Solid Earth Discuss., 6, 2169–2213, 2014 www.solid-earth-discuss.net/6/2169/2014/ doi:10.5194/sed-6-2169-2014 © Author(s) 2014. CC Attribution 3.0 License.



This discussion paper is/has been under review for the journal Solid Earth (SE). Please refer to the corresponding final paper in SE if available.

Finite difference modelling to evaluate seismic *P* wave and shear wave field data

T. Burschil, T. Beilecke, and C. M. Krawczyk

Leibniz Institute for Applied Geophysics, Stilleweg 2, 30655 Hannover, Germany

Received: 16 July 2014 - Accepted: 17 July 2014 - Published: 1 August 2014

Correspondence to: T. Burschil (thomas.burschil@liag-hannover.de)

Published by Copernicus Publications on behalf of the European Geosciences Union.



Abstract

10

High-resolution reflection seismic methods are an established non-destructive tool for engineering tasks. In the near surface, shear wave reflection seismic measurements usually offer a higher spatial resolution in the same effective signal frequency spectrum than *P* wave data, but data quality varies more strongly.

To discuss the causes of these differences, we investigated a P wave and a SH wave reflection seismic profile measured at the same location on Föhr island, and applied reflection seismic processing to the field data as well as finite difference modelling of the seismic wavefield (SOFI FD-code). The simulations calculated were adapted to the acquisition field geometry, comprising 2 m receiver distance and 4 m shot distance along the 1.5 km long P wave and 800 m long SH wave profiles. A Ricker-Wavelet

- and the use of absorbing frames were first order model parameters. The petrophysical parameters to populate the structural models down to 400 m depth are taken from borehole data, VSP measurements and cross-plot relations.
- ¹⁵ The first simulation of the *P* wave wavefield was based on a simplified hydrogeological model of the survey location containing six lithostratigraphic units. Single shot data were compared and seismic sections created. Major features like direct wave, refracted waves and reflections are imaged, but the reflectors describing a prominent till layer at ca. 80 m depth was missing. Therefore, the *P* wave input model was re-²⁰ fined and 16 units assigned. These define a laterally more variable velocity model ($v_P = 1600-2300 \text{ m s}^{-1}$) leading to a much better reproduction of the field data. The *SH* wave model was adapted accordingly but only led to minor correlation with the field data and produced a higher signal-to-noise ratio. Therefore, we suggest to consider for future simulations additional features like intrinsic damping, thin layering, or a near
- ²⁵ surface weathering layer. These may lead to a better understanding of key parameters determining the data quality of near-surface seismic measurements.



1 Introduction

Near surface geophysical methods constitute a non-destructive means to investigate the shallow subsurface. Especially engineering tasks, for instance geo-hazard assessment or groundwater prospecting, profit from structural and parametrical methods (e.g. Miller, 2013; Kirsch, 2008). In some cases, results of geophysical prospecting are compiled into 3-D models and can act as input for, e.g., groundwater flow modelling.

Among other geophysical methods high resolution reflection seismics constitutes a valuable tool to extract structural information. Reflection seismics using compressional waves (*P* waves) is an established method and often produces accurate results for near surface tasks (e.g. Steeples and Miller, 1990; Rumpel et al., 2009; Jørgensen et al., 2012). In many cases, however, a higher spatial resolution is desired than *P* waves offer. This is one important reason why shear waves have become popular. Since shear waves have a lower velocity than *P* waves, they offer shorter wavelengths, i.e., higher spatial resolution, within the same frequency band as *P* waves. Also, shear

- ¹⁵ wave velocity information yields an additional parameter than the *P* wave velocity information alone and offers more detailed studies of elastic properties, like for instance Poisson's ratio. The combination of *P* and *S* wave velocities can help characterize lithology or pore fluid (e.g. Sheriff and Geldart, 1995). For shallow application, recent developments have been successful (e.g. Inazaki, 2004; Pugin et al., 2009a, b; Polom
 et al., 2010, 2013; Krawczyk et al., 2013). However, we experience that shear wave
- reflection seismics more strongly varies in quality compared with compressional wave seismics.

Seismic modelling is an important tool to evaluate seismic field data, yet not often applied for near surface tasks. Most studies applying wavefield modelling concentrate on deep reservoirs and crustal structures (Robertsson et al., 2007). A comprehensive approach is reported by Bellefleur et al. (2012), we use as well in this study. One current method to create synthetic seismograms of complex structures is finite difference (FD) modelling (Alterman and Karal, 1968). The advantage of the FD method is the ability to



choose arbitrary heterogeneous input models without fundamental restrictions. Drawbacks like high computational requirements have become less restricting during the past years. The FD code by Bohlen (2002) has the ability to include intrinsic seismic wave absorption, an advantage with respect to the study of unconsolidated material.

- ⁵ Full waveform inversion with either synthetic or real field data is an evolving field in exploration seismology. It aims at the automatic subsurface model generation from seismic field data. Although there has been a lot of progress in its evolution and it can be applied routinely for simple subsurface structures, especially in marine environments, but its application for near surface studies is still experimental (Romdhane et al.,
- ¹⁰ 2011; Groos et al., 2012; Plessix, 2012). This has to do with the importance of a good starting model for the inversion process but also with the large parameter space in the near surface. Also, many seismic surveys try to avoid low frequencies in order to not generate large surface waves. Yet, the low frequencies are an important prerequisite to find the global optimum in the optimization process of the inversion (e.g. Virieux and Operto, 2009; Fichtner et al., 2011). Therefore, we focus here on direct modelling.
- Operto, 2009; Fichtner et al., 2011). Therefore, we focus here on direct modelling.
 In this paper we describe the acquisition and processing of *P* wave and *SH* wave reflection seismic field data along an example profile. We generated synthetic *P* wave data of the same profile with a FD algorithm on the basis of an existing hydrogeological 3-D model and compared these with the field data. Differences of the *P* wave reflection patterns lead to a modification of this model to better reproduce the field data. To
- assess the lower signal-to-noise ratio of the recorded shear wave field data, we simulated SH wave seismograms on the basis of this modified model to comprehend quality variations in the SH wave reflection field data.

2 Finite difference modelling

²⁵ Seismic wavefield modelling reveals the propagation of seismic waves within a subsurface model. So far, no exact analytical solution exists for the calculation of such wavefields in arbitrary media. Therefore, a number of approximation methods have been



introduced over the years to solve the specific wave equation (Carcione et al., 2002; Fichtner et al., 2011). One method is FD modelling that works for arbitrary media. The medium is divided into a grid small enough to represent the natural phenomena of elastic waves. Changes of elastic parameters for each grid point are approximated for

- defined time steps and simulate seismic waves travelling through the gridded model.
 Forces at any chosen location within the model excite the respective grid points and start the wave propagation. These forces are independent in time and place and constitute seismic sources. Several elastic properties can be extracted at any grid point and any time. These properties represent, e.g., the seismic response to a receiver at
 the surface or in a borehole. FD modelling contains surface waves naturally that only
- recently has become feasible for routine application, because of enhanced computing capabilities.

The FD software we used in this work is described in Bohlen (2002). This code, called SOFI, is based on earlier work by Virieux (1986) and Levander (1988) for the elastic wave simulation but also on work by Robertsson et al. (1994) for the viscoelastic case. It allows the user to also consider intrinsic wave absorption (visco-elasticity, Q), and it provides an alternative rotated grid representation of the subsurface, based on work by Gold et al. (1997) and Saenger et al. (2000) for a more exact simulation of sur-

15

- face waves. Absorption is a common phenomenon in unconsolidated near surface rock units and surface waves pose a typical problem in near surface seismic data processing. The consideration of these phenomena in the simulation offers a better separation of the different subsurface parameters responsible for seismic field data signatures.
- SOFI provides full wavefield simulations for 3-D media and 2-D modelling. The 2-D codes simulate either *P* and *SV* waves within the propagation plane or *SH* waves os-
- cillating orthogonally to the propagation plane. For geometrical reasons *SH* waves will never convert into *P* or *SV* waves in this case. This kind of simulation is often unrealistic because the subsurface has a 3-D structure in which arbitrary wave conversion takes place. Nonetheless, it is a valuable aid for the interpretation of the *SH* wave field surveys. SOFI requires $v_{\rm P}$, $v_{\rm S}$ as well as density (ρ) as input information, and option-



ally accepts absorption models for P and S waves. The SH-version does not require compressional wave parameters.

Another important feature of the code is its ability to run simulations in parallel threads on multi-processor computers to save time. For such parallel simulation, the model can be split up into subgrids that the different CPUs called processing elements (PE) calculate independently. For every time step each PE updates the wave field in its subgrid and parameter exchange needs to be carried out with the grid points of neighbouring subgrids. This exchange can slow down the calculation that much that the use of all CPUs and a respective number of subgrids not necessarily delivers the fastest result. Here, the minimum computational time for one test model was achieved with 48 processors and a corresponding number of subgrids.

3 Test site Föhr

15

The test site is the North Sea island of Föhr (Fig. 1) that was investigated as a pilot area in the Interreg project CLIWAT (Harbo et al., 2011), co-financed by the European Union. The aim of CLIWAT was to analyse the influence of climate change to groundwater systems, and one major outcome was a hydrogeological model to forecast the groundwater evolution (Burschil et al., 2012a).

3.1 Geological evolution

The investigation area is located on the German North Sea island of Föhr, which is ²⁰ part of the UNESCO world heritage Wadden Sea (Fig. 1). In general, the deeper subsurface was sedimented as part of the Northern German Basin, while the landscape of Föhr was formed during the glacial and post glacial epoch (Scheer, 2012). The older sediments were deposited under marine conditions since Cretaceous age until the youngest Tertiary. For that reason, marine clay (mica clay) is found up to Miocene ²⁵ age. Sedimentation changed during Pliocene and sandy material (kaolin sand) was de-



posited until a climate change marked the beginning of the Pleistocene age. Glaciations from the Baltic–Scandinavian area reworked the shallow underground by alternating processes of glacial advance followed by erosion and sedimentation. In the region of Föhr push moraines as well as a system of tunnel valleys were formed and refilled with glacial deposits (Scheer, 2012). The great outwash plains were increasingly flooded during Holocene so that tidal mud deposits were accumulated and formed large marsh-land areas. Finally, heavy floods in historical times eroded large parts and formed the present North Frisian Wadden Sea.

3.2 Geophysical and geological framework

- In the project CLIWAT we accomplished a multidisciplinary geophysical acquisition (Burschil et al., 2012a). Between 2009 and 2011, we acquired seven reflection seismic profiles with *P* waves (in total 8 km) and three profiles with *SH* waves (in total 2.4 km). Five Vertical Seismic Profiles (VSP) were recorded with a 3C borehole geophone and the small electro-dynamical vibrator system ELVIS (Polom et al., 2011) with excitation
 in vertical and horizontal-transversal direction relative to the borehole location (Fig. 1). Maximum depths of five VSPs were in the range of 39–102 m. depending on the bore-
- Maximum depths of five VSPs were in the range of 39–102 m, depending on the borehole.

Additionally, in 2008 the island was mapped with the airborne electromagnetic system SkyTEM (Sørensen and Auken, 2004). The result of the *P* wave seismic survey

- was used as a-priori information for the electromagnetic data inversion (Burschil et al., 2012b). The information transfer between the different geophysical methods improved the electric resistivity model of the island. Borehole logging data were evaluated statistically regarding electric resistivity as well as seismic velocity. This allowed a petrophysical classification of sand, till and clay (Burschil et al., 2012a). These lithological
- ²⁵ units form structures as push-moraines and buried valleys, which are consistent with the geological evolution of the region.



3.3 Hydrogeological model

The hydrogeological 3-D model for Föhr represents a simplification of the geological and geophysical information and only contains hydraulically relevant strata, i.e. aquifers and aquitards. With respect to the different geophysical methods applied (Burschil ⁵ et al., 2012a), no lateral variations or internal structures were added to lithological units.

As a first approach for FD modelling we extracted a cross section along a seismic profile and assigned lithological information (Fig. 2). The cross section shows different units of sand and till above a bed of clay. The prominent till layer is interrupted in the middle of the cross section. Near the surface, thin lenses of till and silt are embedded in sand.

4 Reflection seismic field data

4.1 Seismic acquisition

10

Seismic equipment varied with surveys due to different wave types used for exploration.
For two *P* wave surveys we used the hydraulic vibrator systems of the Leibniz Institute for Applied Geophysics (LIAG), the MHV2.7 in 2009 and the new HVP-30 in 2010. We used a linear sweep in the range of 30–240 Hz with 10 s duration. The source excited on a paved street in the western part of the profile and on grassland in the eastern part. The receivers were vertical geophones (20 Hz), planted every 2 m in the green strip next to the line of the source locations, with a maximum offset of 360 m to enhance the near surface resolution and fold. We used a combination of split-spread/roll along geometry (Fig. 3a) with a source spacing of two-times receiver spacing (4 m). With this geometry we had acquired high quality data before. We operated up to 268 active channels with Geometrics Geode seismographs. This resulted in a fold between 47



the wave field. For the P wave data we set up a processing scheme (Table 1) focusing on the enhancement of the reflections (e.g. Yilmaz, 2001). Processing was carried out with Landmark's ProMAX 2D. The most important processing steps turned out to be muting the surface waves, spectral whitening, and dynamic corrections, including dip move out corrections. The detailed velocity analysis left a certain tolerance within the

P wave and shear wave data processing differs due to different signal locations within

25

25

4.2 Seismic processing 20

- be detected down to 1 s two-way-traveltime (TWT). In contrast, the shear waves offer a smaller signal-to-noise ratio (Fig. 5). Reflection hyperbola signals are faint and within 15 a reverberating background. Chevron patterns, also called herring-bone pattern, appear irregularly among shot gathers as part of the reverberations. The reflection signal bandwidth decreases with time. Below 0.7 s the signal vanishes and suggested further analysis in combination with seismic FD modelling.
- processing. The shear wave seismic profile only covers the western half of one of the 10 P wave profiles. Here, the surface is paved, which helps avoiding the generation of surface waves. All P wave profiles show good signal-to-noise ratio (Fig. 4). Seismic reflections can
- shear wave polarization) are mounted every meter. The whole system was towed by the recording vehicle. The acquisition geometry (Fig. 3b) was similar to the P wave surveys, except for a shorter spread and that we vibrated within the second third of the streamer and sequentially pulled thirds of its length along the profile. Shot point spacing was 4 m. We used a linear sweep between 30 Hz and 160 Hz for 10 s. In contrast to the P wave surveys, we recorded the uncorrelated traces to allow pre-correlation
- seismic traces after vibro-seismic correlation with the Pelton Vib Pro input signal.

For the shear wave survey in 2011 an established system comprising LIAG's hydraulic shear wave vibrator MVP-4S in combination with a 120 m landstreamer system



Discussion

Paper

Discussion Paper



semblance calculations. We therefore included geological a-priori knowledge to reduce the uncertainty, so that the resulting interval velocity distribution better corresponds to the reflectors (Burschil et al., 2012a). At the end of the processing sequence we achieved depth-converted, time-migrated sections (Fig. 6).

The shear wave data contain surface wave interferences related to the specific shear wave reflection move out. This is the reason why we cannot simply mute the surface wave noise and purely focus on reflection signals, as we could for *P* waves. To enhance the reflection signals we applied several techniques, e.g. fk-filtering, spectral whitening, and deconvolution. Finally, automatic gain control (AGC, 300 ms) and fk-filtering with low-cut of velocities below 350 m s^{-1} provided the best results (Table 1). This filter also removes a wide range of the chevron pattern that is present in the lower part of the seismograms around the shot location, depicted in Fig. 5. In contrast to Polom (1997) who investigated a chevron pattern that originated in ghost sweeps, we cannot identify

a comparable increase of the frequency with time in the data. Here, the chevron pattern is rather mono-frequent and no ghost sweeps can be detected within the pattern. Velocity analysis was very difficult because reflections can only be identified sporad-

¹⁵ ically and can hardly be traced through to neighbouring shots. This restrains velocity analysis in CMP-sorted data. After normal move out-correction and common midpoint-stacking we converted the section to depth with a velocity function derived from VSP measurements. The result is rather mono-frequent, but the till layer as well as deeper reflectors can be identified (Fig. 7). However, the quality of this shear wave survey is
 ²⁰ less compared to *P* wave seismic results.

5 Synthetic data from finite difference modelling

To understand data quality differences between shear wave measurements and compressional wave measurements on the island of Föhr, seismic wavefield modelling is introduced here for further data analysis. We chose the 2-D P/SV-version of SOFI for *P* wave simulations and the 2-D SH-version of SOFI for SH wave modelling

 $_{25}$ *P* wave simulations and the 2-D *SH*-version of SOFI for *SH* wave modelling.



The first input model was based on the cross section of the hydrogeological model (Fig. 2). Seismic velocities were assigned to the cross section (Fig. 8a; Table 4) according to the velocities from the petrophysical classification for sand, till, and clay (cf. Sect. 3.2). Typical density values were taken from the literature and added to the layers as well. The model dimensions were 1500 m length and 500 m depth (Fig. 8a).

- To compare model data with field data we calculated a number of single shots with geometries only slightly different from the field geometries (Fig. 3). Differences are related to modelling requirements. Although receivers were simulated 1 m apart and shots 4 m apart (Fig. 3c), only every second receiver was used for later *P* wave processing. The maximum offset of shear wave channels was restricted in later *S* wave processing, to respect the field geometry. Additionally, the efficient use of computational
- ¹⁰ capacities required the splitting of the whole model into a number of model segments of which the westernmost is depicted in Fig. 8b. Our FD modelling approach required the use of absorbing frames at the left, right and lower boundaries of each model segment. Therefore, the model segments were 600 m long and contained an absorbing frame width of 45 m (Fig. 8b and Table 2). Instead of a free surface we also implemented an
- ¹⁵ absorbing frame at the surface (Fig. 8b). For this purpose, we expanded the model top layer by 50 m that hosts the absorbing frame of 45 m. We did this to suppress surface multiples, which is the same approach that was used by Jones (2013). The effect of this absorbing frame is comparable to a weathering layer with high parameter gradients. We used a zero-phase Ricker wavelet for the simulations instead of a vibroseismic corre-
- ²⁰ lated sweep signal, i.e. a Klauder wavelet. This is a practical compromise which takes into account that the field data signals are absorbed to a certain degree and do not show a white frequency spectrum. In contrast to the field data source signals, we used the same central frequency of the Ricker wavelet for *P* wave simulation as well as for *SH* wave simulation.



25 5.1 *P* wave modelling

Although we started with a very simple subsurface model, the basic appearance of single FD-modelled shots (Fig. 9) is similar to the field data (Fig. 4). The direct P and SV waves are detectable as well as several reflections, even in the part of the seismogram where surface waves usually appear. However, the complex pattern of the direct wave that can be identified in the field data is not present in the modelled data, i.e. the dispersive ground-roll cone is missing (cf. noise cone in Fig. 4). Also, the simulated data have apparent higher frequency content, not showing the typical subsurface low

- ⁵ pass filter effect. We applied a simple processing scheme to all 300 modelled single shots comprising amplitude control, frequency filtering, normal move out correction, common mid-point stacking, time-migration, and time-to-depth conversion. Stacking velocities were picked via an interactive velocity analysis from CMP-gathers. The migrated section (Fig. 10) resolves several reflectors that can be found in the field data in a similar manner (Fig. 6). Yet, not all of the main reflectors could be reproduced
- with the modelled data. Among some minor differences the most prominent difference is a discontinuous till layer in the centre of the image at about 80 m depth (Fig. 10). Therefore, we modified the input model.

5.2 Subsurface model modification

- ¹⁵ We interpreted the major structures of the *P* wave seismic field data depth section (Fig. 11a) and assigned *P* wave velocities and densities according to geological and geophysical a-priori information (Table 4 and Fig. 11b). The modified model contains a larger number of lithological units. Because we lacked detailed shear wave velocity information we generated a cross-plot of velocity data (v_P and v_S) from VSP surveys
- on the island of Föhr. Within the cross-plot we calculated mean and median values and the linear regression for different lithological classes. For statistical confidence, the number of classes was limited to those, for which more than 20 velocity samples were available. We then picked shear wave velocities from the linear regression line of this



cross-plot and thereby defined 14 lithological units with known v_P and v_S values that constitute the modified model (Fig. 12, Burschil et al., 2012a). This new model was used for the simulation of the same 300 single shots (e.g. Fig. 13) and stacked with the same processing scheme as for the first simple input model (Fig. 14).

In the simulated single shot data (e.g. Fig. 13) we can detect direct waves, refracted waves, and several reflections. Like in the simulation with the simpler model reflections can be identified in the surface wave cone. In the depth section (Fig. 14) the uppermost reflector at 30 m is faint. Below, two strong reflectors mark the upper and lower bound-aries of the till unit. The upper reflector can be traced through the entire section with

- varying amplitude. Also, a larger number of additional reflectors with different amplitudes is imaged now. In the central part of the seismogram, at 150 m depth, two close reflectors mark the lower end of the complex geological units (Fig. 13). Below, another two nearly horizontal reflectors at 250 m and 380 m depth are present. At the western and eastern edges of the section the migration process generated minor artefacts. Be-
- ¹⁰ cause this *P* wave depth section was basically able to explain the *P* wave field data, we continued with the simulation of the shear wave field data, instead of a further study of additional features present in the *P* wave field data, like surface wave ground roll.

5.3 Shear wave modelling

25

Shear wave propagation was modelled using the modified input model only. We restricted the modelled data to a maximum offset of 80 m that corresponds to the maximum offset in the field data. Due to generally low shear wave velocities we had to consider longer travel times and simulated data up to 2.5 s TWT (Table 3). Resulting shot gathers show the direct *S* wave as well as several shear wave reflections (Fig. 15). The sharp reflection signal does not change its shape with travel time. Because we
used the same frequency band for the *P* wave and *S* wave source simulations, the stacked section (Fig. 16) shows an even more detailed image of the subsurface due to the shorter wavelengths of the shear waves compared with the *P* waves. All structures of the input model are imaged with excellent resolution.



6 Discussion

- In reflection seismic surveys normally only one type of wave is utilized, for instance *P* waves, shear waves or converted waves. The use of more than one wave type or even the integration of multi-component technology (Hardage et al., 2011) is rare but growing. This is even more pronounced for near surface applications. Recently, a few studies reported the combination of shallow *P* wave and shear wave seismics, compa-
- ⁵ rable to the field work presented in this article (e.g. Pugin et al., 2004, 2009b; Malehmir et al., 2013; Sauvin et al., 2014). Even 9C reflection seismics was tested in near surface exploration (Pugin et al., 2009a). All of these studies successfully recorded high resolution data of mainly good quality. The signal-to-noise ratio of the *P* wave data is similar to the *P* wave data presented in this study, except in (Pugin et al., 2009a). In
- contrast, shear wave data of these studies are of good quality that constitute in prominent, coherent reflections. Equipment and acquisition geometry slightly vary among the reported surveys, but the combination of vibrator and land streamer is the favourite choice for shear wave seismic. General data processing reported in some of the studies is similar to the processing we finally applied (Table 1). Sauvin et al. (2014) reported
- the application of elevation statics for only one of their shear wave profiles. None of the authors reported refraction statics for shear waves. In some cases, differences in shear wave processing are related to deconvolution and spectral whitening, which was applied by Pugin et al. (2009b) and Sauvin et al. (2014). Here, deconvolution and spectral whitening did not provide success.
- ²⁰ So far, we have not been able to reproduce the shear wave field data with seismic modelling. A similar observation is reported by Bellefleur et al. (2012). They calculated synthetic *P* wave data of four different input models from the surface to the reservoir and compared these data with field data. Their data excellently correlate with data from a VSP, but they consider the correlation with a surface 3-D reflection seismic dataset as
- rather poor. They explain the poor surface data quality with the appearance of surface waves and a higher amount of scattering at inhomogeneities. Surface waves are not



present in VSP data and do not affect data quality significantly. Scattering also affects the surface data more than VSP data, because the travel path of seismic body waves from the source to the scattering point and to the receiver is longer for surface data than for VSP data. If this explanation is true, we will have to take small scale inhomogeneities and a weathering layer as origin of surface waves into account for future studies.

6.1 Influence on data quality in land seismic surveys

⁵ In general, a number of factors can influence the quality of land seismic data, listed and illustrated in Sheriff (1975). Typical factors, one would assume to be the most likely in our case, are source strength, inappropriate coupling of sources and receivers, superimposed surface waves, multiples, scattering, and intrinsic absorption (Q).

The vertical hydraulic vibrator sources MHV2.7 and HVP-30 have proven their ability to reach reflectors at least 2 km deep (Buness et al., 2009). The LIAG shear wave vibrator source MHV-4S has been able to generate clear reflections at least as deep as 200 m in fluviatile and marine deposits (Polom et al., 2010). Sauvin et al. (2014) used a wheelbarrow-mounted micro-vibrator source for the analysis of quick clays. Their data show clear reflections from 40 m below ground level within fluviatile and marine sediments. In the underlying bedrock reflections can be traced down to 120 m depth. Malehmir et al. (2013) report clear reflections in a similar environment from at least 40 m below ground level with the same source. This means that even small

- sources are able to create reflections from at least 40 m below the source. Pugin et al. (2009b) used an IVI Minivib on a minibuggy carrier, which is comparable to the MHV-
- ²⁰ 4S. They show *SH* wave reflections down to about 50 m in glacial deposits before reaching the bedrock. In the light of these studies, the MHV-4S source can be expected to be strong enough to image the glacially overworked deposits down to 150 m. Indeed, the *SH* wave image shows faint reflections even from ca. 270 m depth (Fig. 7).

The ground coupling of the sources is mainly affected by the vehicle mass and the driving peak force of the system. For *P* wave sources this mass acts as a gravitational hold down force that compensates the vertical force of the vibrator unit (Sheriff and



Geldart, 1995). For *S* wave sources this mass increases horizontal friction of the base plate and thus prevents sliding of the shear wave vibrator unit on the ground. We use the rule of thumb that the gravitational hold down force of the vibrator mass on loose ground should at least be twice the peak shear force. Experience shows that under favourable conditions, the peak force of a vibrator with a rubber base plate on paved roads can reach 70% of the hold down force without sliding. The *P* wave hydraulic vibrator systems MHV2.7/HVP-30 have masses of 2.6 t/4 t and a maximum peak forces

of 27.6 kN/30 kN. Therefore, these vibrator systems should not be affected by bouncing. The shear wave vibrator system MHV-4S has a mass of 4t and a maximum peak force of 30 kN. During the survey, we used a peak force of 17 kN on a paved road. Therefore, the gravitational hold down force of nearly 40 kN should have been sufficient.

Receiver coupling with the ground is another factor. Carefully planted geophones
typically offer proper receiver ground coupling for *P* wave surveys (Krohn, 1984). The *P* wave field data we acquired support this expectation. For the shear wave survey we used the LIAG land streamer on which geophones are directly fixed to aluminium plates that have a gravitational three-point contact to the ground. This system has proven to receive good shear wave signals from the subsurface before (Polom et al., 2010;
Krawczyk et al., 2013; Malehmir et al., 2013). On one *SH* wave profile on gravel Sauvin

- Krawczyk et al., 2013; Malehmir et al., 2013). On one SH wave profile on gravel Sauvin et al. (2014) used the same streamer but on grassland they planted the geophones in the ground. They do not report any difference in data quality. Pugin et al. (2004, 2009b, a) use a different land streamer system that works successfully as well. In the field, we took care that geophone coupling is good. Every time a new streamer position was
- reached, a noise test was carried out and noisy geophones were coupled to the ground by hand. We therefore expect coupling to be sufficient.

Surface waves are an important degradation factor for shear wave reflection surveys. Here, the reflection hyperbola often interferes with surface wave (Love wave) signals; cf. surface waves in Fig. 4 and reflection hyperbolas in Fig. 5. This factor has complicated the application of shear waves in the past and still limits the application of this method. However, the observation that a high velocity layer at the surface suppresses

25



the generation of surface waves in shear wave exploration (e.g. Inazaki, 2004) was an important step to overcome this limitation in many urban applications and even in rural environments, if paved or consolidated roads are present. Even though surface waves are often exited during *SH* wave surveys on unconsolidated surfaces, *SH* wave reflection seismic surveys have been successful in these conditions (e.g. Malehmir et al., 2013; Sauvin et al., 2014). Polom et al. (2013) identify partly dispersive Love waves that show a similar signature as the chevron pattern depicted in Fig. 5. In their case

- and in our case, these waves seem to be linked to the shot point location. Even neighbouring shot points show strong variations in this respect. For instance, in Fig. 5 we show shot gathers with shot points locations of FFID's 1126 and 1127 that are just 4 m apart. To cancel surface waves with a linear move out or mild dispersive character fk-filtering is often successfully used (e.g. Polom et al., 2013; Sauvin et al., 2014). We successfully applied an fk filter as well (Table 2) but this did not imprave the cohorement
- ¹⁰ successfully applied an fk-filter as well (Table 2) but this did not improve the coherency of reflectors in the final depth section (Fig. 7).

In very complex structures, scattering is an important factor. It is closely related to energy loss through multiples, in case tuning layers or strong lateral impedance contrasts are present. In our case, at least in the upper 150 m a mixture of complex structures

- and thin layering can be expected (Fig. 2, Scheer, 2012). Compressional waves and shear waves could be influenced by this kind of energy loss in a different manner. In the same frequency band the wavelengths of P and S waves differ, depending on subsurface velocity. If the sizes of subsurface structures are in the order of the wavelength of the main frequency present in the source signal a strong energy loss for the signals
- can be expected. This could be an important reason for the degradation of our shear wave data. In other cases, the shear wave data could be less degraded compared with the *P* wave data. The latter case is present in Pugin et al. (2009a). They relate the degradation to static problems, only occurring in the *P* wave measurements. Malehmir et al. (2013) report a case where this factor does not seem to negatively affect the data quality.



Intrinsic absorption of seismic waves (*Q*) can be another important factor for data quality. Our exploration focused on near-surface unconsolidated units. Therefore, we expect intrinsic absorption to play an important role in the energy loss phenomenon generally. Kang and McMechan (1994) investigated the separation of intrinsic and scattering *Q* by analyses of synthetic data and measured data. They revealed $Q_{\rm P}$ - and $Q_{\rm S}$ -values of near surface data for four study areas. Because on some traces we can identify faint reflections from ca. 270 m depth with a reasonable bandwidth, we do not believe that a global value for intrinsic damping can explain the lower quality of the shear waves (Fig. 7). Therefore, we have not taken intrinsic absorption into account in our simulations at this point.

6.2 Comparison of *P* wave and *S* wave simulations

We calculated synthetic seismograms for P wave propagation through two different input models as well as shear wave propagation through one of these models. In the following we will compare these modelled data with the corresponding field data and discuss the observations.

6.2.1 *P* wave shot gathers

10

The simulated *P* wave and the corresponding field data single shot seismograms (Figs. 4, 9, and 13) contain reflection events that show a similar basic waveform. However, the field data (Fig. 4) are much noisier, in particular before the first break as well as inside the surface wave cone. No reflections are detectable inside that field data cone, whereas in the synthetic data (Figs. 9 and 13) reflections can be traced through all parts of the seismogram. This can be explained to a large degree by the lack of a weathering layer in the models. The absence of that layer prevents the build-up of simulated surface waves and thus, a surface wave cone is missing in simulated shot records.



Another noticeable observation is the signature of the reflections. In general, the reflection signals of the synthetic data seem to be more focused, whereas many of the reflections within the field data seem to be made up of a number of oscillations/reverberations instead of single reflections (compare reflection signal at 0.3 s in Figs. 4, 9, and 13). It seems that even though internal multiples show up within the simulated records (Fig. 9), their number is not large enough to reproduce the oscillation characteristic of reflectors in the field data. We expect an additional fine layering within the 14 units of the modified model to be able to reproduce that observation (Fig. 13). Perhaps, the simulation of a multi-layer surface unit, related to the weathering zone might also help explaining the reverberation observation. Even though we cannot reproduce an exact copy of the reflections of the field data, the main reflections in the modified model occur in good quality and quantity to use that model for additional shear wave simulations.

6.2.2 SH wave shot gathers

Shear wave shot simulations show larger differences compared with their corresponding field data (Figs. 5 and 15). The clear and continuous reflections in the synthetic
data are not present in the field data. Some of the field records show the mentioned chevron pattern parallel to the first break with varying amplitude (Fig. 5) that does not show up in the synthetic data. In the model we did not consider very shallow structures that could create Love waves.

The spectrum of the synthetic data does not change with time in the seismogram (Fig. 15). The Ricker wavelet has the same spectral shape for shallow reflections as for deep reflections. This no surprise since up to this point we have not included any kind of signal damping in the model, like intrinsic damping or sources for attenuation through scattering or interference. In contrast, the field data signals for longer traveltimes lose some of the higher frequency components (Fig. 5). This indicates some kind of intrinsic

²⁵ or scattering attenuation. However, this cannot explain the lateral appearance variation among shot gathers of the shear wave data.



6.2.3 *P* wave depth section

Poststack migrated *P* wave sections of synthetic data show less noise and less amplitude variability while the corresponding field data show natural levels of different signals and thus contain more information about small-scale and internal structures (Figs. 6, 10, and 14). However, the poststack migrated section, derived from the hydrogeological model, does only reflect some of the main features imaged in the field data section.

Important differences compared with the field data are the discontinuous reflector of the till surface at about at 80 m depth in the synthetic section (Fig. 10), and missing of a strong reflector at about 260 m depth as well as a number of dipping reflectors between about 50 and 180 m depth (Fig. 10).

The depth section of the modified input model better reflects the field data features (Fig. 14). The till top reflector between 50 m and 80 m depth appears continuous and two deep reflectors show as well. Some of the dipping reflectors in this modelled section add details that similarly appear in the field data.

The field data section (Fig. 6) can be divided into two parts: excitation on paved street and on grassland. Within the field data seismic section we detected a lack of resolution in the eastern part (about 900–1400 m) that is not present in the modelled data. However, we did not implement the structural complexity of unconsolidated grassland as a near surface weathering layer, i.e. large velocity contrasts, inhomogeneities, and intrinsic damping, in the model so far.

In general, the reflection signatures in the field data spatially vary more strongly than in the synthetic data (Figs. 6, 10, and 14). Sources for these observations in the field data can be intrinsic damping, scattering attenuation including fine layering, and inhomogeneous lithological units. All of these features were not included in the models (Figs. 8 and 11). In a natural environment, complex structures or fine layers can be sources of multiples and wave conversion that subsequently can pose similar

challenges to data processing like random noise signals do. Since the model consisted of comparatively large units this kind of noise was not simulated.



2189

In summary, this first and simplified input model is not able to reproduce major features in the seismic field data, but the modified model does reproduce these features.

6.2.4 SH wave stacked sections

⁵ The *SH* wave stacked sections of synthetic data (Fig. 16) and field data (Fig. 7) differ more than the *P* wave sections. While no clear interpretation can be carried out for the stacked field data, the stacked section from the modelled dataset reproduces well the input model. For example reflector segments occur at 90 m depth, which correspond to the interface of the sub-horizontal layer at 90 m (top till layer) and at 250 m depth corresponding to the first deep reflector in the *P* wave seismic section. Nonetheless, the reflection signatures in the field data are of course much noisier than in the synthetic data.

7 Summary and outlook

25

Shear wave field data recorded on the island of Föhr showed less quality compared with their compressional wave counterparts. To comprehend the reasons for this quality difference we used seismic wavefield modelling within simple models of the subsurface, using the seismic field geometry. We chose finite difference modelling to try to reproduce the field data because of its ability to simulate the entire wavefield and to allow arbitrary input models. We come to the following conclusions:

- 1. After subsurface model optimization we were able to simulate *P* waves that show clear first order similarities compared with the *P* wave field data.
 - 2. Simplified FD modelling does not explain the small signal-to-noise ratio of the shear wave field data.
 - 3. We can simulate the chevron pattern that is present in the field data by clipping of uncorrelated channels near the source location.



For future analyses we therefore suggest to consider additional complexity in the subsurface model that will presumably be able to explain the different quality of compressional and shear wave field data. The most important additional factors are intrinsic damping, thin-layers within the modelled units, a complex near-surface weathering layer structure, and heterogeneous material within the layers. While 2-D calculations gain faster results and allow testing the effect of different features, the full complexity of field acquisition may be understood using 3-D simulations in the future.

Acknowledgements. We acknowledge Karlsruhe Institute of Technology (KIT) for providing an academic licence of the SOFI software package.

10 **References**

20

- Alterman, Z. and Karal, F.: Propagation of elastic waves in layered media by finite difference methods, B. Seismol. Soc. Am., 58, 367–398, 1968.
- Bellefleur, G., Malehmir, A., and Müller, C.: Elastic finite-difference modeling of volcanic-hosted massive sulfide deposits: a case study from Half Mile Lake, New Brunswick, Canada, Geo-
- ¹⁵ physics, 77, WC25–WC36, 2012.
 - Bohlen, T.: Parallel 3-D viscoelastic finite difference seismic modelling, Comput. Geosci., 28, 887–899, 2002.
 - Buness, H., Gabriel, G., and Ellwanger, D.: The Heidelberg Basin drilling project: geophysical pre-site surveys, Quaternary Science Journal (Eiszeitalter und Gegenwart), 57, 338–366, 2009.
 - Burschil, T., Scheer, W., Kirsch, R., and Wiederhold, H.: Compiling geophysical and geological information into a 3-D model of the glacially-affected island of Föhr, Hydrol. Earth Syst. Sci., 16, 3485–3498, doi:10.5194/hess-16-3485-2012, 2012a.

Burschil, T., Wiederhold, H., and Auken, E.: Seismic results as a-priori knowledge for airborne

- TEM data inversion a case study, J. Appl. Geophys., 80, 121–128, available at: http://www. sciencedirect.com/science/article/pii/S0926985112000365, 2012b.
 - Carcione, J. M., Herman, G. C., and ten Kroode, A.: Seismic modeling, Geophysics, 67, 1304–1325, 2002.



Fichtner, A., Bleibinhaus, F., and Capdeville, Y.: Full Seismic Waveform Modelling and Inversion,

³⁰ Springer, 2011.

20

- Gold, N., Shapiro, S. A., and Burr, E.: Modeling of high contrasts in elastic media using a modified finite difference scheme, in: 68th Annual International Meeting, Soc. Explor. Geophys., Expanded Abstracts, 1997.
- Groos, L., Schäfer, M., Forbriger, T., and Bohlen, T.: On the significance of viscoelasticity in a 2D full waveform inversion of shallow seismic surface waves, in: 74th EAGE Conference & Exhibition, Copenhagen, 2012.
- ⁵ Harbo, M. S., Pedersen, J., Johnsen, R., and Peteren, K.: Groundwater in a Future Climate: the CLIWAT Handbook, avilable at: www.cliwat.eu, The CLIWAT Project Group, 2011.
 - Hardage, B. A., DeAngelo, M. V., Murray, P. E., and Sava, D.: Multicomponent Seismic Technology, Society of Exploration Geophysicists, 2011.

Inazaki, T.: High-resolution seismic reflection surveying at paved areas using an *S* wave type land streamer. Explor. Geophys., 35, 1–6, 2004.

- Jones, I. F.: Tutorial: the Seismic Response to Strong Vertical Velocity Change, First Break, 31, 2013.
- Jørgensen, F., Scheer, W., Thomsen, S., Sonnenborg, T. O., Hinsby, K., Wiederhold, H., Schamper, C., Burschil, T., Roth, B., Kirsch, R., and Auken, E.: Transboundary geophysical map-
- ping of geological elements and salinity distribution critical for the assessment of future sea water intrusion in response to sea level rise, Hydrol. Earth Syst. Sci., 16, 1845–1862, doi:10.5194/hess-16-1845-2012, 2012.
 - Kang, I. B. and McMechan, G. A.: Separation of intrinsic and scattering *Q* based on frequencydependent amplitude ratios of transmitted waves, J. Geophys. Res.-Sol. Ea. (1978–2012), 99, 23875–23885, 1994.

Kirsch, R. (Ed.): Groundwater Geophysics: a Tool for Hydrogeology, Springer, 2008.

Krawczyk, C. M., Polom, U., and Beilecke, T.: Shear wave reflection seismics as a valuable tool for near-surface urban applications, The Leading Edge, 32, 256–263, 2013.

Krohn, C. E.: Geophone ground coupling, Geophysics, 49, 722–731, 1984.

- Levander, A. R.: Fourth-order finite-difference P-SV seismograms, Geophysics, 53, 1425– 1436, 1988.
 - Malehmir, A., Bastani, M., Krawczyk, C. M., Gurk, M., Ismail, N., Polom, U., and Persson, L.: Geophysical assessment and geotechnical investigation of quick-clay landslides – a Swedish case study, Near Surf. Geophys., 11, 341–350, 2013.



- Miller, R. D.: Introduction to this special section: urban geophysics, The Leading Edge, 32, 30 248-249, 2013.
 - Plessix, R.-E.: Waveform inversion overview: where are we? And what are the challenges?, in: 74th EAGE Conference & Exhibition, Copenhagen, 2012.
 - Polom, U.: Elimination of source-generated noise from correlated vibroseis data (the 'ghostsweep'problem), Geophys. Prospect., 45, 571-591, 1997.

Polom, U., Hansen, L., Sauvin, G., L'Heureux, J.-S., Lecomte, I., Krawczyk, C. M., Vanneste, M.,

- and Longva, O.: High-resolution SH wave seismic reflection for characterization of onshore 5 ground conditions in the Trondheim harbor, central Norway, in: Advances in Near-Surface Seismology and Ground-Penetrating Radar, SEG, Tulsa, 297-312, 2010.
 - Polom, U., Druivenga, G., Grossmann, E., Grüneberg, S., and Rode, W.: Transportabler Scherwellenvibrator, Patent application, 2011 (in German).
- Polom, U., Bagge, M., Wadas, S., Winsemann, J., Brandes, C., Binot, F., and Krawczyk, C.: 10 Surveying Near-Surface Depocentres by Means of Shear Wave Seismics, First Break, 31, 2013.
 - Pugin, A. J., Larson, T. H., Sargent, S. L., McBride, J. H., and Bexfield, C. E.: Near-surface mapping using SH wave and P wave seismic land-streamer data acquisition in Illinois, US,
- The Leading Edge, 23, 677-682, 2004. 15
 - Pugin, A. J.-M., Pullan, S. E., and Hunter, J. A.: Multicomponent high-resolution seismic reflection profiling, The Leading Edge, 28, 1248–1261, 2009a.
 - Pugin, A. J.-M., Pullan, S. E., Hunter, J. A., and Oldenborger, G. A.: Hydrogeological prospecting using P and S wave landstreamer seismic reflection methods, Near Surf. Geophys., 7, 315-327, 2009b.
- 20

25

- Robertsson, J. O., Blanch, J. O., and Symes, W. W.: Viscoelastic finite-difference modeling, Geophysics, 59, 1444–1456, 1994.
- Robertsson, J. O., Bednar, B., Blanch, J., Kostov, C., and van Manen, D.-J.: Introduction to the supplement on seismic modeling with applications to acquisition, processing, and interpretation, Geophysics, 72, SM1-SM4, 2007.
- Romdhane, A., Grandjean, G., Brossier, R., Rejiba, F., Operto, S., and Virieux, J.: Shallowstructure characterization by 2-D elastic full waveform inversion, Geophysics, 76, R81-R93, 2011.



2193

- Rumpel, H.-M., Binot, F., Gabriel, G., Siemon, B., Steuer, A., and Wiederhold, H.: The benefit of geophysical data for hydrogeological 3D modelling an example using the Cuxhaven buried
 - valley, Z. Dtsch. Ges. Geowiss., 160, 259-269, 2009.

30

650

- Saenger, E. H., Gold, N., and Shapiro, S. A.: Modeling the propagation of elastic waves using a modified finite-difference grid, Wave Motion, 31, 77–92, 2000.
- Sauvin, G., Lecomte, I., Bazin, S., Hansen, L., Vanneste, M., and L'Heureux, J.-S.: On the integrated use of geophysics for quick-clay mapping: the Hvittingfoss case study, Norway, J. Appl. Geophys., 106, 1–13, doi:10.1016/j.jappgeo.2014.04.001, 2014.
- 5 Scheer, W.: Geologie und Landschaftsentwicklung von Schleswig-Holstein, in: Der Untergrund von Föhr: Geologie, Grundwasser und Erdwärme; Ergebnisse des Interreg-Projektes CLI-WAT, Schriftenreihe LLUR SH - Geologie und Boden, Landesamt für Landwirtschaft, Umwelt und ländliche Räume des Landes Schleswig-Holstein, Flintbek, 11–20, 2012. Sheriff, R. E.: Factors affecting seismic amplitudes, Geophys. Prospect., 23, 125–138, 1975.
- Sheriff, R. E. and Geldart, L. P.: Exploration Seismology, Cambridge University Press, 1995. 645 Sørensen, K. I. and Auken, E .: SkyTEM - a new high-resolution helicopter transient electromagnetic system, Explor. Geophys., 35, 194-202, 2004.
 - Steeples, D. W. and Miller, R. D.: Seismic reflection methods applied to engineering, environmental, and groundwater problems, Geotechnical and Environmental Geophysics, 1, 1-30, 1990.
 - Virieux, J.: P-SV wave propagation in heterogeneous media: velocity-stress finite-difference method, Geophysics, 51, 889-901, 1986.
 - Virieux, J. and Operto, S.: An overview of full waveform inversion in exploration geophysics, Geophysics, 74, WCC1-WCC26, 2009.
- Yilmaz, Ö.: Seismic data analysis: processing, inversion, and interpretation of seismic data, 655 no. 10, in: Investigations in Geophysics, SEG Books, 2001.



Discussion Paper

Table 1. Overview of processing of P wave and SH wave seismic field data including normal move out (NMO) correction, dip move out (DMO) correction, and common midpoint (CMP) stacking.

Processing step	P wave application	SH wave application
Data load	SEG2-data load to ProMAX	SEG2-data load to ProMAX
Geometry installation	1 m bin interval	0.5 m bin interval
Vibroseis correlation	applied in the field	using individual sweep
Vertical stacking of records	applied in the field	2 fold
Quality control	kill bad traces	kill bad traces
Refraction statics	calculated from first breaks; $v_{replace} = 1600 \text{ m s}^{-1}$	not applied
Amplitude scaling	Automatic gain control (300 ms length)	Automatic gain control (200 ms length)
Fan Filtering	not applied	Low cut 350 m s ⁻¹
Deconvolution	Zero-phase spiking deconvolution (80 ms length)	not applied
Time-variant filter	Bandpass filter (36–220 Hz)	Bandpass filter (30–160 Hz)
Trace muting	Remove of noise cone	not applied
Interactive velocity analysis Residual statics correction NMO correction DMO preparation DMO correction Trace muting CMP stacking	100 m node spacing, iteratively correlation auto statics RMS velocity function, 30 % stretch mute 8 m DMO bin spacing, 24 bins average single velocity function top mute	100 m node spacing, iteratively not applied RMS velocity function, 300 % stretch mute not applied not applied not applied
Amplitude scaling	Automatic gain control (300 ms operator length)	not applied
Time-variant filter	Bandpass filter (passage window: 30–220 Hz)	not applied
Finite-Difference migration	smoothed velocity function	not applied
Time-to-depth conversion	Single velocity function from VSP	Single velocity function from VSP



Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper



Table 2. Input parameter for FD modelling. Grid size is specified by dh and FW characterizes the width of the absorbing frame.

	P wave	SH wave
Model size	1200 × 1100 nodes, dh = 0.5 m	1200 × 1100 nodes, dh = 0.5 m
Propagation time Source wavelet Boundary Receiver Seismograms sampling rate	time = 1 s, time steps dt = 5×10^{-5} s Ricker, 100 Hz central frequency, vertical force FW = 90 nodes, 6 % damping per node vertical geophone, spacing = 2 nodes every 10th time step	time = 2.5 s, time steps dt = 5×10^{-5} s Ricker, 100 Hz central frequency, <i>SH</i> wave force FW = 90 nodes, 6% damping per node horizontal (<i>SH</i>) geophone, spacing = 2 nodes every 20th time step

Discussion Pa	SED 6, 2169–2213, 2014 FD modelling to evaluate seismic field data T. Burschil et al.		
per Discussior			
n Paper	Title Abstract	Page Introduction	
	Conclusions	References	
Discus	Tables	Figures	
sion	14	►I	
Pap	•	F	
ē,	Back	Close	
Dis	Full Scre	Full Screen / Esc	
SCUSS	Printer-friendly Version		
ion F	Interactive Discussion		
Daper	C	ву	

Table 3. Seismic velocities and densities assigned to the hydrogeological input model (architecture see Fig. 8a).

Unit	$v_{\rm P} [{\rm ms^{-1}}]$	$v_{\rm S} [{\rm ms^{-1}}]$	ho [kg m ⁻³]
1	1523	335	2100
2	1934	480	2600
3	1600	335	2300
4	1830	436	2700
5	2000	500	2700
6	2300	550	2800

Discussion Pa	SED 6, 2169–2213, 2014		
per Discussior	FD mode evaluate se da T. Bursc	FD modelling to evaluate seismic field data T. Burschil et al.	
ר Paper	Title I Abstract	Page Introduction	
	Conclusions	References	
Discus	Tables	Figures	
sion		►I	
Pap		•	
θŗ	Back	Close	
Dis	Full Scre	Full Screen / Esc	
cuss	Printer-friendly Version		
ion F	Interactive Discussion		
aper	e	D Y	

Table 4. Seismic velocities and densities for refined input model (cf. Fig. 11b). Shear wave velocity was calculated according to cross-plot relation (Fig. 12).

Unit	$v_{\rm P} [{\rm ms^{-1}}]$	$v_{\rm S} [{\rm ms^{-1}}]$	ho [kg m ⁻³]
1	1600	330.74	2200
2	1700	366.37	2300
3	1900	437.62	2600
4	1600	330.74	2200
5	1700	366.37	2400
6	1750	384.18	2350
7	1800	401.99	2350
8	1700	366.37	2300
9	1750	384.18	2300
10	1800	401.99	2300
11	1850	419.81	2600
12	1900	437.62	2700
13	2100	508.88	2700
14	2300	580.13	2700



Figure 1. Overview maps with location of the island of Föhr **(a, b)**. Detail map of the seismic locations on the island of Föhr **(c)**. The profile discussed in this paper is labelled.





Figure 2. Cross section of the hydrogeological model with assigned lithologies, complied from airborne electromagnetic, borehole information, and P wave seismics (after Burschil et al., 2012a). The location of the profile is shown in Fig. 1c.





Figure 3. Acquisition geometries for (a) the P wave surveys, (b) the SH wave surveys, and (c) FD-modelling geometry simplification.

2200



Figure 4. Seismic recordings of five single *P* wave shots at different locations along the profile. The amplitude is displayed with an automatic gain control (AGC) of 150 ms.



Discussion

Paper



Figure 5. Seismic recordings of five single shear wave shots with spatial divergence correction and AGC of 300 ms applied.



ISCUSSION

Paper

Discussion Paper

Discussion Paper





Figure 7. Depth converted stack of the shear wave seismic survey with AGC of 300 m applied after time-to-depth conversion.



ISCUSSION

Paper

Discussion

Paper

Discussion Paper



Figure 8. *P* wave velocity model. **(a)** Structural units according to the hydrogeological model, numbers 1–6 mark the units listed in Table 4. **(b)** Westernmost model segment (cf. Sect. 5).





Figure 9. *P* wave shot gathers (as given in Fig. 4), modelled with the hydrogeological model and displayed with 150 ms AGC.





information (Fig. 8). Processed, time-migrated and depth-converted section of 300 single shots with 100 ms AGC.

Printer-friendly Version

Interactive Discussion

Discussion Paper





Figure 11. (a) Interpretation of measured field data, used to modify the input model. **(b)** Modified P wave velocity model. Numbers 1–14 mark the units listed in Table 4.





Figure 12. v_P/v_S cross-plot from VSP data colour-coded for different lithologies. Additionally median values, mean values, and the linear regression (LinReg) are indicated. The shear wave velocity was calculated for each *P* wave velocity with the relation resulting from the linear regression.

Printer-friendly Version

Interactive Discussion

Discussion Paper



Figure 13. Five different P wave single shots simulated with the modified input model (cf. Fig. 9). Shot gathers are displayed with 150 ms AGC.



Discussion Paper



Figure 14. FD-modelling *P* wave section resulting from the modified input model. Processed, time-migrated and depth-converted section of 300 stacked single shots with AGC of 100 ms (cf. Fig. 10).





Figure 15. Shear wave FD-modelling shot gathers resulting from the modified input model (cf. Fig. 8). Five shot gathers with 120 m spread, amplified by 300 ms AGC, are displayed.







