheology as due to strain-rate dependent viscosity of magmatic crystal suspensions as described by the Costa et al. (2009) model. Additionally, the recent model of Giordano et al. (2008) for silicate liquid viscosity as a function of temperature, liquid composition and dissolved water has been implemented. For any condition in terms of locally-defined silicate liquid composition, dissolved volatiles, temperature and rate of strain encountered in the flow dynamics calculations, the viscosity of the liquid-crystal magmatic mixture is the one implied by the two rheological models referenced above.

For the present purposes, the particles (crystals) dispersed in the liquid magma have been assumed to have a spherical shape, after having verified that elongated shapes with aspect ratio up to 10 involve variations in the calculated mass flow-rate of less than 5% on a log scale.
While the steady flow model can be applied to the long-lasting fire-fountain phases of the 2000 eruption of Mt. Etna, the highly unsteady character of the Strombolian phases prevents its application. The rheologically updated Conduit4 code has, therefore, been applied to the fire-fountain phase first, in order to identify a conduit diameter consistent with the observed mass flow-rates. Besides the mass flow-rate, the eruptive conditions have been constrained by the silicate liquid composition (10 major oxides), magma temperature, total volatiles H$_2$O and CO$_2$ and total crystal content assumed to correspond to 0.35 volume fraction (referred to bubble-free magma). The code then computes a conduit diameter and the corresponding vertical distribution of flow quantities and magma properties corresponding to the assumed mass flow-rate.

A second set of simulations has been performed by assuming this time a conduit diameter consistent with the fire-fountain phase as determined above and progressively increasing the crystal content up to that of the Strombolian phase. Here, the aim is to evaluate what would be the net effect on the eruption dynamics of just erupting more crystal-rich magmas. Figure 6 shows the set of pressure distributions along the conduit obtained as described above, for crystal contents from .35 to .59. For this set of simulations, the ascending magma is never found to reach the conditions for fragmentation, apart from the most crystal-rich cases, and at a level corresponding to the conduit exit. The pressure is larger than lithostatic everywhere, increasing with decreasing crystal content of the erupted magma.

Figure 7 illustrates the effect on mass flow-rate of the discharge of progressively crystal-richer magma. Comparing the conditions at the lowest and highest employed crystal contents - representative of the fire-fountain and Strombolian phases, respectively – reveals that such an increase in crystal content when all other simulation conditions are kept unchanged produces a decrease in mass flow-rate by one order of magnitude. If the total water content decreases when the crystal content is increased, the decrease in mass flow-rate is even more dramatic.

Figures 6 and 7 also show that small variations of the crystal content in the erupted magma have an effect which is comparably small if the crystal content is relatively...
small, but it can be substantial if the crystal content is sufficiently high. Within the large crystal contents, comparable with that of the Strombolian phases at Mt. Etna, small variations of the crystal content are expected to result in large fluctuations of the mass flow-rate (Fig. 7), suggesting a tendency towards unsteady eruption dynamics.

4 Discussion and conclusions

The analysis and modelling carried out in this paper demonstrates that the phases characterised by Strombolian and fire-fountain activity during the 2000 summit eruption cycle at Mt. Etna were characterised by the emission of magma having bulk or multiphase viscosity differing by orders of magnitude. Higher viscosity was associated with the Strombolian phases as a consequence of larger crystal content of magma trespassing a critical value at around 50 vol%, above which the slope of the viscosity vs. crystal content curve rapidly increases. Numerical modelling of steady magma flow performed here suggests that at such large crystal contents small heterogeneities in the solid particles carried by the magma may imply large fluctuations of the flow conditions, effectively hampering the onset of steady flow conditions.

We propose here that the large crystal content >50 vol% of the Strombolian eruption phases represented a rheological barrier for the onset of a sub-steady fire-fountain phase instead like those characterising the discharge of magma with 30–40 vol% crystal content. According to this view, when the deep forces sustaining efficient magma discharge waned, the magma residing at shallow levels in the conduit had sufficient time to crystallize under degassed and cooling conditions. An addition of about 20 vol% crystals to the original magma resulted in 2 to 3 orders of magnitude increase in viscosity, and in the formation of a plug of scarcely mobile magma on top of the magmatic column. Remobilization occurred then through a sequence of strongly unsteady Strombolian pulses until the viscous plug was eliminated and a new fire-fountain phase, discharging less crystal-rich and less viscous magma, took place.
The numerical simulations presented in Figs. 6 and 7 also provide a physical interpretation for the association between fire-fountaining and accompanying lava flows, often observed during the eruptive sequence. In fact, steady magma discharge turns out to be associated with large overpressure in the volcanic conduits (Fig. 6), with maxima around 10 MPa corresponding with the upper portion of the conduit. Such a conduit region corresponds to the cone of SEC, mainly formed by the accumulation of tephra during the last 30 years of activity of Mt. Etna and, therefore, characterised by a minimum in mechanical resistance. It is, therefore, expected that during the fire-fountain phases of the eruption, dyke intrusion occurs at the level of the cone due to the favourable combination of the highest magmatic overpressure and the lowest mechanical resistance of surrounding rocks. Dyke intrusion at this shallow level would, therefore, cause lava flows to emerge from the flanks of the SEC during the fire-fountain phases of the eruption, as it was in fact repeatedly observed.

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### Table 1. Eruptive temperatures and CaO/MgO content in products from explosive activity at Etna in 2000.

<table>
<thead>
<tr>
<th></th>
<th>Strombolian</th>
<th>Fire-fountain</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T$ ($^\circ$C)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Average</td>
<td>1091.9</td>
<td>1117.6</td>
</tr>
<tr>
<td>Minimum</td>
<td>1080.5</td>
<td>1106.8</td>
</tr>
<tr>
<td>Maximum</td>
<td>1103.3</td>
<td>1129.8</td>
</tr>
<tr>
<td>CaO/MgO (wt%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Average</td>
<td>2.29</td>
<td>2.13</td>
</tr>
<tr>
<td>Minimum</td>
<td>2.04</td>
<td>1.88</td>
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<tr>
<td>Maximum</td>
<td>2.48</td>
<td>2.30</td>
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</table>
Table 2. Summary of textural features of scoriae erupted from the explosive activity at Etna in 2000.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Type of activity</th>
<th>Vesicularity(^a)</th>
<th>Microlite crystallinity(^a)</th>
<th>Tot crystallinity</th>
</tr>
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<tbody>
<tr>
<td>040300B</td>
<td>Strombolian</td>
<td>0.66</td>
<td>0.36</td>
<td>0.58</td>
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<td>040300B1</td>
<td>Strombolian</td>
<td>0.64</td>
<td>0.30</td>
<td>0.59</td>
</tr>
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<td>160400D</td>
<td>Strombolian</td>
<td>0.63</td>
<td>0.40</td>
<td>0.55</td>
</tr>
<tr>
<td>150500B</td>
<td>Fire fountain</td>
<td>0.80</td>
<td>0.12</td>
<td>0.39</td>
</tr>
<tr>
<td>150500Ea</td>
<td>Fire fountain</td>
<td>0.72</td>
<td>0.17</td>
<td>0.39</td>
</tr>
<tr>
<td>150500Eb</td>
<td>Fire fountain</td>
<td>0.68</td>
<td>0.23</td>
<td>0.43</td>
</tr>
<tr>
<td>170500</td>
<td>Fire fountain</td>
<td>0.78</td>
<td>0.12</td>
<td>0.30</td>
</tr>
</tbody>
</table>

\(^a\) Vesicularity and microlite crystallinity from Polacci et al. (2006).
Table 3. Input data for the numerical simulations.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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</thead>
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<tr>
<td>Conduit length (m)(^a)</td>
<td>1500</td>
</tr>
<tr>
<td>Pressure at conduit base (Pa)</td>
<td>(4.5 \times 10^7)</td>
</tr>
<tr>
<td>Magma temperature (K)</td>
<td>1390</td>
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<tr>
<td>Average crystal density (kg/m(^3))</td>
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</tr>
<tr>
<td>Magma composition (wt%)</td>
<td></td>
</tr>
<tr>
<td>SiO(_2)</td>
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</tr>
<tr>
<td>TiO(_2)</td>
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<tr>
<td>Al(_2)O(_3)</td>
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<tr>
<td>FeO(_2)O(_3)</td>
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<td>MnO</td>
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<td>MgO</td>
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<tr>
<td>CaO</td>
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<tr>
<td>Na(_2)O</td>
<td>4.14</td>
</tr>
<tr>
<td>K(_2)O</td>
<td>3.07</td>
</tr>
</tbody>
</table>

\(^a\) Vergniolle et al., 2008
Fig. 1. Fire-fountain activity at the South-East crater of Mt. Etna on 8 June 2000. Horizontal edge of photo ~700 m. Courtesy of D. Andronico.
Fig. 2. Backscattered scanning electron images of bulk (top images) and groundmass (bottom images) textures in scoria clasts from Strombolian (a, c) and fire-fountain activity (b, d) at Mt. Etna in 2000. Black voids are vesicles, white, dark grey and light grey features are crystals, groundmass glass is in intermediate grey. Scale bar is 1 mm in (a) and (b) and 20 µm in (c) and (d).
Fig. 3. Calculated vs. measured viscosities for SiO$_2$-undersaturated natural melts (SiO$_2$ in the 40–50 wt% range): (Withington et al., 2000, 2001 (basanitic (NIQ) and tephritic compositions); Giordano and Dingwell, 2003a, b (Eifel basanite; Etna trachybasalt; Vesuvius phonotephrite); Dingwell et al., 2004 (Balmuccia peridotite); Bouhifd et al., 2004 (Stein Frenz tephrite and phonotephrite); Sato, 2005; Ishibashi and Sato, 2007; Giordano et al., 2006, 2007, 2008, 2009 (Slapany basanite, Nyiragongo phoidite, Stromboli materials, 1906 Vesuvius eruption tephrite); Villeneuve et al., 2009; Ishibashi, 2009. The calculations are based on the Giordano et al. (2008) (GRD) model and reproduce high temperature (close to eruptive temperature) and low temperature (close to glass transition) data with less than 0.35 log units RMSE (Root Mean Standard Error). Accuracy of the predictions at close to eruptive temperature is significantly higher, with RMSE less than 0.2 log units.
Fig. 4. (a) Relative viscosity as a function of crystal volume fraction at different strain-rates; (b) relative viscosity as a function of strain-rate for two crystal volume fractions of 0.37 and 0.57, adopted for fire-fountain and Strombolian phases of the Etna 2000 activity, respectively. Calculations made with the model in Costa et al. (2009).
Fig. 5. Calculated liquid-crystal viscosity as a function of temperature for the magmas erupted during the Strombolian (open symbols) and fire-fountain (solid symbols) phases of the 2000 Mt. Etna activity. The calculations assume a crystal volume fraction of 0.37 for the fire-fountain phase and 0.57 for the Strombolian phase (see text and Table 2). The viscosity of pure liquids at anhydrous and dissolved water contents (reported in the figure) of 0.3 and 0.7 wt%, calculated with the GRD model, are also shown as lines in the figure.
Fig. 6. Calculated pressure distribution along the conduit for magmas from 35 to 59 vol% of crystals relative to the liquid-crystal phase. Assumed total water content: 4 wt%. All other conditions reported in Table 3. The calculations are performed with the Conduit4 code (Papale, 2001), assuming a fixed conduit diameter of 4.5 m, corresponding to the conduit diameter required (from the simulations) to produce an observed mass flow-rate of $2.5 \times 10^5$ kg/s for the fire-fountain eruption phase with 35 vol% crystals.
Fig. 7. Calculated mass flow-rate as a function of the crystal content, for the simulations in Fig. 6 plus a few others with assumed total water content of 2 wt%.