A new methodology to train fracture network simulation using Multiple Point Statistics

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Abstract

Natural fracture network characteristics can be known from high-resolution outcrop images acquired from drone and photogrammetry. Such images might also be good analogues of subsurface naturally fractured reservoirs and can be used to make predictions of the fracture geometry and efficiency at depth. However, even when supplementing fractured reservoir models with outcrop data, gaps in that model will remain and fracture network extrapolation methods are required. In this paper we used fracture networks interpreted in two outcrops from the Apodi area in Brazil to present a revised and innovative method of fracture network geometry prediction using the Multiple Point Statistics (MPS) method.

The MPS method presented in this article uses a series of small synthetic training images (TIs) representing the geological variability of fracture parameters observed locally in the field. The TIs contain the statistical characteristics of the network (i.e. orientation, spacing, length/height and topology) and allow representing complex arrangement of fracture networks. These images are flexible as they can be simply sketched by the user.

We proposed to use simultaneously a set of training images in specific elementary zones of the Apodi outcrops in order to best replicate the non-stationarity of the reference network. A sensitivity analysis was conducted to emphasize the influence of the conditioning data, the simulation parameters and the used training images. Fracture density computations were performed on selected realisations and compared to the reference outcrop fracture interpretation to qualitatively evaluate the accuracy of our simulations. The method proposed here is adaptable in terms of training images and probability map to ensure the geological complexity is accounted for in the simulation process. It can be used on any type of rock containing natural fractures in any kind of tectonic context. This workflow can also be applied to the subsurface to predict the fracture arrangement and fluid flow efficiency in water, geothermal or hydrocarbon fractured reservoirs.

I] Introduction

I.1 The importance of the prediction of fracture network geometry

Fractures are widespread in Nature and depending on their density and their aperture, they might have a strong impact on fluid flow and fluid aquifers (Berkowitz, 2002; Rzonca, 2008), and in geothermal (Montanari et al., 2017; Wang et al., 2016) and hydrocarbon reservoirs (Agar and Geiger, 2015; Lamarche et al., 2017; Solano et al., 2010) They are typically organised as networks ranging from nanometre to multi-kilometre scale (Zhang, 2016), and present systematic geometrical characteristics (i.e. type, orientation, size, topology) that are

55 determined from specific stress and strain conditions. These conditions have been used to
56 derive concepts of fracture arrangements in various tectonic contexts and introduced the
57 notion of geological fracture-drivers (fault, fold, burial, facies). Based on these drivers it is
58 possible to some extent to predict reservoir heterogeneity and to define potential permeability
59 pathways within the rock mass (Lamarche et al., 2017; Laubach et al., 2018). Despite the
60 existence of these concepts, a range of parameters including fracture abutment relationships as
61 well as height/length distributions cannot be adequately sampled along a 1D borehole and are
62 mainly invisible on seismic images. In addition, fracture networks may present a spatial
63 complexity (variability of orientation or clustering effect) that is also largely unknown in the
64 subsurface. Long and Witherspoon, (1985) and Olson et al., (2009) showed how those
65 parameters impact the connectivity of the network and consequently affect fluid flow in the
66 subsurface. In outcrops, the fracture network characteristics can be observed in 2D and
67 understood directly. Consequently, outcrops are essential to characterize fracture network
68 attributes that cannot be sampled in the subsurface, such as length or spatial connectivity.
69
70 **I.2 Surface rocks as multiscale reservoir analogues**
71 In this context, the study of outcrop analogues is one of the few ways to constrain the
72 architecture of fracture networks (Bisdom et al., 2014; Bruna et al., 2017; National Research
73 Council, 1996; Lamarche et al., 2012; Lavenu et al., 2013). Outcrops can be considered as a
74 natural laboratory where the structural reality can be observed and quantified at various
75 scales. At the small – measurement station – scale (order of 10's m), fracture type,
76 chronologies and topology relationships can be characterised using classical ground-based
77 structural geology method such as scanlines (Lavenu et al., 2013; Mauldon et al., 2001). At
78 the intermediate – outcrop – scale (order of 10^2's m), length of fractures and geometry
79 variability can be qualified and quantified using unmanned aerial vehicles (UAV - drones).

Working on outcrops allows an understanding of the geological history of the targeted area and possibly to decipher how, when and where fractures were developed. In addition, outcrops constitute an efficient experimental laboratory where some of properties of the fracture network (i.e. fracture distribution, apertures, permeability and fluid flow behaviour) can be known and modelled (Bisdom et al., 2017). At the large – reservoir – scale (order of $10^{3\text{-}4}$m) satellite imagery and geophysical maps provide the characterisation of the 100's of meter long objects such as large fracture systems or faults.

However, not every outcrop can be considered as a good analogue for the subsurface. Li et al., (2018), in their work on the Upper Cretaceous Frontier Formation reservoir, USA, observed significant differences in the fracture network arrangement in subsurface cores compared to an apparent good surface analogue of the studied reservoir. In the subsurface, fractures appeared more clustered than in the outcrop where the arrangement is undistinguishable from random. The origin of these differences is still debated but these authors suggest that alteration (diagenesis) or local change in pressure-temperature conditions, may have contributed to the observed variability. The near-surface alteration processes (exhumation, weathering) may also contribute to misinterpretations of the characteristics of the network. In this case, one should be particularly careful while using observed networks to make geometry or efficiency (porosity, permeability) predictions in the subsurface. Therefore, the application to the subsurface of the characteristics observed in the outcrop is not always straightforward or even possible, and may lead to erroneous interpretations. Relatively unbiased signals such as stylolites or veins and particular geometric patterns build trust that the studied outcrop can be compared to the subsurface.

I.3 Modelling approaches classically used to model fracture network geometries

104 The widely used discrete fracture network (DFN) stochastic modelling tools provide
105 statistical representation of fracture networks constrained generally by univariate and random
106 distribution of orientation, size, spacing and density/intensity data (Bisdom et al., 2014;
107 Bisdom et al., 2017; Huang et al., 2017; Panza et al., 2018). The generated models follow a
108 local stationarity hypothesis. This implies that the statistics used during the simulation are
109 constant in the defined area of interest (Deutsch and Journel, 1997; Gringarten and Deutsch,
110 1999; Gringarten and Deutsch, 2001; Journel and Zhang, 2006). Liu et al., (2009), highlighted
111 the implicit randomisation that conventional DFN models produce and demonstrated that
112 parameters like fracture connectivity are poorly considered in these representations. In
113 addition, it is generally admitted that discrete realisations of thousands of fracture objects at
114 the kilometre scale are computationally very demanding and often even impossible (Jung et
115 al., 2013). Some authors attempted to use a pixel-based method to try to predict fracture
116 network geometries. Bruna et al., (2015), used a dense hydrogeological borehole survey
117 sampling a Lower Cretaceous aquifer in the SE of France to define fracture facies and to
118 model their distribution with two-points geostatistics. In this case, the amount of available
119 data and their consistency helped to provide realistic results. However, far from conditioning
120 data (i.e. boreholes) the fractures simulation are poorly constrained.
121 The work of Hanke et al., (2018) uses a directional semi-variogram to quantify fracture
122 intensity variability and intersection density. This contribution provides an interesting way to
123 evaluate the outputs of classical DFN approaches but requires a large quantity of input data
124 that are not always available in the subsurface. To represent the fracture network geometry in
125 various geological contexts, an alternative method has to be developed. This innovative
126 method needs to i) explicitly predict the organisation and the characteristics of multiscale
127 fracture objects, ii) take into consideration the spatial variability of the network and iii)
128 require a limited amount of data to be realised.

129

130 **I.4 Multi-point statistics as an alternative to classic DFN approaches**

131 Since Liu et al., (2002), few authors highlighted the potential of using multi-point statistics
132 (MPS) to generate realistic fracture networks (Chugunova et al., 2017; Karimpouli et al.,
133 2017). Strebelle, (2002) showed how the MPS are able to reproduce any type of geological
134 heterogeneities of any shape at any size as long as they present a repetitive character. This
135 characteristic seems particularly well adapted to predict the geometry of a fracture network.
136 The MPS method uses training images (TI) to integrate conceptual geological knowledge into
137 geostatistical simulations (Mariethoz, 2009). The TI is a grid containing geological patterns
138 that are representative of a certain type of geological structure, type and arrangement. The TI
139 can be considered as a synthetic model of the geological heterogeneity (i.e. all the elements
140 characterising a geological object) likely to occur in a larger domain (i.e. reservoir, aquifer,
141 outcrop). The TI must contain the range of geobodies that are intended to be modelled, as well
142 as the relationship these geobodies have with each other (Mariethoz, 2009; Strebelle, 2002).

143

144 **I.5 Objectives and contents of this research**

145 In this paper we propose a MPS workflow considering the geological variability of the
146 fracture network geometry in outcrops (size order of 100m) and a methodology on how to use
147 this method at the reservoir scale. The approach is based on the direct sampling method
148 (Mariethoz et al., 2010) and uses multiple TIs for a single realisation (Wu et al., 2008). The
149 concept of the probability map has been revised here to define where a training image should
150 be used in the simulation grid. Our outcrop-based simulations also take into account "seismic-
151 scale" objects (i.e. object longer than 40m) considered as hard conditioning data. The
152 proposed workflow is tested on outcrops where fracture network have been previously
153 characterised and interpreted from drone imagery. The studied outcrops are considered as

analogues of the Potiguar Basin, Brazil (Bertotti et al., 2017; Bisdom, 2016). Uncertainties were evaluated by comparing original outcrop interpretation (done manually by a geologist) with the geometrical characteristics of the network generated from MPS. To evaluate the quality of the simulations, we computed density maps in outcrop fracture interpretation and on selected stochastic models. The proposed approach is innovative and provides a quick and efficient way to represent fracture network arrangements at various scales.

II] Methodology

II.1 The direct sampling method

The direct sampling method (DS) was introduced by Mariethoz et al., (2010). Figure 1, synthesizes the DS modelling process developed thereafter. The method requires a simulation grid where each node is initially unknown and called $\boldsymbol{x}$, a training image grid (TI) where each node is known and called $\boldsymbol{y}$ i.e. V(y) is defined where V is the variable of interest (e.g. facies value). The simulation proceeds as follows. First, the set of conditioning data (if present) is integrated in the simulation grid. Then, each remaining unknown node $\boldsymbol{x}$ is visited following a random or defined path, and simulated as follows. 1) The pattern $\boldsymbol{d_n(x)} = \boldsymbol{(x_1,V(x_1)),\ldots,(x_n,V(x_n))}$ formed by the at most **n** informed nodes the closest to $\boldsymbol{x}$ is retrieved. Any neighbour $\boldsymbol{x_i}$ of $\boldsymbol{x}$ is either a previously simulated node or comes from the conditioning data set. The lag vectors $\boldsymbol{h_i} = \boldsymbol{x_i}\text{-}\boldsymbol{x}$ define the geometry of the neighbourhood of $\boldsymbol{x}$. The combination of the value and position of $\boldsymbol{x}_i$ defines the data event or pattern $\boldsymbol{d_n(x)}$. 2) Then, the TI is randomly scanned to search for a pattern $\mathbf{d_n(y)}$ similar to $\mathbf{d_n(x)}$. For each scan node $\boldsymbol{y}$, the pattern $\boldsymbol{d_n(y) = (y_1,V(y_1)),\ldots,(y_n,V(y_n)),}$ where $\boldsymbol{y_i}=\boldsymbol{y}+\boldsymbol{h_i}$, is compared to $\mathbf{d_n(x)}$ using a distance (Meerschman et al., 2013). When the distance is lower than an acceptance threshold ($\boldsymbol{t}$) defined by the user or if the proportion of scanned nodes in the TI reaches a maximal fraction

178 (**f**) defined by the user, the scan is stopped and the value of the best candidate ***y*** (pattern with
179 the minimal distance) is directly attributed to ***x*** in the simulation grid (i.e. ***V(x) = V(y)***).
180 As the DS method does not use a catalogue of all possible patterns found in the TI, it is
181 extremely flexible and in particular allows taking into account both categorical and
182 continuous variables and managing multivariate cases, provided that the pattern distance is
183 suitable. In this paper we are using the DeeSse version of the direct sampling code
184 (Straubhaar, 2017).
185
186 **II.2 Multiscale fracture attributes**
187 To evaluate how the direct sampling method deals with the fracture network, the present
188 experimentation is based on outcrop data where the present-day structural reality is
189 observable at various scales. Pavements (i.e. horizontal surfaces in the order of 10^2 m scale)
190 were targeted because they contain important information that is not always accessible with
191 vertical outcrops (Corradetti et al., 2017a; Corradetti et al., 2017b; Tavani et al., 2016) or with
192 geophysical imagery (e.g. seismic data). The size of pavements allow the user to interpret a
193 large amount of fracture and to define areas where the geometry of the network varies (Bruna
194 et al., 2018). Pavements also allow to obtain quantitative data on fracture lengths, which are
195 usually difficult to get in vertical cliff. In the subsurface, data can be provided by geophysical
196 3D maps and fracture attribute detection tools (Chopra and Marfurt, 2007; Somasundaram et
197 al., 2017). However, these tools are not always available and detect the longer lineaments
198 only.
199 Working with pavements constitutes an asset as small-scale investigation can be conducted in
200 key zones of the outcrop (i.e. in folded areas, each compartment or dip domain of the fold
201 should be imaged and investigated in detail where the gathered data will help to calibrate
202 larger scale information. Classical fieldwork methods (observation and characterisation,

measurements, statistical analyses, sampling) help interpreting fracture families and are essential to constrain larger scale observation.

In this study, UAV-based photogrammetry is used to obtain an orthorectified mosaic and 3D digital outcrops models (Bemis et al., 2014; Claes et al., 2017; Vollgger and Cruden, 2016). The scale of these images is an intermediate between the scale of measurement station and that of satellite imagery. Digitization of fracture traces, geological contacts, sedimentary structures and structural domain boundaries are currently processed by hand and represent a considerable time investment. In this contribution, fractures were interpreted in orthomosaic images with the help of GIS software. Length, azimuth, fracture family proportions and fracture density statistics were extracted from the interpretation. In addition, a series of measurement station (area of about 2 × 2 m) information was acquired and compared with the dataset from the drone imagery in order to align interpretations and provide coherent fracture history.

II.3 Training images, conditioning data and probability maps

- **Training images**

Training images (TI) are the base input data of the MPS simulation. Building them is a critical step to succeed a realisation (Liu et al., 2009). The TI is a pixelated image based on a local interpretation of a geological phenomenon (i.e. an interpreted photography taken from a local zone of interest in the field) or digitised by a geologist and based on geological concepts (Strebelle, 2002). As the MPS algorithms borrow patterns from the TIs to populate the simulation grid, one should use TIs synthesising all of the recognized geological parameters that characterise the area to simulate. To model non-stationary fields, i.e. fields where the characteristics of the patterns differ depending on their location, one can follow two strategies. The first one consists in using a non-stationary TI containing all wanted spatial

features. This requires to build one or several auxiliary variables describing the non-stationarity in the TI and to define these auxiliary variables in the simulation grid to constrain the simulation and indicate which kind of patterns will be simulated in which locations (Chugunova and Hu, 2008; Mariethoz et al., 2010; Straubhaar et al., 2011). The second approach consists in using several stationary TIs, each one depicting the same kind of patterns everywhere, and defining zones in the simulation grid corresponding to each specific TI. This second approach is chosen in this work, because it allows to define simple geological concepts (TIs) specific to regions delineated in the simulation domain. The facies proportions and their spatial arrangement belongs to each TI and can vary from one image to the other (figures 5, 6, 9 and 10). Each TI has a local impact on the simulation. Moreover, in our approach fractures sets are grouped in facies in the TI, based primarily on their orientation and possibly on their length or additional parameters defined by the user. The fractures classification helps reproducing patterns and simplifies the process of building the TIs. Note also that two TIs used for two adjacent zones should share some common features in order to obtain realistic transitions between the regions in the simulation domain.

- **Conditioning data**

One limitation of the MPS methods is the tendency to disconnect long continuous objects (i.e. typically fractures, Bruna et al., 2017). To manage this issue, long fractures can be identified and incorporated into the simulation as conditioning data. As per the training images, such data can be integrated as pixelated grids. They may come from satellite imagery or they can be interpreted from gravity or magnetic surveys or from 3D seismic imagery (Magistroni et al., 2014).

- **Probability map**

The direct sampling method can be used with multiple training images. In this situation, the user provides a set of TIs, and for each TI a probability map is defined on the simulation grid,

giving at each node the probability to use that TI. The pixel-wise sum of these maps should then be equal to one in every node. If each TI corresponds to a partition of the area of interest, with for each TI one elementary zone, covering the whole simulation grid, the probabilities in the map are set to one for specific TI and to zero for the other ones.

As per the training images, the probability map comes from a simple sketch (i.e. a pixelated image) given by the MPS user. It is based on the geological concepts or interpretations that define the geometry variability over the simulated area and that allow a partition of the outcrop. In each of the zones defined in the area of interest, the simulated property will follow the intrinsic stationarity hypothesis (Gringarten and Deutsch, 2001; Journel and Zhang, 2006; Journel, 2005) but the entire domain will be non-stationary.

While working on outcrops, the partition of the area of interest can be decided based on observations. For instance, when the fracture network interpreted from outcrop images is available, the geologist can visually define where the characteristics of the network are changing (fracture orientation, intensity, length, topology) and draw limits around zones where the network remains the same (internal variability, Hooker and Katz, 2015). However, in other cases outcrops or subsurface observation could be discontinuous between observation sites. If the data are sparse and come mainly from fieldwork ground observations or boreholes, the use of alternative statistical approaches can help to provide a robust and accurate partition of the area of interest. The work of Marrett et al., (2018) interprets the spatial organisation of fractures using advanced statistical techniques such as normalized correlation count and weighted correlations count, on scanlines collected in the Pennsylvanian Marble Falls Limestone. In their approach, the periodicity of fracture spacing (clustering) calculated from the mentioned techniques is evaluated using Monte Carlo to quantify how different the fracture networks are from a random organisation. These approaches can be highly valuable during the process of building a probability maps when less data are

available. The probability maps provide a large-scale framework that may be refined and modified with additional data such as measurement stations or drone surveys coming from surface exploration or wells data containing fracture network information.

II.4 Testing the simulated network: from pixels to segments

MPS realisations are produced as pixelated images. To evaluate the resulting fracture network, pixels alignments corresponding to fractures are extracted as discrete straight-line objects defined by start and end points. Fractures are separated from the background and in different sets by automatic image classification methods. On grayscale images, this is obtained by multilevel image thresholding through the Otsu's method (Otsu, 1979). On color images, fracture sets are classified based on their color components with the k-means clustering algorithm built in MATLAB (Lloyd, 1982). Image classification gives in output a series of binary images, one for each fracture set, where lineaments are represented as foreground (Kovesi, 2000).

III] Results: test case on analogues of the Potiguar Basin, E Brazil

III.1 Geological setting

The Potiguar Basin is a rift basin located in the easternmost part of the Equatorial Atlantic continental margin, NE Brazil (fig. 2). The basin is found both onshore and offshore (fig. 2). The basin was generated after the initiation of the South American and African breakup during the Jurassic - Early Cretaceous times. It was structured by a first NW-SE extension stage latterly rotating to an E-W extensional direction (Costa de Melo et al., 2016). The rift basin displays an architecture of horsts and grabens striking NE-SW and bounded towards the east and south by major fault systems (de Brito Neves et al., 1984), fig. 2). The Potiguar Basin displays three sedimentary sequences deposited since the Early Cretaceous (i.e. syn- and post

rift depositions). The last post-rift sequence was deposited since the Albian and encompasses the Cenomanian-Turonian Jandaíra Formation. This formation consists of up to 700 m thick bioclastic calcarenites and calcilutites deposited in transgressive shallow marine environment. From the Campanian to the Miocene, the compressive principal stress was oriented N-S (Bertotti et al., 2017). From the Miocene to the Quaternary the onshore part of the Potiguar basin was uplifted. Synchronously, a new compressive stress field was established trending to a NW-SE direction (Reis et al., 2013).

III.2 Outcrop data

The area of interest measures 2.1 × 1.3 km and is located about 25 km NE of the city of Apodi in the Rio Grande Do Norte state (fig. 2). It contains two outcrops AP3 and AP4 (Bertotti et al., 2017; Bisdom, 2016, fig. 2) here defined respectively as 600 × 300 m and 400 × 500 m large pavements localized in the Jandaíra Formation. AP3 and AP4 crop out as pavements with no significant incision. The outcrops are sparsely covered by vegetation and consequently they present a clear fracture network highlighted by karstification. In 2013, images of AP3 and AP4 were acquired using a drone (Bisdom, 2016) and processed using the photogrammetry method. Two high-resolution ortho-rectified images of these pavements (centimetre-scale resolution) were used to complete fracture network interpretation and to extract fracture parameters. In AP3, 775 lineaments were traced (fig. 3) and in AP4, 2593 (fig. 4). These lineaments collectively termed fractures in this paper. For each of these outcrops three fractures sets were identified: set1 striking N135-N165, set2 striking N000-N010/N170-N180 and set 3 striking N075-N105. Fractures falling outside of these ranges were not considered in the input data. Consequently, in AP3 we considered 562 only (out of 775 fractures traced in the pavement) and in AP4 we considered 1810 only out of 2593 fractures. In addition, ground-based fieldwork was conducted in AP3 and AP4 to understand the

328 structural history of the area and to calibrate the interpretation conducted on the drone aerial
329 photography. General location and fracture data are presented in figure 3 and 4 and in table 1.
330 In AP3, sets 1 and 2 are distributed over the pavement. However, their intensity is variable in
331 the area of interest. Set 3 is mainly expressed in distinct regions of the outcrop. Small-scale
332 investigations (conducted on measurement stations in the outcrop) showed that set 3 is
333 composed of stylolites and sets 1 and 2 of veins. In addition, sets 1 and 2 present evidences of
334 shear movements and are then considered as a conjugate system.
335 In AP4 small-scale investigations highlight the same characteristics as the ones observed in
336 AP3. Although the conjugate system (set 1 and set 2) is less developed there than in AP3. It is
337 also notable that more crosscutting relationships were observed in AP4 compared to AP3.
338
339 **III.3 Input data for MPS simulation**
340 To evaluate the effect of conditioning data, results of two simulations were compared, with
341 and without conditioning data. The sensitivity of simulation parameters was investigated by
342 varying i) the number of neighbours defining patterns (data events $\boldsymbol{d_n}$), ii) the acceptance
343 threshold ($\boldsymbol{t}$) defining the tolerance the algorithm authorises to find a matching data event in
344 the simulation grid (Mariethoz et al., 2010) and iii) the fraction of the TI to be scanned during
345 the simulation process to search for data events. Results of this sensitivity analysis help to
346 propose the best possible simulation for AP3 and to optimise the choice of input parameters
347 for AP4 fracture simulation.
348 AP3 presents intrinsic fracture network geometry variability. This observation emphasizes
349 that averaging fracture parameters on the entire domain is not well suited to represent the
350 complexity of the network. We observed that the length of fracture per sets and the density of
351 fractures are parameters that vary the most here. The analysis of these variations allow to
352 partition AP3 and AP4 in elementary zones and to synthesize the fracture network

353 characteristics in each of these domains. The following section defines how the TI,
354 probability map and conditioning data were built.

355 • **Partitioning, training images and probability map for AP3 and AP4**

356 We divided AP3 in 5 elementary zones (EZ) based on visual inspection of the pavement (fig.
357 5A-B). The number of fractures per EZ is synthesized in figure 5. The proportion of fracture
358 per elementary zone is available in table 1. A limited part of the fractures belongs to two
359 adjacent elementary zones. This issue is quantified in table 1.

360 A probability map with sharp boundaries (fig. 5B) was created for AP3. Sharp boundaries are
361 justified by the variability of the network geometry, which is known from the visual
362 inspection of the interpreted image. Smooth transitions could also be defined (see discussion).
363 The input data to build the probability map is an image of the partition of the area of interest
364 containing the different outcrops. In this image, the indexed zones (elementary zones EZ) are
365 characterised by a distinctive colour.

366 At the scale of a reservoir where some outcrops analogues and fracture tracing may be
367 available, the interpreted reality of the network (e.g. a binary fracture/non-fracture image) can
368 be directly used as a training image. We chose to ignore the tracing and to rely on parameters
369 that are attained through field observation without having access to drone images of an entire
370 outcrop (i.e. orientation, spacing, abutment) and to compare the interpretation with the
371 simulated network. In that respect fracture orientation were averaged to a single value. Hence,
372 set 1 strikes N090, set 2 strikes N150 and set 3 strikes N180. According to the outcrop
373 partitioning, five training images were created (fig. 5C). In each training image, three facies
374 corresponding to the three fracture sets were created. Set1 is green, set 2 is red and set 3 is
375 blue (fig. 5C). The topology is a crucial problem in fracture simulations because it influences
376 the connectivity of the network. In the MPS simulations the abutments are particularly well
377 reproduced as they represent singular pixels arrangements that are efficiently taken into

account. However, crosscutting relationships imply the use of a different facies at the intersection locus. This method respects and reproduces intersections during the simulation process. In AP3, the analysis of the topology relationships showed three main crosscutting interactions:

- Long fractures from Set 2 and Long fractures from Set 3 mutually crosscut (conjugated sets)
- Set 3 crosscut Set 1
- Set 2 crosscut Set 1

To take into account these topological parameters a different facies colour was attributed to the crosscutting locus (the crossing facies, fig. 6). When the MPS realization will be later discretized, the younger fractures will be truly represented as continuous segments. The older fractures will be cut in pieces but their alignment will be, in most of the case, maintained during the simulation process.

- **Dimensions of the simulation grids and of the training images**

The dimensions of the simulation grid for AP3 and of each training image (in pixels) are shown in fig.5. The number of pixels is automatically determined by the size of the original drawing made by the geologist.

The size of the input training image does not generally influence the simulation. However, it has to be chosen sufficiently large with respect to the complexity of the patterns in order to get reliable spatial statistics. The DS method tends to identify patterns (i.e. $\boldsymbol{d_n}$'s see above) in the TI and to paste the central node of them into the simulation grid. However, at a constant resolution and specifically for fractures patterns, it is likely that a 50 × 50 m training image will carry more complexity and variability than a 10 × 10 m one. This parameter should be taken into consideration when starting digitizing training images, especially when spacing between fractures is not consistent across the simulation grid.

- **Long fractures conditioning**

Because the MPS method has the tendency to cut long individual segments into smaller pieces, the fractures longer than 40 meters – the ones visible from satellite/drone imagery in AP3 – were isolated and considered as hard conditioning data (fig. 5D). This threshold was arbitrarily determined from the dataset we have. In AP3, less than 8% of the fractures are longer than 40 m.

In AP3, long fractures belong only to the sets oriented/striking N180 or N150 (fig. 5D). 18 N180 fractures (3% of the whole) and 30 N150 fractures (5% of the whole) were digitized and integrated as conditioning data in the simulation.

III.4 Outcrop scale simulations

III.4.1 Impact of conditioning data on AP3 simulations

In AP3, the 48 long fractures were manually digitized and imported into the simulation grid as categorical properties to be considered as hard conditioning data during the MPS simulation process. The MPS simulation is consequently in charge of stochastically populating the smaller factures within the grid.

Results of the influence of these data are presented in figure 7. The principal simulation parameters in the considered scenarios (with and without conditioning data) were set up identical (constant acceptance threshold (5%), constant percentage of scanned TI (25%) and constant number of neighbours (50)).

Results showed that the realisation without conditioning data creates 20% less number of fractures than the original outcrop reference. The simulation with conditioning data creates 9% less number of fractures than AP3, which allow to better replicate the long fracture than a non-conditioned simulation. It is also remarkable that the non-constrained simulation represents only 23 fractures above 40 meters (compared to the 48 long fractures interpreted on

428 the AP3 outcrop). In this simulation the long fractures are essentially located in the zone 3 of
429 the outcrop. Because the simulation is a stochastic process, the location of the long fractures
430 is randomly determined in the absence of hard conditioning data. Considering hard-
431 conditioning data also gives a more realistic representation of the fracture network.
432
433 **III.4.2 Sensitivity analysis on the AP3 simulation parameters**
434 • **Simulation parameter set-ups, duration and analyses conducted on the results**
435 Simulation parameters were varied for each simulation in order to emphasize their effect on
436 each realisation. One realisation per test was performed during this analysis. The goal of this
437 analysis is to show how the different parameters influence the reproduction of fracture
438 segments and not to evaluate how good is the matching between the simulation and the
439 reference.
440 The MPS realisations are pixelated images. The sensitivity analysis is based on the discrete
441 segments extracted from these pixelated images (see II.4). All of the simulations present a
442 variable percentage of segment lengths that are below the minimal fracture length interpreted
443 in the AP3 outcrop (i.e. simulation noise). Consequently all segments smaller than 2.2m
444 where removed from the simulation results. A length frequency distribution was compiled for
445 each of the generated simulations.
446 The influence of the number of neighbours was evaluated trough 7 simulations (SIM1 to
447 SIM7). The acceptance threshold and the number of neighbours was investigated by
448 comparing 8 simulations (SIM8 to SIM15) where the scanned fraction of the TI was fixed at
449 25%. The percentage of the scanned fraction of the TI was combined with the two other
450 simulation parameters. This combination was tested over 12 simulations (SIM16 to SIM27).
451 The models set-ups and the duration of the simulations are presented in (table 2). It is notable
452 that SIM8 / SIM9, SIM10 / SIM11 and SIM13 / SIM14 produce exactly the same network

453 despite the modification of the simulation parameters. Also The MPS algorithm successfully
454 performed SIM16 but the segment extraction generated an error preventing the discretisation
455 of all of the objects.
456 The total amount of generated fractures segments was counted and compared with the total
457 amount of fracture traces interpreted from the original outcrop. A deviation of 10% compared
458 to the original amount of interpreted fractures is considered as a satisfactory result as it is very
459 close to the reference amount of fractures. A deviation of 20% compared to the original
460 amount of interpreted fractures is considered as an acceptable result. This deviation is
461 consequent but can be adjusted by varying the simulation parameters. A deviation above 20%
462 was rejected as a complete reconsideration of the parameters is required. Results are
463 synthesized in table 3.
464 The total amount of segments was initially counted in the entire simulation domain. The sum
465 of segments per part is constantly higher than the initial total amount of segments because
466 segments cutting a sharp boundary are divided in two - segments falling within two
467 elementary zones and are consequently counted twice. The number of generated fractures per
468 simulation zone was also computed and the same deviation thresholds were applied to
469 evaluate if the simulation is satisfactory, acceptable or rejected. Tables 4 to 6 synthesize the
470 sensitivity analysis conducted of 27 realisations of the AP3 outcrop.
471 The length of the segments have been computed for each realisation and are presented in
472 figure 8.
473 The influence of the hard conditioning data and of the drawing of the training image was also
474 quantitatively investigated and compared respectively with the length of the generated
475 segments and with the amount of segments generated per zone.
476 • **Summary of the results**

Increasing the number of neighbours lengthens the computation time (table 2, SIM 1 to 7). A small amount of neighbours results in a noisy simulation (table 2, SIM1). The contrary leads to a downsampling of the generated segments that become longer than the interpreted fractures in AP3 (table 2, SIM7). Decreasing the acceptance threshold leads to an increase of the simulation time (table 2 SIM8-15). Increasing the scanned fraction of the TI is the most time consuming operation (table 2 SIM17-27).

Increasing the number of neighbours only is generally not sufficient to accurately generate a satisfactory or acceptable total amount of fractures (table 3). Increasing the scanned fraction of the TI produces in all cases the closest total number of fractures compared to the reference outcrop (table 3).

The counting of fractures in simulation zones revealed that set 2 and set 3 in zone 1, set 3 in zone 4 and set 1 in zone 5 are generally underestimated during the simulation process. In contrast, fracture set 1 in zone 2 is generally overestimated. The consistency of the error over almost the entire set of simulations indicates an issue on the training image representation (table 4-6). Increasing the scanned fraction of the TI generally allows to better represent a low proportion of fracture facies within a TI (Zone TI5, set 2, table 6).

An acceptance threshold below 5% leads to an overestimation of the number of small fractures (between 0-10 m), fig 8. In this case, amount of segments between 0-20 m is generally close to the reality. Increasing the scanned fraction of the TI produces the highest quantity of fractures ranging from 0-10 m (fig. 8). Increasing the number of neighbours and the percentage of the scanned TI will result in an increase of the length of the fractures used as hard conditioning data. However, the fracture elongation does not affect all of the hard conditioned fractures and represents a very small percentage of the whole modelled fracture network.

III.4.3 Attempt at an optimisation: OPT1

OPT1 was parameterised in regard of the previous observations in order to generate a simulation that is the closest-to-reality possible. For this purpose, the amount of fractures from set 2 and set 3 drawn in TI1 and set 3 drawn in TI4 was increased. In contrast, the amount of fractures from set 1 drawn in TI2 was decreased significantly (fig. 9). We choose to setup the number of neighbours at 50 and the acceptance threshold at 2%. TI1 and TI4 will be scanned at 75% and the rest of the TIs will be scanned at 50% (table 2).

The simulation time for the proposed simulation is 2 min 31s (table 2). The total amount of generated fractures is satisfactory compared to the amount of fractures interpreted in the original outcrop.

To evaluate the robustness of the optimised simulation, 6 realisations using the same parametrisation were generated for OPT1. The total amount of fractures generated for these simulations always fall below the 10% deviation compared to the reference outcrop.

The number of segments comprised between 0-20 m in OPT1 is slightly above the satisfactory deviation limit. As per all the generated simulations, the number of fractures between 2.21 m and 10 m is largely overestimated.

OPT1 contains a more satisfactory and acceptable fracture count than any other simulation generated before (table 6). The amount of segments generated in zone 1 and 2 for set 1 is slightly overestimated. In zone 3, OPT1 fails to represent the amount of fractures for set 1 (25% deviation) and for set 3. Fracture set 1 in zone 4 is largely overestimated.

III.4.4 Evaluation of the AP3 and OPT1 simulations: P_{21} calculations

Uncertainty analysis is required when performing simulations of geological parameters, especially far from data. The sensitivity analysis presented in this paper is a way to compare the MPS simulations with the reference outcrop.

To reinforce the evaluation of the proposed method, we quantified the values of fracture intensity in the reference outcrop, in three selected AP3 MPS simulations and in the optimised simulation (OPT1) (fig. 10). The fracture intensity was classified by (Dershowitz and Herda, 1992) in regard of i) the size and dimension (1D, 2D, 3D) of a selected zone of interest and ii) the number, length, area or volume of fractures within this selected zone. In this paper, we chose to calculate the P_{21} fracture intensity, which corresponds to the sum of all fracture lengths within a regularly discretized space, with constant area boxes (10 × 10 m) covering the entire AP3 area of interest.

Visually, the results show an apparent higher P_{21} intensity in the reference outcrop than in the simulations. However, zones of high intensity in the reference outcrop are generally well represented in SIM26 and in OPT1. This is in agreement with the results of the sensitivity analysis showing that SIM26 and OPT1 best represent the number of fractures present in the reference outcrop.

The average fracture intensity in each simulation has also been computed and confirms the observations conducted during the sensitivity analysis. SIM1 and SIM7 present the lowest average fracture intensity (0.095 m^{-1} and 0.079 m^{-1} respectively) and SIM26 and OPT1 present the highest fracture intensity (0.11 m^{-1} and 0.099 m^{-1} respectively). The average fracture intensity in the reference outcrop is higher than in any other simulations (0.126 m^{-1}). However, this value remains close to the ones obtained in SIM26 and OPT1.

The fact that the fractures have been simplified as straight lines in the simulations combined to a relatively small area of calculation (10 × 10 m) could be one element of explanation of the observed fracture intensity variation between the reference outcrop and SIM26 and OPT1. This analysis strengthens the results obtained during the sensitivity analysis and demonstrates the capacity of the MPS method to represent with a high fidelity the geometry of a fracture network.

III.4.5 Using the sensitivity analysis results to model AP4

As per AP3, AP4 present an intrinsic variability of the fracture network geometry. This outcrop was divided in 3 elementary zones (fig. 11A-B). According to AP4 partitioning, a probability map with sharp boundaries (fig. 11B) was created. For AP4, the configuration of the outcrop led to mask the area where no interpretation data were performed. In these particular zones a "no data value" was attributed and these masked areas were excluded during the modelling process. In AP4 three training images were created (fig. 11C). As per AP3, the size of the AP4 simulation grid was doubled compared to its original dimension (available in fig.11). In AP4, fractures longer than 40 meters were also considered as hard conditioning data. Here, less than 1.5% of the fractures are longer than 40m (fig. 11D). In AP4, long fractures were found in the 3 sets and mainly in the south-eastern part of the outcrop (fig. 11D, elementary zone 6). 11 N180 fractures (0.5% of the whole), 13 N150 fractures (0.6% of the whole) and 9 N090 fractures (0.4% of the whole) were digitized and integrated as conditioning data into the simulation.

Based on the results of the sensitivity analysis of AP3 we generated one simulation for the AP4 outcrop (fig. 12). The modelling parameters for SIM AP4-1 were selected as following: the number of neighbours was set up at 50 and the acceptance threshold at 2%. The 3 training images used in the simulation are presented in figure 12 and are considered as representative of the fracture arrangement in each region of the simulation. The scanning percentage of TI6 and TI7 was set up at 50%. The scanning percentage of TI8 was set up at 100%. With this configuration, the simulation lasts slightly more than 5 minutes. The fact of intensely scanning TI8 is probably responsible of this duration. The analysis was conducted on the total amount of segments generated and of segments per set of fractures. In AP4 the total number of segments is 1810. The simulation realises 1682 segments in total, which constitutes a

satisfactory result. The original AP4 presents 252 segments striking N150, 856 segments striking N180 and 702 segments striking N090. The results of simulation AP4-1 are always satisfactory or acceptable with 206 segments striking N150, 834 segments striking N180 and 642 segments striking N090. A detailed analysis was not conducted here because AP4 contains a lot of small fracture intersections (especially in the TI8 zone) and this makes the segment extraction a complex process. However, these results are promising for the future.

IV] Smooth transitions between elementary zones: towards reservoir scale models to manage uncertainties

The strength of the method proposed here relies on the use of a probability maps and on the opportunity to consider multiple training images in a single realisation to generate non-stationary models of fracture network geometries. In the case of AP3 and AP4, the probability maps are essentially constrained by the variation of geometry of the fracture networks observed on the geological interpretation made on the drone imagery. Consequently, the defined areas are pragmatically bounded and the nature of the limit between one zone and another is a sharp boundary.

AP3 and AP4 outcrops are separated by about 2.5 km and very little is known about the fracture network geometry between these two locations. Assuming that there is no major structural deformation (fold or faults) that may cause a change in fracture geometry at the close vicinity of the outcrop “reality”, the zones initially defined on the AP3 and AP4 outcrop can be extended to the limits of the reservoir-scale model boundaries (fig. 13). In this particular case, filling the gap between the two outcrops appears to define how the transition between one side of the simulation grid and the other should be determined.

Fractures are localised objects that do not need to be necessarily continuous from one simulation zone to another. The constant higher proportion of the non-fractured matrix facies

versus localised and thin fracture elements ensures the coherency and relative compatibility from one simulation region to another. The idea of the simulation grid region partitioning was re-evaluated and an alternative method, was proposed here. Contrarily to the definition of sharp boundaries in the probability maps used for AP3 and AP4, a probability map with smooth transitions is defined as follows. An ensemble of elementary zones covering a part of the simulation grid is defined. Each TI corresponds to one elementary zone, which is simulated using exclusively that TI. The probabilities in these zones are then set to one for a specific TI and to zero for the other TIs. The remaining part of the simulation grid is divided in transition zones, for which one has to define which TIs may be involved. In a transition zone, the probabilities of the involved TIs are set proportional to the inverse distance to the corresponding elementary zones. This process creates smooth transitions in low constrained area decreasing the influence of one TI towards another (from one elementary zone to another).

No faults or folds can be initially identified between AP3 and AP4 to condition the drawing of the probability map. In this case, a rectangular compartment representing a gradual probability transition to use the training image associated to one outcrop or to the other filled the blank space between the two outcrops. For instance, fig 13E shows in the Transition_Zone_1 a decreasing probability to use TI1 from left to right (i.e. zone 1 to zone 6) and conversely to use TI6 from right to left.

Recently, investigations conducted on the Rio Grande do Norte geological map (Angelim et al., 2006), demonstrated the presence of a fault crossing the simulation grid near the AP3 zone. This structure may explain the variability of fracture geometry from AP3 (EW stylolites and strong presence of conjugated NS/NW-SE system) to AP4 (EW stylolites associated to NS fracture system, the NW-SE conjugated system is here subordinate). Further geological investigations need to be conducted in this particular place to proof the influence of this fault

on the network geometry. However, fig 13F shows an alternative probability map taking into account this interpretation and present how flexible the probability map can be. The proposed method demonstrates its adaptability in various geological contexts.

V] A method to create a 3D DFN out of 2D MPS realisations

The MPS simulations presented in this paper are on the form of 2D pixelated maps. MATLAB codes were developed to extract starting and end point coordinates (georeferenced) of a series of aligned colorized pixels that represent a fracture trace from these images. Transforming this output in geologically realistic 3D surfaces is not easy. Karimpouli et al., (2017) studied samples coming from coalbed methane reservoirs in the fractured Late Permian Bowen Basin in Australia. They realised multiple 2D and pseudo 3D images (i.e. orthogonal 2D images) and used the cross-correlation based simulation (CCSIM) to represent the internal organisation of coal cleats and the heterogeneity of the coal matrix in 3D. Their approach greatly improved the understanding of the internal complexity of coal samples and gives better results than classical DFN's based on averaged distributions. However, their method requires an important initial amount of information (i.e. CT scans slices used as training images) that is generally not available at a larger scale. The use of MPS in 3D seems particularly not suited for fracture network representation because: i) they require to associate fractures from 2D map view and from 2D section view (3D or pseudo-3D), ii) it appears difficult to consider isolated fractures in this type of approach and iii) in the subsurface fracture height and/or fracture length are generally unknown.

To Tackle these problems we choose to use multiple 2D MPS-generated fracture networks. In the presented approach, the 3D is obtained by extruding 3D fracture planes in fracture units (fig. 14). In this approach we consider that fractures are entirely bound to the units, which can appear as a limitation if isolated fractures occurs inside a layer. However, we can consider

652 variable levels of fracture units. Figure 14 presents an hypothetic scenario where red fractures
653 are confined to a large fracture unit (FU1) crosscutting smaller ones (FU4 containing also
654 smaller red fractures). In such a representation, one 2D planar simulation is required at each
655 top mechanical unit to generate a new set of fractures.
656 In real-world subsurface configurations, mechanical units can be extracted from well logs
657 (resistivity, density, lithology; Laubach et al., 2009). The fracture height distribution, referred
658 as fracture stratigraphy (Hooker et al., 2013) requires here a particular attention and is
659 difficult to extract from borehole data. In outcrops, the use of vertical cliffs adjacent to 2D
660 horizontal pavement should be a way to evaluate these heights and to constrain the 3D model.
661 In outcrops, the resort to vertical cliffs adjacent to 2D horizontal pavements is required to
662 define fracture height. This method is already implemented in gOcad-SKUA software as a
663 macro that extrudes planes of a single fracture family (i.e. all the red fractures in AP3)
664 vertically into a bounded volume (fig. 14). More developments are in process to generate
665 oblique planes and to be able to extrude planes in portions of the fracture sets.
666

667 ## V] Conclusions

668 In this paper a new method to predict the geometry of a natural fracture network using the
669 multiple-point statistic algorithm is presented. The method provides stochastic realisation
670 depicting a realistic non-stationary fracture network arrangement in 2D based on the use of
671 multiple, simplified, small training images capturing the natural fracture attributes in specific
672 zones defined by a probability map. Probability maps are adaptable and follow geological
673 rules of fracture type and arrangement distribution specific to various tectonic contexts (i.e.
674 faulting, folding and poor deformation context/no fault, no folds). We developed methods to
675 be able to consider transition zones into the probability maps (e.g. zones far from hard data)
676 that allow simulating fracture network geometry at a larger scale (i.e. reservoir scale).

The realisations obtained from 2D MPS constitute a statistical laboratory close enough to the reality to be tested in terms of fracture mechanical parameters and response to flow. Comparison between mechanical aperture calculation, fluid flow simulations conducted on both “reality” fracture network interpretations performed on drone imagery and series of MPS realisations gives similar results.

The method proposed here is applicable to all rock types and to a wide range of tectonic contexts. Initially calibrated using outcrop data, the method is fully adaptable to the subsurface in order to better characterise fractures in water, heat or hydrocarbon reservoirs. The challenge there, remains on the definition of the different training images on which the simulation is based. Very few data are generally available in the subsurface and geological rules need to be found to define the geological characteristics of the fracture network (orthogonal or conjugate network) and the associated fracture attributes (length, height, spacing, density, topology).

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reviewers, Stephen Laubach, William Dershowitz and John Hooker for their very useful comments that greatly participated to improve this paper.

Appendix A

The DeeSse algorithm (Straubhaar et al., 2011) was used in this paper to reproduce existing fracture network interpreted from outcrop pavements. The following pseudocode developed by Oriani et al., (2017) have been modified to explain how the algorithm is processing the simulation of fracture. Specific terms can be found in section II.1 of the present paper. In our study the simulation follows a random path into the simulation grid. This grid is step by step populated by values (fracture facies in our case) sampled in the training image. The algorithm proceeds according to the following sequence :

1. Selection of a random location $\boldsymbol{x}$ in the simulation grid that has not yet been simulated (and not corresponding to conditioning data points, already inserted in the grid).
2. To simulate $\mathbf{V(x)} \rightarrow$ the fracture facies into the simulation grid: The pattern $\boldsymbol{d_n(x)} = \boldsymbol{(x_1,V(x_1)),\ldots,(x_n,V(x_n))}$ formed by at most **n** informed nodes the closest to $\boldsymbol{x}$ is retrieved. If no neighbours is assigned (at the beginning of the simulation), $\boldsymbol{d_n(x)}$ will then be empty: in this case, assign the value $\mathbf{V(y)}$ of a random location y in the TI to $\mathbf{V(x)}$, and repeat the procedure from the beginning.
3. Visit a random location y in the TI and retrieve the corresponding data event $\boldsymbol{d_n(y)}$.
4. Compare $\boldsymbol{dn(x)}$ to $\mathbf{dn(y)}$ using a distance $\mathbf{D}(\boldsymbol{dn(x), dn(y))}$ corresponding to a measure of dissimilarity between the two data events.
5. If $\mathbf{D}(\boldsymbol{dn(x), dn(y))}$ is smaller than a user-defined acceptance threshold $\boldsymbol{T}$, the value of $\mathbf{V(y)}$is assigned to $\boldsymbol{V(x)}$. Otherwise step 3 to step 5 are repeated until the value is assigned or an given fraction $\boldsymbol{F}$ of the TI, is scanned.

6. if ***F*** is scanned, **V(x)** is defined as ***V(y)***, with ***y*** the scanned location minimising the distance **D(*dn(x), dn(y)*)**.

7. Repeat the whole procedure until all the simulation grid is informed.

Figure captions

Figure 1: Direct Sampling method workflow applied to fracture network modelling (modified from Meerschman et al., 2013).

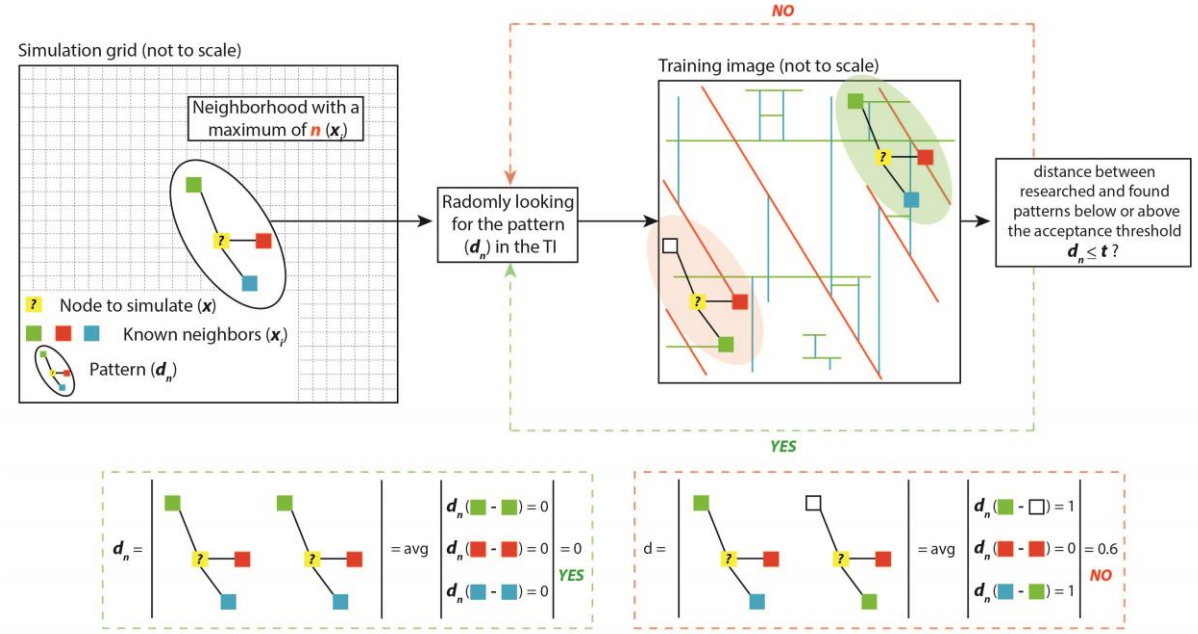


Figure 2: Location of the area of interest and of the studied pavements near Apodi area (red star).

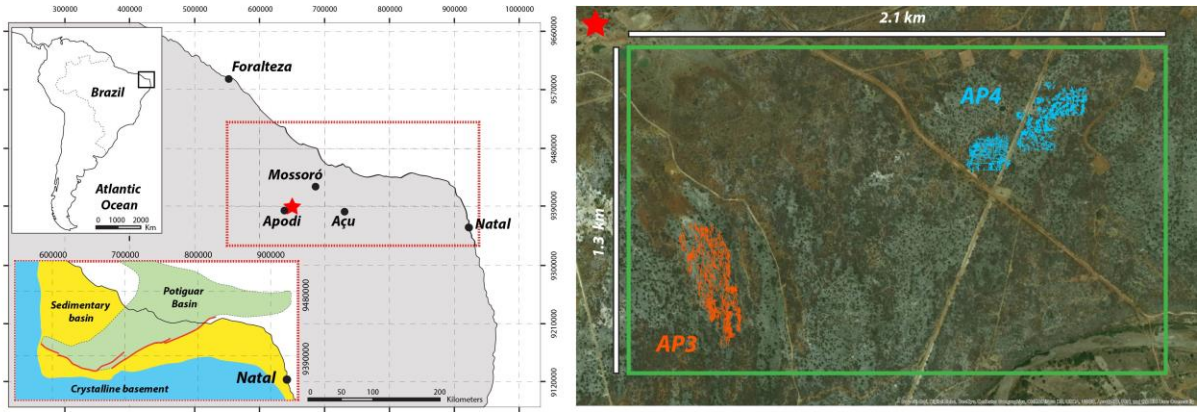
738 

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Table 1: Outcrop characteristics and fracture parameters collected in AP3 and AP4

AP3 outcrop																			
Localisation (WGS84 UTM Z24S)		Orientation	Dimension		Fractures proportion (of the whole fracture population)														Fracture length
X	Y		NS (m)	EW (m)	Set 1 (N135-N165)					Set 2 (N000-N010/N170-180)					Set3 (N075-N105)					Min (m)	Max (m)
650601	9387908	NNW-SSE	600	300	30%					52%					18%					2,21	123
					Elementary zone 1	Elementary zone 2	Elementary zone 3	Elementary zone 4	Elementary zone 5	Elementary zone 1	Elementary zone 2	Elementary zone 3	Elementary zone 4	Elementary zone 5	Elementary zone 1	Elementary zone 2	Elementary zone 3	Elementary zone 4	Elementary zone 5		
					60%	26%	18%	70%	87%	37%	14%	80%	23%	13%	3%	60%	2%	7%	0%		

AP4 outcrop														
Localisation (WGS84 UTM Z24S)		Orientation	Dimension		Fractures proportion (of the whole fracture population)									Fracture length	
X	Y		NS (m)	EW (m)	Set 1 (N135-N165)			Set 2 (N000-N010/N170-180)			Set3 (N075-N105)			Min (m)	Max (m)
652032	9388508	NE-Sw	400	500	20%			40%			40%			1	186
					Elementary zone 6	Elementary zone 7	Elementary zone 8	Elementary zone 6	Elementary zone 7	Elementary zone 8	Elementary zone 6	Elementary zone 7	Elementary zone 8		
					8%	20%	10%	43%	45%	53%	49%	35%	37%		

Figure 3: Data acquired in the area of interest in pavements AP3. A) ortho-rectified high-resolution pavement aerial images acquired with a drone, B) fracture interpretation on ortho-rectified images, C) fracture orientation calculated from the north in GIS-based environment. Corresponding rose diagram for both outcrops, D) length of each fracture trace and E) fracture topology relationship for each pavement observed on fracture network interpretation.

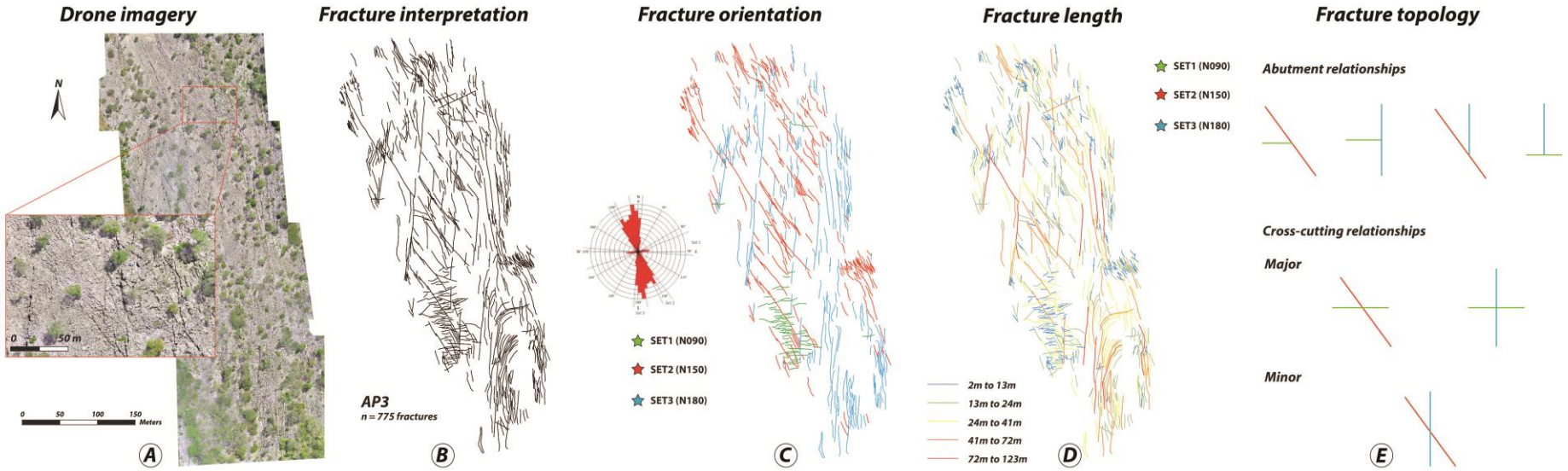


Figure 4: Data acquired in the area of interest in pavements AP4. F) ortho-rectified high-resolution pavement aerial images acquired with a drone, G) fracture interpretation on ortho-rectified images, H) fracture orientation calculated from the north in GIS-based environment. Corresponding rose diagram for both outcrops, I) length of each fracture trace and J) fracture topology relationship for each pavement observed on fracture network interpretation

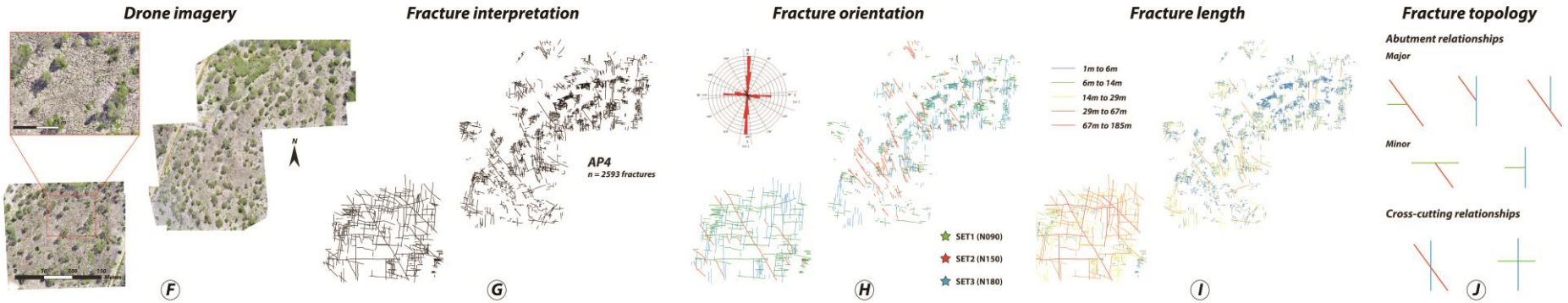
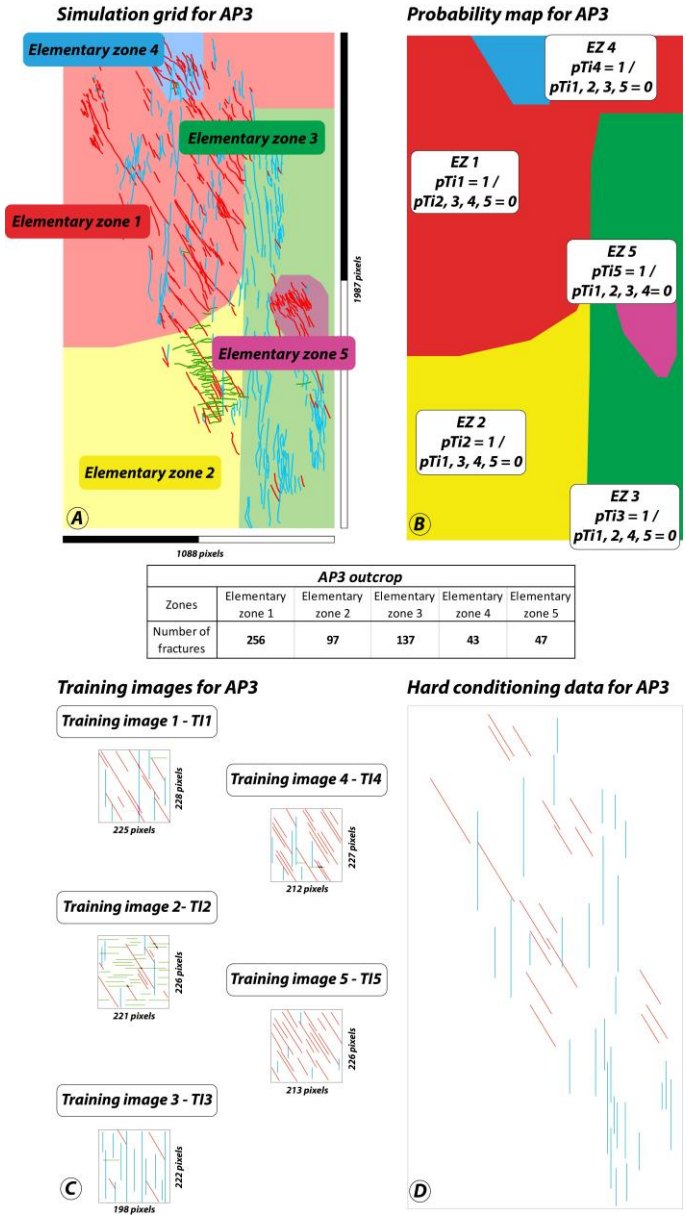
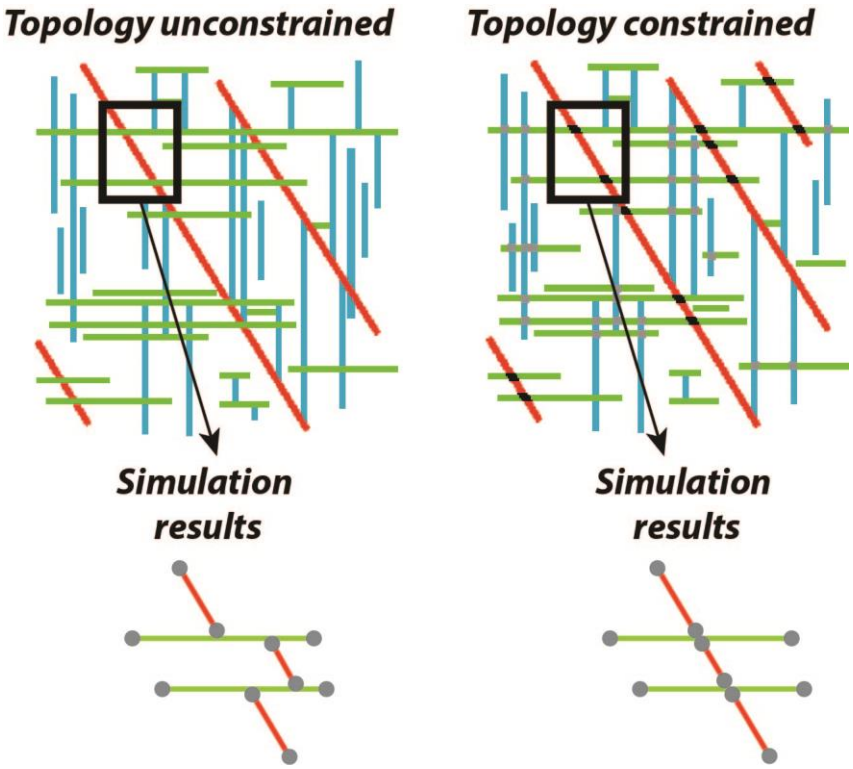


Figure 5: A) Partitioning of AP3 in 5 elementary zones (EZ). This partition is defined (with respect to fracture orientation (fracture facies), fracture density and geometry variability over the entire simulation domain. B) probability map and associated statistics for each EZ. C) training images associated with the partition of AP3. In each EZ, the corresponding training image has a probability (pTI) of 1 to be used. In this zone the other training images are not used (pTI = 0). D) hard conditioning data for AP3. All the fractures longer than 40 m are considered deterministically in the simulation process



782 **Figure 6:** Comparison between results obtained without constraining the topology and with
783 topological facies constraints.



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786 **Figure 7:** Visual comparison between: A) the reference fracture network interpretation (AP3),
787 B) the extraction of the longer segments (50 fracture longer than 40m), C) a simulation
788 conditioned by the long segments, D) a simulation not conditioned by the long segments

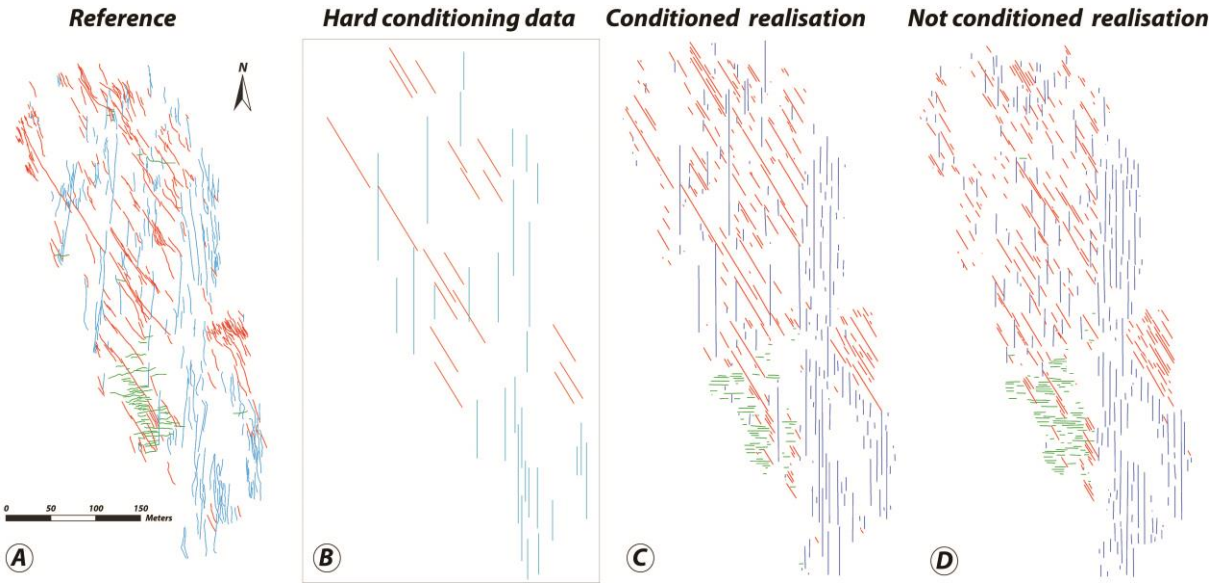

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Table 2: Simulation parametrisation, models set-ups and duration (in seconds) of each run.

Tested parametrisation	Number of neighbours influence							Number of neighbours + Acceptance threshold							
Realisation name	SIM1	SIM2	SIM3	SIM4	SIM5	SIM6	SIM7	SIM8	SIM9	SIM10	SIM11	SIM12	SIM13	SIM14	SIM15
Simulation parameters	A. th. = 5% N. = 10 Scan= 25%	A. th. = 5% N. = 20 Scan= 25%	A. th. = 5% N. = 30 Scan= 25%	A. th. = 5% N. = 40 Scan= 25%	A. th. = 5% N. = 50 Scan= 25%	A. th. = 5% N. = 75 Scan= 25%	A. th. = 5% N. = 100 Scan= 25%	A. th. = 4% N. = 40 Scan= 25%	A. th. = 3% N. = 40 Scan= 25%	A. th. = 2% N. = 40 Scan= 25%	A. th. = 1% N. = 40 Scan= 25%	A. th. = 4% N. = 50 Scan= 25%	A. th. = 3% N. = 50 Scan= 25%	A. th. = 2% N. = 50 Scan= 25%	A. th. = 1% N. = 50 Scan= 25%
Simulation duration	22"	19"	33"	36"	55"	101"	136"	52"	52"	90"	95"	56"	76"	76"	121"

Tested parametrisation	Number of neighbours + Acceptance threshold + % TI scan												Optimisation
Group	Group 1				Group 2				Group3				
Realisation name	SIM16	SIM17	SIM18	SIM19	SIM20	SIM21	SIM22	SIM23	SIM24	SIM25	SIM26	SIM27	OPT1
Simulation parameters	A. th. = 3% N. = 40 Scan= 50%	A. th. = 2% N. = 40 Scan= 50%	A. th. = 3% N. = 50 Scan= 50%	A. th. = 2% N. = 50 Scan= 50%	A. th. = 3% N. = 40 Scan= 75%	A. th. = 2% N. = 40 Scan= 75%	A. th. = 3% N. = 50 Scan= 75%	A. th. = 2% N. = 50 Scan= 75%	A. th. = 3% N. = 40 Scan= 100%	A. th. = 2% N. = 40 Scan= 100%	A. th. = 3% N. = 50 Scan= 100%	A. th. = 2% N. = 50 Scan= 100%	Custom
Simulation duration	80"	148"	123"	124"	105"	196"	152"	154"	104"	203"	150"	149"	151"

Table 3: Comparison between the total amount of segments interpreted in the reference outcrop and in the different sets of simulations (tested parametrisation). Evaluation of the results in terms of satisfactory (green symbol), acceptable (orange symbol) or non-satisfactory (red symbol)

				Results evaluation		
	Reference outcrop	Tested Parametrisation	Number of tested configurations	✔	≈	✘
Total segments	562	Influence of the number of neighbours	n=7	1	1	5
		Number of neighbours + Acceptance threshold	n=8	3	2	3
		Number of neighbours + Acceptance threshold + % TI scan	n=12	5	6	1

Table 4: Results of the sensitivity analysis on the influence of the number of neighbours. The table presents the number of segments per simulation zone for AP3 (used as reference). Red symbols show a total amount of segments of the considered set in the considered zone deviating to more than 20% from the reference case. Yellow symbols show a deviation of more than 10% from the reference case. Green symbols do not deviate significantly from the reference outcrop interpretation.

			Number of neighbours						
		Reference	*SIM1*	*SIM2*	*SIM3*	*SIM4*	*SIM5*	*SIM6*	*SIM7*
		Segments per parts							
Zone TI1	**Set1**	**156**	✗	≈	≈	✗	✗	✗	✗
	Set2	**95**	✗	✗	≈	✗	✗	✗	✗
	Set3	**6**	✗	✗	✗	✗	✗	✗	✗
Zone TI2	**Set1**	**22**	✗	✗	✗	✗	✗	✗	≈
	Set2	**12**	✗	✗	✓	✗	✗	✗	✗
	Set3	**57**	✗	≈	✓	✓	✓	≈	✓
Zone TI3	**Set1**	**20**	✗	✓	✗	✗	✗	✗	✗
	Set2	**113**	✗	≈	✓	≈	≈	✗	✗
	Set3	**2**	✗	✗	✗	≈	≈	✗	✗
Zone TI4	**Set1**	**25**	✗	✗	✗	✓	✓	≈	✗
	Set2	**10**	✓	✓	✓	✓	≈	≈	≈
	Set3	**3**	✗	✗	✗	✗	✗	✗	≈
Zone TI5	**Set1**	**39**	✓	≈	✗	✗	✗	✗	✗
	Set2	**2**	✗	✗	✗	✗	✓	✓	≈
	Set3	**0**	✓	✓	✓	✓	✓	✓	✓
		Satisfactory total	***No***	***Yes***	***Yes***	***No***	***No***	***No***	***No***
		# satisfactory	3	3	5	4	4	2	4
		# acceptable	0	4	2	2	3	3	2
		# not acceptable	12	8	8	9	8	10	9

Table 5: Results of the sensitivity analysis on the influence of the number of neighbours and of the variation of the acceptance threshold. The colour code is the same as the one used in table 4.

			Number of neighbours + Acceptance threshold							
		Reference	SIM8	SIM9	SIM10	SIM11	SIM12	SIM13	SIM14	SIM15
		Segments per parts								
Zone TI1	Set1	156	✓	✓	≈	≈	✗	✓	✓	✓
	Set2	95	✗	✗	✗	✗	✗	✗	✗	✗
	Set3	6	✗	✗	✗	✗	✗	✗	✗	✗
Zone TI2	Set1	22	✗	✗	✗	✗	✗	✗	✗	✗
	Set2	12	≈	≈	✓	✓	✗	✗	✗	✗
	Set3	57	✓	✓	✗	✗	✓	✓	✓	≈
Zone TI3	Set1	20	✗	✗	✓	✓	✗	✗	✗	✗
	Set2	113	✓	✓	≈	≈	≈	✓	✓	≈
	Set3	2	≈	≈	✓	✓	≈	✗	✗	✓
Zone TI4	Set1	25	✓	✓	✗	✗	✓	✓	✓	✓
	Set2	10	✗	✗	≈	≈	≈	≈	≈	✓
	Set3	3	✗	✗	✗	✗	✗	✗	✗	✗
Zone TI5	Set1	39	✗	✗	✗	✗	✗	✗	✗	✗
	Set2	2	≈	≈	≈	≈	✓	≈	≈	≈
	Set3	0	✓	✓	✓	✓	✓	✓	✓	✓
		Satisfactory total	Yes	Yes	Yes	Yes	No	No	No	Yes
		# satisfactory	5	5	4	4	4	5	5	5
		# acceptable	3	3	4	4	6	2	2	3
		# not acceptable	7	7	7	7	9	8	8	7

Table 6: Results of the sensitivity analysis on the influence of the number of neighbours, of the variation of the acceptance threshold and of the variation of the percentage of the scanned fraction of the training image. The colour code is the same as the one used in table

				Number of neighbours + Acceptance threshold + % TI scan											Optimisation
				Group 1			Group 2				Group3				
		Reference	SIM16	SIM17	SIM18	SIM19	SIM20	SIM21	SIM22	SIM23	SIM24	SIM25	SIM26	SIM27	OPT1
		Segments per parts													
Zone TI1	Set1	156		✓	✓	✓	✓	✗	✓	✓	✓	✗	✓	✓	✗
	Set2	95		✗	✗	✗	✗	≈	✗	✗	✗	≈	✗	✗	✓
	Set3	6		✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓
Zone TI2	Set1	22		✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗
	Set2	12		✗	✗	✗	✗	✗	✗	✗	✓	✗	✓	✓	✓
	Set3	57		✓	✓	✓	✓	≈	✓	✓	✓	≈	✓	✓	≈
Zone TI3	Set1	20		✗	✗	✗	✓	✗	✗	✗	≈	✗	✓	✓	✗
	Set2	113		✓	✓	✓	≈	✓	✓	✓	✓	✓	≈	≈	✓
	Set3	2		≈	≈	≈	✗	✓	✓	✓	≈	≈	✗	✗	✗
Zone TI4	Set1	25		✗	✗	✗	≈	✗	✓	✓	✗	✗	≈	≈	✗
	Set2	10		✓	✓	✓	≈	✓	✓	✓	✗	≈	✓	✓	✓
	Set3	3		✗	✗	✗	✗	✗	✗	✗	✗	≈	✗	✗	✓
Zone TI5	Set1	39		≈	≈	≈	✗	✗	✗	✗	✓	≈	✗	✗	≈
	Set2	2		≈	≈	≈	✗	✗	✓	✓	≈	≈	✓	✓	✓
	Set3	0		✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
		Satisfactory total		Yes	Yes	Yes	No	No	Yes	Yes	Yes	Yes	Yes	Yes	Yes
		# satisfactory		5	5	5	4	4	8	8	6	2	7	7	8
		# acceptable		3	3	3	3	2	0	0	3	7	2	2	2
		# not acceptable		7	7	7	8	9	7	7	6	6	6	6	5

Figure 8: Fracture length distributions tested during the sensitivity analysis. A) fracture length distribution for SIM1 to SIM7, B) fracture length distribution for SIM10, SIM12, SIM13, SIM15 and C) fracture length distribution for SIM16, SIM17, SIM20, SIM21, SIM22, SIM24, SIM5, SIM26.

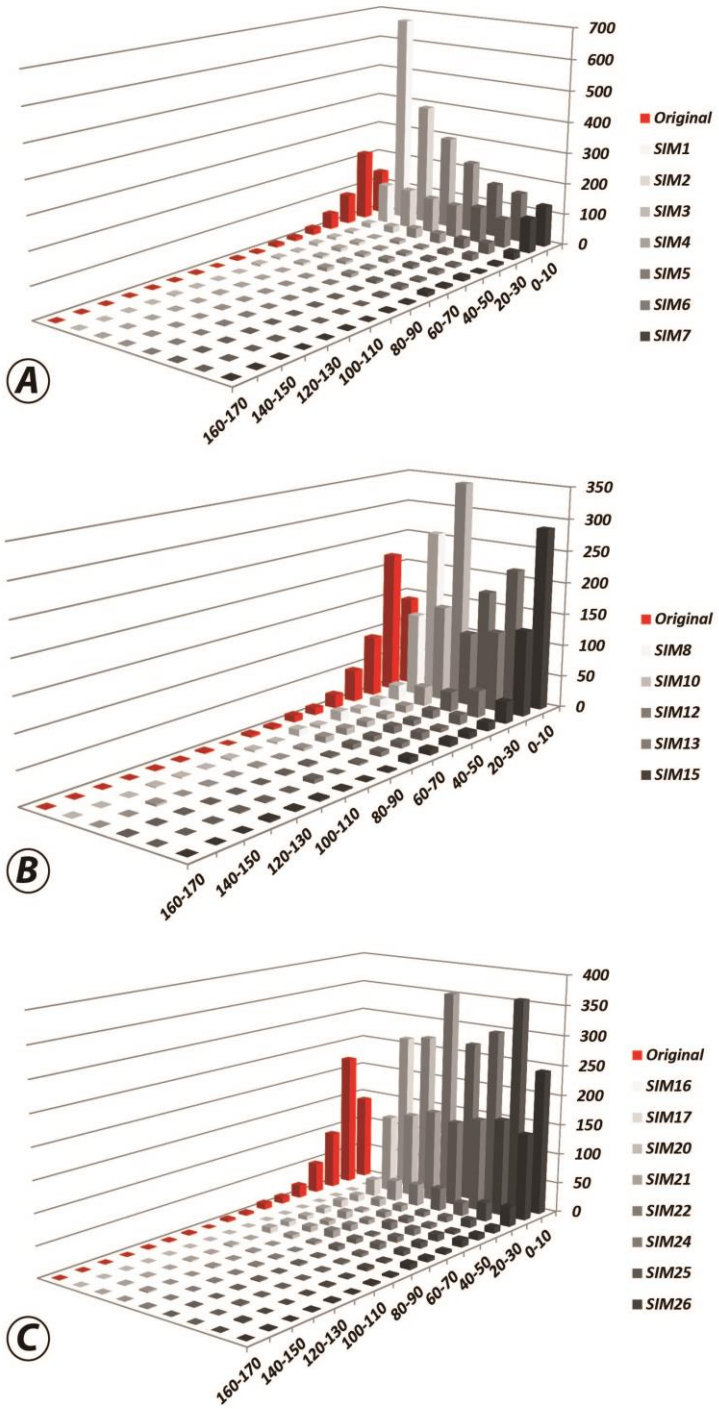


Figure 9: Comparison of the training images 1, 3 and 4 used during the sensitivity analysis (27 simulations) and their modification for SIM 3

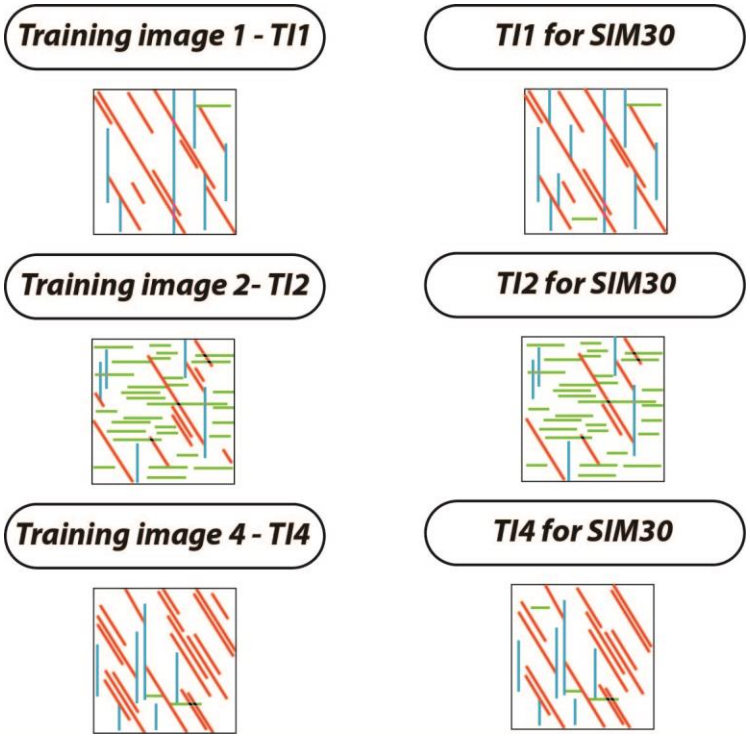


Figure 10: Comparison of the fracture intensity (P_{21}) calculated in the reference outcrop and in four select MPS simulations

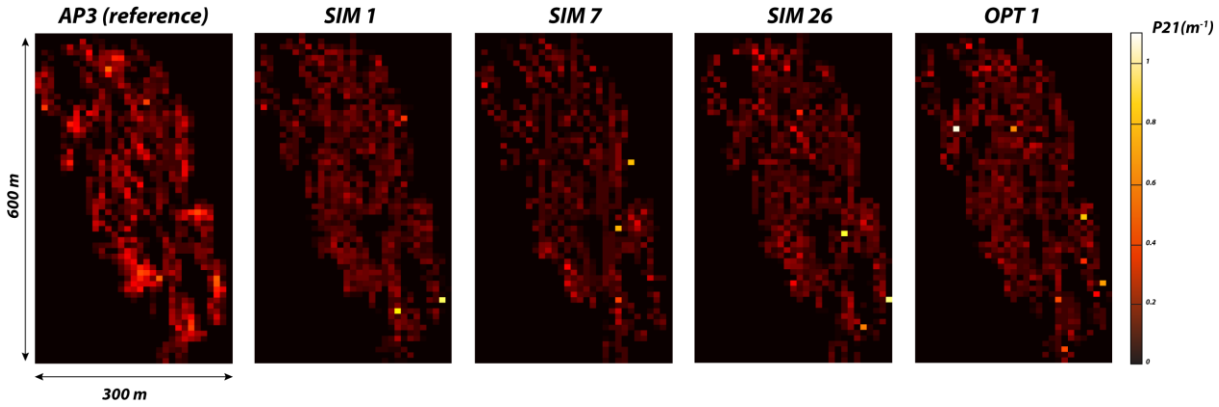


Figure 11: A) Partitioning of AP4 in 3 EZ. B) probability map and associated statistics for each EZ. C) training images associated with the partition of AP4. D) hard conditioning data for AP4

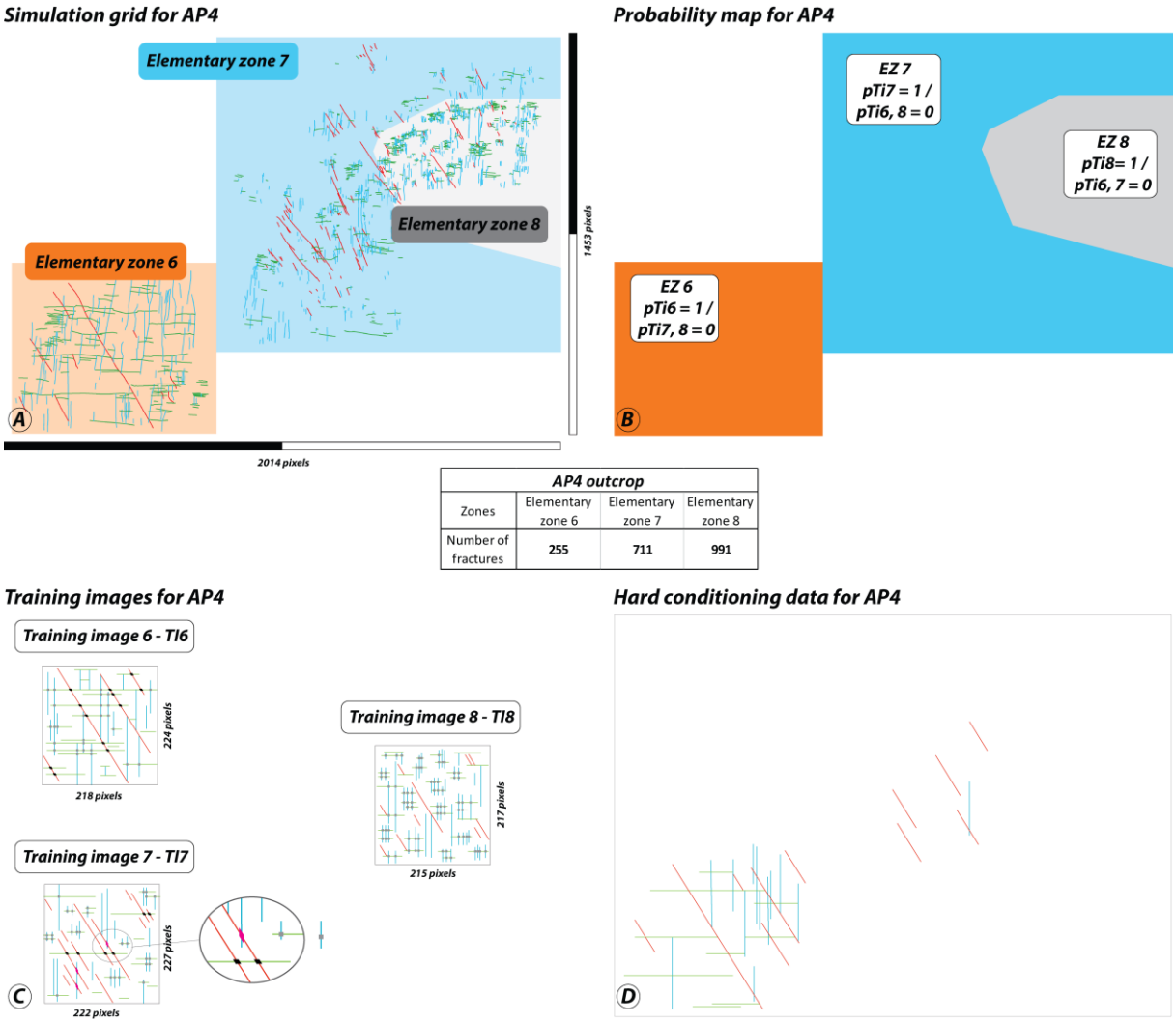


Figure 12: Comparison of the AP4 original outcrop with a MPS simulated version AP4-1

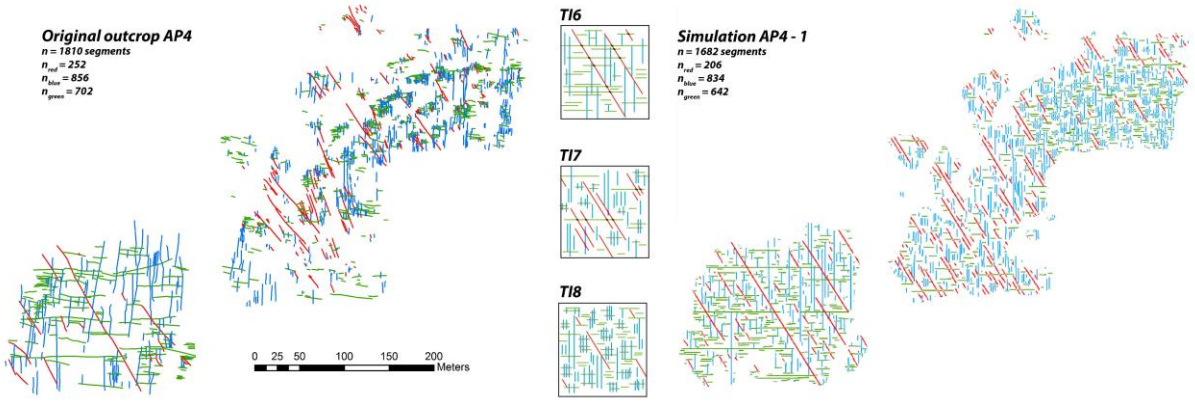


Figure 13: Smooth probability map at the reservoir scale (combination of AP3 and AP4). A) Relative position of AP3 and AP4 outcrops. B) Apodi fault added into the area of interest. Extension of the probability map regions in AP3 and AP4 without geological drivers C) and with the influence of the Apodi fault D). Probability maps with smooth transition zones without geological drivers E) and with the influence of the Apodi fault F).

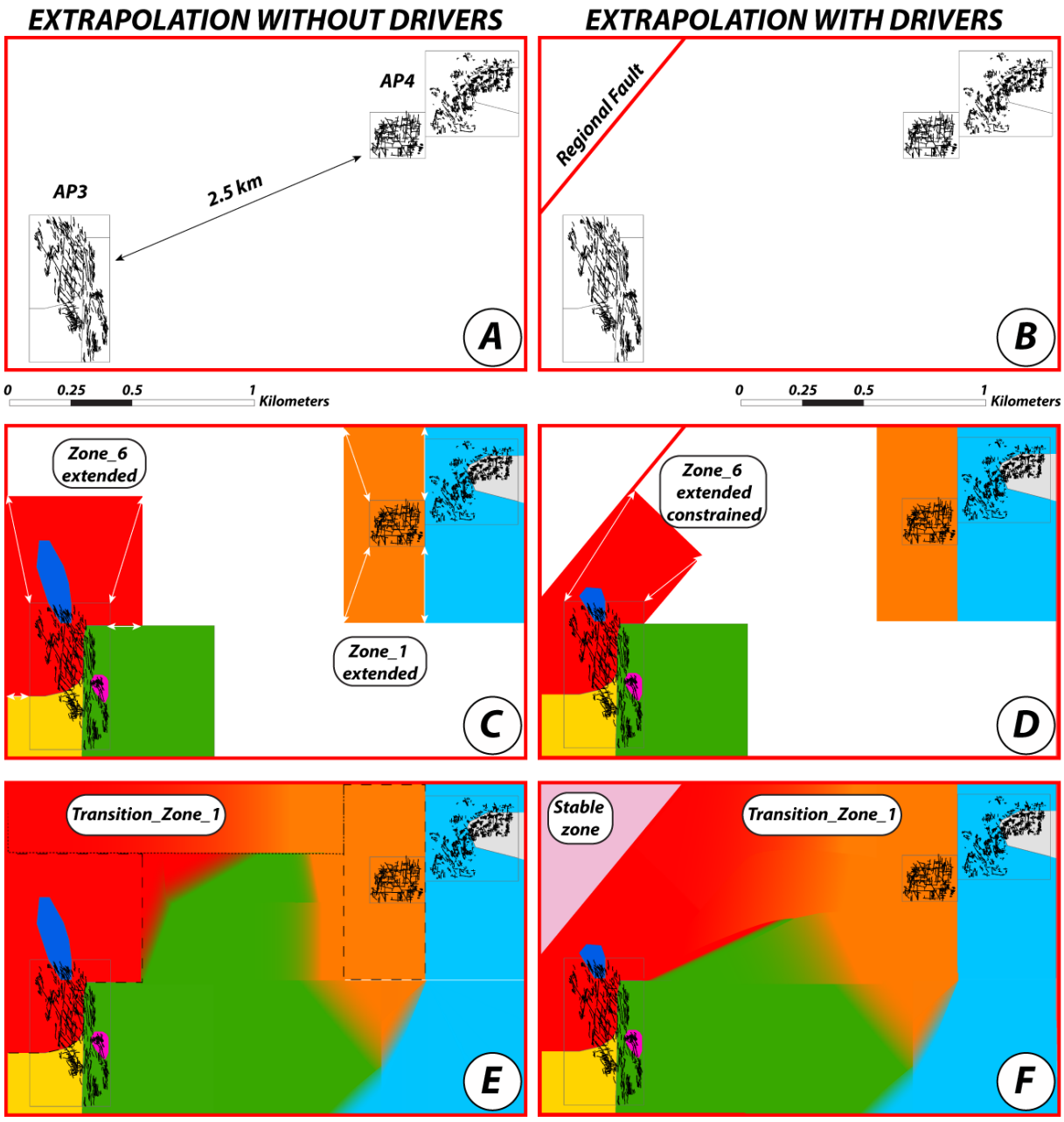
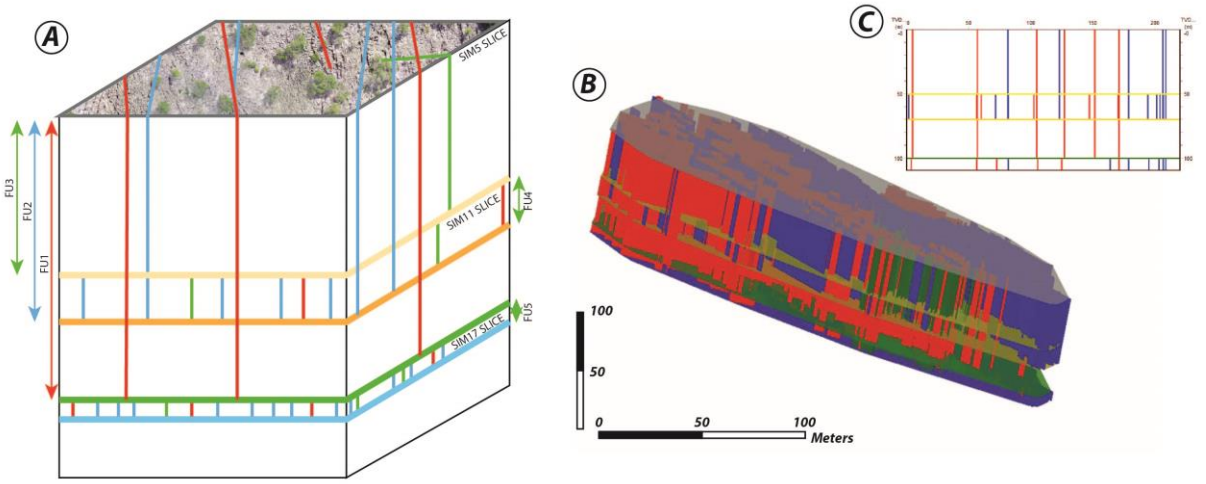


Figure 14: Fracture network extrusion in 3D. The method consists of identifying the different fracture units (FU) on which the fracture height is supposed to be constant (A). This method requires one simulation per top fracture unit (SIM SLICES). (B) is a 3D DFN based on the hypothetical case (A) and realised in gOcad software. (C) is a cross section realised in the centre of the 3D model in the E-W direction.



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