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An improved approach to estimate large-gradient deformation using high resolution TerraSAR-X data

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Abstract

Interferometric Synthetic Aperture Radar (InSAR) has shown unique capabilities in numerous applications for deformation monitoring. However, InSAR will lose effectiveness with large-gradient deformation due to the limitation of maximum detectable phase gra-

- dient and the phase unwrapping step of InSAR. Coalfield is the exact object providing such challenges for InSAR technique. Strong mining activities often induces large scale non-linear deformation with large gradient. This paper integrates offset tracking technique based on Corner Reflector (CR) and InSAR to overcome relevant problems. By applying offset tracking to high resolution TerraSAR-X intensity images, the coarse es-
- timation of large deformation was obtained and extracted, allowing the following InSAR processing to carry out phase unwrapping correctly. Finally, the fine estimation of deformation was done by the Persistent Scatterer InSAR (PSI) technique. The detected deformation time series indicated good root-mean-square errors (RMSE), validated by GPS in situ investigation. All InSAR data were processed in the open source software stoMPS and one in house InSAR processed.
- $_{\mbox{\tiny 15}}$ StaMPS and one in-house InSAR package.

1 Introduction

Interferometric Synthetic Aperture Radar (InSAR) measures the phase differences between two or more SAR images over vast areas with high accuracy (Bamler and Hartl, 1998; Massonnet et al., 1993). In the past 10 years, various advanced InSAR tech-

- ²⁰ niques have been developed in order to detect slow deformation over a long time span or sudden displacements due to earthquakes and so on (Berardino et al., 2002; Lanari et al., 2004; Lu et al., 2004; Hooper et al., 2004; Kampes and Usai, 1999; Bechor, 2006; Li et al., 2011; Zhu and Bamler, 2010; Bachofer et al., 2014). The wellknown methods Persistent Scatterers Interferometry (PSI) and Stanford Method for Dereistent Costterers (CteMPC), which perform analysis of "persistent costterers" pixels.
- ²⁵ Persistent Scatterer (StaMPS), which perform analysis of "persistent scatterer" pixels on a succession of time-ordered images have been employed in different fields, both



in urban and non-urban areas (Bachofer et al., 2014; Hooper et al., 2004; Liu et al., 2014; Raucoules et al., 2007a, b; Osmanoğlu et al., 2011). The interferogram time series techniques, e.g. Small BAseline Subset (SBAS), have also been proposed to estimate time-dependent deformation from InSAR data (Berardino et al., 2002; Lanari et al., 2004; Hooper, 2008). Based on a wavelet decomposition in space and a general parametrization in time, Multiscale InSAR Time Series (MInTS) focuses on unwrapped interferograms from a single viewing geometry, to measure the ground deformation

(Hetland et al., 2012).
 However exciting these developments are, InSAR techniques have some limitations
 and could not provide reliable results in some cases as expected. For instance, In-SAR loses effectiveness in areas with large-gradient deformation due to the loss of coherence (Massonnet et al., 1993; Baran et al., 2005). In addition, considering correct phase unwrapping, the maximum phase gradient should not exceed 0.5 fringes per pixel (Spagnolini, 1995; Chen and Zebker, 2000). In coalfields, these limitations stop people from obtaining the full profile of mining-induced deformation. Mining subsidence hazard map might be derived but with the maximum subsidence parameter missing.

A number of methods have been proposed to solve large-gradient deformation problems in coalfield or other similar fields and have resulted in successful achievements, e.g. combining measurements from GPS and levelling, or using existing deformation records to help InSAR phase recovery (Simons et al., 2002; Bürgmann et al., 2006). Nevertheless, InSAR has to rely on other measurements in those cases, e.g. GPS, but not being a standalone technique for deformation monitoring.

Offset tracking method has been successfully applied to several studies for mapping glaciation, mining subsidence, landslides or co-seismic fault movements (Scam-

²⁵ bos et al., 1992; Strozzi et al., 2002; Giles et al., 2009; Zhao et al., 2013). Differing from PSI, offset tracking using the SAR amplitude is not able to evaluate some error components accurately, such as DEM errors, even though the SAR amplitude is little or even not affected by the atmospheric disturbances due to an independence on the use of phase values (Raucoules et al., 2013; Singleton et al., 2014). Suggested re-



construction of displacement and extraction before unwrapping phase was performed quite well in Tehran Basin (Sadeghi et al., 2013). Unfortunately, this works only when linear deformation component dominates in the InSAR phases. Some important work with regard to precise analysis of offset tracking integrated with SBAS analysis have

- ⁵ been addressed successfully (Casu et al., 2011; Manconi and Casu, 2012). The so-called Pixel Offset (PO)-SBAS technique and relevant applications to volcanos have indicated a more correct evaluation than other techniques of mapping large deformation on the ground by satellite SAR (Manconi and Casu, 2012). Moreover, research about rapid measurements of landslides by PO approach was also well presented,
 ¹⁰ which pointed out an exciting possibility for Earth hazards early warning system (Man-
- . coni et al., 2014).

In this paper, we proposed a StaMPS/InSAR approach integrated with offset tracking method by means of Corner Reflectors (CR). On one hand, considering that SAR sensors with short wavelength could decrease the maximum Detectable Deformation

- ¹⁵ Gradient (DDG), it may be concluded that SAR images with long wavelength are more suitable for large-gradient deformation monitoring using phase measurements. In another respect, DDG might be increased by using high resolution SAR data through the much smaller pixel size. Moreover, TerraSAR-X has a much shorter revisit cycle (11 days or even shorter) than other SAR sensors, which dramatically increases the sam-
- pling rate of deformation monitoring. In this study, the approach was applied to a coal mining area by using the high resolution TerraSAR-X images and two time series of large-gradient and nonlinear deformation induced by mining excavation were extracted with centimetre-level precision validated by in situ investigation.

2 Methodology

²⁵ Offset tracking deals with offsets of two SAR images and detects the pixel change in both range and azimuth directions when the normalized cross-correlation is performed on each pixel by using a moving window (Strozzi et al., 2002). For co-registration of



images, oversampling factor of 2 was applied to the image patches to increase the estimation accuracy. By comparing the height of signal-to-noise ratio (SNR), the estimated offset with the highest SNR is selected to be the pixel offset value (Strozzi et al., 2002). The offsets are induced by two kinds of effects. The first kind is the global off-

- sets, caused by slightly different radar look angle and orbital error. The second kind is local offsets, determined by displacements in two directions. In this algorithm, only the local offsets are used. Therefore, we determined the polynomial coefficients for offsets in both range and azimuth directions over the whole image, in order to estimate and remove the disturbance of offsets caused by the difference in radar imaging geometry.
- ¹⁰ Moreover, the bilinear polynomial function determined over the whole image helps to remove the orbital offsets. In this study, only displacements in range direction was considered since mostly vertical deformation happens at the central area of a subsidence strata (He et al., 1991). In Fig. 1a, assume there is a data stack of SAR images.

$$\phi^{i}_{def,0}(k) = -\frac{4\pi}{\lambda} dis^{i}_{rg,0}(k).$$

¹⁵ $\phi_{def,0}^{i}(k)$ is the coarse estimation of deformation phase component of *k*th PS candidate on its slave image, while $dis_{rg,0}^{i}(k)$ is the coarse estimate of range displacement of *k*th PS candidate on its slave image. Meanwhile, the DInSAR phase series $\boldsymbol{\psi} = [\psi_1, \psi_2, \cdots, \psi_{N-1}]$ and cross-correlation series $\boldsymbol{\gamma} = [\gamma_1, \gamma_2, \cdots, \gamma_{N-1}]$ of each PS candidate are generated. Furthermore, ahead of residual DEM estimation, the PS candi-20 dates are firstly selected based on Eq. (2).

$$\overline{\gamma} \geq S, \overline{\gamma} = \frac{1}{N-1} \sum_{i=1}^{N-1} \gamma_i$$

 $\overline{\gamma}$ is the arithmetical average of the cross-correlation series generated from the previous step, and S is a predefined threshold.

The procedure of residual DEM estimation and PS reselection are then carried out in StaMPS (Hooper et al., 2004). StaMPS approach does not rely on any predefined



(1)

(2)

displacement model and thus is advantageous in terms of utilizing in monitoring natural phenomena. The topographic corrected phases of each reselected PS points are composed with several terms:

$$\psi_{\text{corrected}}^{i}(k) = W \left\{ \phi_{\text{def}}^{i}(k) + \phi_{\text{atm}}^{i}(k) + \phi_{\text{orb}}^{i}(k) + \phi_{\text{noise}}^{i}(k) \right\}.$$
(3)

⁵ $W\{\cdot\}$ is the wrapping operator, $\psi_{\text{corrected}}$ means the wrapped topographic corrected phase. ϕ_{def} means the deformation phase term, ϕ_{atm} means the phase contributed to atmospheric effect, ϕ_{orb} denotes the phase component that results in inaccurate orbital data, while ϕ_{noise} represents the phase contribution generated from other noise terms. In the following step, the first estimation of deformation phase component is extracted from the topographic phase:

$$\begin{split} \psi_{\text{res}}^{i}(k) &= W \left\{ \psi_{\text{corrected}}^{i}(k) - \phi_{\text{def},0}^{i}(k) \right\} \\ &= W \{ \phi_{\text{def}}^{i}(k) - \phi_{\text{def},0}^{i}(k) + \phi_{\text{atm}}^{i}(k) + \phi_{\text{orb}}^{i}(k) + \phi_{\text{noise}}^{i}(k) \}. \end{split}$$

As long as the major part of deformation phase is extracted, the wrapped residual ¹⁵ phase can be successfully unwrapped in spatial and temporal domains. Then, the coarse estimation of deformation phase is added back on the unwrapped residual phase to get the unwrapped topographic corrected phase $\phi_{res}^{i}(k)$:

$$\phi_{\text{corrected}}^{i} = \phi_{\text{res}}^{i}(k) + \phi_{\text{def},0}^{i}(k) = \phi_{\text{def}}^{i}(k) + \phi_{\text{atm}}^{i}(k) + \phi_{\text{orb}}^{i}(k) + \phi_{\text{noise}}^{i}(k).$$
(5)

In order to reconstruct the deformation series from the unwrapped topographic corrected phase, temporal and spatial domain filtering, using window 7 and 16 respectively were conducted. Since the atmosphere phase has the property of high-frequency in time and low-frequency in space, such filtering can estimate atmosphere phase. Subtracting this component from Eq. (5) leaves just ϕ_{def}^{i} and spatially uncorrelated error terms which can be modeled as noise. Using the separated ϕ_{def}^{i} , the deformation series can be generated.



(4)

3 Experiment area and SAR data

The Area Of Interest (AOI) of this study is located in Xishan coal mine, Gujiao city, Shanxi Province of China (Fig. 1b). It is the second largest coking coal mine of the world. Most of this area has large mountains with steep slopes and ravines which are mainly composed of Carboniferous, Permian sandstone, shale and Quaternary loess (Liu et al., 2013, 2014).

This area is full of trees, grasses and bushes which might bring a lot of coherence loss to InSAR observation. Heavy underground mining excavation is quite common in this coalfield inducing lots of surface deformation. According to previous study, the maximum subsidence can reach to meters in months.

Since the algorithm of offset estimation in this study is based on the intensity crosscorrelation algorithm, the quality of SAR backscatter intensity images is the primary issue we have to take into account. Metallic trihedral corner reffectors with 1 m rightangle side were employed here because of its accurate measurement of backscatter

¹⁵ coefficients along with GPS surveying (Fig. 1c and d) (Liu et al., 2014, 2013; Ye et al., 2004). Both the offset tracking and PSI are carried out on CR points and other PS candidates rather than on the whole image.

A total of 21 X-band TerraSAR-X images in strip map mode were acquired in 2012 for this study (Table 1). Most perpendicular baselines were between 3 m and 150 m, which mean they are obviously beneficial for deformation monitoring. A steep incidence angle of 26° was used to avoid strong shadow effects in this mountainous area.

4 Results and analysis

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As discussed previously, the full definition of the DDG in terms of the coherence value is defined by the wavelength and the pixel size (Baran et al., 2005). It is naturally obvious to use small looks for mapping large-gradient deformation field. Therefore, the multilook



number two was chosen in InSAR processing when single look lost most patterns. This InSAR result was then used for the comparison with the proposed novel method.

In this mountainous area full of vegetation, we are happy to see that CR could be detected on the amplitude map very clearly when the vicinity of the CR has low backscat-

⁵ ter intensities (Fig. 2b and c). Therefore, both the co-registration and offset tracking procedure were assisted by using the precise location of CR.

Inteferometric processing profiles phase changes with time as presented in Fig. 3. Dense fringes in the flattened interferograms reflect the strong deformation on the ground induced by mining activities. In terms of the intensity of deformation, it even increased sizes more fringes observed in the interferogram of SAP pair 20120519.

- increased since more fringes observed in the interferogram of SAR pair 20120518–20120529, comparing to that in April 2012. More interferograms refer to (Liu et al., 2014). Offset tracking processing was done for all adjacent pairs among 21 TerraSAR-X images (Fig. 4). The dark and blue rectangles in Fig. 2a were selected to be two test sites as two CRs, numbered as CR1 and CR2 were available in each site. By selecting
- both CRs as PS candidates, the former processing was integrated into StaMPS processing chain. Employing high-pass filter in time then low-pass filter in space, and then modelling the spatially uncorrelated error terms, the time series of deformation at each site were estimated (Fig. 5a and b). In the whole InSAR processing, we assume that deformation happens only vertically at the subsidence strata. InSAR measurements are thus projected from line-of-sight to the vertically direction.

GPS observations were made for two CRs nearly every 11 days and were used to validate the both results derived from normal InSAR and integrated InSAR (Fig. 5). Apparently, the normal InSAR is not able to deal with the detection of maximum subsidence since the large-gradient deformation exceeds the maximum DDG and will result

in phase unwrapping error. Normal offset tracking results indicate sudden subsidence signal which are attributed to strong mining excavation from April 2012 to June 2012. Since July 2012, CR2 has stabilized relatively as it did not locate in the subsidence basin centre any more. Comparing to the coarse estimated displacement series by normal offset tracking, the time series of integrated method are much smoother. When



validating the time series from integrated InSAR and GPS, impressive results with very few discrepancies – less than 5 cm at both points – are shown (Fig. 5). Such discrepancies may be induced by accurate of this approach itself, or the assumption that only vertical displacements were considered in this field. In total, this new approach detected cumulative subsidence of 2.048 m at CR1 and 2.639 m at CR2, from April to November 2012. Making the GPS observation as the truth value, the root-mean-square errors (RMSE) of time series derived by each method were reported in Table 2, which reflects the total difference of the methods with GPS measurements. The integrated InSAR approach indicates significant improvements of RMSE at both sites, comparing

¹⁰ to InSAR and offset tracking methods.

This work has evaluated the possibility of mapping large deformation by integrating offset tracking approach and PSI in the open source package StaMPS, which is available to a larger research community. More exciting works are expected if apply this approach to other SAR sensors with high resolution, which is the key parameter for the

accuracy of offset tracking approach (Jung et al., 2013). Nevertheless, CR is required in this hilly area with lots of vegetation to be a PS point for helping precise measurements, when most of other PS candidates are with low qualities. Moreover, 3-D measurements and rapid mapping ability in other proposed methodologies introduced above are also importance aspects of the future developments of our approach.

20 5 Conclusions

In this paper, the proposed offset tracking and PSI integrated approach demonstrated its capability of measuring large-gradient subsidence induced by coal mining activities where normal InSAR techniques always fail due to the DDG limitation and loss of coherence caused by heavy excavations. It was also inferred that we could benefit from high resolution SAR data and CR in the mountainous area. The important parameter of coal mining engineering, maximum subsidence (approximate 2 m in two months) was estimated in Xishan accurately by TerraSAR-X SAR data firstly. In terms



of RMSE (< 0.1), the integrated approach indicated significant improvements. Along with the Subsidence Hazard Boundary (SHB) presented in the companion paper, full profiles of a mining subsidence could be provided (Liu et al., 2014).

As a main strength, this work was done based on the open source package StaMPS which is available to a larger research community, and one in-house software which is going to be open. 3-D measurements and rapid mapping ability in other proposed methodologies introduced above are importance aspects of the future developments of our approach. Moreover, the capability of working with new SAR missions with high resolution will be the way forward of this approach.

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Table 1. The parameters of the TerraSAR-X data in this study.

Sensor characteristics	Values	
Frequency (GHz)	9.6	
Wavelength (cm)	3.1	
Polarisation	Horizontal–	
	Horizontal	
Swath width (km)	50	
Incidence angle (degree)	~ 26	
Range pixel spacing (m)	0.9	
Azimuth pixel spacing (m)	1.9	
Orbit repeat cycle (days)	11	
Precise orbit accuracy (cm)	~ 10	



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Table 2. RMSE of different approaches comparing to GPS observation.

-		Integrated InSAR	InSAR	Offset tracking
-	CR 1	0.069	1.62	0.169
	CR 2	0.032	1.77	0.109



Figure 1. (a) Flow chart of the proposed approach presenting the integration of StaMPS and offset tracking; **(b)** the study area shown on a TerraSAR-X amplitude image, taken on 15 April 2012. Approximate location of two Corner Reflectors (CR) presented by green triangles; **(c, d)** photos of CR and relevant GPS survey at this coalfield.







Figure 2. (a) Wrapped interferogram of AOI generated by TerraSAR-X images taken on 4 April 2012 and 15 April 2012, where the CR1 and CR2 locate in blue rectangle and dark rectangle, respectively; **(b, c)** a part of AOI taken from the blue rectangle area in **(a)**. The green cross locates CR1 on SAR intensity images taken on 4 April 2012 and 15 April 2012, respectively. The offset is then calculated to be 14 cm.





Figure 3. (a) flattened interferogram of SAR pair 20120404–20120415, **(b)** flattened interferogram of SAR pair 20120518–20120529. Image center coordinates: 37°53′35.51″ N, 112°07′35.25″ E. This area includes the region indicated by the blue rectangle in Fig. 2a.



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Figure 4. Interferogram pairs used in this study. Circles indicate SAR images while lines connecting them are baselines.





Figure 5. Time series of deformation derived from InSAR, offset tracking and integrated InSAR approach, with GPS validation. (a) time series at CR1; (b) time Series at CR2.