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In[13]:= SetOptions[$FrontEndSession, FontProperties -> {"ScreenResolution" -> Automatic}]
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Counter example: The heat equation (parabolic problem)

$$\partial_t T = \kappa \partial_{yy} T$$

A solution to boundary condition and initial condition $T(t_0, y_0) = T(0, 0) = T_s$, $T(0, y) = T_0$ is

$$T = T_0 + (T_s - T_0) \operatorname{erfc}\left[\frac{y}{2\sqrt{\kappa t}}\right]$$

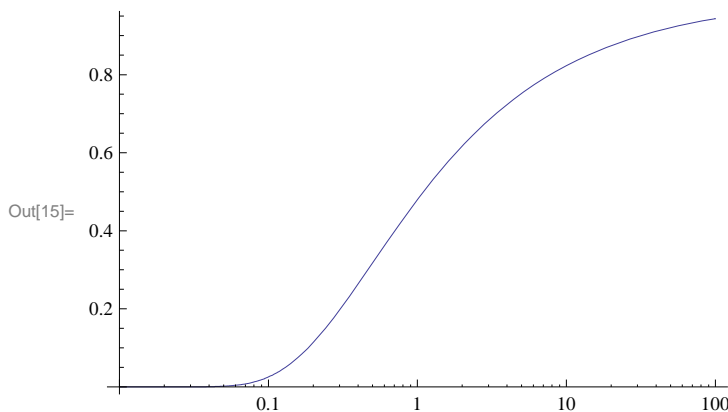
Notice that the diff equation "is linear" in κ . Notice also that the temperature "field" resembles a normal-mode problem; it's homogeneous, and the constants T_s and T_0 in the solution depend only on the initial conditions. We can easily show that the solution is not linear in κ . May be the solution is linear in $\log \kappa$? Judge yourself!

The visco-elastic diff equation has second and higher order spatial derivatives while it is of first order w.r.t. time. The laterally inhomogeneous problem has space-dependent coefficients in the system matrix in 3-d. My example exhibits nonlinear dependence on the single (and constant w.r.t. t and y) parameter already in this - you could say - trivial case. It's not trivial at all, and any proposal that it would disregard basic properties of linear differential equations.

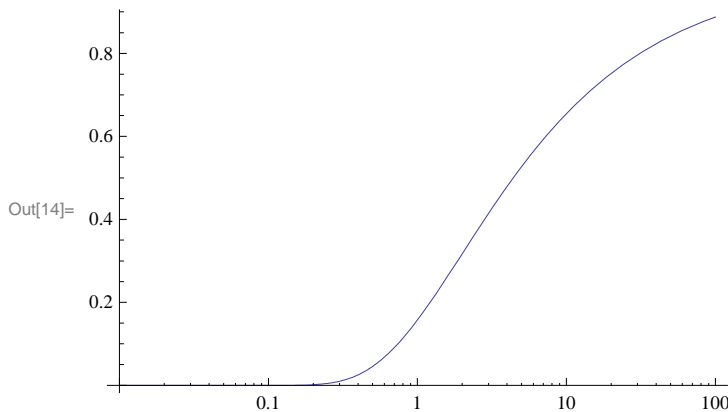
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In[2]:=  $\partial_x \operatorname{Erfc}\left[\frac{y}{2\sqrt{x t}}\right]$ 
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Out[2]=  $\frac{e^{-\frac{y^2}{4tx}} t y}{2\sqrt{\pi} (tx)^{3/2}}$ 
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In[15]:=  $\operatorname{LogLinearPlot}\left[\operatorname{Erfc}\left[\frac{1}{2\sqrt{x}}\right], \{x, 0.01, 100\}\right]$ 
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```
In[14]:=  $\operatorname{LogLinearPlot}\left[\operatorname{Erfc}\left[\frac{2}{2\sqrt{x}}\right], \{x, 0.01, 100\}\right]$ 
```



```
In[16]:= LogLinearPlot[Erfc[ $\frac{0.5}{2\sqrt{x}}$ ], {x, 0.01, 100}]
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