Response to 'Review of a paper by Beckel and Juhlin’ by the Anonymous Referee #1

We would like to thank the anonymous referee for the constructive and helpful review. In the following, we will answer to the referee’s comments and suggestions and describe adjustments made in our manuscript. The referee’s comments are in italic font and our response is given in the intended blocks. Additionally, we will attach a new version of the manuscript with tracked changes as a supplement. Please note that this version of the manuscript contains changes suggested by both referees.

On Page 2, when discussing the attempts to extract 3D info from 2D crooked line profiles, you can add reference to Wu et al. 1995 JGR paper (cross-dip), as well as Nedimovic and West (2003) part 2 paper on 3D pre-stack migration of 2D data + White and Malinowski (2012) paper on 3D post-stack migration of 2D data.

We thank the referee for pointing out the missing reference to Wu et al. (1995) and added it in the manuscript. However, we do not think that referencing the papers by Nedimović and West (2003) and White and Malinowski (2012) on 3D migration of crooked line data is very useful at this point since they do not deal with the crossdip correction and we do not build our research on the work presented in these papers.

Changes: Reference to Wu et al. (1995) added in the Introduction

Page 2 line 19: what is so special about the post-glacial fault, that none of the cross-dip correction methods is suited for its imaging? Please expand or reformulate

We explain this point in more detail later when we discuss the previous applications of the crossdip correction, but we totally agree that a short explanation is required here and have added this in the manuscript.

Changes: Explanation why previous correction methods not suitable added in the Introduction

Page 4 line 31: what is "crossdip angle"; which velocity "v" you are referring to? I think it might be instructive to make a cartoon, illustrating a crooked line acquisition over a reflector with inline/crossline dip

The crossdip angle refers to the dip of a reflector perpendicular to the processing line and the velocity represents the medium velocity. As suggested, we have added an illustration of the ray geometry for a crooked acquisition line above a crossdipping reflector to the manuscript.

Changes: Figure illustrating the ray geometry for crooked line acquisition added (Fig. 3)

Page 6 – section 3.2: it’s unclear what you are really implementing in your module; looks like it’s the Nedimovic and West method just being applied manually? The description of your method can not be easily followed – please make maybe some more explicit link to Fig. 3 + change the caption of Fig. 3 accordingly

Our implementation of the crossdip correction differs significantly from the approach used by Nedimović and West. We manually determine the crossdip angle, calculate the theoretical crossdip correction $\Delta t_{\text{cross}}$ based on the the angle and shift back the data in a window around the reflection by $\Delta t_{\text{cross}}$ so that all data aligns at the origin time $t_0$. In contrast to this, Nedimović and West leave the data at its recorded position ($t_0 + \Delta t_{\text{cross}}$) and simply stack along their estimated crossdip correction time $\Delta t_{\text{cross}}$. As shown in the synthetic CDP gather (Fig. 3 in the manuscript), this slant stack approach can in some cases lead to a duplication of the reflection because the data are not actually shifted. In our approach, this can not happen.

We have attempted to explain this a bit more explicitly in the manuscript.

Changes: Figure 4: figure caption extended to better explain the crossdip correction method; more explicit links to Figure 4 added in Sect. 3.2 (RC1)

Synthetic tests: since there is an interplay between cross dip and velocity analysis I suggest to make a test with the model similar to model 3, but with different velocities between the reflectors.
The interplay between crossdip effects and stacking velocities occurs when the cross-offset distribution correlates to a certain extent with an NMO hyperbola. As a consequence, part of the crossdip effect can be picked up by the NMO correction, i.e. biases the stacking velocity model. Thus, the interplay is mainly related to the distribution of cross-offsets and not to the real underground velocities. Furthermore, the synthetic models are supposed to represent a typical hardrock setting where the velocities often remain approximately constant over very large areas. Therefore, we believe that we have already sufficiently illustrated and discussed the interplay between stacking velocities and crossdip effects in the second synthetic model and do not think adding another model will contribute significantly to our manuscript.

Page 12 line 5-9: your workflow is not very clear: consider adding a cartoon illustrating it; Also, there is an interplay between residual statics and cross-dip correction, which you don’t mention. Can you comment on that? Also, e.g. Wu et al. 1995 applied cross-dip correction first and then the residual statics.

We acknowledge that our description of the workflow might have been a bit confusing, so we re-formulated the description both in sections 4.3 (implementation of the crossdip correction) and 5.1 (data processing) and added an illustration of our crossdip processing scheme.

We did not mention the residual static correction specifically in the description of the workflow, since we applied it as we would have done for any other dataset: We calculated the first pass after the initial NMO correction and tested a second pass after re-analysing the velocities. In our case, a second pass of residual statics did not lead to any significant improvements.

In the previous applications, the order between crossdip correction and residual statics was never consistent. Larner et al. (1979) calculated both simultaneously, Kim and Moon (1992) applied them in a cascaded sequence, DuBois et al. (1990) and Nedimović and West (2003) applied residual statics before the crossdip correction and Wu et al. (1992) and Rodriguez-Tablante et al. (2007) applied residual statics after the crossdip correction. This might be due to the fact that some authors, like Wu et al. (1992), have applied the crossdip correction as a static shift and others while stacking. Since we do not apply the crossdip correction as a static shift but as a local shift around specific reflections (depending on the cross-offset of the trace), we do not expect a large interplay with the surface consistent residual statics. In our opinion, it is best to remove residual static effects as far as possible before trying to correct for crossdip because this should improve the quality of all reflections and make them easier to track. However, we think that it is always worth to try to calculate a second, third, ... pass of residual statics as long as it improves the overall quality of the stack. We added a short comment about this in the manuscript, as well.

Changes: Description of the implementation scheme in Sect. 4.4 reformulated and extended; description of the application of the crossdip correction to the Burträsk data in Sect. 5.1 reformulated and extended; Figure illustrating the workflow added (Fig. 9)

Page 13 line 9-11: information on the refraction tomography is popping up here out of context; while I see your point later, when you show in Fig. 11 the low velocity zones close to the fault location, in my opinion this information could be omitted (and Fig. 11 as well). I’m sure that this velocity anomaly must be already present in your refraction statics model + be visible in the first-breaks. If so, just add a comment. I don’t like the results of the first-arrival tomography to be shown without the proper discussion on how it was performed, what is the resolution, checkerboard tests, etc.

It is not possible to reproduce the low velocity zones with the refraction statics model because the refraction statics model is by design more sensitive to variations in the overburden and, more importantly, the model is two-dimensional to fit the line geometry. When testing the tomography, we also started with a 2D model, but had to switch to a 3D model to get any sensible results. However, we understand the concerns of the referee about just showing the results of a tomography. Since we think that the low velocity zones provide important constraints for our interpretation, we ran a checkerboard test to estimate the resolving power of our tomography. We perturbed the starting model with a 3D checkerboard pattern with a checker size of (x, y, z) = (500 m, 500 m, 100 m) and amplitude of 15 % and computed synthetic travel times for this model using a very fine slowness grid. For the inversion of the synthetic data, we used the same parameters as in the main inversion, but did not estimate a static solution. The ray paths of the checkerboard model are reasonably similar to the ray paths in the actual inversion. The results are shown in Figure S1. The uppermost
checkers are reconstructed well but most of the lower checkers are poorly reconstructed or not reconstructed at all, indicating that only velocity variations close to the bedrock surface can be resolved properly and that the lower part of the tomographic model is poorly constrained. We expanded the description of the tomography in the manuscript and added a summary of the checkerboard test. We hope that this addresses the concerns of the referee sufficiently.

**Changes:** Description of the tomography method extended and a short paragraph summarizing the checkerboard test added in Sect. 5.1; Figure showing the results of the checkerboard test added in the Supplements (Fig. S1)

*Figure 9: is it a DMO stack? Just a comment: it’s hard to determine to what extend the new results are influenced by the new reprocessing scheme or by cross-dip correction only. Even though the statics and velocities are linked together and you revised both of them, it might be worth to show the new reprocessing data stacked with the old velocities (and possibly statics).*

We never intended to claim that all improvements are due to the crossdip correction. In Figure 9, we included both a reprocessed version of the stack without crossdip correction (c) and one with crossdip correction (d) to isolate the effects of both parts of the reprocessing. The comparison of the original stack and the reprocessed version without crossdip correction (both conventional DMO stacks) illustrates how the improved static corrections and velocity model lead to a significantly more coherent stack. The effects of the crossdip correction can be assessed by comparing the reprocessed stack without (c) and with crossdip correction (c). Just to clarify: both stack represent the best image we could get without and with crossdip correction and have been stacked with different velocity models. This is necessary since the stack is very sensitive to the choice of the stacking velocities and these are both affected by inline dip and crossdip. Thus, stacking the dataset with crossdip correction with the velocity model from the dataset without crossdip correction would seriously damage the stack quality and vice versa. Updating the velocity model is an integral part of our procedure to apply the crossdip correction and therefore we believe that separating them, as suggested, does not make sense. However, we now try to emphasize in the manuscript how the comparison of the different versions of the stack helps to isolate the effects of the conventional reprocessing and the effects of the crossdip correction.

**Changes:** Clarification how the comparison between the different stages of reprocessing of the Burträsk data illustrates both improvements due to the conventional reprocessing and the crossdip correction added in Sect. 5.2 and in the caption of Fig. 10

Furthermore, we would like to thank the referee for pointing out the following issues in the manuscript. We have implemented the suggested changes in the new version of the manuscript.

*Page 4 line 8: a south side up dip-slip system – please reformulate (e.g. using hangingwall)*

*Page 11 line 3: reformulate the sentence about the acquisition*

*Figure 2: lines are too thin + colors not well visible (e.g. acquisition line in blue)*

**Changes:** Suggested changes implemented in manuscript
Figure S1. Checkerboard test illustrating the resolving power of the tomography. From top to bottom: velocity distribution of the checkerboard model; relative velocity perturbation of the checkerboard model; reconstruction of the checkerboard model after inversion; ray path coverage below the receiver line. Note that the checkerboard model is three-dimensional and that the sections displayed here only show the model below the receiver line. The Checkerboard test indicates that the velocities in the uppermost part of the bedrock are well resolved. In the lower parts of the model, the checkers are not well reconstructed, indicating that the velocities in this part should be interpreted with care.
Response to 'Comment' by the Anonymous Referee #2

We would like to thank the anonymous referee for the constructive and helpful review. In the following, we will answer to the referee’s comments and suggestions and describe adjustments made in our manuscript. The referee’s comments are in italic font and our response is given in the intended blocks. Additionally, we will attach a new version of the manuscript with tracked changes as a supplement. Please note that this version of the manuscript contains changes suggested by both referees.

P 2 / L 18-19: “none of the existing correction methods is optimally suited to image a feature like a post-glacial fault” I would welcome some more discussion why these methods are not optimal in this specific case.

We explain this point in more detail later when we discuss the previous applications of the crossdip correction, but we fully agree that a short explanation is required here and we added this to the manuscript.

Changes: Explanation why previous correction methods not suitable added in the Introduction

P13 / L3-8: Which types of migration were tested?

We tested a couple of different migration algorithms with different parameters including: Stolt migration with constant velocity and a stretching factor (best results), a phase shift migration with turning rays (very similar to the Stolt migration), Gazdags’s phase shift migration with a 1D velocity model (quite strong artifacts), Kirchhoff migration using the smoothed stacking velocities (very smeared image, disrupted reflections) and FD migration with an interval velocity model derived from the stacking velocities (steeper reflections basically disappeared). We even tried the Kirchhoff and FD migration using a constant velocity model but the results were still not comparable to the results from the Stolt migration.

We added a short listing of the tested migration methods to the manuscript.

Changes: Short list of tested migration algorithms added to Sect. 5.1

P13 / L9-11: What was the velocity model used for? Was migration also tested with this velocity model? How was the migration result using the tomography result, compared to the 5.4 km/s constant velocity?

We did not test using the velocity model from the tomography for migration since most rays did not penetrate the bedrock and therefore, the model only covers the top 50-200 m of the profile. Consequently, we would have to choose a velocity function for the deeper parts anyway. Directly below the surface, the tomography model has of course a much higher resolution, but in this part, we have very poor data coverage due to groundroll muting. Since all migration algorithms that can handle 2D velocity models yielded blurred results, even for constant velocities, we decided to stick to the constant velocity Stolt migration.

Consequently, the tomography model was only used to get a better image of the velocity distribution in the shallow subsurface for comparison with potential shear zones.

Changes: Short statement why the polarity and shape of the reflections were not analyzed added in Sect. 6.3

P16 There is a discussion about the origin of the reflectivity. You are discussing about positive and negative impedance contrast which would mean either a mineralized, or a shear zone. Were the polarity and shape of the reflections analyzed? Are there any indications about impedance contrasts or e.g. tuning effects?

The discussion of impedance contrasts and tuning effects is meant to point out potential geological structures that can cause the reflections. Unfortunately, the data quality does not allow a more detailed analysis of polarity and waveform of the reflections. The noise level is quite high in most parts of the profile and the source wavelet does not have a very impulsive nature – most likely due to interactions between the free surface and the very shallow sediment-bedrock contact. Even after deconvolution, the signal retains its ringy character. Therefore, a detailed analysis of the shape of the reflections would be, in our opinion, over-interpreting the data.

We have added a short comment about this to the manuscript.

Changes: Short statement why the polarity and shape of the reflections were not analyzed added in Sect. 6.3
I think it would be illustrative to add a figure showing a CDP gather for the real data example: before and after crossdip correction and a comparison of the stacked sections (as for the synthetic model in Fig. 3).

We agree that showing an example of a CDP gather before and after crossdip correction helps illustrating the correction. We have added one example including a (comparably) very strong reflection, but we would like to stress that this example is not representative since most reflections are hardly identifiable in the CDP gathers and show up first clearly in the stack as coherent events contrasting with mostly uncoherent noise. This is likely similar in many hardrock environments and therefore, the crossdip analysis should be carried out on constant crossdip stack panels instead of CDP gathers.

Changes: Figure illustrating the crossdip correction for a real CDP gather from the Burträsk dataset added (Fig. 12)

Furthermore, we would like to thank the referee for pointing out the following, more technical issues in the manuscript. We implemented the suggested changes in the new version of the manuscript.

P4 / L10-13: It would be helpful to mark some of the mentioned aspects in Fig. 2. E.g. with A,B,...

P4 / eq. 1: use p_x instead of p for the inline slowness.

P 5 / L5: add A and B: "crossdip at 0.4 s (A) and 1.2 s (B)"

P 5 / L6: mark the CDP 350 and 1350 in Fig. 2.

P 5 / L7: "visible in the stack (Fig. 3b)."

P11: The reference to Fig. 9 appears before the reference to Fig. 8 in the text. This should be in order.

P13 / L13-14: Add b c and d in the text.

P17 / L8: "has has"

Fig 2: Some colors are hard to see (e.g. the gray box and the white numbers)

Fig 3b: Mark the shifted reflection B as you did it in Fig. 3c for the double reflection

Fig 9: Add A1 - 3 and B1 - 4 also to c and d. This would make it easier to follow the descriptions in the text.

Changes: Suggested changes implemented in manuscript
Relevant changes in the manuscript

The following list includes relevant changes in the manuscript. RC1 marks changes suggested by Referee #1 and RC2 marks changes suggested by Referee #2.

- Explanation why previous correction methods not suitable added in the Introduction (RC1, RC2)
- Reference to Wu et al. (1995) added in the Introduction (RC1)
- Figure 2: colour contrast and line visibility enhanced, marks added to different segments of the fault scarp, figure caption slightly extended (RC1, RC2)
- Figure illustrating the ray geometry for crooked line acquisition added (Fig. 3, RC1)
- Figure 4: figure caption extended to better explain the crossdip correction method (RC1)
- More explicit links to Figure 4 added in Sect. 3.2 (RC1)
- Description of the implementation scheme in Sect. 4.4 reformulated and extended (RC1)
- Figure illustrating the workflow added (Fig. 9, RC1)
- Description of the application of the crossdip correction to the Burträsk data in Sect. 5.1 reformulated and extended (RC1)
- Figure illustrating the crossdip correction for a real CDP gather from the Burträsk dataset added (Fig. 12, RC2)
- Short list of tested migration algorithms added to Sect. 5.1 (RC2)
- Description of the tomography method extended and a short paragraph summarizing the checkerboard test added in Sect. 5.1 (RC1)
- Figure showing the results of the checkerboard test added in the Supplements (RC1)
- Clarification how the comparison between the different stages of reprocessing of the Burträsk data illustrates both improvements due to the conventional reprocessing and the crossdip correction added in Sect. 5.2 and in the caption of Fig. 10 (RC1)
- Fig. 10: labels of reflections added in (c) and (d), figure caption extended (RC2, RC1)
- Short statement why the polarity and shape of the reflections were not analyzed added in Sect. 6.3 (RC2)

Furthermore, there are some minor changes in the manuscript. These changes include both more technical suggestions from the referees like reformulating expressions, adding references to Figures in the text and adding arrows in Figures as well as small corrections and additions from the authors.
The crossdip correction as a tool to improve imaging of crooked line seismic data: A case study from the post-glacial Burträsk fault, Sweden

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Abstract.
Understanding the development of post-glacial faults and their associated seismic activity is crucial for risk assessment in Scandinavia. However, imaging these features and their geological environment is complicated due to special challenges of their hardrock setting, such as weak impedance contrasts, often high noise levels and crooked acquisition lines. A crooked line geometry can cause time shifts that seriously de-focus and deform reflections containing a crossdip component. Advanced processing methods like swath 3D processing and 3D pre-stack migration can, in principle, handle the crooked line geometry, but may fail when the noise level is too high. For these cases, the effects of reflector crossdip can be compensated for by introducing a linear correction term into the standard processing flow. However, existing implementations of the crossdip correction rely on a slant stack approach which can, for some geometries, lead to a duplication of reflections. Here we present a module for the crossdip correction that avoids the reflection duplication problem by shifting the reflections prior to stacking. Based on tests with synthetic data, we developed an iterative processing scheme where a sequence consisting of crossdip correction, velocity analysis and DMO correction is repeated until the stacked image converges. Using our new module to reprocess a reflection seismic profile over the post-glacial Burträsk Fault in Northern Sweden increased the image quality significantly. Strike and dip information extracted from the crossdip analysis helped to interpret a set of southeast dipping reflections as shear zones belonging to the regional scale Burträsk Shear Zone (BSZ), implying that the BSZ itself is not a vertical, but a southeast dipping feature. Our results demonstrate that the crossdip correction is a highly useful alternative to more sophisticated processing methods for noisy datasets. This highlights the often underestimated potential of rather simple, but noise-tolerant methods, in processing hardrock seismic data.

1 Introduction

Today, northern Scandinavia is generally considered to be a low seismic hazard area. There are a number of intraplate earthquakes connected to the post-glacial rebound, but only very few of them exceeding a magnitude of 4-4 (Bödvarsson et al., 2006). In the past, however, the post-glacial adjustments seem to have been more intense. Throughout northern Scandinavia, up to 15 m high fault scarps extending for tens of kilometers (Fig. 1) suggest the occurrence of violent earthquakes at the end or directly after the last glacial retreat (e.g. Lagerbäck and Sundh, 2008; Olesen et al., 2013; Kuivamäki et al., 1998). Based on sediment
deformation and liquefaction features, the magnitude of the earthquakes associated with some of these post- or end-glacial faults has been estimated to be in the order of magnitude of 7-8 (Arvidsson, 1996; Mörner, 2005). Since the discovery of the first faults in the late 1980s, they have been of special interest to scientists and society. The most important question is, of course, if the large intraplate earthquakes are repeatable or unique events.

Understanding the post-glacial faults requires imaging their deeper structure – which is a challenge of its own. On the one hand, finding a balance between signal penetration and resolution to be able to image a (potentially) very narrow shear zone at several kilometers depth is required. On the other hand, inaccessibility of the terrain in northern Scandinavia confines seismic data acquisition to existing roads and tracks, often resulting in profiles with a very crooked geometry. If a reflector has a crossdip component, this can lead to focusing problems and time shifts that significantly reduce the quality of the stacked image.

These challenges are not unique to post-glacial faults and several different processing approaches exist. Among the possible approaches are advanced methods like 3D processing and 3D pre-stack migration. Although treating a swath 3D survey over a 3D geological structure as a proper 3D dataset is doubtlessly the most appropriate approach, there are some limitations due to the small crossline aperture and uneven midpoint distributions (Nedimović and West, 2003). Moreover, binning the traces in 3D reduces the average data fold considerably. In typical hardrock settings, often exhibiting a comparably low signal-to-noise level, this might affect the quality of the final image considerably. A more simplistic, but more noise-tolerant, approach is to correct for the effects of crossdipping reflectors and continue processing the dataset in 2D. This idea is not new (e.g. Larner et al., 1979; Du Bois et al., 1990; Kim and Moon, 1992; Nedimović and West, 2003)

(e.g. Larner et al., 1979; Du Bois et al., 1990; Kim and Moon, 1992; Wu et al., 1995; Nedimović and West, 2003), but none of the existing correction methods is optimally suited to image a feature like a post-glacial fault since either the quality of the imaging deteriorates by applying the correction as a static shift or an unrealistically patchy crossdip distributions results because of the automatic detection of the crossdip angles. This will be discussed in more detail in section 3.1. Thus, we decided to adapt the crossdip correction to our needs and develop a module that is easy to use within our processing software. Moreover, the implications of the crossdip correction have never been tested extensively. Possible interactions with other processing steps, like the dip-moveout (DMO) correction, should especially be studied in more detail.

Since 2007, a couple of reflection seismic profiles over post-glacial faults have been recorded. In case of the Pärvie (Juhlin et al., 2010; Ahmadi et al., 2014) and Suasselkä faults (Kukkonen et al., 2009; Abdi et al., 2015), the fault scarps could be linked with dipping reflections but for the Burträsk fault (Juhlin and Lund, 2011), no reflection directly connected to the fault scarp was observed. However, Juhlin and Lund (2011) imaged a dipping reflection which they could indirectly link to the fault.

They attributed the lack of a clear reflection at the fault scarp to the crookedness of the profile and the complex geometry of the fault at the intersection with the seismic line (Fig. 2). The Burträsk fault is, however, of special interest since it is the seismically most active post-glacial fault and one of the most seismically active areas in the whole of Sweden. Therefore, we decided to reprocess the Burträsk dataset, applying an adapted crossdip correction to the data.

This paper is divided into two parts. The objectives of the first part are to develop a local crossdip correction module and to test its interactions with other processing steps to establish an optimized processing scheme. In the second part, we apply
Figure 1. Post-glacial fault scarps in northern Sweden derived from LiDAR data (Mikko et al., 2015). The majority of the post-glacial faults strike north-northeast or northeast but both the Burträsk and Röjnoret faults deviate significantly from this trend. Deformation zones ©Geological Survey of Sweden.

our crossdip correction module to the Burträsk dataset to improve both the imaging of the fault and other reflectors below the profile and to refine the geological interpretation using information about the strike and dip of the reflections obtained by the crossdip analysis.

2 Geological setting

The survey area is situated in the Paleoproterozoic rock formations of the southern Skellefteå District. The main structural feature of the area is a wide, dextral shear zone, suggested to have formed by lateral escape during the Svecokarelian orogeny (Romer and Nisca, 1995). Following Romer and Nisca (1995), we will refer to this feature as the Burträsk Shear Zone (BSZ). It was subdivided further by Rutland et al. (2001), but for simplicity we continue using the original definition.

The BSZ marks the transition from metasedimentary rocks in the south to an area dominated by magmatic rocks in the north (Fig. 2). The metasedimentary rocks belong to the Bothnian supergroup – a sequence of sediments of mostly turbiditic origin that was accreted and metamorphosed during the Svecokarelian orogeny. They consist mainly of highly deformed and migmatized meta-graywackes, meta-argillites and paragneisses (Kathol and Weihed, 2005). The magmatic rocks in the northern
part are attributed to have originated from two different phases of magmatism: The early Svecokarelian calc-alkaline intrusive rocks are mostly of granodiorite or tonalitic composition and are tentatively dated to 1.96-1.86 Ga (Kathol and Weihed, 2005). The late to post Svecokarelian granites likely originated from magmas derived from the middle and upper parts of the crust during a period of intense deformation and regional metamorphism at approximately 1.82-1.76 Ga (Kathol and Weihed, 2005).

However, the exact tectonic evolution and timing of the magmatism in the area is still debated and a couple of different models exist (Rutland et al., 2001; Rutland et al., 2001; Weihed, 2003; Juhlin et al., 2002; Lahtinen et al., 2009; Skyttä et al., 2012).

Similarly, the age of the BSZ is still discussed and suggestions range from 1.825 Ga (Romer and Nisca, 1995) to 1.86 Ga (Rutland et al., 2001; Rutland et al., 2001; Skiöld and Rutland, 2006) and 1.895 Ga (Weihed et al., 2002). However, most authors agree that the peak of regional metamorphism in the area was around 1.825 Ga (Rutland et al., 2001; Rutland et al., 2001; Weihed et al., 2002) and no major re-activation has so far been documented after 1.79 Ga. Since no borehole or seismic data are available, the geometry of the BSZ at depth is interpreted from surface observations and tectonic considerations. Romer and Nisca (1995) suggest a vertical strike-slip zone whereas Rutland et al. (2001) prefer an oblique fault with the hanging-wall on the southern side.

The Burträsk fault scarp consists of a series of mostly southwest-northeast oriented segments, together forming a c. 35 km long lineament (Fig. 2). In the easternmost part, it follows a deformation line belonging to the BSZ (Fig. 2-1) and in the central part, it continues sub-parallel to the BSZ, cutting through a large intrusion east of Bygdeträsk (Fig. 2-2). In the westernmost part, the deformation zones of the BSZ change direction to a more east-west orientation and the fault scarp starts to diverge from the BSZ (Fig. 2-3). The fault scarp is usually 5-10 m high and generally covered by a variable layer of Quaternary sediments dominated by till, clay and silt. In a few locations, scarp outcrops forming slightly overhanging cliffs are observed (Lagerbäck and Sundh, 2008). Based on sediment liquefaction features close to Umeå, Mörner (2005) suggested a M>7 event for the formation of the fault scarp. On the other hand, Lagerbäck and Sundh (2008) found several sediment liquefaction and water escape structures during an extensive study of sediment deformation in the area, but were not able to establish any relationship between the intensity of deformation and the proximity to the fault scarp.

### 3 The local crossdip correction

#### 3.1 Previous applications of the crossdip correction

One of the main challenges of crooked acquisition lines is that the trace midpoints have an offset component perpendicular to the profile direction (Fig. 3). In the following, we will refer to this component as ‘cross-offset’. As a consequence, the depth to a reflector with a crossdip component can vary for individual traces in a CDP gather, leading to an additional term in the traveltime equation (Nedimović and West, 2003):

$$ t^2(x, y, h) = (t_0(x) + p_y y)^2 + p_x^2 h^2 $$

where $t$ is the traveltime; $t_0$ is the zero time of the reflection; $x$ is the inline offset; $y$ is the cross-offset; $h$ is the source-receiver distance; $p_x$ is the slowness in profile direction and $p_y$ the slowness perpendicular to the profile.
Figure 2. Geological map of the survey area and location of the Burträsk profile. The Burträsk fault (red line) can roughly be divided into three parts, marked with the red numbers. The yellow lines mark the surface projection of reflector planes corresponding to the most prominent reflections in the seismic data with solid lines used for well constrained surface locations and dotted lines for poorly constrained locations. Note that the actual reflection points are shifted laterally for reflectors with a large crossdip component. The map inset shows an enlargement of the fault scarp and the red arrows indicate the location of the fault scarp. The location of the map is indicated in Fig. 1. Geological map ©Geological Survey of Sweden; elevation data ©Lantmäteriet.

These time shifts are not accounted for in the standard NMO processing which can result in focusing problems. Larner et al. (1979) defined the crossdip correction $\Delta_{tcross}$ in the form of:

$$\Delta_{tcross} = \frac{2 \sin \phi}{v} y = p_y y$$  \hspace{1cm} (2)

where $\phi$ is the crossdip angle and $v$ is the velocity medium velocity (Fig. 3).

The underlying assumption of this correction is that the reflector has no dip component in the profile direction (see Nedimović and West (2003) for a more general form of the crossdip correction).
Figure 3. Ray geometry for a crooked acquisition line above a crossdipping reflector. \( y \) denotes the cross-offset, \( h \) the offset between shot and receiver, \( \phi \) the crossdip angle, \( v \) the medium velocity and \( t_0 \) the zero-offset traveltime for a ray without cross-offset.

The effect of uncorrected crossdip on the stacked seismic section depends mainly on the distribution of the cross-offset, i.e. on the geometry of the acquisition line. Figure 4 shows a synthetic example of an NMO corrected gather including two reflections affected by crossdip at 0.4 s (A) and 1.2 s (B), respectively. The cross-offset distributions of these reflections correspond to the distributions at CDP 350 and 1350 of the Burträsk profile (Fig. 2). The energy of the upper reflection (A) is completely smeared and is hardly visible in the stack (Fig. 4b). For the lower reflection (B), one cross-offset value is dominating the whole distribution, causing the energy to focus at 0.8 s instead of 1.2 s. As a result, the reflection appears in the stack, but shifted in time (Fig. 4b).

Unlike the case for a reflector dipping in the profile direction, the crossdip correction has no lateral component, but it requires specific knowledge of both crossdip angle and velocity in the cross-profile direction or cross-slowness, respectively. Since these parameters are usually unknown, they have to be derived from the data.

Despite the simple form of Eq. 2, the correction has been applied in quite different ways by different authors. Initially, Larner et al. (1979) calculated the crossdip correction simultaneously with the residual statics solution. In their fundamental paper, Nedimović and West (2003) developed a procedure for an automated crossdip correction where they invert for the cross-slowness by a grid search using the product of semblance and a local running average of the amplitudes as the objective function. For each estimated cross-slowness, they evaluate the reliability by thresholding the stack’s amplitude and modal filtering. Finally, they correct for the estimated crossdip while stacking using a slant stack approach. Other authors have used the same slant stack approach, but with manually determined crossdip values (Kim and Moon, 1992; Kim et al., 2014). A more simplistic approach is applying the crossdip correction as a static shift to the whole trace (Lundberg and Juhlin, 2011; Ahmadi et al., 2014) (Wu et al., 1995; Rodriguez-Tablante et al., 2007; Lundberg and Juhlin, 2011; Ahmadi et al., 2014). However, this approach generally decreases the quality of all other reflections in the trace and is consequently mostly used for analyzing the crossdips without applying the correction (Urosevic et al., 2007; Rodriguez-Tablante et al., 2007; Malehmir et al., 2009; Dehghannejad et al., 2010, 2012; Hedin, 2015). (Urosevic et al., 2007; Malehmir et al., 2009; Dehghannejad et al., 2010, 2012; Hedin, 2015).

While the problems with applying the crossdip correction as a static shift are obvious, there are some more subtle disadvantages with implementing it using the slant stack approach. First of all, the slant stack procedure makes any further processing after the crossdip correction impossible. This might be problematic since there are very likely interactions between crossdip,
Figure 4. Synthetic CDP gather illustrating the principle of the crossdip correction. Panel (a) shows a NMO corrected CDP gather including two reflections with 10° crossdip originating at 0.4 s and 1.2 s. The cross-offset distribution corresponds to the cross-offset distribution of CDPs 350 and 1350 of the Burträsk data and the dotted blue lines mark a window around the biased reflection time $t_0 + \Delta t_{cross}$. The comparison of the uncorrected stack (wiggle trace) with the theoretical stack (red line) in panel (b) indicates that reflection A is missing and reflection B is shifted. In the slant stack in panel (c), reflection A is correctly imaged but reflection B appears twice in the trace. After The CDP gather after crossdip correction, the energy is aligned at the correct time in the CDP gather panel (d) shows that reflections A and in B are shifted back to their origin time, $t_0$. In the corrected stack of the corrected CDP gather in panel (e), both reflections are correctly imaged.

DMO and NMO corrections. Another issue occurs when a CDP gather is dominated by one cross-offset value. In this case, the reflection occurs twice in the stack: at the origin time as well as at the shifted time corresponding to the dominating cross-offset (red arrows in Fig. 4c). To avoid this reflection duplication, we decided to use a method which moves the energy of a crossdipping reflection to its origin time. Furthermore, we opted for a manual analysis of the crossdip angles since automatic detection, as in the method of Nedimović and West (2003), is susceptible to noise and might pick up inline dip variations and NMO residuals resulting in unreasonably patchy dip distributions.

3.2 A new module for local crossdip correction

We developed a module for a local crossdip correction of individual reflections that can be directly used in a commercial software package. In our module, the reflections are approximated by a polygonal chain with the crossdip values defined at the vertices of the chain. Between the vertices, the crossdip values are linearly interpolated. For the actual correction, we use a cut-and-shift method where reflections affected by crossdip are cut in a window around the biased reflection time $t_0 + \Delta t_{cross}$.
Figure 5. Reflector geometry used in the synthetic modeling. Model 1 (a) comprises reflectors with 5°, 10°, 20°, 30° and 45° crossline dip from top to bottom. Model 2 (b) consists of a series of reflectors with 5°, 10°, 20°, 30° and 45° inline dip. Model 3 (c) features reflectors with inline dips of 8.5°, 16.1°, 22.2°, 26.6° and 29.1° and crossline dips of 29.1°, 26.6°, 22.2°, 16.1° and 8.5°. The blue line represents the acquisition line and the black line the CDP line of the Burträsk dataset.

(area between the blue dotted lines in Fig. 4a), shifted back by the correction term Δt_{cross} and added to the trace at their origin time t₀ (area between the blue dotted lines in Fig. 4d). This procedure can lead to gaps in the corrected traces, but is necessary to prevent reflection duplication as in the case of reflection B in Fig. 4c.

Along with the crossdip values, the user defines the width of the correction window at each vertex and a constant velocity for the whole profile. We have decided to use the crossdip angle as the main parameter since it is more intuitive than the crossslowness, but it is very important to be aware of the coupling between crossdip angles and velocities. Therefore, we recommend to translate variations and uncertainties in the velocity into a range of possible crossdip angles for geological interpretation.

The module also includes an interactive function for analyzing the crossdip angles. Analogous to velocity analysis, the crossdip values can be picked interactively on stack panels corrected with a constant crossdip angle. Thereby, it is possible to observe the effect of the correction on a whole reflection and not just on a CDP gather.

4 Synthetic tests

We created a series of synthetic test datasets using the same acquisition geometry as in the Burträsk dataset. The modeling is based on the simple modeling approach outlined by Ayarza et al. (2000). In this method, the traveltimes are calculated from the geometry of the acquisition line and the reflectors, while the amplitudes are obtained using the formulas of Aki and Richards (1980). The seismic traces are created by convolution of a scaled spike at the calculated traveltime with a Ricker wavelet.
Figure 6. Results of the first synthetic model with reflectors dipping in the crossline direction. The reflections in the stacked section without crossdip correction (a) are heavily deformed and smeared. Using the optimum stacking velocities instead of the model velocity (b) reduces the smearing locally, but the reflections remain distorted. After crossdip correction, the reflections become focused and flattened (c).

4.1 Model 1

The first model consists of a series of reflectors with increasing crossdip in a constant velocity medium (Fig. 5a). The objectives of this model were to test the correction method and to analyze the effects of crossdip on the stacked section. Figure 6a shows a stack of the synthetic data from model 1 using the true model velocities. Depending on the geometry of the acquisition line and the dip angle, the reflector crossdip manifests itself as interference effects and smearing of the reflections in the stacked section. A subsequent analysis of the optimum stacking velocities yielded alternating high-/low-velocity patches mimicking the mean cross-offset. However, the stack quality remained poor for the reflections with larger crossdips since the NMO correction can only account for hyperbolic traveltime distortions (Fig. 6b). When applying our crossdip correction module, we were able to retrieve the correct crossdip angles for all reflectors and the reflections in the stacked section were effectively focused and flattened (Fig. 6c).
Figure 7. Results of the second synthetic model with reflectors dipping in the inline direction. The top panel (a) shows a stack without crossdip correction that exhibits the normal smearing due to inline dip. The bottom panel (b) shows a stack with a constant crossdip correction of -10° applied. The reflections get clearly distorted due to the falsely applied crossdip correction. In most areas, smearing is increased but locally, reflections focus slightly.

4.2 Model 2

The second model was set up to evaluate how much inline dip can be picked up by the crossdip correction and consisted of a series of plane reflectors with increasing inline dip in a constant velocity medium (Fig. 5b). As expected, it was not possible to find any crossdip angles that consistently improved the stack of this dataset. Applying the crossdip correction clearly distorts the reflections (Fig. 7). Some very localized focusing also occurs, but overall, the smearing of the reflections increases considerably.

4.3 Model 3

The aim of the third model was to test the interactions of the crossdip correction and the DMO correction and to establish the preferred order of these steps in the processing flow. The model features a series of reflectors with different ratios of inline and crossline dip in a constant velocity medium (Fig. 5c). Figure 8 shows two versions of the stacked section with (a) crossdip correction applied before DMO correction and (b) after DMO correction. In the first case, picking the optimum crossdip angle proved to be a bit challenging due to local maxima caused by the uncorrected inline dip. However, these occurred within a few degrees of the correct value and we were able to retrieve the expected values when picking with a focus on consistency. In the
Figure 8. Results of the third synthetic model with reflectors dipping in the inline and crossline direction. Comparison of the stacked section with crossdip correction before DMO correction (a) and with crossdip correction applied after DMO correction (b). In both cases, the reflections become focused and flattened but in the second case, artifacts are stronger.

second case, similar difficulties arose because of artifacts introduced by the DMO correction. Again, focusing on consistency helped to identify the optimum crossdip angles. In both versions of the stack, the reflections become flattened and focused, but the first version, with the crossdip correction applied before the DMO correction, contains less artifacts and is slightly more coherent.

4.4 Implications for the implementation of the crossdip correction

As demonstrated clearly by the results of the first model, crossdip effects can be picked up by stacking velocities, manifesting themselves as alternating high-/low-velocity patches. Therefore, it is important to re-analyze stacking velocities after correcting for crossdip and to review the obtained crossdip angles with the updated velocity model. Furthermore, the results from the second and third model highlight the importance of picking only crossdip angles that consistently improve the image of a whole reflection (segment) in order to exclude local optima caused by interactions between the effects of inline and crossline dip. The advantage of the manual crossdip correction approach is that it is possible – to a certain extent – to identify and avoid these interactions whereas the automatically conducted DMO correction is inevitably influenced by them.

Based on these results, we recommend an iterative processing sequence, where the crossdip correction is applied after an initial velocity analysis, followed by repeated velocity analyses and DMO correction. As mentioned above, the crossdip angles should be reviewed after this sequence and the whole sequence should be repeated, if necessary.
Figure 9. Illustration of the iterative processing scheme for the implementation of the crossdip and DMO corrections. The repetition of the residual statics correction after each velocity re-analysis is optional.

sequence of NMO correction, crossdip correction and velocity re-analysis followed by a second sequence of DMO correction and repeated velocity analysis. Both sequences should be repeated with the updated velocity models until no more significant improvements are achieved (Fig. 9). A surface consistent residual static correction should be included at least once before the first iteration of crossdip correction sequence and can be repeated after each velocity analysis, if required. However, the interactions between residual statics and crossdip correction are limited since the former is a surface consistent shift of the whole trace whereas the latter is a local shift of a small part of the trace depending on the mean cross-offset of each trace.

These recommendations are only valid for a manual crossdip correction. If the correction is derived automatically from the data, DMO should be applied first to avoid picking up local effects of inline dip.

5 Reprocessing of the Burträsk dataset

5.1 Data Processing

The ca. 22 km long Burträsk profile was recorded on acquired using an asymmetric split spread of 280 channels with 20 m spaced geophones with a natural frequency of 28 Hz single component geophones. The receiver spacing and the nominal shot spacing were 20 m and the signal was generated using a VIBSIST hydraulic hammer source (Cosma and Enescu, 2001) with a nominal shot spacing of 20 m. Since the source could not be activated in the vicinity of buildings, shot coverage is quite sparse close to inhabited areas. As a result, the fold varies considerably over the profile (Fig. 10a). Similarly, the data quality is affected by random noise and coherent noise originating e.g. from the source, surface waves and ground roll to a varying extent. All shot gathers have a relatively high background noise level, but some feature very distinct first arrivals and clearly visible reflections whereas others show mostly noise with first arrivals barely identifiable after a few hundred meters
(Fig 11). As a first order estimate of the average signal-to-noise ratio, Fig. 10a illustrates the ratio between the mean amplitude of the background noise in a 200 ms window before the first arrival and the mean amplitude of the first arrival in a 200 ms window starting at the first arrival (see also Fig 11).

The first part of the reprocessing followed the original processing flow from Juhlin and Lund (2011) quite closely. Due to the high noise level in some areas, we re-picked the first arrivals manually and re-analyzed the stacking velocities. We applied an additional ground roll and first break muting step following Oren and Nowack (2018). In their method, ground roll and first breaks are estimated by soft thresholding in the local time-frequency domain (Liu and Fomel, 2013) and subtracted from the data. Apart from that, there are only minor differences to the original processing, including slightly lower bandpass filter frequencies and a spherical divergence correction instead of an automatic gain control. A summary of the processing is given in Table 1.

Following the procedure outlined in the Sect. 4.4, we incorporated the crossdip correction directly after residual statics corrections, re-analyzed the velocities, applied a DMO correction and analyzed the velocities again and re-analyzed the velocities. With the new pre-DMO-velocity model, we updated the crossdip angles and repeated the DMO correction using the post-DMO-velocity model. Repeating this, we iteratively applied DMO correction and velocity re-analysis. Repeating the residual static correction did not lead to any significant improvements. Figure 12 illustrates the effect of the crossdip correction in CDP gather 926. However, this CDP is not representative as most gathers feature much higher noise levels, making it very difficult to observe the focusing of reflections. Therefore, the crossdip analysis was carried out on constant crossdip stack panels. During the first pass of this procedure the crossdip and DMO correction sequences, the velocities changed substantially after each step, but converged during the second pass. The final stacking velocity model is much more consistent along individual corrections than the initial one, but seems to be still biased by dip effects. For comparison, we also tested applying another processing scheme, where the crossdip correction is applied after the DMO correction, but could not produce a stack of comparable clarity.

Migration testing using a smoothed stacking velocity model for migration yielded poor results, confirming that the stacking velocities do not correspond to true subsurface velocities. The are still biased by residual dip effects. Among tests with Kirchhoff migration, Finite Difference migration, different phase-shift migration algorithms and Stolt migration, the best results were archived for a Stolt migration with a constant velocity of 5400 ms⁻¹. This velocity is also consistent with the velocities obtained during the refraction statics correction. Finally, the section was depth converted using the same constant velocity. However, it is important to note that the depth values are only an estimation of the real depth since considerable uncertainties exist in the deeper part, where the velocity is poorly constrained.

Additional to the reflection seismic processing, we carried out first break tomography using the PStomo_eq solver by Tryggvason et al. (2002, 2009). We carried out the inversion in To simulate a thin velocity layer above the bedrock, we used a 2D starting model with a steep velocity increase from 1500 ms⁻¹ to 5400 ms⁻¹ in the first 40 m below the surface and a gradual velocity increase to 5800 ms⁻¹ towards the bottom of the model. We conducted the inversion on a 3D grid with a cell size of (x, y, z) = (20 m, 20 m, 10 m) while simultaneously estimating a statics solution to eliminate the influence of sub-grid scale velocity variations on the model. To estimate the resolving power of the tomographic model, we ran a checkerboard test using
### Table 1. Summary of the processing flow used for reprocessing the Burträsk dataset.

<table>
<thead>
<tr>
<th>Step</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Manual firstbreak picking</td>
</tr>
<tr>
<td>2</td>
<td>Trace balance: 0-3000 ms</td>
</tr>
<tr>
<td>3</td>
<td>Groundroll and firstbreak muting in local time-frequency domain: 25% threshold</td>
</tr>
<tr>
<td>4</td>
<td>Spectral equalization: 30 Hz window, 25-40-120-150 Hz bandpass</td>
</tr>
</tbody>
</table>
| 5    | Time variant bandpass filtering:  
|      | - 0-200 ms: 35-60-120-180 Hz  
|      | - 250-500 ms: 30-50-120-180 Hz  
|      | - 600-900 ms: 25-40-110-165 Hz  
|      | - 1100-3000 ms: 20-35-100-150 Hz |
| 6    | Refraction statics: floating datum, replacement velocity from model |
| 7    | Trace editing |
| 8    | Horizontal median filter: 11 traces, 5300 ms<sup>−1</sup> & 3000 ms<sup>−1</sup> |
| 9    | Butterworth filter: 20-40-90-120 Hz |
| 10   | Spherical divergence correction: 0.8 tpower, 2.0 vpower |
| 11   | Velocity analysis |
| 12   | NMO correction: 40% stretch mute |
| 13   | Residual statics |
| 14   | Crossdip correction: 5400 ms<sup>−1</sup>, 20% taper;  
|      | Velocity Analysis |
| 15   | DMO correction;  
|      | Velocity Analysis |
| 16   | Stacking |
| 17   | FX Deconvolution: 19 trace window |
| 18   | Trace balance |
| 19   | Stolt migration: 5400 ms<sup>−1</sup>, 0.6 stretch factor |
| 20   | Zeromute |
| 21   | Approximate depth conversion: 5400 ms<sup>−1</sup> |

The starting model perturbed with a 3D pattern of 500 m wide and 100 m thick checkers (Fig. S1). For the inversion of the checkerboard model, we used the same parameters as in the main inversion, but did not estimate a static solution. The results show that the uppermost checkers, including the bedrock surface, are reconstructed well but most of the lower checkers are poorly reconstructed or not reconstructed at all, indicating that only velocity variations close to the bedrock surface can be resolved properly and that the lower part of the tomographic model is poorly constrained.
Table 2. Estimated strike and dip the most prominent reflections.

<table>
<thead>
<tr>
<th>Reflector</th>
<th>Inline dip</th>
<th>Crossdip range assuming ±15% velocity variation</th>
<th>Inferred strike</th>
<th>Inferred dip</th>
</tr>
</thead>
<tbody>
<tr>
<td>A1</td>
<td>13°</td>
<td>2° ± 0.3°</td>
<td>234°–237°</td>
<td>~ 13°</td>
</tr>
<tr>
<td>A2</td>
<td>26°</td>
<td>−6° ± 0.9°</td>
<td>213°–217°</td>
<td>26°–27°</td>
</tr>
<tr>
<td>A3</td>
<td>17°</td>
<td>16° ± 2.5°</td>
<td>265°–274°</td>
<td>22°–25°</td>
</tr>
<tr>
<td>B1</td>
<td>49°</td>
<td>−2° ± 0.3°</td>
<td>48°–49°</td>
<td>~ 49°</td>
</tr>
<tr>
<td>B2</td>
<td>34–40°</td>
<td>−14° ± 2.2°</td>
<td>61°–70°</td>
<td>36°–41°</td>
</tr>
</tbody>
</table>

Reflection B2 branches in the upper part, therefore we used two different inline dip values in the estimation.

5.2 Results

Figure 10 shows a comparison between the unmigrated original stack (b), a reprocessed version of the stack excluding the crossdip correction (c) and a reprocessed version including the crossdip correction (d). The comparison of (b) and (c), both conventional DMO stacks, illustrates the effects of the basic reprocessing of the data (mainly an improved refraction and residual static correction, an improved velocity model and first break and ground roll muting). The comparison of (c) and (d) isolates the changes caused by the crossdip correction. The original stack contains a series of northwest dipping reflections and reflection packages, referred to as A1-A4, and a series of southeast dipping reflections, named B1-B3. Even without the crossdip correction, the reprocessing enhanced the continuity and coherency of the reflections considerably. Especially reflections A3, B3 and B4, which are barely visible in the original stack, are imaged much clearer after the basic reprocessing. Analysis of the crossdip angles yielded mostly values in the range of ±16° except for two deeper reflection packages, both with a crossdip of 24° (Fig. 10d). Northwest of CDP 1600, cross-offsets proved to be too small to determine any crossdip angles. The effect of the crossdip correction on the individual reflections depends to a large extent on their respective cross-offset distribution and crossdip angle. Not surprisingly, there is little change for the mainly inline oriented reflections A1 and B1 (Fig. 10). Reflections A2 and A3, which are in an area with comparably small cross-offsets, become more focused and can be followed to greater depth after crossdip correction, but stay essentially in the same position. In contrast to this, reflections B2 and B3 have vertical shifts of up to 100 ms caused by large, unevenly distributed cross-offsets. As a results of these shifts, reflection B2 looses its slightly listric appearance (Fig. 10). Moreover, two reflections appear only after crossdip correction: a rather weak reflection directly above reflection package B3 and a sub-horizontal reflection package close to the lower end of reflection B2, called C1 in the following (Fig. 10d).

Before converting inline and crossdip angles into strike and dip of the reflection, the possible range of velocities should be translated into a possible range of crossdip values. Table 2 shows inferred strike and dip values for a ±15% velocity variation, corresponding to a velocity range of 4590 ms⁻¹ to 6210 ms⁻¹. Note that this is not an error estimate since it does not include uncertainties in the picking of the crossdip values.
None of the above mentioned reflections are associated to the segment of the fault scarp intersecting the seismic line at CDP 1720. There are some indications of dipping reflections which might be connected to the fault scarp, but these are too weak to interpret with confidence (Fig. 13). However, the surface projection of reflection B1 coincides with the extrapolation of the scarp segment west of the seismic line around CDP 1600 (Fig. 2). At the same location, the geological map features a deformation zone, but the strike does not agree well with the estimated strike of reflection B1 (Fig. 2).

Figure 14 shows the velocity model from the first break tomography. Due to the sparse spatial coverage, we reduced the 3D model to a 2D image displaying the mean of the model within 100 m distance from the receiver line in bright colors and otherwise the average of the model in the crossline direction in pale colors. Due to the high velocity contrast between the Quaternary sediments and the bedrock, most rays were guided along the bedrock surface and did not penetrate into the deeper parts.

In the upper part of the bedrock, the velocity is mainly around 5300–5500 m\text{s}^{-1} and increases slightly with depth (Fig. 14) but this might be an artifact of the starting model since the checkerboard test indicated that the velocity is not well resolved in the lower parts of the model. The model features several low velocity zones; the largest one at around \(x = 4.0\) km to \(x = 4.5\) km and coinciding with the location of the fault scarp, some smaller ones around \(x = 5.0\) km, \(x = 5.5\) km and \(x = 9.0\) km and a couple of very localized ones throughout the whole profile.

6 Discussion and Interpretation

6.1 Crossdip correction

Both synthetic modeling and the field data example have clearly demonstrated the benefits of applying the crossdip correction to crooked line seismic data. As several previous studies have already illustrated, crossdip can de-focus and smear reflections, resulting in a poor stacked image (e.g. Larner et al., 1979; Kim and Moon, 1992; Nedimović and West, 2003). Another quite rarely mentioned aspect is that it can lead to vertical shifts, distortion and duplication of out-of-plane reflections, as well. Our local crossdip correction addresses this problem by shifting back reflections affected by crossdip and thereby projecting them into the CDP plane. However, the drawback of this procedure is that it cannot handle crossing reflections very well. Therefore, the applicability of our method to areas with complex, distributed reflectivity patterns is limited. In such areas, more extensive testing is needed to develop an appropriate correction scheme since existing schemes, like the one of Nedimović and West (2003), do not account for the reflection duplication problem.

Apart from improving the imaging of crooked line seismic data, the crossdip correction has the advantage of extracting information on the 3D orientation of reflections, information which can be crucial for the geological interpretation of the seismic data. This can be especially important in low signal-to-noise data with low fold where sparse swath 3D processing is not an option.
6.2 Data Reprocessing

Processing crooked line seismic data from hardrock settings includes a whole range of different challenges. Apart from crossdip effects, imaging quality is often affected by residual static shifts, surface waves, coherent noise, strong ground roll, etc. As in many other studies (e.g. Juhlin, 1995; Pretorius et al., 2003; Urosevic et al., 2007; Place and Malehmir, 2016), the most important steps in the basic reprocessing of the data proved to be the manual picking of first arrivals for improving the static correction and a careful velocity analysis. Furthermore, the comparison between Fig. 10b and 10c illustrates that the final image benefited considerably from using an analytical gain instead of applying an AGC since the contrast between the main reflections and the background reflectivity is preserved.

6.3 Origin of the reflections

The reflections in the final stack are mostly planar and occur in a relatively low reflectivity surrounding (Fig. 13). There are different possible origins for such reflections. The first possibility is a contact between different lithological units. Along the CDP line, the surface geology map features several lithological contacts (Fig. 2 & 13), but these contacts will only produce reflections if there is a significant difference in seismic impedance between the two lithological units. Both the output bedrock velocity from the refraction statics correction and the first break traveltime tomography do not show any significance changes in bedrock velocity along the profile. This observation along with the lack of correlation between the seismic reflections and surface geology (Fig. 13) and the fact that some reflections are clearly cross-cutting sub-horizontal background reflections (Fig. 13), make lithological contacts a rather unlikely candidate. A second possibility is deformation or shear zones with either decreased or increased seismic impedance due to fracturing and/or re-mineralization processes. Whether or not such zones are visible in seismic data depends not only on the impedance contrasts, but also on the width of the zones. Theoretically, features with a minimum width of $\lambda/30 - \lambda/20$ (Sheriff and Geldart, 1995), corresponding to 2.4–4.5 m for a peak frequency of 60–75 Hz and a velocity of 5400 ms$^{-1}$ in this survey, are detectable in seismic reflection images. In practice, the detectability limit depends strongly on the signal-to-noise ratio of the data. In the Burträsk survey, the signal level is relatively low, so a more realistic estimation of the detectability limit is $\lambda/12 - \lambda/8$, corresponding to a width of 6–11.25 m. Since the profile intersects a couple of deformation zones belonging to the BSZ (Fig. 2), it is quite plausible that some of the reflections are caused by shear zones. Another possible scenario is that some reflections originate from magmatic dykes and/or sills. The Burträsk area was subject to intense migmatization and hosts intrusions from different magmatic pulses prior to, during and after the Svecokarelian orogeny (Kathol and Weihed, 2005). Thus, both sills and dykes are likely to occur along the profile. Due to the quite non-impulsive nature of the signal (even after deconvolution) and the high noise level, it is not possible to infer any reliable information about the internal structure of the reflections from an analysis of polarity and tuning effects.

In the following, we will discuss the nature of the most important reflections in the Burträsk profile. B1 is a relatively weak planar reflection that can only be observed clearly over a short depth interval, but in the unmigrated stack there are some indications that it might continue to greater depths. (Fig. 10) Moreover, it seems to cut through the mostly sub-horizontal background reflectivity (Fig. 13), arguing against a lithological boundary. Since the surface projection of reflection B1 coincides
both with a projection of the western scarp segment (Fig. 2) and a low velocity zone in the tomography model (Fig. 14), we interpret B1 as a reflection from either the western scarp segment itself, or from the continuation of the shear zone along which the western scarp segment has ruptured. The small vertical extent of the reflection might be explained by a rather narrow shear zone that drops below the detection limit as the frequency content and signal strength decrease with depth.

Similar to B1, reflection B2 cross-cuts sub-horizontal background reflections (Fig. 13) and its surface projection coincides with a narrow low velocity zone in the tomography model (Fig. 14). Again, we interpret B2 as a reflection from a shear zone, but the relation to the Burträsk fault is less obvious. The prominence of the reflection might suggest that the movement of the post-glacial fault at depth took place along reflection B2 and that the visible fault scarp segments are merely the branches of that fault where the surface rupture occurred. Branching of post-glacial fault scarps seems to be a common phenomenon and has been observed for the Pärvie and Lansjärv faults (Talbot, 1986; Juhlin et al., 2010; Ahmadi et al., 2015). Since the Burträsk fault is seismologically very active, earthquake locations might give a hint which fault plane is active at depth. Recent studies show the micro-earthquakes clustering along a southeast dipping plane, but unfortunately, the accuracy of the locations is not sufficient to distinguish between the closely spaced reflections B1 and B2 (Lund et al., 2016). In any case, B2’s estimated strike of 61°–70° is not consistent with the strike of the fault scarp but rather matching the trend of the BSZ in the southern part (Fig. 2). Therefore, we prefer to interpret B2 as a reflection from a local shear zone belonging to the BSZ and not connected to the Burträsk fault. It is, however, still possible that B2 extends further to the southwest and connects with the westernmost scarp segment.

Since reflection B4 projects to the surface close to a mapped deformation zone (Fig. 2), we tentatively interpret it as another local shear zone belonging to the BSZ.

Both of the two deepest reflections, B3 and C1, exhibit strong reflectivity and terminate very abruptly at the upper end. Neither data fold and amplitude ratio (Fig. 10a), nor the overall impression of the image quality (Fig. 10d & 13), indicate a significant drop in data quality, so the abrupt terminations seem to be real features. Together with the high reflectivity, this suggests that reflections B3 and C1 are caused by sill or dike intrusions (Planke et al., 2005).

Unlike most of the other reflections, A2 and A3 are dipping to the northwest and their approximate surface projections are well south of the BSZ (Fig. 2). At 0.8 s, reflection A2 is clearly intersecting with a sub-horizontal reflection segment (Fig. 10d & 13), precluding the possibility of a lithological contact. The geometry of reflections B2, A2 and A3 and the apparently lower dip of reflection A3 could be interpreted as a positive flower structure, consistent with the proposed oblique convergence of the Skellefteå district from the southeast (Bergman-Weihed, 2001). However, the true dips of reflections A2 and A3 are relatively small and very similar (Table 2) and the estimated strikes of reflections A2, A3 and B2 do not match at all (Fig. 2). So in this case, the additional information from the crossdip analysis argue against the hypothesis of a flower structure. Instead, the occurrence of several magmatic bodies southeast of the profile points towards a magmatic origin of the reflections, possibly as feeder dikes following pre-existing weak zones in the upper crust. It is not clear from the present data set how reflection A1 should be interpreted.

Even though only reflections B1 and B4 can be directly correlated to deformation zones in the geological map, the dominance of southeast dipping reflections in the northwestern part of the profile suggests that the BSZ formed as a south-side-up dip-slip...
an oblique fault system as interpreted by Rutland et al. (2001) and not as a vertical strike-slip zone as suggested by Romer and Nisca (1995).

6.4 Imaging of the fault scarp

The lack of a clear reflection connected to the fault scarp at CDP 1710 might be due to several different reasons. First of all, it could be caused by the absence of a resolvable contrast in physical properties. As discussed above, the fault zone needs to have a certain minimum width to be detectable in the seismic data. However, the post-glacial Pärvie and Suasselkä faults have successfully been imaged with reflection seismic using very similar acquisition parameters (Juhlin et al., 2010; Abdi et al., 2015, respectively). So if the Burträsk fault has similar characteristics, it should be well detectable in the seismic data. Another possibility is that the reflections from the fault scarp are not stacked properly due to the complex, three-dimensional geometry of the fault at the profile location. In this case, the reflections should still be clearly visible in the shot gathers. The shot gathers, however, exhibit only very blurred dipping reflections covered by various forms of noise. Figure 10a shows that between CDP 1600 and 1800, both the data fold and the average amplitude ratio between first arrival and the background noise are exceptionally low, indicating a poor signal-to-noise ratio. Therefore, the most likely explanation for the lack of a reflection connected to the fault scarp is simply the result of insufficient data coverage and quality.

6.5 Relation between post-glacial fault and BSZ

The relation between the Burträsk fault and the BSZ is still not fully understood. Compared to the majority of the known post-glacial faults, which predominantly strike north-northeast, the Burträsk fault has an unusually strong east-west component. In contrast to this, the neighboring Röjnoret fault is mostly north-south oriented, following yet another set of Paleoproterozoic shear zones (Fig. 1). This divergence from the main trend of post-glacial faults might indicate that the faults in the Skellefteå area were to a very large extent guided by pre-existing weak zones in the crust. However, the Burträsk fault only follows individual deformation zones closely in the northernmost part (Fig. 2(1)) and runs sub-parallel to the BSZ in the central part (Fig. 2(2)). Since the reflection seismic image has shown that there are potentially many more shear zones than the ones marked in the geological map, it is likely that the fault still follows weakness zones belonging to the BSZ. South of the large jump north of Bygdsiljum (Fig. 2), the fault scarp starts to diverge significantly from the BSZ where the latter turns to a more east-west orientation (Fig. 2(3)), suggesting that the orientation of the BSZ was no longer conducive to the prevailing stress field controlling the rupture direction. Therefore, we speculate that the BSZ acted as a guide for the Burträsk fault, causing its orientation to deviate from the orientation of the majority of post-glacial faults. During the rupture, the fault probably jumped between different weak zones to accommodate differences between the orientation of the BSZ and the orientation of the minimum horizontal stress.
7 Conclusions

In the first part of this paper, we presented a new software module for a local crossdip correction and tested the influence of crossdip on synthetic seismic data. An often forgotten effect of crossdip is that – depending on the cross-offset distribution – it can not only de-focus and smear reflections, but also shift them in time. Most existing crossdip routines rely on a slant stack approach for the correction which has the drawback that shifted reflections will appear twice in the stack. Within our new module, we use a shift and stack method to overcome this reflection duplicating problem and enable further processing after the correction. The synthetic test examples demonstrate that the crossdip correction can interact both with the stacking velocities and the DMO correction. Based on these tests, we proposed an iterative processing scheme where a sequence of crossdip correction, velocity analysis, DMO correction and velocity analysis is repeated until the stacked image converges.

In the second part of this paper, we presented results of reprocessing data from the Burträsk profile using our new module. After crossdip correction, several reflections became significantly more continuous and coherent. An improved static solution and the use of an analytical gain also contributed considerably to the quality of the final image. The improvements we achieved during reprocessing illustrate the often underestimated potential of relatively simple methods, like the crossdip correction and the traditional filtering and muting, in processing noisy hardrock seismic datasets. Moreover, strike and dip values estimated from the crossdip angles helped in associating the seismic reflections to geological features. We interpreted most of the southeast dipping reflections as shear zones belonging to the BSZ, implying that the BSZ is not a vertical, but a southeast dipping feature. The north to northwest dipping reflections in the southernmost part of the profile are likely attributed to magmatic intrusions. Due to the low data fold and high noise level close to the Burträsk fault, the scarp segment intersecting with the profile could not be imaged. However, we obtained a clear reflection from another scarp segment slightly further west, dipping southeast at approximately 49°.

Author contributions. C.J. and R.B. conceived the analysis method. R.B. developed the software module (written for GLOBE Claritas, available on personal communication) and carried out the data analysis and interpretation. R.B. prepared the manuscript and C.J. reviewed it.

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Figure 10. Comparison between the original processing of the Burträsk dataset and the reprocessing at different stages: (a) Fold distribution along the profile and mean amplitude ratio between the first 200 ms of data and the background noise; (b) original stack from Juhlin and Lund (2011); (c) reprocessed stack without crossdip correction; (d) reprocessed stack with crossdip correction overlain by the crossdip angles used in the correction. The blue arrows indicate a possible continuation of reflection B1. The comparison of (b) and (c) highlights improvements due to the conventional reprocessing steps like statics, updated velocity model etc. and the comparison of (c) and (d) illustrates the effects of the crossdip correction.
Comparison between the original processing of the Burträsk dataset and the reprocessing at different stages: (a) Fold distribution along the profile and mean amplitude ratio between the 200 ms of data and the background noise; (b) original stack; (c) reprocessed stack without crossdip correction; (d) reprocessed stack with crossdip correction overlain by the crossdip angles used in the correction. The small blue arrows indicate a possible continuation of reflection B1.

Figure 11. Unprocessed shot gathers illustrating variations in the background noise level. The upper shotgather (a) displays very clear first arrivals along the whole spread whereas the lower shotgather (b) is dominated by noise for larger offsets. The light blue and red lines mark the windows used for estimating the amplitude ratio between background noise and first arrival (c). The dark blue arrows indicate reflections.
Figure 12. Crossdip correction of an NMO corrected reflection in CDP 926 of the Burträsk data. In the uncorrected CDP gather (a) the reflection is approximately flat in the first traces and inclined in the later traces (correction window marked with blue lines). Consequently, the stack of this gather (b) features two weak maxima (red arrows). After crossdip correction, the reflection gets flattened (c) and the weak maxima in the stack have merged to one stronger maximum (d). Note however, that the reflections are very difficult to observe in most other CDP gathers and that the crossdip analysis has therefore been carried out on constant crossdip stack panels.
Figure 13. Migrated section along the Butträsk profile. For comparison, the surface geology is plotted on top of the section and the location of the fault scarp and deformation zones are marked. The small blue arrows highlight a very weak reflection that might be associated to the fault scarp. The vertical exaggeration of the section is approximately 1.

Figure 14. 2D slice of the ray coverage and the velocity model from the first break tomography. The upper panel shows the ray coverage in a 100 m wide zone below the receiver line. The lower panel displays the velocity below the receiver line in bright colors. In areas without velocity information below the receiver line, the average of the velocity model in the y direction is plotted in dim colors. The black triangles mark the location of the fault scarp, the white triangles indicate deformation zones and the grey diamonds correspond to the surface projection of reflections B1 and B2. The vertical exaggeration of the model section is 5.