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Eliciting geologists' tacit model of the uncertainty of mapped geological boundaries

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Abstract

It is generally accepted that geological linework, such as mapped boundaries, are uncertain for various reasons. It is difficult to quantify this uncertainty directly, because the investigation of error in a boundary at a single location may be costly and time consuming, and many such observations are needed to estimate an uncertainty model with confidence. However, it is also recognized across many disciplines that experts generally have a tacit model of the uncertainty of information that they produce (interpretations, diagnoses etc.) and formal methods exist to extract this model in usable form by elicitation. In this paper we report a trial in which uncertainty models for mapped boundaries in six geological scenarios were elicited from a group of five experienced geologists. In five cases a consensus distribution was obtained, which reflected both the initial individually elicted distribution and a structured process of group discussion in which individuals revised their opinions. In a sixth case a consensus was not reached. This concerned a boundary between superficial deposits where the geometry of the contact is hard to visualize. The trial showed that the geologists' tacit model of uncertainty in mapped boundaries reflects factors in addition to the cartographic error usually treated by buffering linework or in written guidance on its application. It suggests that further application of elicitation, to scenarios at an appropriate level of generalization, could be useful to provide working error models for the application and interpretation of linework.

1 Introduction

1.1 What geological boundaries are, and why they are uncertain

The geological map, with boundaries delineating the surface expression of different stratigraphic or lithological units, is the classical form of spatial geological information. These boundaries are drawn by a geologist on the basis of field observations

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and interpretation of borehole records, remote sensor data and other information. The boundaries delineated by the geologist eventually are presented as boundaries on the published map, be this a paper or a digital product, and may also appear on the basis of subsequent interpretation, as boundaries in other derived maps: susceptibility maps for geohazards, for example, or maps of mineral resources or soil parent material. Recent developments in computer-based geological modelling make it easier for the geologist to represent their three-dimensional (3-D) understanding of geology, but mapped geological boundaries in two-dimensions (2-D) remain an important source of information in the era of 3-D modelling. Boundaries in 2-D represent important information, e.g. on the position of outcrop lines, which assist and constrain the 3-D interpretation. Mapped geological boundaries, particularly those held in the records of large national geological surveys, remain an important source of geological information. For this reason it is important to understand and to quantify their inherent uncertainties.

Geological boundaries are uncertain for various reasons. The first is *conceptual* uncertainty. In some cases a geological boundary on a map can reasonably be expected to correspond (subject to other sources of uncertainty) to an unambiguous physical reality, a contact between two contrasting units. In other cases a mapped boundary may represent an interpretation of variation that is essentially spatially continuous, i.e. a gradational boundary. In these latter cases the boundary subdivides the geological material into units which differ, and the difference between units may be of practical value, but the precise position of the boundary is, essentially, arbitrary. This is true of many boundaries on soil maps, for example. Metamorphic boundaries, particularly those resulting from regional metamorphism are often diffuse; defined by geochemical or mineralogical assemblage. In this case the identification of a specific boundary is rare, relying upon a balance of evidence that supports the transition from one assemblage to another. Similarly, facies boundaries representing different sedimentological environments can present a range of boundary types (gradual, interdigitating, complex) where a clear separation of the units is difficult to establish, but must occur within an implicit zone. In this paper we do not consider conceptual sources of uncertainty,

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but consider cases where the geological reality that the mapped boundary aims to represent could, in principle, be observed directly and unambiguously. This would require the removal of overlying material – all vegetation and material altered by pedogenesis and anthropogenic processes such as cultivation where the delineated units are superficial deposits, and all superficial material when the solid geology is mapped.

The second type of uncertainty is *scale-dependent* uncertainty. Even where a boundary is conceptually unambiguous the precise position at which it should be described as a continuous line may depend on the spatial scale at which it is observed, and entails some degree of generalization of fine-scale variation. This is a consequence of fractal or quasi-fractal behaviour (Burrough, 1983). While "the coast of Britain" is a conceptually unambiguous boundary, its representation as a continuous line, and hence its measured length, depends on the scale of observation (Mandelbrot, 1967). Scale-dependent uncertainty is a consideration when a boundary generalized at some scale of field survey is used to make decisions at a larger cartographic scale. It may be inappropriate, for example, to use certain mapped boundaries to make decisions about the location of a proposed structure at a resolution of tens of metres. Further investigation would be needed to improve the information. A survey organization may ensure that scale-dependent uncertainty is allowed for in the use of its products by attaching a scale-dependent "buffer" to published boundaries, or by giving written guidance on their proper usage, or both.

Cartographic uncertainty is introduced when the field-surveyor's mapped boundaries are converted to a cartographic product. It encompasses scale-dependent uncertainty because a cartographer will usually generalize field-mapped boundaries to a smaller cartographic scale, and will do so more or less successfully. Cartographic uncertainty includes other errors that are introduced in this process including errors arising from digitizaton (Gong et al., 1995). In this paper we do not consider scale-dependent or cartographic uncertainty, considering only the sources of error in boundaries as mapped on a field sheet at the typical UK mapping scale of 1 : 10 000.

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The source of uncertainty that we consider here is *interpretation uncertainty*. This arises because, in many settings, the geological boundary of interest cannot be observed everywhere. Over most of the mapped length of a boundary, therefore, the position is based on the mapper's interpretation of available information. Consider a simple case where the boundary position is constrained at two locations. The constraint may be strong (e.g. the contact of interest can be observed directly in a quarry or other exposure) or weak (e.g. it can be inferred that the crop line for a unit occurs somewhere on a line between one borehole where the unit is in outcrop and a second where the contact is below the surface). At intervening locations the possible position of the boundary is constrained by limited local direct observations, by topographic features such as breaks of slope, spring-lines etc. and by available seismic data or other geophysical observations. The mapped position of the boundary is the geologist's best expert interpretation of the available information. It is therefore subject to error because it is based, inevitably, on conceptual models (e.g. of the control of surface features by subsurface structure) which are themselves imperfect, which do not fully determine the position of boundaries even when good and dense observations are available (Brodaric et al., 2004) and which must be implemented with imperfect and partial information.

1.2 Past work on the uncertainty of geological boundaries

The uncertainty of linear features in geographical information has been the subject of considerable research. Much of the research on *conceptual* uncertainty has been done in the context of soil mapping where mapped boundaries do not, in general, attempt to reproduce unambiguous boundaries between soils on the ground, but represent an interpretation of continuous variation. The utility of such boundaries is that they parcel up the landscape into regions which should be more internally homogeneous than the landscape as a whole, and so provide a basis for spatial prediction (by the regional mean). Webster and Beckett (1968) and successors such as Leenhardt et al. (1994) have examined the utility of such information by analysis of the variance components of terrain properties that one might predict from the delineated units.

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There has been considerable interest in *scale-dependent* uncertainty, including the modelling of boundaries as fractal objects. The extent to which the generalization of a boundary at some scale introduces uncertainty into the resulting map can be measured by the proportion of sites within a delineated map unit which correspond to the notional class (soil, stratigraphic etc) to which the unit nominally corresponds. This proportion may also be affected by interpretation uncertainty, but Lark and Beckett (1998) presented a model for errors in soil maps which can be attributed to the generalization of the spatial pattern below some threshold scale.

Cartographic uncertainty is a large topic. Chrisman (1982) provided an early quantitative framework for its evaluation, and it has been the subject of empirical studies (e.g., Gong et al., 1995). At the British Geological Survey (BGS), all digital data products are provided with guidance for users concerning appropriate use at scale, given the cartographic uncertainty. Typically the advice uses the following form of words:

"The cartographic accuracy is nominally 1 mm which equates to 50 m on the ground at 1 : 50 000 scale. This is a measure of how faithfully the lines are captured; it is not a measure of the accuracy of the geological interpretation."

Interpretation uncertainty is challenging to quantify. It arises from the imperfection of the conceptual models that the geologist uses to interpret available data, but also from the sparsity of those data. As noted by Brodaric et al. (2004), for some set of observations and a conceptual model for interpretation, the underlying distribution of boundaries is generally underdetermined, i.e. the rational interpreter is not constrained to a single interpretation. The interpretation may be expected to be more constrained the denser the data. For this reason one may think of the interpretation error in geological boundaries as a random process the variability of which depends on the density of available data, the complexity of the geological processes in the conceptual model and factors (experience etc) which may influence individual interpretation.

The parameterization of a model of boundary uncertainty is not straightforward. Most progress has been made in cases where boundaries are part of a statistical model for some densely sampled or quasi-continuous measurements of some variables (e.g.

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geochemical data, geophysical variables). In this case a statistical model may be invoked for how the boundary uncertainty affects predictions from the model. Examples of this are given by Lilland and Boisvert (2013), Silan-Cárdenas et al. (2009) and Guillot et al. (2006). However, in the case of conventional geological survey, boundaries do not emerge from a statistical model for a response variable, but are the result of expert interpretation. Their uncertainty can therefore not be obtained directly from a statistical model. One way to examine the uncertainty would be to do so empirically.

Empirical assessments of interpretation error have been undertaken in the context of seismic interpretation (Bond et al., 2012), soil survey (Burrough et al., 1971) and 3-D geological modelling (Lark et al., 2013, 2014). These workers evaluated uncertainty in expert interpretation empirically, based on validation data. This allows one to examine the variability of interpretation errors, and the contribution of between-interpreter effects as well as differences between geological settings and the density of available observations. A similar empirical approach is reported by Albrecht et al. (2010) who examined between-interpreter variation of boundaries around objects in remotely sensed images.

The problem with the empirical approach is that it requires substantial effort. If one wishes to evaluate the uncertainty of geological boundaries empirically then one requires a number of geological maps of the same area, produced independently conditional on a (common) set of observations, and with sufficient local validation observations of the boundaries of interest, perhaps from geophysical data, boreholes, excavations or geological exposures. These validation data must not have been available to the surveyors. Such studies are very resource-intensive, and provide information on uncertainty only for the geological setting of the particular study, and the nature and density of available supporting observations. For this reason we consider expert elicitation as an alternative approach.

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1.3 Expert elicitation

Expert elicitation is based on the assumption that the experienced geological mapper has a mental model of the uncertainty that is attached to mapped boundaries. This model comes from the geologist's awareness and experience of the variability of geological phenomena. It also reflects the geologist's awareness of how, in a particular setting, direct observations and the interpretative model of topographic features and other surface expression of geological structure and lithology constrain the possible distribution of boundaries. This model is almost certainly tacit rather than explicit, still less can the geologist write it down in statistical terms. Nonetheless, the expert, through his or her experience, has an intuitive sense of the reliability of information. This fact is recognized in some survey procedures. For example, traditional geological mapping has always distinguished between boundaries that can be regarded as directly observed at the scale of survey and those inferred from other evidence. This expert assessment of uncertainty may be communicated on a conventional map by using solid lines for observed boundaries and dashed lines for those that are inferred. Expert elicitation methods have been used elsewhere in earth sciences, for example Martí et al. (2008), Truong et al. (2013).

We chose to elicit the tacit model of uncertainty in geological boundaries in the context of a notional test of a mapped boundary along a 1-D line. Consider a transect perpendicular to a mapped geological boundary. The mapped boundary intersects the transect at a location x_m units from an arbitrary origin of the transect. We assume (see above) that the boundary is not subject to conceptual, scale-dependent or cartographic uncertainty, but only to interpretation uncertainty. This arises from the fact, for example, that the units separated by the boundary are largely covered by a thin, but possibly irregular blanket of concealing material including vegetation, soil and superficial deposits, so the interpretation is based on topographic features and some limited information from boreholes and exposure. This means that, if we were to excavate the overlying concealing material along the transect, we could identify the position where

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the actual boundary intersects the transect (true intersection) at a location x_t units from the arbitrary origin of the transect. Because of the interpretation uncertainty the difference between these positions, $\varepsilon = x_t - x_m$, is not, in general, equal to zero but is a variable with a distribution. The geological mapper's tacit model of boundary uncertainty implies some form for this distribution such that there exists a probability that $\varepsilon \in [\varepsilon_l, \varepsilon_u]$ where ε_l and ε_u are real-valued limits and $\varepsilon_l < \varepsilon_u$. This probability would be called the mapper's personal or subjective probability that the difference between the true and mapped intersection falls in this interval. "Personal" or "subjective" imply that the tacit model depends on the particular expert's experience and understanding. The process of identifying the form of the statistical distribution implicit in the personal probabilities under an expert's tacit model of boundary uncertainty is known as expert elicitation (O'Hagan et al., 2006).

In this paper we use established methods of expert elicitation to arrive at consensus distributions for the variable ε in a number of scenarios. The objective of this was to evaluate the feasibility of running such elicitations with groups of experienced geological mappers as a prelude to larger-scale elicitations to assess the uncertainty of mapped boundaries in some specific settings.

2 Methods

2.1 The elicitation framework

The principles of the elicitation framework that we used in this study are presented in detail by O'Hagan et al. (2006). The Sheffield elicitation framework (SHELF) is described by Oakley and O'Hagan (2010). It is based on research into elicitation reviewed by O'Hagan et al. (2006), and more recent developments. SHELF has been used for expert elicitation in various fields including veterinary medicine (Higgins et al., 2012), modelling of atmospheric processes (Lee et al., 2013), modelling of water distribution networks (Scholten et al., 2013), forecasting of energy demands (Usher and Strachan,

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2013), and power analysis for clinical trials (Ren and Oakley, 2014). SHELF provided the basis for the elicitation procedure that we used. However, we cannot formally describe our elicitation as conducted according to the SHELF framework because we did not record personal interest and expertise statements from the participants. This is because all participants are current or recently retired members of staff at the British Geological Survey whose field experience and external interests are a matter of record. Furthermore, we held a final feedback meeting after completion of the elicitation to give participants an overview of the outcomes and to allow them to register any concerns or change of opinion. In other respects we used the proformas and software of the SHELF procedure.

In our elicitation procedure we followed SHELF guidelines, as described in detail in Sect. 2.3 below. We defined a set of scenarios for which we wanted to elicit probability distributions of ε. These were defined by an experienced geological surveyor (AJMB) who did not serve as an expert for purposes of the elicitation, but rather as a geological facilitator. RML served as statistical facilitator of the elicitation, having facilitated previous elicitations at the British Geological Survey using a framework based on SHELF.

In accordance with SHELF procedures, a briefing document setting out some principles of probability, elicitation and explaining the scenarios of interest was prepared and sent to all participants. There was then a briefing session to explain this material and address any questions, and to conduct a practice elicitation to familiarize participants with the procedure. The main elicitation was then conducted in a single day, elicitation records were kept in line with SHELF protocols. After this a summary of results was presented to the participants, and a final feedback meeting was held to ensure that participants agreed that the outcomes reflected group opinions.

2.2 Selection of panel and definition of scenarios

The geological facilitator (AJMB) and a BGS geologist with both field experience and specialist experience of geological product development (RSL) met with RML to agree on a common understanding of the goals of the project and to agree on a set of par-

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ticipants to constitute the panel. SHELF guidelines are to recruit a panel that is not too large (about 5 members) and who can work together rather than individually. A panel was identified comprising five geologists with field experience in a range of settings. AJMB then defined a set of scenarios, designed to encompass a range of conditions reflecting the mapped geological boundaries held by the British Geological Survey. A scenario was defined in terms of a general geological setting for a boundary. It was not defined with respect to particular stratigraphic units, but rather in terms of contrasting lithologies or deposits that would correspond to a common setting. The scenario was also defined in terms of land cover, any local exposure, and the frequency of augering in the case of superficial material. In some cases discussion of the scenario during the elicitation identified ways in which its definition required clarification. Since AJMB was present as a facilitator, this could be done consistently, and any such modifications were recorded.

Scenario definitions are given in the Appendix along with modifications agreed during the elicitation. Figure 1 illustrates the mapped settings and the dispositions of the units relative to the notional transect. It is important that this is understood by all the group. For example, in scenario 1, Fig. 1 shows that a negative value of ε, which means that $x_t < x_m$, implies that the mapped boundary, indicated by the vertical blue line, is too far onto the river terrace deposit. Figures showing these dispositions were provided to participants during the elicitation.

2.3 Conduct of the elicitation

2.3.1 Briefing and practice elicitation

The SHELF guidelines (Oakley and O'Hagan, 2010) require an appropriate briefing for all participants. To this end a briefing document was produced. This explained why the elicitation was to be undertaken and what, in outline, an elicitation is. It gave a brief introduction to the model of errors in mapped boundaries, as set out in Sect. 1.3 above, and a reminder of the concepts of probability and of distributions and per-

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centiles (specifically quartiles) of random variables. The elicitation task was then set out in terms of a frequency representation. That is to say the participants were told that they would be considering a notional set of 100 randomly and independently selected locations drawn from any one scenario. At each location a transect is considered, perpendicular to the mapped boundary as illustrated in Fig. 1. At each location the position, x_t of the true intersection of the boundary is identified, and an error ε evaluated. The distribution to be elicited is the one realized in the histogram of the notional 100 observations of the error and, under the elicitation used, this entails making expert judgements about quartiles of the distribution. O'Hagan et al. (2006) note that this approach, in which a panel is required to visualize a range of instances of one scenario, can be useful for ensuring that the experts consider a full range of possibilities under the scenario and not just those (most frequently or recently observed) to which they are said to have greatest access. The scenario descriptions were also included in the briefing document.

The briefing document was circulated to participants a little over two weeks before a briefing meeting, and they were requested to read it in advance. In the briefing session, which took place the day before the main elicitation, the content of the document was reviewed, and participants had the opportunity to raise questions about any aspect of the procedure. In accordance with Oakley and O'Hagan (2010) the briefing session concluded with a practice elicitation to familiarize participants with the elicitation procedure. In this case the distribution which was elicited was that of ages of delegates to the 2013 European Geosciences Union congress.

Ideally more time would be available between the briefing and the main elicitation to allow agreement of any modifications to the scenarios or procedure, but this was not possible due to the participants' availability. No difficulties of understanding or disagreements over the scenarios and their description emerged in the course of the briefing session.

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2.3.2 Group elicitation

The main elicitation was conducted on 13 November 2013. The elicitation took place in a meeting room where all participants and facilitators could sit undisturbed around a large table. Hard copies of the scenario descriptions and associated Figures (see Fig. 1) were provided to all participants. The room was equipped with a data projector which allowed elicited distributions and other feedback generated by the SHELF procedures to be seen by all participants. A flip chart was also used to record results from the individual elicitations so that these could be viewed by all participants. The geological facilitator (AJMB) and the statistical facilitator (RML) were present throughout the elicitation, as were all participants, the project administrator and a student who attended to gain experience of the elicitation method.

We used the Quartile method in the SHELF framework for both initial individual elicitations and the group elicitation Oakley and O'Hagan (2010). This was chosen because it had previously been successfully applied with a panel of geologists to elicit distributions pertaining to shallow geohazards. The method proceeded in three stages.

1. The scenario was presented. The group as a whole was then asked to provide upper and lower absolute bounds on the error variable, ε. This was done through a group discussion. The group was reminded that these bounds are minimum and maximum possible values of the variable, and the probability of a value of ε occurring in a range near these bounds may be very small. The group was reminded of the meaning of negative and positive values of ε in terms of the position of the mapped boundary on each unit that defines the scenario.

2. Each individual was then required independently to choose values of the median (second quartile) and the first and third quartiles of the distribution of ε which reflect their expectations. Since we were considering (see Sect. 2.3.1) a notional independent random sample of 100 intersections with boundaries corresponding to the scenario, this was framed in terms of, respectively, the value such that 50 locations had a larger value of ε and 50 a smaller; the value such that 25

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locations had a smaller value of ε and 75 a larger value, and the value such that 25 locations had a larger value of ε and 75 a smaller value. Each participant recorded their values on a sheet with their name. Individual best-fitting distributions were then found for each set of quartiles, given the upper and lower bounds, using the elicit.group.values procedure in the SHELF2.R source presented by Oakley and O'Hagan (2010) for use on the R platform (R development core team, 2013). Version 2.01 of the SHELF2.R source, modified on 11 November 2012 was used. This procedure generated a plot with the PDF for each panel member. Figure 2 shows an illustrative plot for scenario 2 (although the axis labels and the legend have been somewhat modified from the original code). This plot was visible to all participants on the projector screen. The individual quartiles were also written on the flip-chart. Note that the participant code varied arbitrarily from one scenario to the next, so the distributions were anonymized, although participants in all cases chose to acknowledge their initial results in later discussion. The individual sheets with the initial values were retained at the end of the elicitation.

3. The participants, as a group, were then asked to determine a group consensus set of quartiles. The discussion was allowed to proceed spontaneously, with the facilitators intervening when a particular question arose or, in the case of the statistical facilitator, if any comments made in the discussion indicated a misunderstanding of the nature of the probability model or the error variable. A visual display to facilitate this is generated by the elicit.group.values procedure, and this is illustrated in Fig. 3 for scenario 2. As values for the median, first and third quartiles are adjusted the values are displayed (panels in the top row and bottom right panel). A probability density function, the best fitting PDF of a set of distributions, to the quartiles, given the limits, was estimated and displayed (black line in bottom right panel) along with the mean and SD and the 0.05 and 0.95 quantile, encompassing a 90 % probability interval. However, this feedback was generally consulted by the group at the end of the discussion.

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2.3.3 Feedback

After the elicitation was completed a summary document was prepared. This contained the group elicited quartiles and the lower 2.5th and upper 97.5th percentiles of the fitted distributions encompassing a range within which one would expect to find 95 % of boundary errors along the transect. These were also displayed graphically. The first output that we plotted displayed the elicited quartiles as a piecewise-uniform distribution, i.e. one in which the probability density is uniform over each of the four intervals defined by, respectively, the lower bound, first quartile, median, third quartile and upper bound. The density function for the best-fitting distribution among the set considered in the elicit.group.values procedure was also plotted on the same axes (see Fig. 4). Three distributions were used. The most common was the Beta distribution, scaled from the range [0,1] on which it is defined to the range defined by the minimum and maximum values in Table 1, $x_{\min}$ and $x_{\max}$. This has the density function

$$f_{\text{scaled}\beta}(x|a,b) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} y^{a-1}(1-y)^{b-1}, \quad (1)$$

where

$$y = \frac{x - x_{\min}}{x_{\max} - x_{\min}},$$

a and b are parameters and $\Gamma(\cdot)$ denotes the Gamma function.

The Gamma distribution has the density function

$$f_{\text{Gamma}}(x|c,s) = \frac{1}{s^c \Gamma(c)} x^{c-1} e^{\frac{-x}{s}}, \quad (2)$$

where s and c are parameters.

The normal distribution has the density function

$$f_{\text{Normal}}(x|\mu,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}, \quad (3)$$

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where μ and σ are parameters, the mean and SD respectively.

In one case (scenario 1) the goodness of fit of two competing distributions was very similar, so both were included in the summary document. The document was completed fifteen days after the elicitation and circulated to all participants. They then participated in a discussion meeting after a further twelve days, at which they were asked whether they were still content with the group consensus statistics and, in the case of scenario 1, which of the two competing distributions, given the density plot and the 95 % interval, best represented their own expectation of the error distribution in the scenario.

3 Results

The initial group-agreed plausible range and the individually elicited quartiles for each scenario are presented in Table 1. Table 2 presents the group-elicited quartiles and the fitted distributions with parameters. Figures 4 and 5 are fitted distributions and piecewise-uniform distributions of the elicited interquartile ranges.

We now present brief summaries of key discussion points that arose in the course of each elicitation.

3.1 Scenario 1 – edge of river terrace deposit on bedrock

The first 15 min of the group discussion to agree on upper and lower bounds for this scenario was taken up with more general issues about the elicitation which had clearly occurred to participants since the briefing meeting, but these are reported here because they were raised only after the scenario had been introduced. One concern was whether results from this elicitation would be applied as quality measures or buffers to BGS's boundary-based products. Participants were assured that the present elicitation, about generalized scenarios, was an exploratory study, to inform any future use of elicitation for products. Some further issues to do with the kinds of uncertainty to

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be considered in this elicitation were clarified, specifically that effects of cartographic error or location error on the field map should be ignored, and that error at the scale of generalization of a field map sheet on a scale of 1 : 10 000 should be considered.

The discussion specifically to agree upper and lower bounds took 40 min. In the course of this discussion the principal issues were as follows:

1. In practice the mapping of superficial material has been influenced by the thickness of this deposit. The question was therefore raised of whether the boundary would be defined where the river terrace thinned to some minimum thickness rather than where the bedrock was at surface. After some discussion it was agreed that, in the particular setting (as opposed to a setting where superficial material is patchy) this consideration could be set aside.

2. Different surveyors would make different decisions as to whether to map head arising from cryoturbation in this setting, which could lead to variation in the boundary location.

3. The extent to which the boundary is expressed as a sharp break of slope of the land surface will affect the variability of boundary error.

The geological facilitator indicated that it should be assumed that head is not mapped in this scenario and that the break of slope is a subtle feature. On this basis it was agreed that the surveyor would aim to map the break of slope as a feature indicating the boundary, but would not identify it precisely. Slightly asymmetric bounds were agreed, implying that the largest possible absolute error would be with the mapped boundary too far onto bedrock.

The individual and group elicitation of quartiles took 26 min in total. Three participants proposed a zero median error, and the main difference was between one participant who argued for a slightly positive median, arguing that surveyors would tend to map the boundary too far onto bedrock, misled by isolated patches of terrace material, while another argued that there would be a tendency to map too far onto the terrace

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material due to problems identifying the edge as the deposit thins out. This latter participant convinced the others that a negative median was appropriate, and agreed on a smaller absolute median error than in his individual elicitation, given the frequency of augering in the scenario description. Once this was agreed a consensus on the first and third quartiles was quickly achieved.

3.2 Scenario 2 – base of sandstone in mudstone/siltstone succession

The discussion to agree upper and lower bounds took 24 min. The principal consideration determining the interval in this setting was the scope to extrapolate from observations in the quarry, and the factors that would control the precision of this, specifically the urban setting. Once these bounds were agreed the individual and group elicitation of quartiles took 14 min. Again, the process of extrapolating from the quarry was critical in the group discussion. It was agreed that where this boundary was inferred solely from surface topography the first and third quartiles would be asymmetric about the median, with a tendency to map the boundary too far downslope, but that in the setting as described symmetrical quartiles were appropriate.

3.3 Scenario 3 – edge of alluvium/tidal river deposit against contrasting underlying geology

The discussion to agree upper and lower bounds took 10 min. It was agreed that this boundary should be relatively easy to identify in the field, so the interpretation uncertainty would be small relative to subsequent cartographic sources of error. There was some discussion as to whether a larger upper limit should be considered, because of the possibility in some circumstances of putting the boundary too far upslope (onto the bedrock) due to recent deposition of flood material, but it was agreed that cultivation, as indicated in the scenario description, made this unlikely. The individual and group elicitation of quartiles took 12 min. It was agreed that errors downslope (putting

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the boundary too far onto the alluvium) would be likely to predominate, and so it was appropriate to have a negative median and an upper quartile of zero.

3.4 Scenario 4 – stratigraphic boundary between two distinctive sedimentary rocks

The discussion to agree upper and lower bounds took 14 min. There was some initial disagreement as to whether this scenario was one in which field survey would be appropriate. One participant felt that it was not, but changed his view on this given the modification to the scenario that the superposition relationships of the units are assumed known, the scenario is not approached "cold" but as part of a broader survey campaign in which this information would be developed.

The individual and group elicitation of quartiles took 10 min. One participant put asymmetrical quartiles in his individual elicitation, and argued in the group elicitation that this was necessary because down-slope movement of surface brash could result in larger errors in this direction. One participant, in response, queried whether the field surveyor would use brash in mapping. A third participant suggested that the use of brash would depend on whether the particular survey was being undertaken rapidly or for a more detailed project so, over the population of BGS linework, some instances of this scenario would be cases where brash was used as information to identify the boundary. As a result of this discussion the group agreed at a consensus agreeing to specify asymmetric quartiles.

3.5 Scenario 5 – faulted boundary between granite and hard non-igneous rock

This scenario was discussed after a one-hour lunch break. The discussion to agree upper and lower bounds took 14 min. The individual and group elicitation of quartiles took 10 min. In both these discussions there was some debate as to whether the error distribution would be asymmetrical due to greater exposure of the country rock near the fault due to induration. However, the consensus agreed in the group elicitation was

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the exposure would be primarily due to increased weathering near recent faulting, and so not, in general, greater over one unit than the other. The consensus quartiles were therefore symmetrical.

3.6 Scenario 6 – boundary between two distinctive tills, unknown relationship

The discussion to agree upper and lower bounds took forty minutes. There was some disagreement as to whether such a scenario would be mapped in practice with units that are very similar, except in respect of colour and clast content. The modification of the scenario to specify the spacing between auger traverses allowed progress in the discussion. However, there remained disagreements. One participant, inclined to put wide bounds, thought that low-angle contact between the units could make the boundary very uncertain. While others accepted that the geometry of the contact is harder to visualize in this scenario than others, they thought that low-angle contacts would be a worse-case scenario rather than typical. On the basis of this discussion wide absolute bounds were agreed. However, in discussion after the individual elicitation, it was clear that a consensus was not possible. Three distributions are therefore presented, two reflecting strongly contrasting views of two participants (both with experience in superficial mapping), and the third a majority view.

The feedback session resulted in no substantial changes to the outcomes of the elicitation session. The participants agreed that the Gamma distribution for scenario 1 (Fig. 4) was most appropriate. As shown in Table 2 Participant D made a small modification to his quartiles for scenario 6 (individual distribution), but the basic disagreement over this scenario remained. It was agreed that the scenario was a difficult one, with many unknown factors that it would be hard to control with differences in approach between mappers, particularly over time.

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4 Discussion

This exercise showed that it is possible to use a method based on the SHELF framework to elicit the tacit model of uncertainty that geologists employ when interpreting linework. The general framework of the elicitation was workable, and the approach was accepted as meaningful by the five geologists from whom the distributions were elicited.

The group voiced a reservation about the extent to which distributions elicited for a general scenario could be usefully applied to individual instances of that scenario. For practical purposes it was thought that elicitations should be undertaken for more tightly framed situations such as a boundary between specific units in a particular region or mapsheet, or a fault near a frack zone or proposed site for a development. It was also thought that elicitation should include the field observation of settings of the problem. As the expert opinion on the valid application of the elicited tacit expert model this opinion must be considered carefully. However, it is also important to pay attention to the psychological research on the judgement heuristics which affect people's assessments of uncertain outcomes (O'Hagan et al., 2006). In particular the consideration of very specific settings, and even more so, of a necessarily limited number of field settings may serve to "anchor" expert judgement of particular statistics near values consistent with particular interpretations of a few boundaries and their field settings. It may also limit the range of possible conditions consistent with the elicited problem which the participants consider during the elicitation (accessibility judgement heuristic), which would result in elicited distributions which are too narrow. Further work is needed to compare elicited error distributions for geological boundaries in more or less narrowly defined sets of cases. One might also consider the possibility of considering substantial numbers of field locations in virtual field work in a 3-D visualization suite.

It is interesting and encouraging that the group of geologists, with experience in varied settings, were able to agree on consensus distributions for five out of six settings, the exception being a scenario in which two superficial units were mapped. In the elic-

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itation one could see both the influence of individuals (e.g. expert E in scenario 4 who convinced the group that the distribution should be asymmetric), and the way in which initially contrasting views converged during discussion. The process does not necessarily entail convergence to a what was initially a majority opinion, nor to some linear pool of these opinions. In a complex problem such as this the process of discussion to agree a consensus may be more robust than attempts to weight contrasting individual distributions numerically.

At the same time the process of elicitation was not dominated by single voices. While E influenced the group significantly on scenario 4, the consensus was somewhat different from his original individual distribution. This shows how the structured discussion in the elicitation procedure can help with convergence to a consensus which reflects the variation of individual experience within the group. The fact that some experts had more experience in particular settings than did others was explicitly recognized in discussion.

The one scenario in which a consensus was not achieved was a boundary between two contrasting superficial deposits. On reflection the group agreed that, in this case, the geometry of the contact represented by a boundary was harder to visualize than in the other cases with at least one solid geological unit. This may indicate that the approach is less applicable to superficial material, or that the scenario needs more careful description, perhaps with some visual examples.

It would be useful further research to find a case study where new geophysical measurements allow the identification of a boundary belonging to one of these scenarios over mapsheets where it has been surveyed in the field. This would allow us to compare the elicited error distribution with an empirically estimated one.

It is notable that there was considerable variation in the time taken for elicitation of each scenario. Not surprisingly, the first scenario took considerable time. In part this was because of complexities in the scenario itself, but it also reflects the time needed for familiarization with the process and associated concepts despite the briefing meeting and practice elicitation. Given this, there may be advantages in including a practice elicitation closer to the target problem. For example, in this case we might have under-

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taken a practice elicitation on the error distribution for a mapped fault. In each scenario the longest single component of the elicitation was the initial group discussion to agree limits for the boundary error. It was during this discussion that the group identified sources of uncertainty in the delineation of boundaries in the particular scenario.

The presence of the geological facilitator during the elicitation was important. The facilitator was able to make controlled changes to the scenarios during the elicitation, in particular adding elements to the description of the supporting field observations when participants raised queries. or adjusting elements of the initial description if participants thought these atypical. The statistical facilitator was also required, not just to operate the software but also to advise on questions such as interpretation of asymmetry in the distributions and to identify emerging confusions, such as a tendency to conflate the transect in the elicitation (which is a notional construct to frame the problem) with an actual transect in the original field survey. The meaning of errors of different sign required careful attention, and one topic for further work is whether it is better to consider the mapped boundary as fixed and the true boundary as variable (as here) or to fix the true boundary.

For purposes of this elicitation we considered what is effectively a 1-D model for boundary errors, specifically in terms of the intersection of boundaries with a notional transect. Further work is needed to make this approach fully applicable to the error in 2-D map polygons. The first issue is the uniformity of the error distribution along a boundary. Important details of the setting (such as the presence of exposures, or variations in land use) may vary along a single boundary. This increases the number of scenarios for which elicitation is required, and raised practical difficulties for how a distribution is selected for a particular problem from a set of available ones. Nonetheless, elicitation for many settings is more practically feasible than the empirical assessment of mapped boundaries. The more fundamental problem is how to treat the entire boundary of a polygon as an uncertain object. One possible approach would be based on the contour box-plots proposed by Whitaker et al. (2013) to characterize the uncertainty in multiple realizations of some isarithm such as a contour or isohyet. The concept of the

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"depth" of a particular isarithm in an ensemble might be used as a basis for elicitation of an uncertainty model of boundaries.

5 Conclusions

In conclusion, expert elicitation using the SHELF-based methodology provides a method to extract the tacit model which geologists use when interpreting linework. In particular, the SHELF approach based on a combination of individual and group elicitation, allowed our group to reach a consensus in five out of six scenarios. In several cases the final outcome was not the same as any one expert's initial distribution, indicating how the procedure allows us to arrive at a consensus through structured discussion. The elicitation process is most suitable for scenarios where the geometry of the contact represented by the boundary can be visualized by the experts. In our experience this precludes boundaries between superficial deposits.

Further work is needed to develop this approach. In particular we need to examine just how general a scenario can be used to elicit uncertainty models which are useable for the interpretation of specific boundaries. This could be examined by elicitations for scenarios of comparable generality to those reported here, and nested cases within each scenario which are more narrowly defined either in terms of lithology or specific units, or particular mapsheets in which the target boundaries appear. The panel felt that clearer visualization of the scenario, ideally in the field, would help. It would be interesting to explore how far this can be achieved given the need to avoid "anchoring" and to ensure that the expert panel accesses a sufficiently wide distribution of cases for any scenario. This might be achieved by visualization in 3-D virtual reality using DTMs with overlaid airphotography or satellite imagery. Associated validation of the elicited error model by geophysical inference of the location of a boundary at test locations would also be useful.

In addition to these general conclusions, we have drawn some practical conclusions for the use of elicitation. First, the use of a structured and transparent process is essen-

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tial. The SHELF framework ensures that there is a combination of individual thought and group discussion. In this trial the procedure ensured that ideas were pooled and that individual voices were heard but not allowed to dominate. Our experience showed that some general issues in the elicitation may arise only when specific examples are being tackled (hence the long general discussion which took place during the elicitation for the first scenario). This is probably inevitable, but it may be good practice to use a practice elicitation which is closer to the main target elicitation in character. Both the statistical and geological facilitator were essential to the process, as were figures to keep the disposition of units in front of the panel at all times. Finally, many of the key issues in the understanding of boundary error in any scenario emerged in the initial discussion on the feasible range of error values. Sufficient time must therefore be allowed for this part of the discussion.

Appendix:

Scenario descriptions as provided to participants. The uppercase codes in brackets indicate a range of possible lithologies for the units according to the BGS Rock Classification Scheme (Cooper et al., 2006). For some scenarios additional qualifications agreed during the elicitation are included, and indicated as such.

Scenario 1 – edge of river terrace deposit on bedrock

Back/uphill limit of a Quaternary river terrace deposit composed of brown sand and gravel (SV/XSV/SVZ/VS/XVS) resting on/against rockhead on a bedrock unit of contrasting lithology (Mesozoic/Cenozoic sedimentary rocks).

- Grassland, short cropped grass, scattered molehills.
- Traverse parallel to clear but not freshly dug/cleaned ditch 1 m deep.

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– Field is flat, with very subtle concave change/break-of-slope across the slope to gentle (< 2°) upward slope over 50 m distance.

– Field work included dutch augering every 15 m.

– *During the elicitation it was agreed that* no significant anthropogenic modification would be present at any instance of this scenario.

Scenario 2 – base of sandstone in mudstone/siltstone succession

Sharp or rapid-passage base of well-cemented grey-brown medium-grained silicate sandstone (SDST) bed 5 m thick within well-indurated grey mudstone +/- siltstone succession (Palaeozoic – e.g. Coal Measures/Millstone Grit).

– Urban street, approximately at right angles to strike.

– Beds dipping into slope.

– Sight of soil in 50 % of gardens.

– Quarry in the sandstone bed about 200 m away to one side exposes base, measurable dip, correctly shown on map with good contour information. No evidence of faulting in intervening ground.

– Street slopes up at about 4°, with subtle concave change/break-of-slope across the slope to steeper (7°) upward slope over a distance of 30 m.

Scenario 3 – edge of alluvium/tidal river deposit against contrasting underlying geology

Lateral limit of Holocene/modern alluvium/tidal river deposits composed of dark brown clay and silt (CZ/XCZ) resting on/against any contrasting superficial deposit or bedrock lithology.

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– Arable field, bare or short crops, soil easily visible.

– Field is flat, with conspicuous concave break-of-slope across the slope to moderate (< 5°) upward slope over 5 m distance.

Scenario 4 – Stratigraphic boundary between two distinctive sedimentary rocks

Stratigraphic boundary between two distinctive (by colour, grain-size, grain type and weathering habit) limestone (LMST/LMOOL/SALMST), or two sandstone (SDST/CALSST) or two chalk (CHLK) lithologies (Mesozoic sedimentary rocks).

– Arable field, bare or short crops

– Soil easily visible with sparse to dense brash of dirty angular pieces, some of which can be inferred to have been derived (by ploughing/cryoturbation etc.) from underlying bedrock, easily broken by hammer. A fair scattering of other stones – e.g. pebbles from nearby superficial deposits, brash of other local bedrock units, possible exotics (may be natural anthropogenics, concrete etc.)

– Field is sloping 2° to north-west, but gently undulating with no clear linear features.

– Regional dip is about 2° to south-east.

– Three small quarries within 200 m radius show tabular beds with dips of 0, 3° to 090 and 5° to 160.

– *During the elicitation it was agreed that* that the mapper does know the superposition relationship between the units.

Scenario 5 – faulted boundary between granite and hard non-igneous rock

Fault between large granite body and well-indurated sedimentary or metasedimentary rock succession. Assume fault is high angle and there is a single plane of displacement.

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– Moorland, long grass, heather etc. soil not generally visible, scattered large rock exposures spaced about 50 m apart – some may be ex situ. May detour up to 50 m to side.

– Uneven ground, some declivities, may form some alignments in various directions.

Scenario 6 – boundary between two distinctive tills, unknown relationship

Two juxtaposed Pleistocene tills of unknown superpositional relationship, with contrasting matrix colour/character – brown and smooth vs. grey and silty, and contrasting clast content – chalk, flint, quartz and quartzite pebbles and common igneous erratics vs. chalk, flint, underlying bedrock of mudstone and rare oyster fossils, very rare erratics.

– Arable field, bare or short crops

– Soil easily visible with sparse to dense scattering of till clasts and ploughed-up subsoil (weathered till clay matrix). A fair scattering of other stones – pebbles from nearby superficial deposits and probable anthropogenically-introduced stones.

– Field is flat with no linear features.

– Field work included dutch augering every 10 m.

– *During the elicitation it was agreed that* interpretation would be based on the assumption that augering traverses are 250 m apart. The notional transect for the elicitation crosses the boundary at a random location so does not necessarily coincide with a traverse.

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References

Albrecht, F., Lang, S., and Höbling, D.: Spatial accuracy assessment of object boundaries for object-based image analysis, in: Proceedings of GEOBIA 2010-Geographic Object-Based Image Analysis, edited by: Addink, E. A., and van Coillie, F. M. B., vol. XXXVIII-4/C7, Ghent University, Ghent, Belgium. 153

Bond, C. E., Lunn, R. J., Shipton, Z. K., and Lunn, A. D.: What makes an expert effective at interpreting seismic images?, Geology, 40, 75–78, 2012. 153

Brodaric, B., Gahegan, M., and Harrap, R.: The art and science of mapping: computing geological categories from field data, Comput. Geosci., 30, 719–740, 2004. 151, 152

Burrough, P. A.: Multiscale sources of spatial variation in soil. I. The application of fractal concepts to nested levels of soil variation, J. Soil Sci., 34, 577–597, 1983. 150

Burrough, P. A., Beckett, P. H. T., and Jarvis, M. G.: The relation between cost and utility in soil survey, J. Soil Sci., 22, 359–394, 1971. 153

Chrisman, N.: Theory of cartographic error and its measurement in digital data basesm, Proceedings of AUTO-CARTO, 5, 159–168, 1982. 152

Cooper, A. H., Kessler, H., and Ford, J.: A revised scheme for coding unlithified deposits (also applicable to engineering soils), British Geological Survey Internal Report IR/05/123, British Geological Survey, Nottingham, 2006.

Gong, P., Zheng, X., and Chen, J.: Boundary errors on digitized maps: an experiment on digitization errors, Lect. Notes Comput. Sc., 1, 65–72, 1995. 150, 152

Guillot, G., Kan-King-yu, D., Michelin, J., and Huet, P.: Inference of a hidden spatial tessellation from multivariate data: application to the delineation of homogeneous regions in an agricultural field, J. Roy. Stat. Soc. C-App., 55, 407–430, 2006. 153

Higgins, H. M., Dryden, I. L., and Green, M. J.: A Bayesian elicitation of veterinary beliefs regarding systemic dry cow therapy: Variation and importance for clinical trial design, Prev. Vet. Med., 106, 87–96, 2012. 155

Lark, R. M. and Beckett, P. H. T.: A geostatistical descriptor of the spatial distribution of soil classes, and its use in predicting the purity of possible soil map units, Geoderma, 83, 243–267, 1998. 152

Lark, R. M., Mathers, S. J., Thorpe, S., Arkley, S. L. B., Morgan, D. J., and Lawrence, D. J. D.: A statistical assessment of the uncertainty in a 3-D geological framework model, P. Geologist. Assoc., 124, 946–958, 2013. 153

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7, 147–184, 2015

Lark, R. M., Thorpe, S., Kessler, H., and Mathers, S. J.: Interpretative modelling of a geological cross section from boreholes: sources of uncertainty and their quantification, Solid Earth, 5, 1189–1203, doi:10.5194/se-5-1189-2014, 2014. 153

Lee, L. A., Pringle, K. J., Reddington, C. L., Mann, G. W., Stier, P., Spracklen, D. V., Pierce, J. R., and Carslaw, K. S.: The magnitude and causes of uncertainty in global model simulations of cloud condensation nuclei, Atmos. Chem. Phys., 13, 8879–8914, doi:10.5194/acp-13-8879-2013, 2013. 155

Leenhardt, D., Voltz, M., Bornand, M., and Webster, R.: Evaluating soil maps for prediction of soil water properties, Eur. J. Soil Sci., 45, 293–301, 1994. 151

Lillah, M. and Boisvert, J. B.: Stochastic distance based geological boundary modeling with curvilinear features, Math. Geosci., 45, 651–665, 2013. 153

Mandelbrot, B. B.: How long is the coast of Britain? Statistical self-similarity and fractional dimension, Science, 156, 636–638, 1967. 150

Martí, J., Aspinall, W. P., Sobradello, R., Felpeto, A., Geyer, A., Ortiz, R., Baxter, P., Cole, P., Pacheco, J., Blanco, M. J., and Lopez, C.: A long-term volcanic hazard event tree for Teide-Pico Viejo stratovolcanoes (Tenerife, Canary Islands), J. Volcanol. Geoth. Res., 178, 543–552, 2008. 154

Oakley, J. E. and O'Hagan, A.: SHELF: the Sheffield Elicitation Framework (version 2.0), School of Mathematics and Statistics, University of Sheffield, UK, available at: http://tonyohagan.co.uk/shelf, 2010. 155, 157, 158, 159, 160

O'Hagan, A. Buck, C. E., Daneshkhah, A., Eiser, J. R., Garthwaite, P. H., Jenkinson, D. J., Oakley, J. E., and Rakow, T.: Uncertain Judgements: Eliciting Experts' Probabilities, John Wiley and Sons, Chichester, 2006. 155, 158, 167

R Development Core Team: R: a language and environment for statistical computing, R Foundation for Statistical Computing, Vienna, Austria, ISBN 3-900051-07-0, available at: http://www.R-project.org/, 2013. 160

Ren, S. and Oakley, J. E.: Assurance calculations for planning clinical trials with time-to-event outcomes, Stat. Med., 33, 31–45, 2014. 156

Scholten, L., Scheidegger, A., Reichert, P., and Maurer, M.: Combining expert knowledge and local data for improved service life modeling of water supply networks, Environ. Modell. Softw., 42, 1–16, 2013. 155

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7, 147–184, 2015

Silan-Cárdenas, J. L., Wang, L., and Zhan, F. B.: Representing geographical objects with scale-induced indeterminate boundaries: a neural network-based data model, Int. J. Geogr. Inf. Sci., 23, 295–318, 2009. 153

Truong, P. N., Heuvelink, G. B. M., and Gosling, J. P. Web-based tool for expert elicitation of the variogram, Comput. Geosci., 51, 390–399, 2013. 154

Usher, W. and Strachan, N.: An expert elicitation of climate, energy and economic uncertainties, Energ. Policy, 61, 811–821, 2013. 155

Webster, R. and Beckett, P. H. T.: Quality and usefulness of soil maps, Nature, 219, 680–682, 1968. 151

Whitaker, R. T., Mirzargar, M., and Kirby, R. M.: Contour boxplots: a method for characterizing uncertainty in feature sets from simulation ensembles, IEEE T. Vis. Comput. Gr., 19, 2713–2722, 2013. 169

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Table 1. Agreed plausible range and initial individual quantiles for boundary error distributions under each scenario.

Scenario	Lower limit /m	Upper limit /m	Quantile /m	Expert A	B	C	D	E
1	−20	30	Q1	−5	−5	−10	−5	−15
			Median	5	0	0	0	−10
			Q3	20	5	15	15	10
2	−20	20	Q1	−8	−10	−10	−10	−5
			Median	0	0	0	0	0
			Q3	8	10	10	5	5
3	−4	1	Q1	−2.5	−2	−2	−2	−1
			Median	−1.5	0	−1	−1	0
			Q3	0	0.5	0	0	0.25
4	−75	75	Q1	−30	−30	−35	−40	−40
			Median	0	0	0	0	−20
			Q3	30	30	35	40	10
5	−25	25	Q1	−5	−20	−15	−10	−8
			Median	5	0	0	0	0
			Q3	15	10	15	10	8
6	−1000	1000	Q1	−30	−50	−75	−250	−100
			Median	0	0	0	0	0
			Q3	50	50	75	250	100

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Table 2. Group quantiles for each scenario and best-fitting distribution.

Scenario	Q1	Median	Q3	Distribution					
		/m		Type	Parameters		Mean /m	Percentile 2.5th	Percentile 97.5th
1	−10	−5	10	Beta	$a = 0.97$	$b = 1.56$	−0.02	−19.2	24.9
				Gamma[a]	$c = 1.90$	$s = 0.09$	0.0	−17.8	37.2
2	−8	0	8	Beta	$a = 1.53$	$b = 1.53$	0.0	−17.5	17.5
3	−2	−1	0	Beta	$a = 1.70$	$b = 1.21$	−1.07	−3.5	0.9
4	−35	−5	25	Beta	$a = 1.44$	$b = 1.62$	−4.45	−67.4	63.5
5	−9	0	9	Beta	$a = 1.87$	$b = 1.87$	0.0	−20.7	20.7
6(D)	−120[b]	0	120[b]	Normal	$\mu = 0$	$\sigma = 178$	0	−349	349
6(B)	−50	0	50	Normal	$\mu = 0$	$\sigma = 74$	0	−145	145
6(A,C,E)	−75	0	75	Normal	$\mu = 0$	$\sigma = 119$	0	−233	233

[a] The sum of squares for the fits of the Beta and Gamma distributions were very similar (6.3×10^{-3} and 6.5×10^{-3} respectively) so both are reported here and were presented to the panel at the feedback. The panel agreed unanimously that the Gamma distribution best represented their perception of uncertainty of the linework for this scenario.

[b] These are the only quantities that was adjusted during feedback. The expert in this group adjusted his quartiles to these values from −150 m and 150 m respectively.

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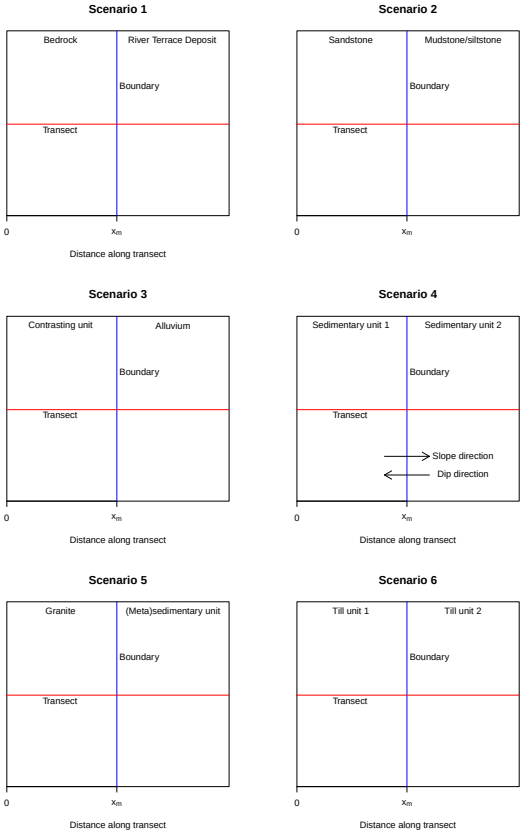

Figure 1. Diagrams indicating dispositions of units in each scenario with the mapped boundary shown as a blue vertical line and the notional transect as a red line, perpendicular to the boundary and with an origin on the left.

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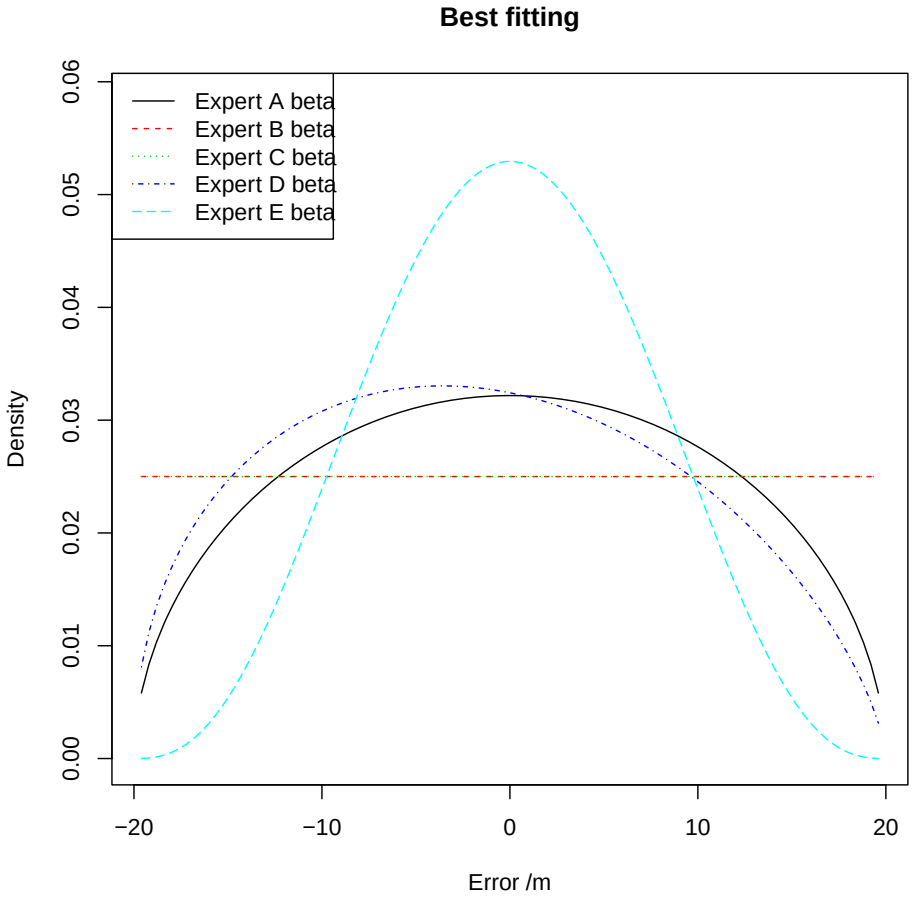

Figure 2. Individual best-fitting distributions for initial expert quartiles, scenario 2.

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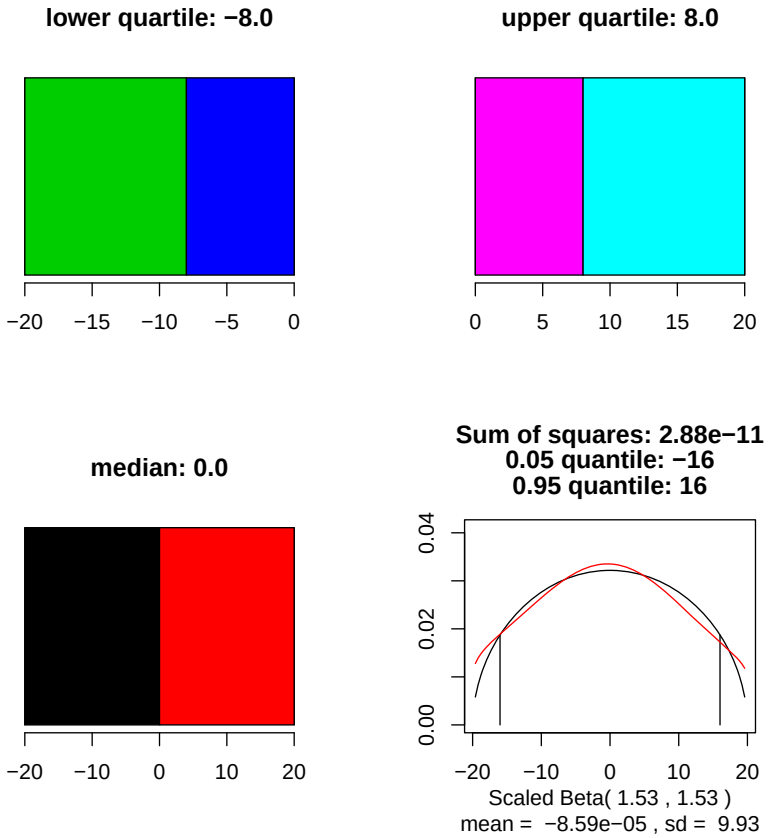

Figure 3. Feedback plot during group elicitation of the distribution for scenario 2.

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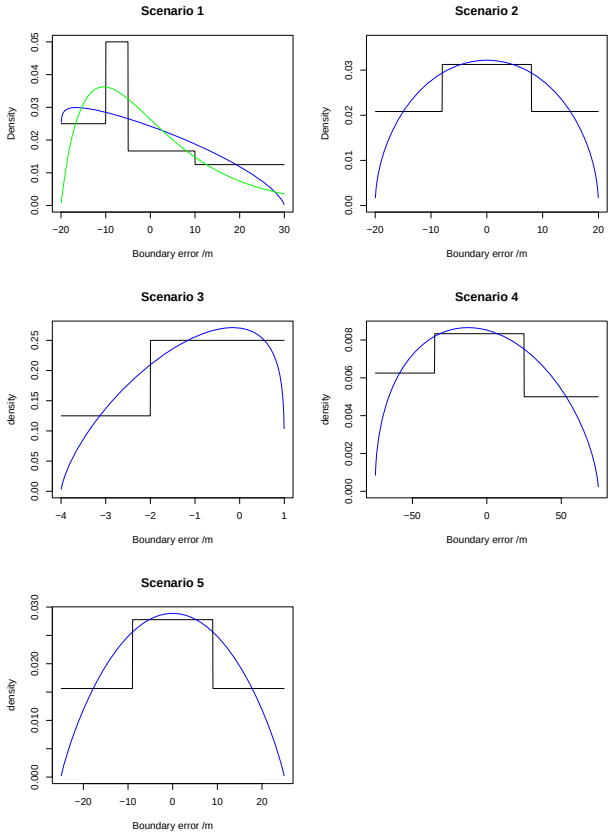

Figure 4. Best-fitting distributions for expert group quartiles, scenarios 1–5. Solid black line shows uniform density over elicited interquartile ranges, blue line show best-fitting distribution, green line shows closely competing alternative distribution.

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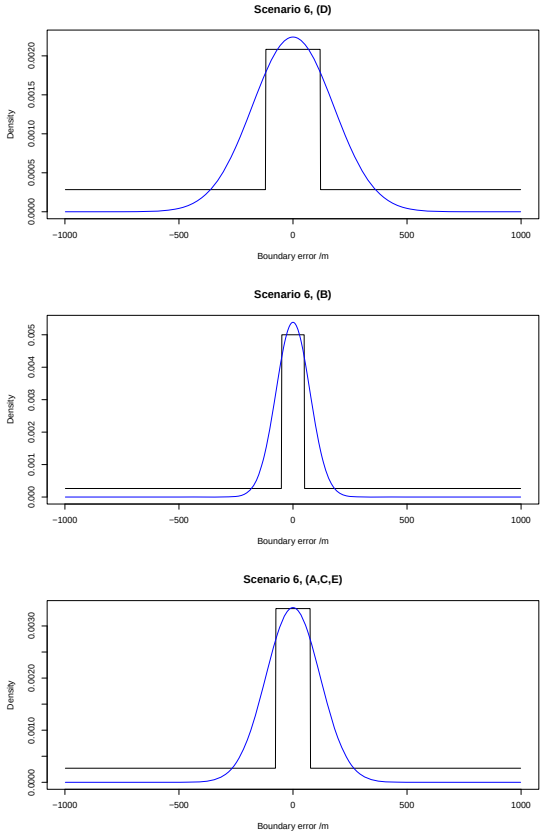

Figure 5. Best-fitting distributions for quartiles scenario 6 according to three expert subgroups (letters are expert codes). Solid black line shows uniform density over elicited interquartile ranges, blue line show best-fitting distribution.

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