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RUSSIAN GEOLOGY AND GEOPHYSICS

Russian Geology and Geophysics 54 (2013) 181-199

www.elsevier.com/locate/rgg

# Self-consistent pressure scales based on the equations of state for ruby, diamond, MgO, B2–NaCl, as well as Au, Pt, and other metals to 4 Mbar and 3000 K

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Received 17 April 2012; accepted 14 August 2012

#### Abstract

Based on the modified formalism of Dorogokupets and Oganov (2007), we calculated the equation of state for diamond, MgO, Ag, Al, Au, Cu, Mo, Nb, Pt, Ta, and W by simultaneous optimization of the data of shock-wave experiments and ultrasonic, X-ray diffraction, dilatometric, and thermochemical measurements in the temperature range from ~100 K to the melting points and pressures of up to several Mbar, depending on the material. The obtained room-temperature isotherms were adjusted with a shift of the R1 luminescence line of ruby, which was measured simultaneously with the unit cell parameters of metals in the helium and argon pressure media. The new ruby scale is expressed as  $P(\text{GPa}) = 1870 \cdot \Delta \lambda / \lambda_0 (1 + 6 \cdot \Delta \lambda / \lambda_0)$ . It can be used for correction of room-pressure isotherms of metals, diamond, and periclase. New simultaneous measurements of the volumes of Au, Pt, MgO, and B2-NaCl were used for interrelated test of obtained equations of state and calculation of the room-pressure isotherm for B2-NaCl. Therefore, the constructed equations of state for nine metals, diamond, periclase, and B2-NaCl can be considered self-consistent and consistent with the ruby scale and are close to a thermodynamic equilibrium. The calculated *PVT* relations can be used as self-consistent pressure scales in the study of the *PVT* properties of minerals using diamond anvil cell in a wide range of temperatures and pressures.

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Keywords: equations of state; pressure scales; ruby pressure scale; diamond; Ag; Al; Au; Cu; Mo; Nb; Pt; Ta; W; MgO; B2-NaCl

### Introduction

Significant progress in study of the *PVT* properties of minerals and other materials as applied to the investigation of the Earth's core and mantle has been achieved in recent decades (Bassett, 2009; Hemley and Percy, 2010). For example, in study of perovskite to postperovskite transition and iron structures in the Earth's core, which was carried out in diamond anvil cell with laser heating, the measured temperatures exceeded 3000–5000 K at 150–350 GPa (Hirose et al., 2008; Komabayashi et al., 2008; Tateno et al., 2009, 2010). On the room-temperature isotherm, the measured pressures exceeded 560 GPa (Dubrovinsky et al., 2012; Ruoff et al., 1992). Sakai et al. (2011b) presented the results of numerous measurements of the Fe, Ni, Mo, and NaCl compressibility at

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>300 GPa. One of the most crucial problems in such studies is correct measurement of pressure. Unfortunately, there are no barometers for direct measurements in this pressure region. Therefore, pressure in diamond anvil cells is calibrated using special scales, proposed based on the equations of state (EOSs) for materials with a known dependence of pressure on volume and temperature. The EOSs for Au, Pt, MgO, and NaCl and the ruby pressure scale are most commonly used for this purpose.

Most of the EOSs for Au, Pt, MgO, and NaCl that are used as pressure scales were constructed based on the shock compression data (Al'tshuler et al., 1987; Anderson et al., 1989; Carter et al., 1971; Decker, 1971; Hixson and Fritz, 1992; Holmes et al., 1989; Jamieson et al., 1982), using the Mie–Grüneisen–Debye formalism. In this case, however, the difference in pressures determined by different scales reaches 10 GPa in the region of >100 GPa at ~2000 K (Dorogokupets and Oganov, 2007; Fei et al., 2007; Hirose et al., 2008; Shim

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et al., 2002). A choice of pressure scales depends on the experimental conditions and is determined not by strict thermodynamic approaches but by the individual preference of the research team. For example, Sakai et al. (2011a), who studied the EOS for B2-NaCl at ≤304 GPa, chose the EOS for Pt as a pressure scale. They compared the pressures calculated with four EOSs for Pt by Holmes et al. (1989), Fei et al. (2007), Dorogokupets and Oganov (2007), and Matsui et al. (2009) and concluded that the EOS with room-temperature isotherm (Matsui et al., 2009) specified by the Birch-Murnaghan equation is the best pressure scale. At the same time, Matsui et al. (2009) constructed this EOS by analysis of shock compression data and their own measurements of the platinum cell parameters at ≤1600 K and ≤42 GPa, calibrated against pressure scale based on the EOS for MgO (Matsui et al., 2000). The EOS for MgO (Matsui et al., 2000) was constructed by the methods of molecular dynamics and presented only as a table of the values of  $x = V/V_0$  as a function of pressure and temperature, up to 100 GPa and 3000 K. Its parameterization was not published, which does not permit it to be used as a pressure scale, though the pressure can be calculated from the table data, if necessary. Nevertheless, the EOSs for Pt and MgO in this case can be considered consistent with each other, but this gives rise to the question whether the EOS for MgO theoretically obtained by Matsui et al. (2000) is valid.

There are many EOSs for MgO calculated by different methods. Some of them are based only on shock compression data (Jamieson et al., 1982; Jin et al., 2010, 2011; Molodets et al., 2006); others, on results of shock wave, thermochemical, X-ray diffraction, and ultrasonic measurements (Brosh et al., 2008; Dorogokupets and Dewaele, 2007; Dorogokupets and Oganov, 2007; Garai et al., 2009; Gerya et al., 1998, 2004; Hama and Suito, 1999; Jacobs and de Jong, 2003; Jacobs and Oonk, 2000; Kennett and Jackson, 2009; Kuskov et al., 1982; Pan'kov and Kalinin, 1974; Polyakov and Kuskov, 1994; Speziale et al., 2001; Stamenkovic et al., 2012; Stixrude and Lithgow-Bertelloni, 2005; Tange et al., 2009); and in the rest, results of theoretical calculations are corrected using experimental data (Anderson and Zou, 1989; Inbar and Cohen, 1995; Isaak et al., 1990; Otero-de-la-Rosa and Luana, 2011a,b; Wu et al., 2008; Zhang and Bukowinski, 1991). There is also an EOS for MgO that was constructed only by the results of ultrasonic measurements (Spetzler, 1970). Several EOSs for MgO were obtained by X-ray diffraction (Dewaele et al., 2000; Fei, 1999; Martinez-Garcia et al., 2000; Utsumi et al., 1998). Recently, an independent EOS for MgO has been constructed (Kono et al., 2010) (i.e., without using other scales) by simultaneous measurement of sound velocity and X-ray diffraction measurements of the cell parameters at  $\leq 1650$  K and  $\leq 23.6$  GPa.

Almost all from the above-mentioned EOSs for MgO can be used as a pressure scale for measurements in diamond anvil cells or in multianvil apparatuses. However, here, as in the case of the EOS presented by Matsui et al. (2000), the question arises of which of them yields the most reliable pressure estimate. Moreover, though periclase in the B1 structure is stable up to multimegabar pressures and temperatures of several thousand degrees (Belonoshko et al., 2010; Oganov and Dorogokupets, 2003), its single crystals and polycrystalline samples differ in experimentally measured properties, as evidenced from shock compression data (Carter et al., 1971; Duffy and Ahrens, 1995; Zhang et al., 2008), results of ultrasonic measurements (Chung and Simmons, 1969; Fukui et al., 2008; Spetzler, 1970), and X-ray diffraction measurements in diamond anvil cells in the helium pressure medium ensuring quasi-hydrostatic conditions (Jacobsen et al., 2008; Speziale et al., 2001) (see Fig. 5 in (Dorogokupets, 2010)). Therefore, the EOSs for MgO cannot be chosen as a primary pressure scale.

Thus, a question arises: What can serve as a basis for constructing pressure scales? In the megabar pressure region, this is shock adiabats of metals, which can be used to calculate (with particular approximations) the metal isotherms at 0 or 300 K and correlate them with each other. At lower temperatures, the pressure can be calculated from results of simultaneous measurement of the sound velocity and X-ray diffraction. Such procedures were performed for MgO on the room-temperature isotherm (Li et al., 2006) and at higher temperatures (Kono et al., 2010). As yet, similar measurements for metals that are commonly used as pressure scales have not been carried out.

Therefore, the most logical way to obtain internally consistent pressure scales is to calculate metal isotherms at room-temperature from results of shock-wave measurements and compare them with results of independent measurements in diamond anvil cells in the same pressure region. At the same time, an opposite viewpoint was suggested by Holzapfel (2010): The EOSs for metals should be constructed on the basis of low-temperature ultrasonic measurements. In recent time, the EOSs based on thermochemical, ultrasonic, and X-ray diffraction measurements at zero pressure and on shock compression experiments at high pressures (Tange et al., 2009; Yokoo et al., 2009), i.e., without using secondary pressure scales, have again attracted considerable interest. Tange et al. (2009) argue that such EOSs solve the problem of measuring absolute pressure in diamond anvil cells at high temperatures and pressures.

Such isotherms, taken individually, do not solve the problem of consistent pressure scales. First of all, they must be compared with each other at least on the room-temperature isotherm, as was made earlier (Chijioke et al., 2005b; Dewaele et al., 2004b, 2008; Dorogokupets and Oganov, 2006, 2007), to obtain a sufficient number of statistical data. We also showed (Sokolova and Dorogokupets, 2011) that the same shock compression data (Yokoo et al., 2008, 2009) can be used to obtain several EOSs for Au, which almost do not differ in formal features but yield different pressures on isotherms.

We propose the following scheme of obtaining near-absolute (in this work we use the term "optimized") pressure scales for quasi-hydrostatic conditions (such conditions exist in diamond anvil cells with noble gases as a pressure medium as well as in high-temperature experiments with laser annealing to reduce deviatoric stress): (1) using results of thermochemical, ultrasonic, and X-ray diffraction measurements at zero pressure and of high-pressure shock wave experiments, the EOSs for diamond, periclase, Al, Cu, Nb, Mo, Ag, Ta, W, Pt, and Au are constructed by the formalism (Sokolova and Dorogokupets, 2011) with the minimum set of fitting parameters; (2) with the room-temperature isotherms obtained in the measurements (Dewaele et al., 2004a,b, 2008; Jacobsen et al., 2008; Occelli et al., 2003; Speziale et al., 2001; Takemura and Dewaele, 2008; Takemura and Singh, 2006; Tang et al., 2010), a pressure dependence of the shift of the R1 luminescence line of ruby is constructed; (3) using this calibration plot for ruby, the room-temperature isotherms of other materials are corrected; (4) new EOSs based on the corrected isotherms are constructed; and (5) the obtained EOSs are tested by independent methods.

#### Thermodynamic model

The Helmholtz free energy of metals in its classical form (Zharkov and Kalinin, 1968) is expressed as:

$$F = U_{\rm r} + E_{\rm r} (V) + F_{\rm th} (V, T) - F_{\rm th} (V, T_{\rm r}) + F_{e} (V, T) - F_{e} (V, T_{\rm r}) + F_{\rm anh} (V, T) - F_{\rm anh} (V, T_{\rm r}) , \qquad (1)$$

where  $U_r$  is reference energy,  $E_r(V)$  is the potential (cold) part of free energy on the reference isotherm  $T_r$  (which depends only on volume V),  $F_{th}(V, T)$  is the thermal part of Helmholtz free energy (which depends on volume and temperature), and  $F_e(V, T)$  and  $F_{anh}(V, T)$  are the contributions of free electrons and intrinsic anharmonicity to the free energy, respectively (which depend on V and T).

The pressure on the room-temperature isotherm is determined from the equation proposed by Holzapfel (2001, 2010):

$$P_{\rm r}(V) = 3K_0 X^{-5} (1-X) \exp[c_0 (1-X)] \cdot [1+c_2 \cdot X (1-X)], (2)$$

where  $X = (V/V_0)^{1/3}$ ,  $c_0 = -\ln(3K_0/P_{FG0})$ ,  $P_{FG0} = 1003.6 \times (nZ/V_0)^{5/3}$ ,  $K' = 3 + 2(c_0 + c_2)/3$ , V is volume (cm<sup>3</sup>/mol),  $V_0$  is volume under standard conditions (T = 298.15 K, P = 1 bar), *n* is the number of atoms in the chemical formula,  $K_0 = -V(\partial P/\partial V)_T$  is the isothermal bulk modulus (GPa) under standard conditions,  $K' = dK_0/dP$ , and Z is the atomic number.

The atomic number of elements in compounds is determined from (Knopoff, 1965):

$$Z^{2/3} = \frac{\sum n_i Z_i^{5/3}}{\sum n_i Z_i},$$
(3)

where  $n_i$  is the number of atoms *i* with atomic number  $Z_i$ , according to the chemical formula.

Equation (2) is used because it is interpolation between low pressure ( $x \ge 1$ ) and infinite-compression range (x = 0) corresponding to the Thomas–Fermi model. Therefore, it is an analog of the Debye and Einstein models, which interpolate thermodynamic functions from 0 K to high temperatures. Differentiating Eq. (2) with respect to volume yields isothermal bulk modulus  $K_T = -V(\partial P/\partial V)_T$ . Differentiating Eq. (2) with respect to volume (using numerical methods) yields energy  $E_r(V)$  in Eq. (1).

In the physics of metals, an equation proposed by Vinet et al. (1987) is widely used, which determines  $E_r(V)$ ,  $P_r(V)$ ,  $K_{T_r}(V)$ , and K' as

$$E(V) = 9K_0 V_0 \eta^{-2} \{1 - [1 - \eta (1 - y)] \exp[(1 - y) \eta]\}, \quad (4.1)$$

$$P(V) = 3K_0 y^{-2} (1 - y) \exp[(1 - y) \eta], \qquad (4.2)$$

$$K_T(V) = K_0 y^{-2} [1 + (\eta y + 1) (1 - y)] \exp[(1 - y) \eta], \qquad (4.3)$$

$$K' = \frac{1}{3} \left[ 2 + y \eta + \frac{y (1 - \eta) + 2y^2 \eta}{1 + (1 - y) (1 + y \eta)} \right], \tag{4.4}$$

where  $y = x^{1/3}$  and  $\eta = 1.5(K' - 1)$ .

As shown earlier (Dorogokupets, 2010; Dorogokupets and Dewaele, 2007), thermodynamic functions at >300 K can be calculated using the Debye or Einstein model. For a more precise calculation of entropy, let us apply the Einstein model with two characteristic temperatures and write the thermal part of Helmholtz free energy as

$$F_{\rm th}(V,T) = m_1 \operatorname{R} T \ln \left(1 - \exp \frac{-\theta_1}{T}\right) + m_2 \operatorname{R} T \ln \left(1 - \exp \frac{-\theta_2}{T}\right) - \frac{3}{2} n \operatorname{R} e_0 x^g T^2,$$
(5)

where  $\theta_1$  and  $\theta_2$  are characteristic temperatures depending on volume and temperature, which permits the intrinsic anharmonicity to be taken into account;  $x = V/V_0$ ; *n* is the number of atoms in the chemical formula of compound;  $m_1 + m_2 = 3n$ ;  $e_0$  determines the contribution of electrons to the free energy; *g* is an electronic analog of the Grüneisen parameter; and R is the gas constant.

The dependence of characteristic temperatures on volume and temperature can be expressed (Dorogokupets and Oganov, 2004) as:

$$\theta = \theta (V, T) = \theta (V) \exp\left(\frac{1}{2}aT\right) = \theta (V) \exp\left(\frac{1}{2}a_0 x^m T\right), \quad (6)$$
  
where  $a = \left(\frac{\partial \ln \theta (V, T)}{\partial T}\right)_V$  and  $m = \frac{d \ln a}{d \ln V}.$ 

For simplicity, we use one characteristic temperature in the next equations. Differentiating Eq. (5) with respect to temperature at constant volume, we obtain entropy and the thermal part of free energy:

$$S = -\left(\frac{\partial F}{\partial T}\right)_{V} = 3nR \left[ -\ln\left(1 - \exp\frac{-\theta}{T}\right) + \frac{\theta/T}{\exp(\theta/T) - 1} \times \left(1 - \frac{1}{2}a_{0}x^{m}T\right) \right] + 3nRe_{0}x^{g}T,$$

$$E_{\text{th}} = F_{\text{th}} + TS = 3nR \left[\frac{\theta}{\exp(\theta/T) - 1} \times \left(1 - \frac{1}{2}a_{0}x^{m}T\right) \right]$$
(7)

$$E_{\rm th} = F_{\rm th} + TS = 5n \,\mathrm{K} \left[ \exp(\theta/T) - 1 \,\times \left[ 1 - \frac{2}{2} \,a_0 \,x - T \right] \right] \\ + \frac{3}{2} \,n \,\mathrm{R} \,e_0 \,x^g \,T^2.$$
(8)

Differentiating Eg. (5) with respect to volume at constant temperature, we obtain thermal pressure:

$$P_{\rm th} = -\left(\frac{\partial F_{\rm th}}{\partial V}\right)_T = 3n \,\mathrm{R} \,\frac{\gamma - \frac{m}{2} \,a_0 \,x^m \,T}{V} \left[\frac{\theta}{\exp\left(\theta / T\right) - 1}\right] + \frac{3}{2} \,n \,\mathrm{R} \,e_0 \,x^g \,T^2 \,\frac{g}{V}.$$
(9)

Thus, using only the first derivatives, we obtained pressure and entropy. Differentiating Eq. (8) with respect to temperature at constant volume and Eq. (9) with respect to volume at constant temperature, we obtain isochoric heat capacity and isothermal bulk modulus:

$$C_V = \left(\frac{\partial E}{\partial T}\right)_V = 3n \operatorname{R}\left[\left(\frac{\theta}{T}\right)^2 \frac{\exp\left(\frac{\theta}{T}\right)}{\left[\exp\left(\frac{\theta}{T}\right) - 1\right]^2} \times \left(1 - \frac{1}{2} a_0 x^m T\right)^2\right]$$

$$-\frac{(1/4)(a_0 x^m)^2 T \theta}{\exp(\theta/T) - 1} + 3n \operatorname{R} e_0 x^g T, \qquad (10)$$

$$K_{T_{\text{th}}} = -V \left( \frac{\partial P_{\text{th}}}{\partial V} \right)_T = -3n \operatorname{R} \left[ \frac{\theta}{\exp(\theta/T) - 1} \times \frac{q \gamma - \gamma}{V} - \frac{\gamma \theta}{V(\exp(\theta/T) - 1)} \left( \gamma - \frac{m}{2} a_0 x^m T \right) + \frac{\gamma \theta^2 \exp(\theta/T)}{V T(\exp(\theta/T) - 1)^2} \left( \gamma - \frac{m}{2} a_0 x^m T \right) + \frac{m}{2} a_0 x^m T \frac{\theta}{V(\exp(\theta/T) - 1)} \left( \gamma - \frac{m}{2} a_0 x^m T \right) - \frac{m}{2} a_0 x^m \frac{\theta^2 \exp(\theta/T)}{V(\exp(\theta/T) - 1)^2} \left( \gamma - \frac{m}{2} a_0 x^m T \right) - \frac{m}{2} a_0 x^m T \frac{\theta(m-1)}{V(\exp(\theta/T) - 1)} - \frac{1}{2} e_0 x^g T^2 (1 - g) \frac{g}{V} \right]. \qquad (11)$$

Differentiating Eq. (11) with respect to temperature at constant volume, we obtain

$$(\partial P / \partial T)_{V} = 3nR \left[ \frac{\frac{1}{2} a_{0} x^{m} \theta (\gamma - m - \frac{1}{2} a_{0} x^{m} m T)}{V(\exp(\theta / T) - 1)} + \frac{\theta^{2} (\gamma - \frac{1}{2} a_{0} x^{m} m T) (1 - \frac{1}{2} a_{0} x^{m} T) \exp(\theta / T)}{T^{2} V(\exp(\theta / T) - 1)^{2}} + e_{0} x^{g} T \frac{g}{V} \right].$$
(12)

Now it is easy to calculate the coefficient of thermal expansion,  $\alpha = (\partial P/\partial T)_V/K_T$ ; heat capacity at constant pressure,  $C_P = C_V + \alpha^2 T V K_T$ , and adiabatic bulk modulus  $K_S = K_T + V T (\alpha K_T)^2/C_V$ , which can also be obtained by direct

experimental methods. Enthalpy and Gibbs free energy are determined from the formulas H = E + PV and G = F + PV.

The pressure on the shock adiabat is calculated by the equation from (Zharkov and Kalinin, 1968):

$$P_{H} = \frac{P(V) - \frac{\gamma}{V} [E(V) - E(V_{0})]}{1 - \gamma (1 - x) / (2x)}.$$
(13)

As seen from Eqs. (9), (11), (12), and (13), two new parameters have appeared:  $\gamma = -\left(\frac{\partial \ln \theta}{\partial \ln V}\right)_T$  and  $q = \left(\frac{\partial \ln \gamma}{\partial \ln V}\right)_T$ ,

whose dependence on volume has not been determined yet. In the previous works (Dorogokupets, 2002, 2007, 2010; Dorogokupets and Dewaele, 2007; Dorogokupets and Organov, 2003, 2006, 2007) we used the dependence  $\gamma = \gamma_{\infty} + (\gamma_0 - \gamma_{\infty}) x^{\beta}$  (Al'tshuler et al., 1987), where  $\gamma_0$  is the Grüneisen parameter under standard conditions,  $\gamma_{\infty}$  is the Grüneisen parameter on infinite compression (x = 0), and  $\beta$  is the fitting parameter. However, this equation is rather flexible. There are direct equations relating the Grüneisen parameter to volume on isotherms at 0 or 300 K. The relation on the 0 K isotherm is expressed (Burakovsky and Preston, 2004; Zharkov and Kalinin; 1968) as

$$\gamma = \frac{\frac{K'}{2} - \frac{1}{6} - \frac{t}{3} \left( 1 - \frac{P}{2K} \right)}{1 - \frac{2tP}{3K}} + \delta,$$
 (14)

where *t* can be equal to 0, 1, and 2, which corresponds to the Slater, Dugdale–MacDonald, and Zubarev–Vashchenko models, respectively, and  $\delta$  is the additive normalizing constant.

Zharkov and Kalinin (1968) obtained three variants of the EOS for metals and other materials with three fixed values of t, but we will use the latter as an fitting parameter. If t does not depend on volume and  $\delta = 0$ , then, the characteristic temperature, depending on volume, can be calculated from the simple equation:

$$\theta = \theta_0 x^{1/6} K_0^{-1/2} \left( K - 2t P/3 \right)^{1/2} , \qquad (15)$$

or by the numerical integration of Eq. (14), if  $\delta \neq 0$ . Thus, we determined all thermodynamic functions necessary to construct the EOSs. The procedure of optimization of fitting parameters is described in our previous work (Dorogokupets and Oganov, 2007).

Let us consider in more detail the correlation between the obtained relations and the shock compression data. The classical methods for calculating isotherms at 0 or 300 K and normal adiabats (isentropes) from shock-wave data are well known (Al'tshuler et al., 1987; Fortov and Lomonosov, 2010; Ruoff, 1967; Zharkov and Kalinin, 1968). The velocity of shock wave,  $U_S$  (km/s), and mass velocity of material behind the shock front,  $U_P$  (km/s), are in linear or quadratic relations:

$$U_S = a_0 + a_1 U_P$$
 or  $U_S = a_0 + a_1 U_P + a_2 U_P^2$ . (16)

The pressure (GPa) and volume on the shock adiabat are determined from the equations ( $c_0$  in g/cm<sup>3</sup>):

$$P_H = \rho_0 U_P U_S, \ x = \rho_0 / \rho = V / V_0 = (U_S - U_P) / U_S.$$
(17)

Coefficients  $a_0$  and  $a_1$  in Eq. (13) are related to adiabatic bulk modulus  $K_{So}$  and its pressure derivative (Al'tshuler et al., 1987; Ruoff, 1967; Zharkov and Kalinin, 1968) as follows:

$$K_{S} = \rho_{0} a_{0}^{2}, \ (\partial K_{S} / \partial P)_{S} = 4a_{1} - 1.$$
(18)

Here the problem arises: How can we find parameters  $K_0$  and K' determining the room-temperature isotherm from the known shock adiabat parameters under standard conditions, Eq. (16)? Parameters  $K_0$  and  $K_{So}$  are related to each other by the equation  $K_S = K_T + VT(\alpha K_T)^2/C_V$ , which can also be expressed as  $\frac{1}{K_S} = \frac{1}{K_T} - \frac{\alpha^2 VT}{C_P}$ . The coefficient of thermal expansion, volume, and heat capacity at constant pressure under standard conditions are known for most materials; therefore, it is not difficult to calculate  $K_0$  from  $K_S$ , which can be obtained from ultrasonic measurements.

To obtain *K'* consistent with  $(\partial K_S / \partial P)_S$  from the shock compression data, let us use the relation (Ruoff, 1967)

$$(\partial K_S / \partial P)_S = (\partial K_S / \partial P)_T + \gamma (\partial \ln K_S / \partial \ln T)_P.$$
(19)

All the above relations can be calculated from our EOS. Earlier we optimized the above system of equations so that the shock pressure and calculated value of  $(\partial K_S / \partial P)_S$  would be consistent with shock adiabat in Eq. (13) and Eqs. (16)–(18) (Dorogokupets and Sokolova, 2011; Sokolova and Dorogokupets, 2011). But this approximation is too strict because the shock adiabat can also be expressed via quadratic relation in Eq. (16). Therefore, in this work we refused this approximation and used a smooth adiabat calculated from Eqs. (16) and (17) and a shock pressure estimated from Eq. (13).

# The equations of state based on results of thermochemical, ultrasonic, and X-ray diffraction measurements and shock compression data

Parameter  $a_0$  in Eq. (16) was calculated based on the most reliable and generally accepted values of  $K_{S_0}$  obtained in

Table 1. Input parameters of shock adiabats of studied materials

ultrasonic measurements (Table 1), which made it possible to correlate them with the shock compression data for standard conditions. Using the shock compression database (Levashov et al., 2004) and data of later measurements (Yokoo et al., 2008, 2009; Zhang et al., 2008), we again calculated  $a_1$  in Eq. (16). Both parameters were invoked to calculate the smooth adiabats used for optimization. The accepted values of  $a_0$  and  $a_1$ , adiabatic bulk modulus, and its pressure derivative as well as the reference values of volume, density, and atomic number are listed in Table 1.

The optimization parameters of the EOSs in thermochemical, ultrasonic, and X-ray diffraction measurements and the shock compression data are listed in Tables 2 and 3. Optimization was made by two models. In the first model, the room-temperature isotherm was specified by Eq. (2) (Holzapfel, 2001, 2010) (Table 2), and in the second, by Eq. (4.2) (Vinet et al., 1987) (Table 3). The models show no significant difference, but the second yields higher values of K'. Both models smooth the measured isobaric heat capacity at  $\geq 100$  K; therefore, the calculated standard entropy is close to the reference values. It is remarkable that one of the characteristic temperatures is close to the Debye temperature, whereas the other is usually twice as low. The tables present the values of parameters  $(\partial K_S / \partial P)_T$  and  $(\partial K_S / \partial P)_S$  calculated from our EOSs. They are not always close to the values obtained from the shock compression data (Table 1). This evidences that the velocities are usually related to each other by quadratic rather than linear equations. The degree of consistence of the calculated thermodynamic functions with the experimental data obtained for the studied materials by the first model using Eq. (2) (Holzapfel, 2001, 2010) was considered by Dorogokupets et al. (2012). Figure 1 shows the calculated thermodynamic functions of periclase in comparison with the results of direct experimental measurements. The second model using Eq. (4.2) (Vinet et al., 1987) yields nearly the same degree of consistence.

As seen from the example with periclase (Fig. 1), we described rather accurately all major thermodynamic functions, using a simple EOS with the minimum set of fitting parameters. Now it is necessary to reduce the EOSs for metals and compounds, otherwise any of them can be considered absolute. We will do this first of all on the room-temperature

| Parameters                      | С     | MgO    | Al    | Cu    | Nb     | Мо     | Ag     | Та     | W     | Pt    | Au     |
|---------------------------------|-------|--------|-------|-------|--------|--------|--------|--------|-------|-------|--------|
| $V_0$ , cm <sup>3</sup> /mole   | 3.414 | 11.248 | 9.98  | 7.112 | 10.828 | 9.369  | 10.25  | 10.861 | 9.552 | 9.091 | 10.215 |
| $\rho_0$ , g/cm <sup>3</sup>    | 3.518 | 3.583  | 2.704 | 8.935 | 8.58   | 10.240 | 10.524 | 16.66  | 19.25 | 21.46 | 19.282 |
| <i>a</i> <sub>0</sub> , km/s    | 11.21 | 6.733  | 5.295 | 3.923 | 4.48   | 5.05   | 3.14   | 3.40   | 4.01  | 3.62  | 2.995  |
| $a_1$                           | 1.20  | 1.30   | 1.361 | 1.506 | 1.18   | 1.27   | 1.645  | 1.25   | 1.262 | 1.543 | 1.653  |
| <i>a</i> <sub>2</sub> , km/s    | -     | -      | -     | -     | -      | -      | -      | -      | -     | -     | -0.013 |
| K <sub>S0</sub> , GPa           | 442.0 | 162.5  | 75.9  | 137.4 | 172.1  | 261.7  | 103.9  | 193.0  | 309.7 | 281.2 | 173.0  |
| $(\partial K_S / \partial P)_S$ | 3.80  | 4.20   | 4.44  | 5.02  | 3.74   | 4.08   | 5.58   | 4.0    | 4.05  | 5.17  | 5.61   |
| Ζ                               | 6     | 10.34  | 13    | 29    | 41     | 42     | 47     | 73     | 74    | 78    | 79     |

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Table 2. Parameters of the equations of state, optimizing results of thermochemical, ultrasonic, and X-ray measurements and shock compression data.

| Parameter                       | С      | MgO    | Al     | Cu    | Nb     | Мо     | Ag    | Та     | W      | Pt     | Au     |
|---------------------------------|--------|--------|--------|-------|--------|--------|-------|--------|--------|--------|--------|
| K <sub>0</sub> , GPa            | 441.5  | 160.3  | 72.8   | 133.5 | 170.5  | 260.0  | 100.0 | 191.0  | 308.0  | 275.3  | 167.0  |
| Κ'                              | 3.98   | 4.23   | 4.56   | 5.27  | 3.63   | 4.17   | 6.16  | 3.91   | 4.10   | 5.21   | 5.79   |
| $(\partial K_S / \partial P)_T$ | 3.977  | 4.20   | 4.40   | 5.24  | 3.61   | 4.15   | 6.12  | 3.89   | 4.08   | 5.15   | 5.67   |
| $(\partial K_S / \partial P)_S$ | 3.973  | 4.16   | 4.26   | 5.14  | 3.58   | 4.12   | 5.97  | 3.86   | 4.06   | 5.07   | 5.54   |
| θ <sub>10</sub> , K             | 1560   | 749    | 381    | 298   | 296    | 369    | 197   | 235    | 310    | 163    | 176    |
| $m_1$                           | 2.437  | 3      | 1.5    | 1.5   | 1.5    | 1.5    | 1.5   | 1.5    | 1.5    | 1.5    | 1.5    |
| θ <sub>20</sub> , Κ             | 684    | 401    | 202    | 168   | 136    | 213    | 115   | 109    | 172    | 153    | 84.5   |
| <i>m</i> <sub>2</sub>           | 0.563  | 3      | 1.5    | 1.5   | 1.5    | 1.5    | 1.5   | 1.5    | 1.5    | 1.5    | 1.5    |
| t                               | 1.140  | 0.555  | -0.861 | 1.417 | -0.829 | -0.655 | 2.253 | -0.279 | -0.564 | -0.890 | -0.512 |
| δ                               | -0.537 | -0.226 | -0.247 | 0     | -0.354 | -0.686 | 0.175 | -0.205 | -0.642 | 0      | 0      |
| $a_0 (10^{-6} \text{ K}^{-1})$  | _      | 14.6   | _      | -     | -      | -      | -     | _      | -      | -      | _      |
| m                               | _      | 5.3    | -      | -     | _      | _      | -     | _      | -      | -      | -      |
| $e_0 (10^{-6} \text{ K}^{-1})$  | 0      | -      | 64.1   | 27.7  | 114.6  | 143.1  | 17.6  | 80.7   | 100.3  | 75.5   | 0      |
| g                               | -      | -      | 0.66   | 0.66  | 0.98   | 2.65   | 0.62  | 0.2    | 2.70   | 0.32   | -      |

Note. Isotherm at 300 K is specified by Eq. (2) (Holzapfel, 2001, 2010).

Table 3. Parameters of the equations of state, optimizing results of thermochemical, ultrasonic, and X-ray measurements and shock compression data.

| Parameter                       | С      | MgO    | Al     | Cu    | Nb     | Mo     | Ag    | Та     | W      | Pt     | Au    |
|---------------------------------|--------|--------|--------|-------|--------|--------|-------|--------|--------|--------|-------|
| K <sub>0</sub> , GPa            | 441.5  | 160.3  | 72.8   | 133.5 | 170.5  | 260.0  | 100.0 | 191.0  | 308.0  | 275.3  | 167.0 |
| Κ'                              | 4.00   | 4.38   | 4.70   | 5.44  | 3.77   | 4.32   | 6.02  | 4.08   | 4.25   | 5.28   | 5.81  |
| $(\partial K_S / \partial P)_T$ | 3.99   | 4.35   | 4.55   | 5.41  | 3.75   | 4.29   | 5.99  | 4.06   | 4.23   | 5.23   | 5.71  |
| $(\partial K_S / \partial P)_S$ | 3.99   | 4.31   | 4.40   | 5.31  | 3.72   | 4.26   | 5.86  | 4.03   | 4.21   | 5.16   | 5.58  |
| θ <sub>10</sub> , K             | 1549   | 747    | 380    | 297   | 305    | 419    | 201   | 247    | 313    | 169    | 179   |
| $m_1$                           | 2.468  | 3      | 1.5    | 1.5   | 1.5    | 1.5    | 1.5   | 1.5    | 1.5    | 1.5    | 1.5   |
| θ <sub>20</sub> , Κ             | 669    | 401    | 202    | 168   | 132    | 190    | 116   | 104    | 169    | 150    | 83.5  |
| <i>m</i> <sub>2</sub>           | 0.532  | 3      | 1.5    | 1.5   | 1.5    | 1.5    | 1.5   | 1.5    | 1.5    | 1.5    | 1.5   |
| t                               | 1.367  | 1.064  | -0.451 | 2.172 | -0.171 | -0.342 | 2.722 | 0.330  | -0.259 | -0.102 | 0.164 |
| δ                               | -0.470 | -0.165 | -0.182 | 0.136 | -0.183 | -0.512 | 0.442 | -0.073 | -0.557 | 0.278  | 0.254 |
| $a_0 (10^{-6} \text{ K}^{-1})$  | _      | 16.5   | _      | -     | _      | _      | _     | _      | _      | -      | -     |
| m                               | _      | 4.96   | _      | _     | _      | _      | _     | _      | _      | _      | -     |
| $e_0 (10^{-6} \text{ K}^{-1})$  | 0      | _      | 64.1   | 27.7  | 116.5  | 150.4  | 19.2  | 82.1   | 104.3  | 78.5   | 0     |
| g                               | _      | _      | 0.61   | 2.27  | 0.89   | 1.94   | 0.56  | 0.100  | 2.29   | 0.26   | -     |

Note. Isotherm at 300 K is specified by Eq. (4.2) (Vinet et al., 1987).

isotherm by calibrating the ruby pressure scale against the room-temperature isotherms from Tables 2 and 3.

### Calibration of the ruby pressure scale against the equations of state for other materials

In recent decade, the cell parameters of the considered materials and the shift of the R1 luminescence line of ruby have been measured in diamond anvil cells in the helium pressure medium. As shown by Takemura (2001), using helium as a pressure medium ensures a hydrostatic pressure of at least 50 GPa, and at higher pressures, helium ensures quasi-hydrostatic conditions (Dewaele et al., 2004a,b, 2008; Klotz et al., 2009; Occelli et al., 2003). This problem was reviewed in detail by Syassen (2008).

The ruby pressure scale was repeatedly calibrated under nonhydrostatic conditions (Mao et al., 1978), in the argon (Mao et al., 1986) and helium pressure media (Aleksandrov et al., 1987; Chijioke et al., 2005b; Dewaele et al., 2004b, 2008; Dorogokupets and Oganov, 2003, 2006, 2007; Jacobsen et al., 2008; Holzapfel, 2003; Silvera et al., 2007; Syassen, 2008). Our new calibration of the ruby pressure scale is based on the EOSs for materials that were constructed using the

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Fig. 1. Thermodynamic functions of MgO (solid lines). (*a*) Calculated heat capacity (isobaric and isochoric) in comparison with selected reference and experimental data. (*b*) Calculated bulk moduli (isothermal ( $K_T$ ) and adiabatic ( $K_S$ )) in comparison with that from ultrasonic measurements. (*c*) Calculated coefficient of volumetric thermal expansion in comparison with experimental data. (*d*) Calculated shock compression adiabat in comparison with experimental data. Thin line is a room-temperature isotherm constructed from the parameters in Table 2.

same formalism with thermochemical, ultrasonic, and X-ray diffraction measurements at zero pressure as well as shock compression data at high pressures. It is expressed as

$$P (\text{GPa}) = 1870 \,\frac{\Delta \lambda}{\lambda_0} \left( 1 + 6.0 \,\frac{\Delta \lambda}{\lambda_0} \right), \tag{20}$$

where  $\lambda_0 = 694.24$  nm.

This scale is based on the EOSs for 11 materials and averages the scales obtained by the equations of Holzapfel (2001, 2010) and Vinet et al. (1987). It was described in detail earlier (Dorogokupets et al., 2012). The comparison between the modern ruby scales and the scale proposed by Mao et al. (1986) shows that at 150 GPa, the latter scale underestimates pressure by 10–15 GPa (Fig. 2).

Let us correct the room-temperature isotherms with the ruby scale (Eq. 20) and again consider the EOSs for the studied materials. This is necessary because the shock adiabat does not correspond to equilibrium thermodynamic functions (Zharkov and Kalinin, 1968 (section 5.1); Holzapfel, 2010 (section 11)). Among our isotherms, there are probably ones

close to the equilibrium isotherms as well as nonequilibrium ones. Therefore, the ruby pressure scale averages the roomtemperature isotherms of studied materials, based on the results of thermochemical, ultrasonic, and X-ray diffraction measurements at zero pressure and shock compression measurements at high pressures.

## The optimized equations of state under quasi-hydrostatic conditions

The parameters of the optimized EOSs are presented in Table 4. They were obtained as follows. First, the room-temperature isotherms were corrected with the ruby scale by Eq. (20). Then, optimization of the results of thermochemical, ultrasonic, and X-ray diffraction measurements and shock compression data was repeated for the fixed room-temperature isotherms ( $K_0$  and K' for (2) (Holzapfel, 2001)). This procedure was performed for all studied materials, but the EOSs for Au, Pt, and MgO were studied in more detail because they



Fig. 2. Difference between the recent calibrations of the ruby pressure scales (P) and the classic ruby pressure scale (Mao et al., 1986) ( $P_{Mao}$ ). Pressure was calculated from the parameters in the original work by Mao and by Eq. (20).

are the most demanded pressure scales for experiments in high-pressure multianvil apparatuses.

The difference between the ruby pressure scale and the corrected room-temperature isotherms is shown in Fig. 3. A comparison shows that the pressures of almost all studied materials are characterized by a  $\sim 2\%$  deviation in the region of quasi-hydrostatic compression. The only exclusion is gold. In the region of hydrostatic compression (<50 GPa), the pressure deviation is most often >2%. The 1.5 GPa deviations for Al, Mo, and Ta in the pressure region of  $\sim 30$  GPa are unexpected and call for additional experimental analysis.

Verification of the equations of state by the independent determination

The EOSs for MgO, Au, and Pt have been the most widely discussed as possible pressure scales in the recent decade. We have already performed their optimization (Dorogokupets and Dewaele, 2007; Dorogokupets and Oganov, 2006, 2007). The proposed approach to the construction of EOSs and the published new data of simultaneous measurements of the volume of these materials (Dewaele et al., 2008; Hirose et al., 2008; Komabayashi et al., 2008; Kono et al., 2010; Matsui et

Table 4. Optimized parameters of the equations of state

| Parameter                           | С      | MgO    | Al     | Cu    | Nb     | Mo     | Ag    | Та     | W      | Pt     | Au    |
|-------------------------------------|--------|--------|--------|-------|--------|--------|-------|--------|--------|--------|-------|
| K <sub>0</sub> , GPa                | 441.5  | 160.3  | 72.8   | 133.5 | 170.5  | 260.0  | 100.0 | 191.0  | 308.0  | 275.0  | 167.0 |
| Κ'                                  | 3.90   | 4.10   | 4.51   | 5.32  | 3.65   | 4.20   | 6.15  | 3.83   | 4.12   | 5.35   | 5.90  |
| $(\partial K_S / \partial P)_T$     | 3.90   | 4.07   | 4.35   | 5.28  | 3.62   | 4.17   | 6.10  | 3.81   | 4.10   | 5.29   | 5.81  |
| $(\partial K_S / \partial P)_S$     | 3.89   | 4.03   | 4.21   | 5.18  | 3.60   | 4.15   | 5.96  | 3.79   | 4.08   | 5.22   | 5.68  |
| $\theta_{10}, K$                    | 1561   | 748    | 381    | 296   | 302    | 353    | 199   | 254    | 309    | 177    | 179.5 |
| $m_1$                               | 2.436  | 3      | 1.5    | 1.5   | 1.5    | 1.5    | 1.5   | 1.5    | 1.5    | 1.5    | 1.5   |
| $\theta_{20}, K$                    | 684    | 401    | 202    | 169   | 134    | 222    | 115   | 101    | 172    | 143    | 83.0  |
| <i>m</i> <sub>2</sub>               | 0.564  | 3      | 1.5    | 1.5   | 1.5    | 1.5    | 1.5   | 1.5    | 1.5    | 1.5    | 1.5   |
| t                                   | 1.085  | 0.301  | -0.958 | 1.401 | -0.763 | -0.791 | 2.210 | -0.148 | -0.591 | -0.343 | 0.087 |
| δ                                   | -0.506 | -0.235 | -0.242 | -0.07 | -0.326 | -0.802 | 0.178 | -0.101 | -0.686 | 0.167  | 0.134 |
| $a_0 (10^{-6} \text{ K}^{-1})$      | -      | 17.4   | -      | -     | -      | -      | -     | -      | -      | -      | -     |
| m                                   | -      | 4.95   | -      | -     | -      | -      | -     | -      | -      | -      | -     |
| $e_0 \ (10^{-6} \ \mathrm{K}^{-1})$ | _      | _      | 64.1   | 27.7  | 115.9  | 143.2  | 22.1  | 82.3   | 100.1  | 80.6   | -     |
| g                                   | _      | _      | 0.33   | 2.18  | 0.90   | 2.66   | 0.19  | 0.12   | 2.77   | 0.06   | -     |

Note. Parameters  $K_0$  and K' are given for Eq. (2).



Fig. 3. Difference between the pressure calculated with the ruby scale ( $P_{\text{ruby}}$ , Eq. (20)) and the pressure on the room-temperature isotherm of metals, diamond, and periclase ( $P_M$ ) calculated from the parameters in Table 4. The ratios between  $\Delta \lambda / \lambda_0$  and  $x = V/V_0$  were obtained in experiments in the argon pressure medium (Tang et al., 2010) and in the helium pressure medium (other works).

al., 2009; Takemura and Dewaele, 2008; Sakai et al., 2011a; Sata et al., 2010; Ueda et al., 2008; Yokoo et al., 2008, 2009) permit their correction for better consistency with each other.

This procedure was performed as follows. We compiled a database of simultaneous measurements of the MgO, Au, and Pt volumes on the room-temperature isotherm and at elevated temperatures, introduced them into our EOSs, and inserted the

relations between Excel tables with different EOSs. Unfortunately, this database is not full because the results of many measurements were published only graphically (Dubrovinsky et al., 2010; Fei et al., 2007). Then we calculated the difference between the pressures that yield different EOSs: first, for those on the room-temperature isotherms, and then, for those at high temperatures. Variation in K' values is accompanied by



Fig. 4. Difference between the pressures measured in diamond anvil cells in the helium pressure medium (He) (Jacobsen et al., 2008; Speziale et al., 2001) and then recalculated using a ruby pressure scale (Eq. (20)) and the room-temperature isotherm of MgO (the parameters in Table 4). Lines show the difference between the room-temperature isotherms of MgO obtained with the EOSs from the above works and with our EOS (Table 4). DD-07 and DO-07 are the EOSs for MgO proposed by Dorogokupets and Dewaele (2007) and Dorogokupets and Oganov (2007), respectively.



Fig. 5. Difference (in %) between the measured ( $K_{S \text{ obs}}$ ) (Kono et al., 2010) and calculated ( $K_{S \text{ cal}}$ ) (by our EOS (Table 4)) adiabatic bulk moduli of MgO. Measurements in other mentioned works were performed on the room-temperature isotherm.

changes in the relations between the EOSs. At high pressures (>300 GPa), the obtained EOSs for MgO, Au, and Pt were tested by simultaneous measurements of the volumes of these materials and B2–NaCl. As an initial approximation, we took our previous data (Dorogokupets and Dewaele, 2007; Dorogokupets and Oganov, 2006, 2007).

The room-temperature isotherm of MgO agrees with the results of measurements in the helium pressure medium (Jacobsen et al., 2008) (Fig. 4). Up to 100 GPa, it is consistent



Fig. 6. Difference between the pressures determined from the EOS proposed by Kono et al. (2010) ( $P_{obs}$ ) and our EOS for MgO ( $P_{cal}$ ).

only with the EOSs proposed by Jin et al. (2010) and Matsui et al. (2000). Other modern EOSs yield much higher pressures and agree with the results of measurements by Speziale et al. (2001).

Recently, Kono et al. (2010) have obtained an EOS for MgO by simultaneous measurement of sound velocities and X-ray diffraction, without using other scales. Similar procedures were earlier performed by Li et al. (2006) and Zha et al. (2000). Therefore, it was important to obtain an EOS for MgO which would be consistent with the results of not only PVT but also direct ultrasonic measurements of the adiabatic bulk modulus.

The difference between the measured adiabatic bulk moduli of MgO and those calculated by the proposed EOS (Table 4) is shown in Fig. 5, and the difference between the pressures from (Kono et al., 2010, Table 1) and our calculated pressures, in Fig. 6. It is seen that our EOS for MgO approximates (with a reasonable accuracy) the results of ultrasonic measurements of the adiabatic bulk modulus. The systematic discordance between the pressures in the measurements by Kono et al. (2010) (Fig. 6) might point out the nonhydrostatic conditions. This is confirmed (Kono et al., 2010; Fig. 8) by the fact that the calculated thermal expansion of MgO disagrees with the direct measurements of the MgO volume (Dubrovinsky and Saxena, 1997; Fiquet et al., 1999) at high temperatures and 1 bar. In general, the calculated adiabatic bulk modulus agrees with the experimental one within 2%, though the discordance between these moduli in the experiments carried out by Zha et al. (2000) reaches 6%.

In Fig. 7, comparison of the EOSs for MgO and Au at  $\leq$ 30 GPa and  $\leq$ 2173 K is made. Most of the *PVT* points calculated from the EOSs for MgO and Au agree with each other within ±0.5 GPa, and almost all of them are in the



O 1273–2173 K (Fei et al., 2004a) □ 300–2000 K (Oguri et al., 2000) ▲ 1473–1773 K (Inoue et al., 2006) × 1873 K (Matsui and Nishiyama, 2002) + 1273–1873 K (Litasov et al., 2005) × 1673–2173 K (Fei et al., 2004b) ■ 300–473 K (Litasov et al., 2010) ■ 673–873 K (Litasov et al., 2010) ■ 1473–1673 K (Litasov et al., 2010)

Fig. 7. Difference between the pressures obtained from our EOSs for MgO and Au, calculated from the results of simultaneous measurements of their cell parameters at the given temperature.



Fig. 8. Difference in pressure between our EOSs for MgO and Au and the EOS for Pt, calculated from the results of simultaneous measurements of the MgO–Pt and Au–Pt cell parameters on the room-temperature isotherm borrowed from literature. Also, the difference between the EOSs for Pt from (Chijioke et al., 2005a; Dorogokupets and Dewaele, 2007; Dorogokupets and Oganov, 2007; Holmes et al., 1989; Jamieson et al., 1982; Jin et al., 2011) and our EOS for Pt is shown.

variation interval of  $\pm 1$  GPa. However, the EOSs for MgO and Au differ by >1 GPa at 1873 K (Matsui and Nishiyama, 2002).

Comparison of the EOSs for MgO, Au, and Pt on the room-temperature isotherm at  $\leq 200$  GPa is shown in Fig. 8. Our isotherm of Pt agrees with the isotherms of other researchers (Chijioke et al., 2005a; Jamieson et al., 1982; Jin

et al., 2011; Holmes et al., 1989) and significantly exceeds our earlier estimates (Dorogokupets and Dewaele, 2007; Dorogokupets and Oganov, 2007) based on nonhydrostatic measurements (Akahama et al., 2002). At high temperatures, the difference in pressures estimated from the EOSs for MgO, Au, and Pt does not exceed 3 GPa, which is close to the error of determination (Fig. 9).



Fig. 9. Difference in pressure between our EOSs for MgO and Au and the EOS for Pt, calculated from the results of simultaneous measurements of the MgO–Pt and Au–Pt cell parameters at high temperatures. Also, the difference between the EOSs for Pt from (Dorogokupets and Dewaele, 2007; Dorogokupets and Oganov, 2007; Jin et al., 2011; Matsui et al., 2009; Sun et al., 2008) and our EOS for Pt is shown.

#### The B2-NaCl isotherm at 300 K

Results of simultaneous measurements of the volumes of Au, Pt, MgO, and B2-NaCl were published elsewhere (Hirose et al., 2008; Komabayashi et al., 2008; Ono et al., 2006; Sakai et al., 2011a; Sata et al., 2002, 2010; Ueda et al., 2008). They can be used to calculate an isotherm for B2-NaCl at 300 K and verify the EOSs for Au, Pt, and MgO obtained at >300 GPa. Figure 10 shows the compression curve for

B2-NaCl in comparison with direct experimental data recalculated by our EOSs. The data of Heinz and Jeanloz (1984b) are based on the ruby pressure scale (Mao et al., 1978), but laser heating was used to reduce deviatoric stress (which is consistent with the data of other researchers) in only one measurement. The EOS for B2-NaCl (Ueda et al., 2008) agrees with our previous estimates (Dorogokupets and Dewaele, 2007), but they significantly underestimate pressure at >100 GPa.



Fig. 10. NaCl compressibility curve on the room-temperature isotherm. Original experimental data were recalculated using our MgO, Pt, Au (Table 4), and hcp-Fe (Dorogokupets et al., 2012) pressure scales. Line is the B2-NaCl isotherm calculated by Eq. (2) with parameters  $V_0 = 40.351$  Å<sup>3</sup>,  $K_0 = 30.2$  GPa, and K' = 5.15. The error bars for volumes determined by Sakai et al. (2011a,b) are given. Mao-78 is the scale proposed by Mao et al. (1978).



Fig. 11. Difference between the smoothed B2-NaCl isotherm at room-temperature (Fig. 10) and MgO, Pt, Au (Table 4), and hcp-Fe (Dorogokupets et al., 2012) pressure scales, according to the results of measurements from the above-mentioned references. Mao-78 is the scale proposed by Mao et al. (1978). 3%—line of 3% deviation of calculated data.

Figure 11 is the key to verify the room-temperature isotherms for Au, Pt, and MgO, whose parameters are listed in Table 4. The difference in pressure according to the platinum scale (Sakai et al., 2011b) reaches  $\pm 5$  GPa, but most of the pressures differ within  $\pm 2$  GPa. The gold scale yields a somewhat smaller difference, but it cannot be verified by the ruby scale at >150 GPa because of lack of experimental data. As seen from the figure, the results of almost all measurements made after stress relieving (by the gas pressure medium or laser heating) agree within 3%.

Independent verification of the EOSs for Au, Pt, and B2-NaCl can be made by a simultaneous measurement of sound velocities in B2-NaCl, the volumes of Au, Pt, and B2-NaCl, and the shift of the R1 luminescence line of ruby. Lakshtanov et al. (2005) reported such measurements at 35–73 GPa, but their data have not been published yet.

#### Independent comparison with other pressure scales

Recently, Dorfman et al. (2012) have published results of comparison of the Au, Pt, Mo, MgO, and B2–NaCl pressure scales up to 265 GPa for the room-temperature isotherm. They made a simultaneous measurement of the volumes of Au and NaCl, MgO and NaCl, Mo and MgO, Pt and MgO, Pt and MaCl, and Pt:NaCl and MgO in diamond anvil cells in the Ne and He pressure media. Therefore, it is of great interest to compare our EOSs with the independent measurements by Dorfman et al. (2012). Figure 12 shows a difference between the pressure calculated from the equation of state proposed by Dorfman et al. (2012) and the pressure calculated from the parameters presented in Table 4. These EOSs are in good agreement, but Dorfman et al. (2012) considerably expanded the pressure range as compared with the previous measurements. Using these data, we can correct our EOSs for MgO,

Au, and Mo. The parameters of the corrected EOSs are as follows: MgO— $K_0 = 160.3$  GPa, K' = 4.25,  $\theta_{10} = 748$  K,  $\theta_{20} = 401$  K, t = 0.583,  $\delta = -0.25$ ,  $a_0 = 17.4 \times 10^{-6}$  K<sup>-1</sup>, m = 5.5; Au— $K_0 = 167.0$  GPa, K' = 5.75,  $\theta_{10} = 176$  K,  $\theta_{20} = 84$  K, t = -0.463,  $\delta = 0.045$ ; and Mo— $K_0 = 260.5$  GPa, K' = 4.05,  $\theta_{10} = 356$  K,  $\theta_{20} = 218$  K, t = -0.735,  $\delta = -0.755$ ,  $e_0 = 123.9 \times 10^{-6}$  K<sup>-1</sup>, g = 3.5. We recommend the following parameters for the room-temperature isotherm of B2–NaCl:  $V_0 = 41.00$  Å<sup>3</sup>,  $K_0 = 27.6$  GPa, K' = 5.31,  $c_0 = 2.768$  (for Eq. (2)).

Tables 5, 7, and 9 present thermodynamic functions of MgO, Mo, and Au, which were calculated from the corrected parameters of the EOS based on data by Dorfman et al. (2012). They were tabulated against temperature at zero pressure, at 100 GPa, and on compression,  $x = V/V_0$  of up to 0.6. The tables present the calculated coefficient of volumetric thermal



Fig. 12. Difference between the pressures calculated by the pressure scales from Dorfman et al. (2012) and the pressured calculated by the EOSs for MgO, Pt, Au, and B2–NaCl from Table 4.

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Table 5. Thermodynamic functions of MgO at different pressures and temperatures, calculated using the EOS of MgO corrected by the data from Dorfman et al. (2012) (see the text).

| P, GPa  | <i>Т</i> , К | $x = V/V_0$ | $\alpha$ E-6, K <sup>-1</sup> | S, J mole <sup>-1</sup> K <sup>-1</sup> | $C_P$ , J mole <sup>-1</sup> K <sup>-1</sup> | $C_V$ , J mole <sup>-1</sup> K <sup>-1</sup> | KT, GPa | Ks, GPa | $\gamma_{\rm th}$ | K'   | $\Delta G$ , kJ mole <sup>-1</sup> |
|---------|--------------|-------------|-------------------------------|---|--|--|---------|---------|-------------------|------|------------------------------------|
| 0       | 298.15       | 1           | 30.38                         | 26.90                                   | 36.95  | 36.45  | 160.30  | 162.48  | 1.502             | 4.25 | 0.000                              |
| 0       | 500          | 1.00705     | 37.93                         | 48.43                                   | 45.45  | 44.19  | 154.80  | 159.22  | 1.505             | 4.29 | -7.716                             |
| 0       | 1000         | 1.02828     | 44.59                         | 82.08                                   | 51.01  | 47.78  | 140.31  | 149.78  | 1.514             | 4.40 | -41.153                            |
| 0       | 2000         | 1.08025     | 54.28                         | 118.91                                  | 55.51  | 47.60  | 110.44  | 128.78  | 1.530             | 4.73 | -143.504                           |
| 0       | 3000         | 1.14778     | 68.19                         | 142.22                                  | 59.91  | 45.60  | 79.41   | 104.32  | 1.533             | 5.28 | -274.706                           |
| 100     | 298.15       | 0.72633     | 7.03                          | 13.83                                   | 26.33  | 26.26  | 518.43  | 519.66  | 1.133             | 3.26 | 933.854                            |
| 100     | 500          | 0.72764     | 10.38                         | 30.90                                   | 38.85  | 38.62  | 514.96  | 517.99  | 1.133             | 3.26 | 929.300                            |
| 100     | 1000         | 0.73196     | 12.68                         | 61.22                                   | 47.24  | 46.57  | 505.31  | 512.57  | 1.132             | 3.27 | 905.636                            |
| 100     | 2000         | 0.74173     | 13.63                         | 95.18                                   | 50.33  | 48.83  | 485.78  | 500.76  | 1.131             | 3.30 | 825.660                            |
| 100     | 3000         | 0.75208     | 14.05                         | 115.83                                  | 51.47  | 49.13  | 466.72  | 488.94  | 1.129             | 3.33 | 719.496                            |
| 100     | 4000         | 0.76285     | 14.37                         | 130.75                                  | 52.28  | 49.11  | 448.34  | 477.34  | 1.126             | 3.36 | 595.871                            |
| 235.839 | 298.15       | 0.6         | 3.26                          | 9.06                                    | 20.43  | 20.41  | 938.20  | 939.13  | 1.012             | 2.97 | 1934.600                           |
| 236.694 | 500          | 0.6         | 5.50                          | 23.36                                   | 34.48  | 34.38  | 937.79  | 940.40  | 1.012             | 2.97 | 1937.098                           |
| 239.778 | 1000         | 0.6         | 7.19                          | 51.48                                   | 45.40  | 45.07  | 938.19  | 945.01  | 1.010             | 2.97 | 1938.694                           |
| 246.856 | 2000         | 0.6         | 7.70                          | 84.17                                   | 49.29  | 48.54  | 941.05  | 955.63  | 1.007             | 2.97 | 1916.952                           |
| 254.144 | 3000         | 0.6         | 7.74                          | 104.01                                  | 50.35  | 49.20  | 944.63  | 966.65  | 1.003             | 2.97 | 1871.403                           |
| 261.464 | 4000         | 0.6         | 7.72                          | 118.20                                  | 50.93  | 49.41  | 948.51  | 977.78  | 1.000             | 2.97 | 1809.365                           |

Table 6. Volume dependence of Gruneisen parameter and volume- and temperature-depending pressures (GPa) calculated using the parameters of the EOS of MgO corrected by the data from Dorfman et al. (2012) (see the text)

| $x = V/V_0$ | γ     | Temperature, K |         |         |         |         |         |         |         |         |  |
|-------------|-------|----------------|---------|---------|---------|---------|---------|---------|---------|---------|--|
|             |       | 0              | 298.15  | 500     | 1000    | 1500    | 2000    | 2500    | 3000    | 3500    |  |
| 1           | 1.514 | -0.690         | 0.000   | 1.104   | 4.167   | 7.276   | 10.337  | 13.332  | 16.254  | 19.100  |  |
| 0.95        | 1.427 | 8.538          | 9.166   | 10.235  | 13.267  | 16.378  | 19.464  | 22.501  | 25.483  | 28.406  |  |
| 0.9         | 1.350 | 20.528         | 21.101  | 22.137  | 25.150  | 28.276  | 31.396  | 34.485  | 37.532  | 40.535  |  |
| 0.85        | 1.281 | 36.169         | 36.690  | 37.695  | 40.699  | 43.852  | 47.018  | 50.165  | 53.284  | 56.371  |  |
| 0.8         | 1.218 | 56.684         | 57.156  | 58.132  | 61.137  | 64.329  | 67.550  | 70.766  | 73.966  | 77.143  |  |
| 0.75        | 1.161 | 83.792         | 84.218  | 85.166  | 88.179  | 91.422  | 94.712  | 98.009  | 101.298 | 104.574 |  |
| 0.7         | 1.108 | 119.951        | 120.333 | 121.251 | 124.281 | 127.588 | 130.962 | 134.353 | 137.745 | 141.132 |  |
| 0.65        | 1.059 | 168.745        | 169.085 | 169.973 | 173.027 | 176.414 | 179.887 | 183.390 | 186.902 | 190.415 |  |
| 0.6         | 1.013 | 235.540        | 235.839 | 236.694 | 239.778 | 243.261 | 246.856 | 250.491 | 254.144 | 257.804 |  |
| 0.55        | 0.970 | 328.578        | 328.838 | 329.658 | 332.777 | 336.377 | 340.117 | 343.912 | 347.732 | 351.566 |  |
| 0.5         | 0.929 | 460.960        | 461.182 | 461.962 | 465.121 | 468.861 | 472.776 | 476.764 | 480.788 | 484.830 |  |

expansion ( $\alpha$ ), entropy (*S*), heat capacity at constant pressure (*C<sub>P</sub>*) and at constant volume (*C<sub>V</sub>*), isothermal (*K<sub>T</sub>*) and adiabatic (*K<sub>S</sub>*) bulk moduli, thermodynamic Grüneisen parameter ( $\gamma_{\text{th}} = \alpha V K_T / C_V = \alpha V K_S / C_P$ ), parameter *K'* from Eq. (2), and Gibbs free energy increment relative to the standard state, which coincides with the Gibbs energy increment from the known thermodynamic database (Holland and Powell, 1998, 2011). Tables 6, 8, and 10 present pressure for MgO, Mo, and Au depending on temperature and compression as well as Grüneisen parameter  $\gamma = -(\partial \ln \theta / \partial \ln V)_T$  depending on volume.

#### Conclusions

We have obtained the EOSs for 11 materials, which agree with each other within 2–3% uncertainty. These equations can be considered optimized pressure scales for quasi-hydrostatic conditions on the room-temperature isotherm. They agree both with the ruby scale (Eq. (20)) and with each other, as shown by the example of the EOSs for Au, Pt, and MgO. The EOSs for Au, Pt, and MgO agree with each other not only on the room-temperature isotherm but also at high temperatures, as shown by their intercomparison. Using the room-temperature

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Table 7. Thermodynamic functions of Mo at different pressures and temperatures, calculated using the EOS of Mo corrected by the data from Dorfman et al. (2012) (see the text)

| P, GPa  | Т, К   | $x = V/V_0$ | $\alpha$ E-6, K <sup>-1</sup> | S, J mole <sup>-1</sup> K <sup>-1</sup> | $C_P$ , J mole <sup>-1</sup> K <sup>-1</sup> | $C_V$ , J mole <sup>-1</sup> K <sup>-1</sup> | K <sub>T</sub> , GPa | Ks, GPa | $\gamma_{\rm th}$ | K'   | $\Delta G$ , kJ mole <sup>-1</sup> |
|---------|--------|-------------|-------------------------------|---|--|--|----------------------|---------|-------------------|------|------------------------------------|
| 0       | 298.15 | 1           | 14.04                         | 28.55                                   | 24.09  | 23.94  | 260.50               | 262.06  | 1.431             | 4.05 | 0.000                              |
| 0       | 500    | 1.00305     | 15.96                         | 41.55                                   | 26.11  | 25.80  | 255.99               | 259.03  | 1.488             | 4.06 | -7.170                             |
| 0       | 1000   | 1.01205     | 19.84                         | 60.54                                   | 28.90  | 27.99  | 242.83               | 250.69  | 1.632             | 4.10 | -33.159                            |
| 0       | 2000   | 1.03735     | 30.58                         | 82.45                                   | 35.69  | 31.93  | 206.78               | 231.11  | 1.924             | 4.22 | -105.531                           |
| 0       | 3000   | 1.08049     | 55.51                         | 99.27                                   | 51.07  | 37.08  | 149.43               | 205.79  | 2.264             | 4.44 | -196.468                           |
| 100     | 298.15 | 0.78852     | 4.44                          | 22.31                                   | 22.29  | 22.26  | 622.36               | 623.11  | 0.916             | 3.37 | 819.871                            |
| 100     | 500    | 0.78928     | 5.03                          | 34.48                                   | 24.51  | 24.46  | 619.89               | 621.36  | 0.942             | 3.37 | 814.054                            |
| 100     | 1000   | 0.79143     | 5.78                          | 52.07                                   | 26.16  | 26.01  | 612.92               | 616.50  | 1.011             | 3.38 | 791.960                            |
| 100     | 2000   | 0.79655     | 7.13                          | 70.81                                   | 28.11  | 27.66  | 595.74               | 605.46  | 1.145             | 3.39 | 729.555                            |
| 100     | 3000   | 0.80283     | 8.63                          | 82.59                                   | 30.17  | 29.21  | 574.09               | 593.04  | 1.276             | 3.41 | 652.526                            |
| 100     | 4000   | 0.81049     | 10.41                         | 91.60                                   | 32.65  | 30.85  | 547.48               | 579.48  | 1.403             | 3.43 | 565.275                            |
| 190.789 | 298.15 | 0.7         | 2.78                          | 20.11                                   | 21.56  | 21.55  | 918.72               | 919.31  | 0.777             | 3.18 | 1449.759                           |
| 191.345 | 500    | 0.7         | 3.16                          | 31.96                                   | 24.02  | 23.99  | 918.45               | 919.60  | 0.794             | 3.18 | 1448.074                           |
| 192.896 | 1000   | 0.7         | 3.55                          | 49.16                                   | 25.55  | 25.47  | 917.69               | 920.43  | 0.839             | 3.18 | 1437.511                           |
| 196.412 | 2000   | 0.7         | 4.11                          | 67.20                                   | 26.83  | 26.63  | 915.36               | 922.34  | 0.927             | 3.18 | 1401.421                           |
| 200.416 | 3000   | 0.7         | 4.65                          | 78.18                                   | 27.95  | 27.56  | 911.86               | 924.71  | 1.009             | 3.18 | 1354.647                           |
| 204.896 | 4000   | 0.7         | 5.20                          | 86.23                                   | 29.11  | 28.47  | 907.18               | 927.69  | 1.087             | 3.18 | 1301.652                           |

Table 8. Volume-depending Gruneisen parameter and volume- and temperature-depending pressure (GPa) calculated using the parameters of the EOS of Mo corrected by the data from Dorfman et al. (2012) (see the text)

| $x = V/V_0$ | γ     | Temperature, | Temperature, K |         |         |         |         |         |         |         |  |  |  |
|-------------|-------|--------------|----------------|---------|---------|---------|---------|---------|---------|---------|--|--|--|
|             |       | 0            | 298.15         | 500     | 1000    | 1500    | 2000    | 2500    | 3000    | 3500    |  |  |  |
| 1           | 1.348 | -0.692       | 0.000          | 0.784   | 2.986   | 5.493   | 8.294   | 11.385  | 14.766  | 18.436  |  |  |  |
| 0.95        | 1.201 | 14.199       | 14.823         | 15.548  | 17.585  | 19.893  | 22.460  | 25.282  | 28.360  | 31.692  |  |  |  |
| 0.9         | 1.079 | 33.395       | 33.964         | 34.641  | 36.540  | 38.680  | 41.046  | 43.637  | 46.450  | 49.486  |  |  |  |
| 0.85        | 0.975 | 58.274       | 58.796         | 59.433  | 61.218  | 63.215  | 65.411  | 67.800  | 70.383  | 73.159  |  |  |  |
| 0.8         | 0.887 | 90.741       | 91.224         | 91.829  | 93.519  | 95.396  | 97.445  | 99.661  | 102.043 | 104.592 |  |  |  |
| 0.75        | 0.810 | 133.485      | 133.935        | 134.513 | 136.125 | 137.903 | 139.827 | 141.894 | 144.104 | 146.454 |  |  |  |
| 0.7         | 0.743 | 190.367      | 190.789        | 191.345 | 192.896 | 194.592 | 196.412 | 198.354 | 200.416 | 202.596 |  |  |  |
| 0.65        | 0.684 | 267.064      | 267.462        | 268.002 | 269.505 | 271.137 | 272.874 | 274.712 | 276.650 | 278.687 |  |  |  |
| 0.6         | 0.631 | 372.135      | 372.512        | 373.041 | 374.512 | 376.095 | 377.768 | 379.524 | 381.362 | 383.282 |  |  |  |

Table 9. Thermodynamic functions of Au at different pressures and temperatures, calculated using the EOS of Au corrected by the data from Dorfman et al. (2012) (see the text)

| P, GPa  | <i>T</i> , K | $x = V/V_0$ | $\alpha E$ -6, $K^{-1}$ | S, J mole <sup>-1</sup> K <sup>-1</sup> | $C_P$ , J mole <sup>-1</sup> K <sup>-1</sup> | $C_V$ , J mole <sup>-1</sup> K <sup>-1</sup> | K <sub>T</sub> , GPa | Ks, GPa | $\gamma_{th}$ | K'   | $\Delta G$ , kJ mole <sup>-1</sup> |
|---------|--------------|-------------|-------------------------|---|--|--|----------------------|---------|---------------|------|------------------------------------|
| 0       | 298          | 1           | 41.77                   | 47.54                                   | 25.39  | 24.51  | 167.00               | 173.05  | 2.908         | 5.75 | 0.000                              |
| 0       | 500          | 1.00883     | 45.33                   | 60.93                                   | 26.46  | 24.79  | 157.11               | 167.65  | 2.960         | 5.84 | -11.053                            |
| 0       | 1000         | 1.03467     | 56.93                   | 80.08                                   | 29.35  | 24.91  | 129.51               | 152.57  | 3.128         | 6.11 | -46.774                            |
| 0       | 1300         | 1.05425     | 69.22                   | 88.11                                   | 32.27  | 24.93  | 109.49               | 141.74  | 3.274         | 6.35 | -72.036                            |
| 100     | 298          | 0.75908     | 9.71                    | 31.65                                   | 23.50  | 23.37  | 638.35               | 642.15  | 2.056         | 4.26 | 866.713                            |
| 100     | 500          | 0.76061     | 10.21                   | 44.13                                   | 24.62  | 24.37  | 632.90               | 639.55  | 2.060         | 4.26 | 858.967                            |
| 100     | 1000         | 0.76459     | 10.61                   | 61.47                                   | 25.34  | 24.80  | 619.31               | 632.89  | 2.069         | 4.28 | 832.091                            |
| 100     | 2000         | 0.77295     | 11.13                   | 79.27                                   | 26.07  | 24.91  | 591.80               | 619.31  | 2.088         | 4.32 | 760.744                            |
| 100     | 3000         | 0.78181     | 11.68                   | 89.97                                   | 26.77  | 24.93  | 563.81               | 605.45  | 2.109         | 4.35 | 675.789                            |
| 350.386 | 298          | 0.6         | 3.79                    | 21.63                                   | 21.42  | 21.37  | 1618.86              | 1622.08 | 1.761         | 3.71 | 2565.984                           |
| 351.704 | 500          | 0.6         | 4.18                    | 33.33                                   | 23.65  | 23.57  | 1619.06              | 1625.02 | 1.761         | 3.71 | 2568.433                           |
| 355.188 | 1000         | 0.6         | 4.36                    | 50.09                                   | 24.78  | 24.59  | 1620.34              | 1632.79 | 1.761         | 3.71 | 2568.476                           |
| 362.305 | 2000         | 0.6         | 4.40                    | 67.24                                   | 25.24  | 24.85  | 1623.50              | 1648.66 | 1.761         | 3.71 | 2552.460                           |
| 369.456 | 3000         | 0.6         | 4.40                    | 77.33                                   | 25.48  | 24.90  | 1626.79              | 1664.61 | 1.761         | 3.71 | 2523.663                           |

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| Table 10. Volume-depending Gruneisen parameter and volume- a    | nd temperature-depending pressu | re (GPa) calculated using t | he parameters of the EOS of Au |
|---|---------------------------------|-----------------------------|--------------------------------|
| corrected by the data from Dorfman et al. (2012) (see the text) |                                 |                             |                                |

| $x = V/V_0$ | γ     | Temperature, | Temperature, K |         |         |         |         |         |         |  |  |  |
|-------------|-------|--------------|----------------|---------|---------|---------|---------|---------|---------|--|--|--|
|             |       | 0            | 298.15         | 500     | 1000    | 1500    | 2000    | 2500    | 3000    |  |  |  |
| 1           | 2.908 | -1.693       | 0.000          | 1.418   | 4.957   | 8.504   | 12.052  | 15.602  | 19.151  |  |  |  |
| 0.95        | 2.655 | 8.350        | 9.921          | 11.279  | 14.677  | 18.083  | 21.493  | 24.903  | 28.313  |  |  |  |
| 0.9         | 2.454 | 22.287       | 23.761         | 25.080  | 28.391  | 31.714  | 35.040  | 38.368  | 41.696  |  |  |  |
| 0.85        | 2.290 | 41.658       | 43.051         | 44.348  | 47.614  | 50.896  | 54.182  | 57.470  | 60.758  |  |  |  |
| 0.8         | 2.153 | 68.683       | 70.006         | 71.292  | 74.547  | 77.823  | 81.104  | 84.388  | 87.672  |  |  |  |
| 0.75        | 2.036 | 106.622      | 107.879        | 109.164 | 112.437 | 115.738 | 119.046 | 122.357 | 125.669 |  |  |  |
| 0.7         | 1.934 | 160.352      | 161.547        | 162.837 | 166.156 | 169.511 | 172.875 | 176.242 | 179.612 |  |  |  |
| 0.65        | 1.843 | 237.344      | 238.474        | 239.777 | 243.165 | 246.603 | 250.052 | 253.507 | 256.964 |  |  |  |
| 0.6         | 1.761 | 349.324      | 350.386        | 351.704 | 355.188 | 358.737 | 362.305 | 365.878 | 369.456 |  |  |  |
| 0.55        | 1.687 | 515.256      | 516.243        | 517.578 | 521.181 | 524.877 | 528.596 | 532.326 | 536.060 |  |  |  |
| 0.5         | 1.617 | 766.887      | 767.788        | 769.136 | 772.884 | 776.764 | 780.678 | 784.606 | 788.541 |  |  |  |

isotherms of Au, Pt, and MgO as pressure scales, we obtained a new B2–NaCl isotherm, which can serve as a pressure scale at >300 GPa and is consistent with the Pt pressure scale under these conditions. We also corrected the room-temperature isotherm of hcp-Fe, using the new ruby pressure scale and the EOS for W (Dorogokupets et al., 2012). The high-temperature EOSs for B2-NaCl and hcp-Fe will be considered in a special paper.

Thus, we have obtained the best EOSs for Au, Pt, MgO, and B2-NaCl on the room-temperature isotherm, taking into account the data from Dorfman et al. (2012) and using the second-order equation (Eq. (2)) from Holzapfel (2001, 2010). A subsequent increase in the accuracy of pressure scales based on the EOSs for Au, Pt, MgO, and B2-NaCl is possible but with the use of third-order equations.

The used calculation procedure will also be applied to study the EOSs for silicates, carbonates, and metal compounds obtained recently by our research team for thermodynamic description of phases in the Earth's (Dobretsov and Shatskiy, 2012) and other planets' interior and comparison of results with experimental data on mantle systems, including ones with volatiles (Litasov, 2011). The procedure of calculation of *PVT* relations and phase thermodynamics using the proposed EOSs can be found online at http://labpet.crust.irk.ru.

We thank N.V. Sobolev, A.B. Belonoshko, O.G. Kuskov, and O.G. Safonov for great work on reviewing and editing our paper and valuable remarks. We also thank A. Dewaele (CEA, France) for providing unpublished data on the B2-NaCl compressibility.

This work was supported by grants 12-05-00758-a and 12-05-33008 from the Russian Foundation for Basic Research, Project 14.B37.21.0457 from the Ministry of Education and Science of the Russian Federation, and Integration Project 97 (2012-2014) from the Siberian Branch of the Russian Academy of Sciences.

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Editorial responsibility: N.V. Sobolev