

Dear Editors,

We highly appreciate the constructive suggestions of the reviewers and your editorial comments. The manuscript has been revised accordingly. In particular, we strengthen the discussion about the data quality and robustness of the results. We have also improved the quality of the figures following the reviewers' comments. For example, following the advice of Dr. Root, in the revised manuscript we add a zoomed figure, which demonstrates variations of the maximal value of the horizontal gradient of the isostatic anomalies for Sinai and surrounding area together with the seismicity. With this figure, we also show the magnetic anomaly map, which demonstrates interesting correlation with the gravity field.

We provide a point by point response to the reviewers' comments and attach the manuscript with marked changes.

We thank you for your suggestions and the attention that you are giving to our paper.

10 With kind regards

M. Kaban on behalf of the co-authors

Response to the comments of the 1st reviewer (Dr. Alexander Minakov).

The original comments are in italic.

15 *Mikhail Kaban and colleagues present in their paper an interesting study linking the seismicity distribution, mantle density structure and isostasy in Egypt and the southeastern Mediterranean region. They compile an extensive database of controlled source and passive seismology data to constrain the crustal model. The conversion of global shear wave velocity model for the mantle is done using mineral physics constraints. The starting density model is further improved using the inversion of both gravity anomalies and residual topography. Their results show that the dense lithosphere in northern*
20 *Egypt corresponds to a low-seismicity region whereas the less dense lithosphere in the northern Red Sea and the Gulf of Aqaba are more seismically active. The authors also find an interesting relation between isostatic anomalies and distribution of seismicity.*

We are grateful to the reviewer for the positive evaluation of our work. His comments are very useful and help us to improve the manuscript.

25 *The presentation of the paper can be improved. The first-order structure of the lithosphere: the regions of continental cratonic and extended/oceanic lithosphere is not easy grasp from the figures. The location of plate boundaries and continent-ocean boundaries would be very useful to show in the figures (both in Red Sea and Mediterranean). Would useful to emphasize which lithospheric plates are involved (Africa, Arabia, Sinai. . .). The figures can be improved. The small symbols for earthquakes are hardly seen (both in maps and cross-sections). Perhaps, zoomed plots for the seismically active*
30 *regions can be included. The density perturbation plots are a bit confusing. Perhaps, a couple of transects with absolute densities and seismic velocities can be shown. Could the location of transects located be added to the maps showing the distribution of seismic events?*

The figures will be improved according to the reviewer's suggestions. In the revised manuscript we will demonstrate locations of the main plate boundaries in the study area. We will also improve visibility of the earthquakes in all figures.

35 The absolute densities will be shown instead of density perturbations in Figs. 5 and 7.

Detailed comments to address for improving the paper:

Page 2. Line 2. *“...compositional variations” in the mantle. What about compositional variations in the crust vs temperature* Line 12. *Which studies: controlled-source, ambient noise etc. please, detail.*

We specify these details in the revised manuscript. This is also described in details in the section 3.3 „Model of the crust“.

Line 25. *“..satellite and terrestrial data” including land areas (complementary to satellite radar altimetry).*

5 This clarification is added.

Line 30. *“1-2 parameters” what are these parameters? Thicknesses, densities? Line 31-32. “..gravity approach”. Do you mean inversion?*

Yes, this is clarified in the revised manuscript.

Page 3. Line 1. *“entirety” do you mean entire? Line 5. “marginally touches” ? do you mean “partly covers”?*

10 Correct, this is clarified.

Line 6. *“low seismicity in northern Egypt..”. Why does it appear anomalous? Please, explain.*

We clarify that these seismically passive zone are bounded by very active regions. One of the main goals of this study is to explain the anomalously low seismicity in northern Egypt.

15 Line 9. *“shear zones”. Where are these shear zones located? Hardly can be seen in the figures..Please, show these shear zone more in the figure. Figure 1 can be improved to make visible earthquakes and faults.*

We have removed this unclear statement. This figure is improved according to the reviewer’s suggestions.

Line 24 *Do you mean Arabian Plate? Please, detail..*

Yes, this is clarified.

20 Page 4. *Figure is very busy. Perhaps, presenting zoomed northern Egypt would be useful. Please, show more clearly shear zones.. What are the “principal trends” of plate motion?*

Following the reviewer’s suggestion, we demonstrate a zoomed figure for northern Egypt.

Page 5 Line 23. *“existing global dynamic models”. Which one is used in this study?*

This is clarified in the following parts of the paper.

Page 6. *How do you find the isostatic topography? Do you do iterations? Do you have analytic formula?*

25 Here we mention the isostatic gravity anomalies. Their computation is described in the following parts.

Page 7. *Please, add COB and location and type of plate boundaries in the figure.*

The figure is improved based on the reviewer’s suggestions.

Page 8. *“p-wave” velocity, “P-wave” velocity or “Vp” ? please, choose one.*

P-wave velocity is used as a definition for the term Vp. This is clarified.

Page 9. Location of seismic determinations are confusing because of association with seismicity distribution. Could you improve it? Is the interpolation/extrapolation of crustal thickness based on singular measurements (e.g. southern part of figure)? Perhaps, would be necessary to blank the area beyond certain search radius of interpolation. Could you add an uncertainty estimate from kriging?

- 5 We clarify that these are seismic determinations of the crustal structure. It is difficult to estimate the overall accuracy of the Moho map because it is based on several existing models and even the accuracy of the existing seismic determinations is undefined. It is used as an initial approximation, which is adjusted then in the inversion.

Line 18. "initial density model". Sometimes absolute densities and density perturbations are interchanged in the text and formulas. Could you make it clear what you are talking about in each particular case?

- 10 We have clarified this issue.

Page 10. Line 17. The absolute densities would be important for computation of residual topography. Please, detail.

We agree that the residual topography depends on the absolute densities. However, the reference model chiefly influences the average level of this parameter, which is not interpreted in this study. We consider only variations of the residual topography, which are less sensitive to absolute densities. This is clarified in the revised manuscript.

- 15 Page 11. Line 7. 1x1 degree resolution. What do you mean? Grid cell size? Line 9. Why 325 km depth? Please, explain why you chose with depth as a lower limit of the model.

Yes, this is the grid cell size. The 325 km depth is chosen based on our previous studies as a depth, which exceeds the maximal depth of the lithospheric roots. This is important since the inversion is performed globally. This is clarified in the revised manuscript.

- 20 Page 12. Line 6. "rho_ref". Does it refer to Table 1? Please, comment on the application of this formulation to oceanic domains..

In the description of the Eqs. 1 it is specified that "rho - rho_ref" is the relative density below sea level including water, which means that rho=rho_water at corresponding depths in the ocean.

- 25 Page 13. What is the difference between "t_res" and "t_dyn" do you use the different "B" operators to compute them. Do you obtain isostatic topography using the compensation depth of 325km given mantle density model? Do you iterate? Please, detail..

- 30 The dynamic topography is a part (chiefly long-wavelength) of the residual topography. In the mantle, we are already considering all dynamic effects, which depend on the viscosity of the mantle, but not a simple isostatic column as in Eqs. 1 for the crust. This is clarified in the text. We also add an additional reference to the original papers, where this method was initially introduced and fully tested.

Line 14. "The anomalies at the 45 km depth". What kind of anomalies (not clear)?

These are the density anomalies obtained in the inversion. This is clarified.

Page 14. Can you show a difference plot between starting and final density model? This would be very useful to appreciate the inversion results. How much the initial model was updated comparing various regions?

- 35 Page 15. Please, show a profile with absolute density/seismic velocity to better present the lithospheric structure. Please, show the location of transects and epicenters on the same map.

We have demonstrated in Fig. 7 (now Fig. 8) in the revised manuscript the corrections together with the final density variations. In this figure we show absolute densities of the mantle. In the profiles we still keep their perturbations, which are essential for the interpretation. Also, the reference density in each layer is not adjusted in the inversion and therefore is somewhat arbitrary. This is clarified.

5 *Page 15. Line 3. "vertical resolution". What resolution you are talking about? Do you have a reference for that?*

The vertical resolution is limited by the model set-up in the inversion. This is clarified.

Page 17. Line 3. "neutral or slightly positive densities". Better small positive density anomalies. "Shallow Moho discontinuity..material". Do you mean this material is mantle rocks and located below the Moho?

Yes, we mean the material below the Moho. Both statements are changed accordingly.

10 *Line 12. Please, replace "section" to "Profile" to denote transects in the text. Otherwise, to me it is confusing with the manuscripts sections.*

We have replaced "section" to "profile" in the whole manuscript.

Line 31. Reference to "Steckler, M. and U. ten Brink 1986. Lithospheric strength variations as a control on new plate boundaries: examples from the northern Red Sea. Earth and Planetary Science Letters, v. 79, nos. 1 and 2, p. 120-132" would be useful here.

15

Thank you for this recommendation. We have added this reference.

Page 18. Line 1-3. What does it low and high density anomalies reflect? Temperature, different composition? Please, explain. Line 14. "mantle batholiths in the upper crust". Do you mean granite batholiths or mantle plumes? Please, explain.

20 We clarify that these are likely temperature related anomalies. To clarify, we have changed "mantle batholiths" to "mantle intrusions".

Line 17-18. "Standard simple models . . . differ from the real density structure". "Models" and "structures" not exactly comparable things.. Line 23. "long-wavelength FIELD" do you mean gravity anomalies? What are these wavelengths that you are considering long?

25 We have changed to "Standard simple models . . . don't adequately describe the real density structure". The boundary wavelength corresponds to the maximum resolution of the density model (1x1 degree), therefore it is equal to approx. 222 km, which is clarified.

Line 24. Do you mean about 10 mGal variation?

Correct.

30 *Page 19. Figure 9. Symbols are too small to be seen. Leave just "mGal" for colorbar. The plot is very busy the symbols are masked by the color of the background.*

The figure is enlarged. We are obliged to keep the SI unit, however also add mGal for clarity.

Response to the comments of the 2nd reviewer (Dr. Bart Root).

The original comments are in italic.

5 *The authors present a regional study of the lithosphere underneath Egypte. The density structure is studied by combining gravity data with other geophysical information of the crust and upper mantle. The motivation of the study is to see if there is a relation between the observed seismicity and the density structure of the subsurface. I find this an interesting approach and application for the presented gravity field modelling done in the study. And in my opinion this relation could even be relatively more addressed. The study is performed with a well documented methodology. I believe this paper could become interesting after some improvements:*

10 Thank you for the positive evaluation of our study. We appreciate all the comments and will implement them in the revised manuscript.

My suggestions for improvement:

15 *R1: Transparency of data and methods. I find the data and models used should be more explicitly discussed. This would give a better understanding of the robustness of the presented model. on page 5 line 19-20, data from Stolk et al. (2013) is used. But what data is this in Egypte (location, value, uncertainty.) page 6 line 4 "available seismic models" -> which models? page 7 line 5 "...several regional datasets" -> which ones and how did this affect the model? line 8 "... various data-sets..." similar questions?*

Actually, in this section we describe only the „general modelling approach“, which is applicable to any region, without specifying particular data sets. All the data are described in the following section 3.3 “Model of the crust”. This is clarified. Also, we strengthen discussion of the robustness of the used data-sets in the revised manuscript.

20 *page 11 line 9-10: which seismic model is used for the deep Earth and how does it relate to Schaeffer and Lebedev (2013) model? Is it compatible? And by removing the deep Earth, is only the gravity field of the mantle anomalies removed or also the dynamic signal due to the mantle convection?*

25 The Schaeffer and Lebedev (2013) model provides velocities only for the upper mantle. Therefore, for the deeper layers we use the model s40rts of Ritsema et al. (2011). For the upper mantle it well corresponds to the first model, but its resolution is lower. We take into account the dynamic effects of the mantle convection. These issues are clarified.

How is this related to your later isostasy study? page 13 line 6-8 "The technical details... (2015a, Supplementary)", could this be described in a few line, such that the reader does not have to go to this other literature. It will improve the readability of the manuscript.

30 For the isostasy study, we intend to separate the gravity anomalies, which are chiefly related to the density inhomogeneities in the crust, which are not compensated in both ways: via density heterogeneity of the lithosphere or dynamically from the mantle. Therefore, the residual anomalies not adjusted in the inversion represent a large scale part of the isostatic anomalies, which might be responsible for the stress concentration and seismicity. This is clarified.

Page 19 line 11-12 "many other factors controlling seismicity" -> which are?

Primarily, these are deformations related to plate motions. This is clarified.

R2: Overall, I find the authors could elaborate and discuss more on their findings, because this is the most interesting part of the paper. Some examples: page 12 line 20 "however, they have several principal differences" -> which are, please discuss them.

- 5 These differences are chiefly related to different relative amplitudes of the anomalies depending on the depth to the anomalous body responsible for them. This is clarified.

page14 Figure 7 shows the densities in the upper mantle. I miss the discussion between figure 5, where also densities of the upper mantle are shown. Why are there differences and what can they teach use about the subsurface. And maybe to keep the comparison fair, similar depths and wavelength bandwidths should be used, because now it is difficult to compare the quantitative differences. Could the differences tell use about different compositions in the upper mantle?

10

The densities in Fig. 5 represent the initial model of the mantle, and in Fig. 7 – the final model after the inversion. In the revised manuscript we show in Fig. 7 also the corrections to the initial model, which fully demonstrate the changes after the adjustment. In the revised manuscript we show density variations in Fig. 5 at the same depths as in Fig. 7.

R3: One of the most interesting issues is the relation of the seismicity to the (non-)isostasy. I find this should get more attention in the manuscript, only after page 18 I read about it. One of the conclusions is (page 19 lines 7-13) is that seismicity occurs in zones with high gradients. Would it be better to plot the gravity gradients and find out? Maybe use invariant of gradients, this would remove the reference frame dependencies, or another method? It would back-up this conclusion.

15

Thank you for this advice. In the revised manuscript we show a zoomed figure, which demonstrates variations of the maximal value of the horizontal gradient of the isostatic anomalies for Sinai and surrounding area together with the seismicity.

20

Minor comments:

m1 table 1: might be better to use a graph, because than it is better to compare to other literature that uses graphs. Or might be good to use both.

- 25 We still prefer to use the table format since it is important to see exact values of the reference densities. An additional graph would be excessive to our opinion.

m2: Figure 2, please add to what degree and order is used in this figure in the caption.

Added.

m3 Figures with longitude and latitude: I miss the labels in many of the maps.

- 30 They have been added to the figure captions (Fig. 1).

m4 Figure 8: Why was the Moho not inserted in this figure. It would be a good addition to the cross-sections and give the reader a better understanding of the constructed model.

We have added the Moho in the profiles in Fig. 8.

5 *m5: page 5 line 21: how does the uncertainty in the empirical relationships of Christensen and Mooney 1995 affect your results?*

These uncertainties might be significant and correspond up to approximately 30 mGal in terms of the gravity field. Therefore, making the inversion we allow for additional corrections of the crustal densities. This is clarified in the revised manuscript.

10 *m6: textual detail: page 13 line 18 and 21 "as mentioned above" was used twice. Also, this is a bit ambiguous, is it about the sentence, section, or whole paper above this line.*

Corrected.

m7: page 18 line 23: "long-wavelength field" -> field. What is meant with longwavelength, specify with d/o.

The boundary wavelength corresponds to the maximum resolution of the density model (1x1 degree), therefore it is equal to approximately 180 d/o, which is clarified.

15

Density structure and isostasy of the lithosphere in Egypt and their relation to seismicity

Mikhail K. Kaban¹, Sami El Khrepy^{2,3}, Nassir Al-Arifi²

¹GFZ German Research Centre for Geosciences, Telegrafenberg A 20, D-14473 Potsdam, Germany

5 ²King Saud University, Riyadh, Saudi Arabia, P.O. Box 2455, Riyadh 11451, Saudi Arabia

³National Research Institute of Astronomy and Geophysics, NRIAG, 11421, Helwan, Egypt

Correspondence to: Mikhail K. Kaban (kaban@gfz-potsdam.de) and Sami El Khrepy (selkhrepy@ksu.edu.sa)

Abstract. A joint analysis of the new satellite-terrestrial gravity field model with the recent data on the crustal structure and seismic tomography model was conducted to create an integrative model of the crust and upper mantle; and to investigate the relation of the density structure and the isostatic state of the lithosphere to the seismicity of Egypt. We identified the distinct fragmentation of the lithosphere of Egypt into several blocks. This division is closely related to the seismicity patterns in this region. The relatively dense and strong lithosphere in the Nile Delta limits the seismic activity within this area, while earthquakes are mainly associated with the boundaries of this block. In the same way, the relatively strong lithosphere in the Suez Isthmus and northern Mediterranean prevents the Gulf of Suez from opening further. The central part of Egypt is generally characterized by an increased density of the mantle, which extends to the Mediterranean at a depth of 100 km. This anomaly deepens southward to Gilf El Kebir and eastward to the Eastern Desert. The average density of the crystalline crust is generally reduced in this zone, indicating the increased thickness of the upper crust. The low-density anomaly under the northern Red Sea is limited to 100–125 km, confirming the passive origin of the extension. Most of the earthquakes occur in the crust and uppermost mantle in this structure due to the hot and weak upper mantle underneath. Furthermore, an asymmetric lithosphere structure is observed across the Northern Red Sea. The isostatic anomalies show the fragmentation of the crust of Sinai with the high-density central block. Strong variations of the isostatic anomalies are correlated with the high level of seismicity around Sinai. This tendency is also evident in the North Red Sea, east of the Nile Valley, and in parts of the Western Desert.

1 Introduction

25 A thorough understanding of the solid Earth system is an essential step towards deciphering the link between the dynamic processes in the Earth system and near-surface processes. In particular, the density heterogeneity of the lithosphere and upper mantle largely controls tectonic processes, which in turn produce strong density perturbations in the upper crust. Therefore, the knowledge of density variations is essential to understand the structure and dynamics of the lithosphere. Up to now, seismological methods have been a key to unravelling the structure of the crust and upper mantle and provide an increasingly detailed image of the interior of the Earth. However, they cannot provide a complete image of the structure of the crust and upper mantle. For example, seismic velocities in the upper mantle are more sensitive to temperature than to

compositional variations (e.g., Tesauro et al., 2014); therefore, tomography images primarily reflect temperature variations. A clear example is represented by high-density eclogitic rocks, which are characterized by seismic velocities that are close to normal upper mantle conditions and therefore are almost invisible in seismic models (Krystopowicz and Currie 2013). It is also important that different seismological methods provide different estimates of various parameters. On the other hand, the gravity field of the Earth, which directly images density variations, cannot be used separately to model density heterogeneity. The inverse gravity problem is essentially ill-posed and its solution depends completely on initial model assumptions. Therefore, the identification of density variations in the crust and upper mantle is challenging and this problem cannot be solved by a particular geophysical method alone. Recent efforts aimed at integrating multiple geophysical and petrological datasets in a common interpretation framework (e.g., Fullea et al., 2009; Gradmann et al., 2013; Kaban et al., 2001; Kaban et al., 2014a).

Many seismic studies (chiefly reflection and refraction profiles and receiver function observations) have been performed in Egypt; however, most of them are related to the northern and eastern parts of the country, along the Red Sea and Mediterranean. With respect to recent results, we refer to Abdelwahed et al. (2013) showing the Conrad and Moho discontinuities of Eastern Egypt and the Red Sea. Corchete et al. (2017) determined the crustal and uppermost mantle structure in northeastern Egypt based on Rayleigh wave analysis. Hosny and Nyblade (2016) determined the vertical V_s sections-profiles of the crust and Moho depth for 26 stations in Egypt; however, only few of them are located in the central and south-eastern parts. Most of the previous seismic determinations of the crustal structure were summarized in Stolk et al. (2013) in the crustal model of Asia, which also includes Northeast Africa. These studies show that the coverage of the territory of Egypt based on seismic methods is very heterogeneous. While the areas adjoining the Red Sea and Mediterranean are well studied (El Khrepy et al., 2015 and 2016, Hosny and Nyblade (2016), Mohamed et al., (2014), the data for the central, western, and southern parts are sparse. Several important questions remain unresolved. The main question relates to the structural division of the lithosphere and to what extent the surface tectonic units are related to the deep heterogeneity of the crust and upper mantle.

Recent satellite gravity missions (mainly GRACE and GOCE) provided the possibility to produce new generation gravity models based on the combination of satellite and terrestrial data including land areas (complementary to satellite radar altimetry) (e.g., Förste et al., 2014). These models stimulated new studies of the crustal structure and particularly the determination of the Moho boundary in Egypt and surrounding areas (e.g., Azab et al., 2015; Cowie and Kuszniir, 2012; Prutkin and Saleh, 2009; Salem et al., 2013; Sobh et al., 2016). The results obtained in these studies are very controversial. As already mentioned, the solution of the ill-posed inverse gravity problem highly depends on initial assumptions. The Earth's gravity field is induced by the density heterogeneity of the entire planet; therefore, its inversion with respect to 1–2 parameters (e.g. for determination of the Moho depth and density contrast at this boundary) often provides biased results. Only an interpretation integrating all available geophysical, geological, and mineral physics data might help to overcome this

internal weakness of the gravity approach (inversion). Kaban et al. (2016c) presented an integrative model based on a joint analysis of seismic and gravity data for the entirety of the whole Middle East, which partially covers the area of the present study. However, for the territory of Egypt this model is not defined in that study due to the lack of data, in particularly on the crustal structure. Another problem is related to the evaluation of the isostatic state of the lithosphere, which is often related to seismicity (e.g., Assumpção and Sacek, 2013; Sobiesiak et al., 2007). Segev et al. (2006) published a comprehensive study on this topic for the Levant continental margin and the southeastern Mediterranean area; however, this study covers only marginally touches a small part of Egypt.

One of the motivating objectives is to find an interpretation for the very low seismicity pattern in northern Egypt (e.g. in the Nile Delta, Fig. 1), which is bounded by seismically active regions (ENSN earthquake Catalogues, 1997-2016) in relation to lithosphere structure in this region, which includes highly populated areas and intensive international trade ways. On the other hand, the high level of seismicity, the shallow depth of hypocenters in the northern Red Sea including the shear zones along its western coast should be also investigated with respect to the structure of the crust and upper mantle and to the isostatic state of the lithosphere. The asymmetric seismicity pattern in the northern Red Sea is another subject for discussions. Furthermore, the termination of the Gulf of Suez rift without continuation to the Mediterranean Sea will be also discussed-analysed in relation to the density structure of the lithosphere.

In the present study, we use an integrative interpretation of gravity, seismic, geological, and mineral physics data for the investigation of the density structure of the crust and upper mantle in Egypt and its surroundings, and to evaluate the isostatic state of the lithosphere and its relation to the seismicity in this region. Such kind of an integrative geophysical study is applied to the study area for the first time; this was made possible due to the availability of new data after establishing in 1997 the Egyptian National Seismic Network (ENSN), which provided the input for new receiver function and tomography models of the Egyptian lithosphere (e.g. El khrepy et al., 2015, 2016; Abdelwahed et al., 2013; Hosny and Nyblade 2016; and Mohamed et al., (2014).

2 Tectonic settings and seismicity of Egypt

The lithosphere of Egypt formed in a very active tectonic frame. In the north, it is bounded by the continental collision zone in which the African Plate subducts under Eurasia with a velocity of approximately 6 mm/year (McClusky et al., 2000). The left-lateral strike-slip Dead Sea Transform continues to the Aqaba Fault Zone at the north-eastern boundary. On the eastern side, the Red Sea represents an active extension zone dividing the African and Eurasia-Arabian plates at a variable extension rate, which increases from the north (~5.6 mm/year) to the south (14 mm/year; McClusky et al., 2003). This active environment produces high and continuous seismic activity in the region (Fig. 1). Sinai represents a sub-block of the lithosphere (microplate), which is bounded by the Aqaba and Suez fault zones. It is still under debate as to which principal

continental plates, African or Eurasian, it can be attributed with respect to its deep structure and dynamics. West of the Red Sea, the Eastern Desert extends to the Nile Valley. In the south, it is a part of the Nubian Shield, while the northern and north-eastern parts are covered by Eocene sediments. The Western Desert covers the majority of Egypt west of the Nile Valley. The Gilf Kebir Plateau is located in the southwestern corner of Egypt (Fig. 1).

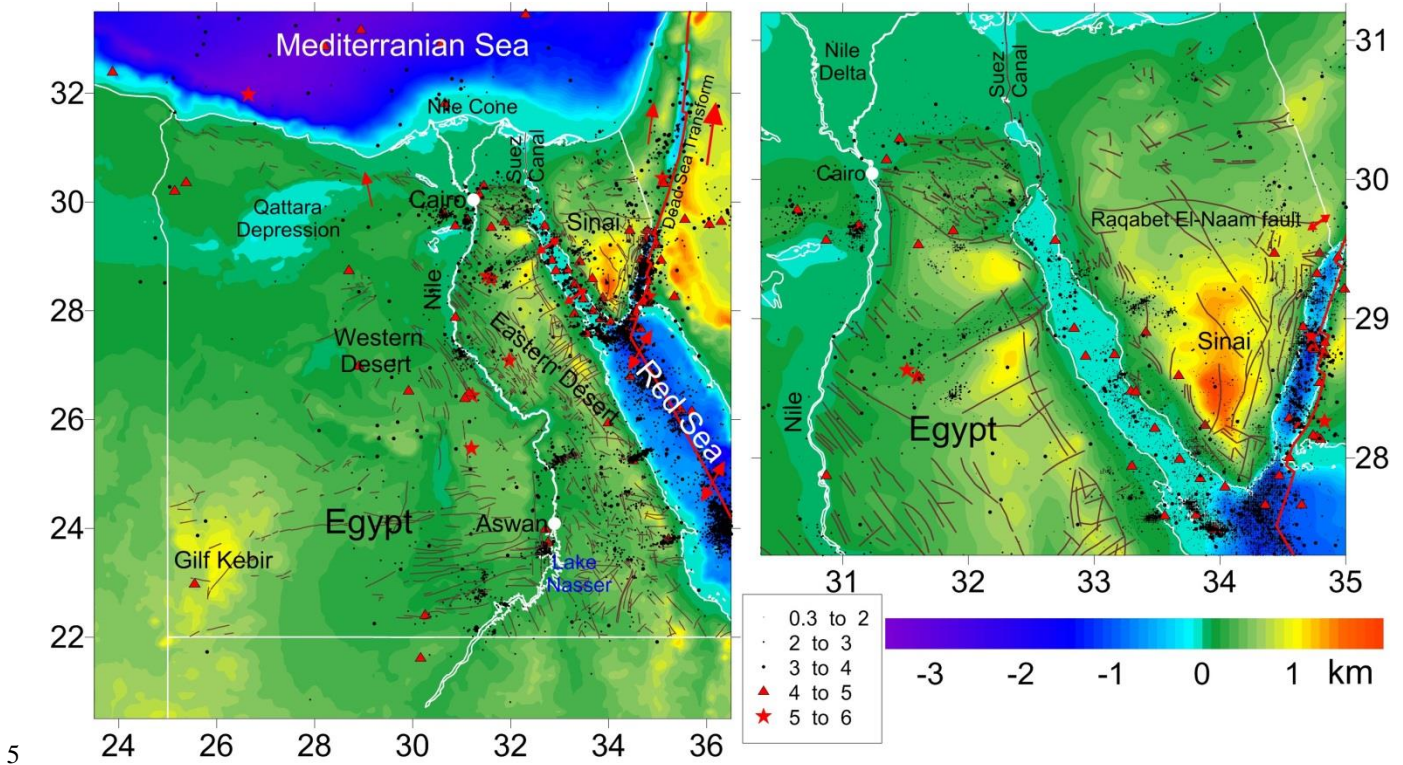


Figure 1. Topography of Egypt and surrounding area. Zoomed image of the north-eastern part of the study area, which is seismically most active, is shown in the right. Black dots, red triangles and stars show seismicity of Egypt- (Egyptian National seismological Catalogue ENSN 1998-2011) seismicity. In the map of the whole region, only earthquakes with magnitudes > 2 are demonstrated. Black-Brown lines show faults (Egyptian Geologic Survey and Mining Authority, EGSM, 1992). Red arrows demonstrates principal trend of the plate motions (Stern and Johnson, 2010). Red line delineates the boundary between the African and Arabian plates. The axes show the geographical coordinates in degrees.

Due to its location in the north-eastern African continent, seismic activity in Egypt is mainly controlled by regional stresses from active tectonic surroundings. The interaction of tectonic processes results in different levels of seismicity in Egypt, mostly limited to the crust and upper mantle (Fig 1). Clustered and scattered earthquake activity are well defined to the parallel shear zones along the western Coast of the Red Sea, the entrance and axial trough of the Gulf of Suez, the Cairo

Suez Region, and the eastern part of Egypt. The most intensive zones of earthquake activity and earthquake swarms are located in the North Red Sea, the southern Sinai tip, and the two gulfs of Aqaba and Suez—especially at the intersection of the plate boundaries—while the western part of Egypt is seismically stable, with no remarkable activity (El Khrepy et al., 2015, 2016). The seismicity pattern is directed NW–SE in the Red Sea and Gulf of Suez, in accordance with the Red Sea rift direction. The earthquakes in the Gulf of Aqaba tend NE in the direction of the Dead Sea Rift. The seismicity of the northern coast of Egypt is related to Eastern Mediterranean tectonics associated with the surrounding plate boundaries (Cyprian and Hellenic arcs, Anatolian Fault System) (Fig 1). The seismicity along the Nile River occurs in scattered cluster patterns; the seismic zones along the Nile Valley correspond to its structural configuration (Fig. 1). In southern Egypt, two types of earthquakes occur in the Aswan Area: natural earthquakes due to the activity of the Kalabsha Fault in the southwest of Aswan, and induced earthquake activity corresponding to the artificial Aswan Lake.

Therefore, the seismic activity in Egypt and its surroundings is controlled by many factors. One of our objectives is to determine the relationship between earthquake activity and the density structure of the crust and upper mantle, which are directly related to active geodynamics in this region.

3 Method and initial data

3.1 General modelling approach

In this section we describe a general approach for ~~The~~ integrative analysis of the gravity and other geophysical data follows the procedure that was developed and applied before for Europe, North America, and some parts of Asia (Kaban et al., 2010, 2014, 2015, 2016). All details on the used methods and data sets will be provided in the following sections. This approach implies the following steps:

1. Construction of the initial model of the crust based on available seismic and geological data. This procedure for irregularly distributed data is extensively discussed in Stolk et al. (2013). The crustal model includes at least two layers, sediments and crystalline crust, which are characterized by horizontal and vertical variations of the seismic velocities and density. The densities of the sediments and crystalline crust are determined in a different way. For sediments, we define several types of basins, from “soft” to “hard”, which are characterized by different density–depth relations. These relations are determined based on borehole, compaction, and seismic data (Stolk et al., 2013). The density of the crystalline crust is determined from empirical relationships with seismic velocities (Christensen and Mooney, 1995).

2. The gravity effect of the crust is computed and removed from the observed gravity field. In addition, we remove the effect of deep mantle (below 325 km) heterogeneity based on existing global dynamic models (Kaban et al., 2014b, 2015). The residual gravity anomalies mainly represent the effect of the uppermost mantle and density anomalies of the crust not

included in the initial model, with other uncertainties of the crustal parameters. In the same way, we calculate the residual topography that represents the part of the observed topography/bathymetry, which is not compensated for by crustal density variations including the Moho Boundary. Both these parameters depend on upper mantle density variations but in essentially different ways, which provides the possibility to resolve the vertical density structure (Kaban et al., 2015).

5 3. To study of the upper crust and evaluate the isostatic state of the lithosphere, high-resolution local isostatic anomalies are computed (Kaban et al., 2016b).

4. The initial 3D density model of the upper mantle is created based on available seismic models. The velocity-to-density conversion factor is computed based on mineral physics relations (e.g., Tesauro et al., 2014).

10 5. The residual mantle gravity anomalies and residual topography are jointly inverted to estimate the 3D density variations in the upper mantle. The inversion is constrained by the initial model (step 4); the corrections should be minimal. This way, a stable and unique solution can be found. The joint inversion of the residual gravity and residual topography provides the possibility to resolve the vertical density stratification much better than the inversion of the residual gravity anomalies alone because the residual gravity and topography depend on the density heterogeneity but in fundamentally different ways, depending on the size and depth of the density anomalies. A clear example is a vertical dipole density structure, which is
15 characterized by near zero residual topography however, the gravity field anomaly is very distinctive (Kaban et al., 2015).

~~The uncertainties related to the initial crustal model might be significant, especially in the areas without seismic constrains; therefore, making the inversion we allow for additional corrections of the crustal densities and Moho variations. Compared with previous studies, we also adjust the Moho Boundary in the inversion in places that are not defined well by seismic data.~~

~~More details and the computational setup will be described in the following parts.~~

20 **3.2 Initial gravity field**

The initial gravity field (free air gravity disturbances) is based on the combined satellite-terrestrial model EIGEN-6c4 (Förste et al., 2014), Fig.2. Maximal resolution corresponds to 2190 spherical harmonic degree/order (~10 km spatially), however the actual one depends on the terrestrial observations included in the model. The long-wavelength part, which is constrained by satellite data (chiefly GRACE and GOCE), is limited to degree/order 240. This resolution is sufficient for modelling of
25 the upper mantle structure since maximal resolution of the initial data doesn't exceed $1^\circ \times 1^\circ$. However, for computation of the local isostatic anomalies the full gravity field is employed.

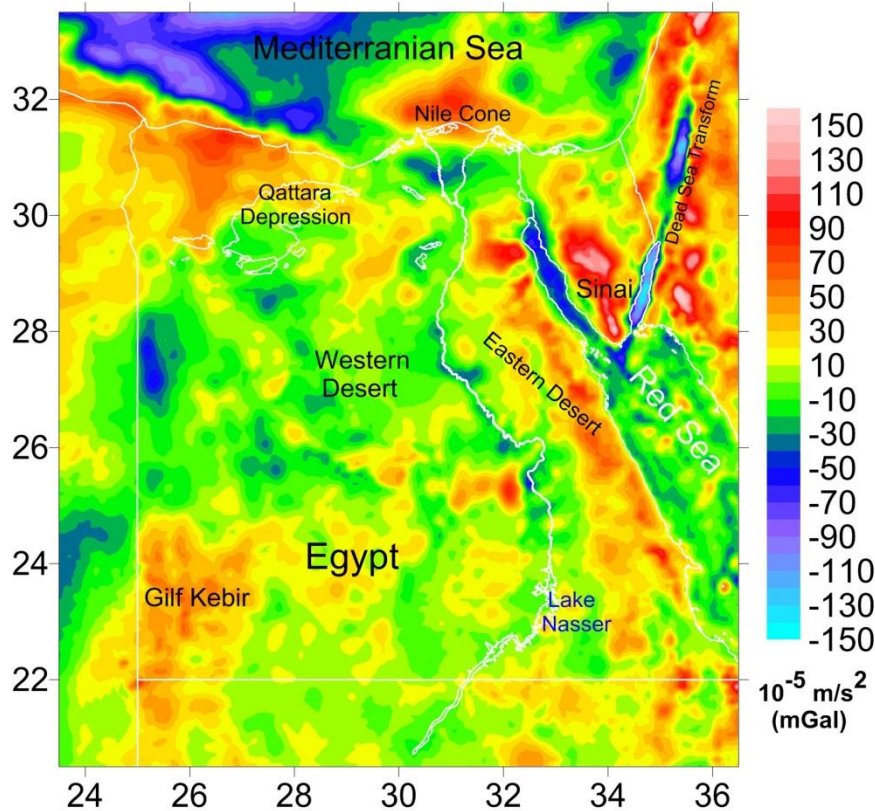


Figure 2. Free air gravity disturbances from the combined satellite-terrestrial gravity model EIGEN-6c4 (Förste et al., 2014). The maximum resolution ($\sim 10 \times 10$ km) corresponds to degree/order 2190.

3.3 Model of the crust

5 We use the EPcrust model (Molinari and Morelli, 2011) as a basis for the western part of the study area and the crustal model of Kaban et al. (2016) for the eastern part. These models have been improved by using several regional datasets. The detailed map of Rybakov and Segev (2004) has been employed for the position of the basement in the northern part of the study area. The resulting thickness of sediments is shown in Fig. 3a. Density of sediments was estimated according to the average density-depth relationship (Fig. 3b), which is based on compilation of various data-sets taking into account density-
 10 compaction by Stolk et al. (2013) and then adjusted for the regional data by Kaban et al. (2016). This relationship reflects only a regional trend; therefore small-scale residual anomalies still reflect local density heterogeneity of the sedimentary layer.

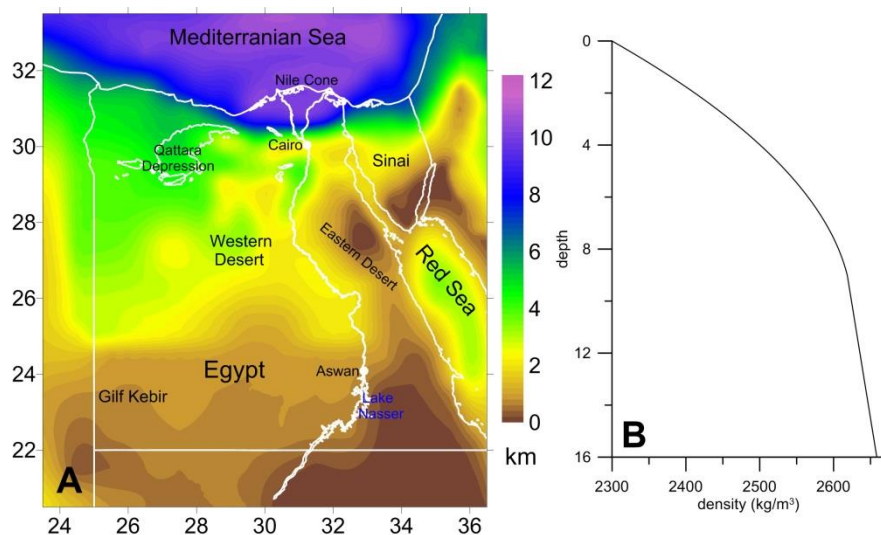


Figure 3. (A): Thickness of sediments for Egypt with surroundings. Gray lines show faults. **(B):** Density-depth relationship used for calculation of the gravity effect of sediments.

The Moho model is verified by using original seismic determinations. Most of them are taken from the database of the US Geological Survey (Mooney, 2010, with updates until April 2017). In addition, the recent receiver function determinations of Hosny and Nyblade (2016) are included (Fig. 4a). For interpolation we used a remove-compute-restore technique developed earlier by Stolk et al. (2013). At the first stage, the measured Moho depths were corrected for the Airy type of isostasy by employing the surface load, which includes the topography/bathymetry and density heterogeneity of sediments. Here, a type of the isostatic compensation is not of primary importance since this correction is restored at the last stage. As demonstrated by Stolk et al. (2013), the residual Moho values show much less variations than the original ones and can be easily interpolated. After interpolation with the ordinary Kriging technique, the isostatic correction was restored. Therefore, the resulting Moho map fully fits to the original determinations, but demonstrates much better correspondence to the tectonic features than it would be for a direct interpolation. In this way, for example, it is possible to trace extended topography features like the Red Sea in the study area, which are measured only in limited places. This map was then merged at the boundaries with above-mentioned basic models (Fig. 4a). It should be clarified that that the Moho depths are defined only in the vicinity of the primary data points (Fig. 4a); in other areas the model represents an initial approximation, which should be improved in further inversion. ~~The final results will be discussed taking into account distribution of the primary data points.~~

For the crystalline crust, the average P-wave seismic velocities (V_p) were determined. For this, the s-wave vertical profiles of Hosny and Nyblade (2016) were converted to ~~p-wave velocities~~ V_p using the V_p/V_s ratios provided. The limited amounts of seismic determinations do not provide the possibility to construct a multilayer model; however, for the gravity

calculations, average values are sufficient to estimate the cumulative effect of the crystalline crust (Kaban et al, 2016a). The interpolated data were merged with basic regional models (Fig. 4b).

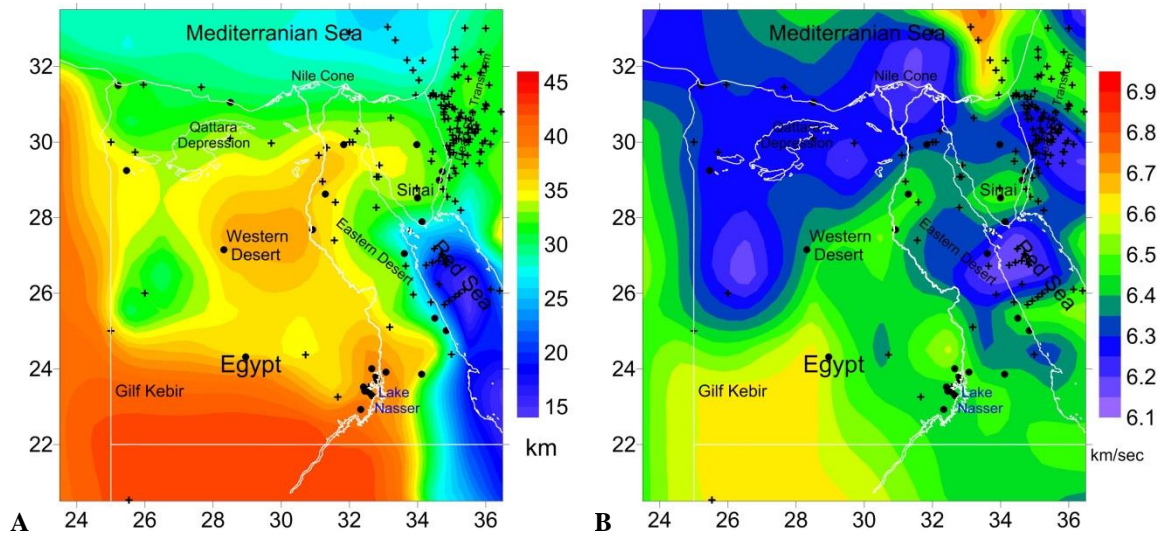


Figure 4. (A). Depth to the Moho. Crosses show crustal determinations of the crustal structure from the data-base of the US Geological Survey (Mooney, 2010, with updates up to April, 2017) and circles – the receiver function results of Hosny and Nyblade (2016). (B) Average pP-wave velocities in the crystalline crust. Crosses show determinations from the data-base of the US Geological Survey (Mooney, 2010, with updates up to April, 2016) and circles – the receiver function results of Hosny and Nyblade (2016). The last ones have been converted from sS-wave velocities.

The variations of the p-wave velocities V_p show the fragmentation of the crystalline crust in Egypt and surrounding areas. The central and northern parts of Egypt and the Sinai massif are characterized by nearly normal velocities (6.4–6.6 km/s), which are typical for the continental crust (Christensen and Mooney, 1995). The velocities in the northern and northwestern parts significantly decreased to 6.1–6.3 km/s; the same is true for parts of the Western Desert and the North Red Sea. We also observe a W–E trend from low to high velocities in the Mediterranean, which likely corresponds to the transition from the oceanic to continental crust (Fig. 4). The maximum around Gifl Kebir is not well defined because it is based on two marginal determinations only. The velocities of the crystalline crust were converted into densities by employing the nonlinear relationships of Christensen and Mooney (1995).

3.4 Initial density model of the upper mantle

The initial density model of the upper mantle is based on the tomography model of Schaeffer and Lebedev (2013), which is converted to densities density variations by applying the mineral physics method of Stixrude and Lithgow-Bertelloni (2005).

A complete description of this technique can be found in (Tesauro et al., 2014; Kaban et al., 2016a). ~~Two-Three~~ slices of density variations for the depths of ~~75-100, 150~~km and ~~150-200~~ km are shown in Fig. 5. The model demonstrates general trends in the area; the density mainly decreases towards the Red Sea at a depth of ~~75-100~~ km in W-E direction (Fig. 5A). At a greater depth, a strong positive anomaly associated with the subducting African lithosphere ~~appears in the north~~ extends to ~~the south~~ (Fig. 5B, C).

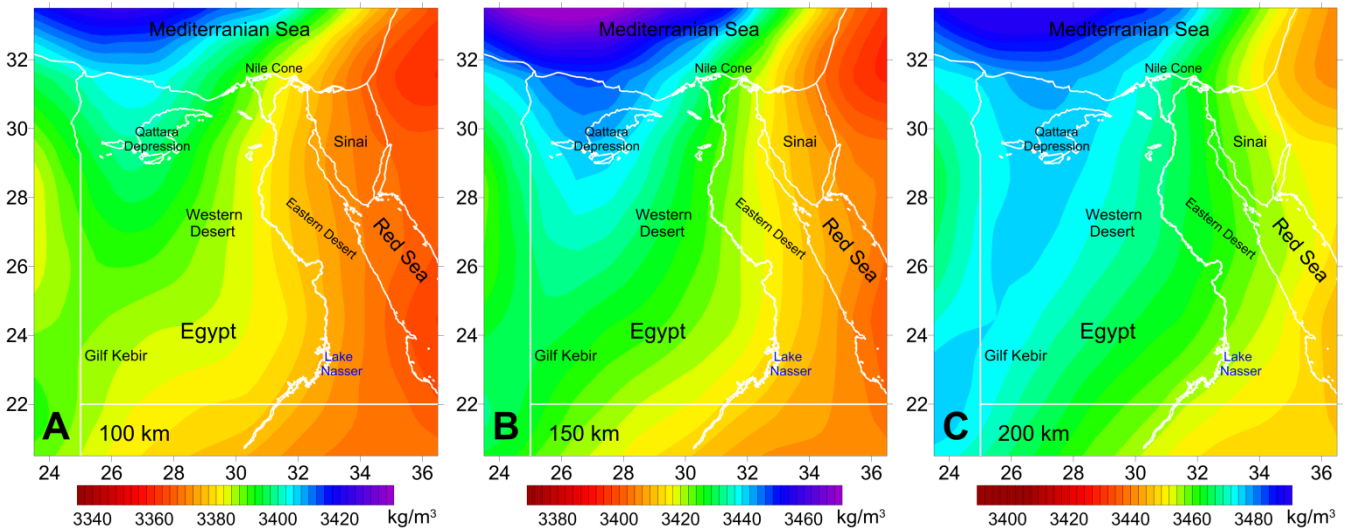


Figure 5. Initial density model of the upper mantle based on the tomography model of Schaeffer and Lebedev (2013). (A): depth ~~75-100~~ km; (B): depth 150 km; (C): ~~depth 200~~ km.

4 Results

10 4.1 Residual mantle gravity anomalies and residual topography

The gravity effect of the crust was determined based on the constructed crustal model. All calculations are performed relative to a reference density model (Table 1). The density of the crustal layers corresponds to the estimates of Christensen and Mooney (1995). The mantle densities are determined as the global averages estimated based on the seismic velocities provided by the model of Schaeffer and Lebedev (2013), assuming a ‘fertile’ composition of the upper mantle material (Tesauro et al., 2014). The parameters of this model are the same as those used in studies of other regions and on larger scales (e.g., Kaban et al., 2016), which provides the possibility for direct comparison of the results. It should be noted that the parameters of the reference model are not critical for the results since they mainly affect the average level of ~~the-both, the residual gravity field and residual topography, computed field, which is not considered in this study~~ while we interpret only lateral variations of these fields (Mooney and Kaban, 2010).

Table 1. Reference density of the crustal and upper mantle layers.

	Upper crust	Lower crust	Uppermost mantle	
Depth (km)	0–15	15–40	50	100
Density (kg/m ³)	2700	2940	3357	3384
	Upper mantle			
Depth (km)	150	200	250	300
Density (kg/m ³)	3419	3457	3510	3560

Because the effect of deep layers strongly depends on remote areas and might represent significant trends (even between the northern and southern hemispheres), the high-resolution model of Egypt including the surrounding areas has been embedded in the global model. For this purpose, we used CRUST1.0, which was improved for North America and Eurasia based on recent models for these continents (Mooney and Kaban, 2010; Stolk et al., 2013). The details of the computational technique are described in Kaban et al. (2016b). The residual anomalies obtained by removing the crustal effect from the observed gravity field, are shown in Fig. 6A. The resolution of this field is limited to $1^\circ \times 1^\circ$ (grid cell size), since the resolution of the crustal model don't provide more details even in the places with dense seismic observations (Fig. 4). As already mentioned, we also removed the effect of the deep mantle heterogeneity below 325 km based on a global dynamic model described in Kaban et al. (2015, 2016a). This depth is chosen based on our previous studies as the depth, which exceeds the maximal depth of the lithospheric roots. This is important since the inversion is performed globally (Kaban et al., 2015). These calculations are based on the global tomography model s40rts of Ritsema et al. (2011). For the upper mantle it well corresponds to the model of Schaeffer and Lebedev (2013), but its resolution is lower. While calculating the dynamic topography, we take into account the dynamic effects of the mantle convection (Kaban et al., 2015).

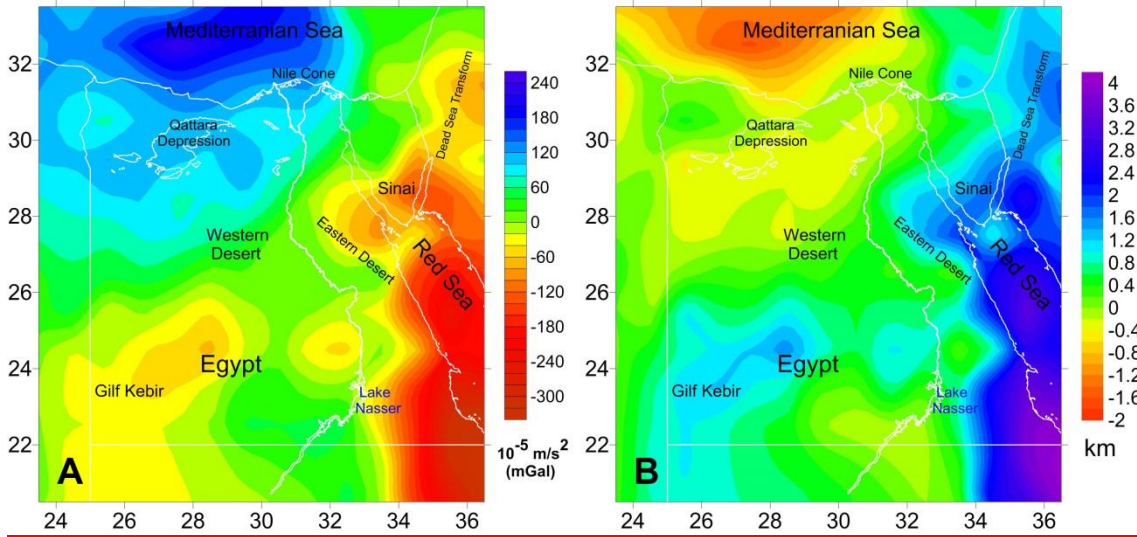


Figure 6. Residual mantle gravity anomalies (A) and residual topography (B) calculated by removing of the crustal and deep mantle fields from the observed gravity.

In addition to the residual gravity anomalies, the residual topography was also computed based on the same crustal model (Fig. 6B). The residual topography acts as load, which is not compensated for by crustal density variations including the Moho.

$$t_{res} = \frac{1}{\bar{\rho}} (\rho_{top}) t_{obs} + \frac{1}{\bar{\rho}} \int_0^M \Delta\rho(h) dh, \quad (1)$$

where ρ_{top} is the average density above sea level (including sediments and ice); t_{obs} is the topography (zero offshore); $\bar{\rho} = 2670 \text{ kg/m}^3$, the standard density; $\Delta\rho(h) = \rho - \rho_{ref}$ is the relative density below sea level including the negative relative density of water in the oceanic domain; h is the depth from sea level; and M is the depth to the Moho (below Moho $\Delta\rho(h) = 0$). The dynamic effect of the mantle below 325 km was removed from the residual topography in the same way as for the residual gravity.

Potential uncertainties of the residual field were analyzed in detail in Mooney and Kaban (2010) and Kaban et al. (2016a). They conclude that for relatively extended anomalies, which are based on several crustal determinations, the uncertainty of the residual gravity should not exceed $\sim 40 \times 10^{-5} \text{ m/s}^2$ (mGal), which is much less than the total anomaly (-300 to $250 \times 10^{-5} \text{ m/s}^2$). Szwillus and Ebbing (2016) provide even smaller values for uncorrelated uncertainties of the crustal model. The corresponding error of the residual topography is ~ 0.35 km. However, this conclusion only corresponds to the areas with

seismic determinations of the crustal structure (Fig. 4). In the following inversion of the residual fields together with seismic tomography we consider a possibility for further corrections of the initial density model.

The residual fields significantly differ from the previous study of the whole Middle East (Kaban et al., 2016c). This is mainly due to the new data on the crustal structure, which are included in the present model. One can observe a clear division of the area into several distinctive patterns. The northwestern part is characterized by positive residual gravity anomalies, while negative anomalies dominate in the Red Sea, with some extension to the continental part including Sinai (Fig. 6A). The residual topography generally mirrors the residual gravity; however, they have several principal differences amplitudes of the anomalies are not related straightforwardly, since the effect of any density anomaly on the surface gravity field and topography differently depend its depth and size (Fig. 6B). These fields will be used to adjust the density models of the crust and upper mantle in the following sections.

4.2 Density model of the upper mantle

The 3D density model of the mantle has been constructed through joint inversion of the mantle gravity anomalies (Fig. 6A) and residual topography (Fig. 6B) constrained by the initial density model based on seismic tomography (Fig. 5). The inverse problem implies the minimization of the functional:

$$\min\{\|A\rho - g_{res}\|^2 + k\|B\rho - t_{res}\|^2 + \alpha\|\rho - \rho_{ini}\|^2\}, \quad (2)$$

where A and B are the integral operators converting the densities ρ into gravity and dynamic topography (for the mantle part we consider a full dynamic effect of the density anomalies contributing to the residual topography, which depends on the mantle viscosity), g_{res} and t_{res} are the mantle gravity anomalies and residual topography, and $k = 2\pi G\rho_t$ is the scaling coefficient normalizing the topography with respect to gravity (G is the gravitational constant and ρ_t is the density of the topography). The regularization condition requires that the calculated density anomalies are close to the initial model ρ_{ini} , where α is the damping factor. The inversion is performed in the spherical harmonic domain. For the dynamic topography $t_{dynamic} = B\rho$, we use a vertical viscosity–depth profile constrained by mineral physics and geodynamic models (Kaban et al., 2015). The method has been extensively tested on synthetic models (Kaban et al., 2015a). It has been demonstrated that shapes of the calculated density anomalies are correctly reproduced even when they are not resolved in the initial model. However, the amplitude of the obtained in the inversion density variations might be reduced by dumping. We take into account this condition when interpreting the results. The technical details and numerical tests proving the resistance of the solution to plausible changes of the inversion parameters can be found in Kaban et al. (2015a, Supplementary Material).

The model setup is the same as that in Kaban et al. (2015, 2016c). The residual fields and initial density model were extended to the whole Earth, which is required for the decomposition into spherical harmonics. The same global model as

described above was used for these purposes. The initial tomography model of Schaeffer and Lebedev (2013) is global; therefore, it was converted to densities using the same approach as in the study area. Density variations were calculated for seven layers with the central depth at 15, 45, 100, 150, 200, 250, and 300 km, respectively. The density perturbations in the upper layer adjust the potential uncertainties of the crustal densities. The ~~anomalies~~ calculated density perturbations to the initial model at the depth 45 km in the continental part were recalculated in the corrections of the initial Moho model using the crust–mantle density contrast from the reference model (Table 1).

~~The obtained 3D density model based on joint inversion of the residual gravity and topography constrained by the tomography based initial model is shown in Fig. 7. As was mentioned above, the corrections for the initial~~ The corrected Moho map ~~were also estimated, which gives a new map~~ is shown in Fig. 7A. As expected, the maximal correction (-3.6 km) is calculated in the northern part of the study area, which is not covered by seismic data. In other areas, it does not exceed ± 2 km; this value corresponds to the uncertainty of the seismic determinations. ~~As mentioned above, the~~ The Moho correction was applied to the continental part only, where the Moho depth exceeds 30 km. It remains unmodified for the Red Sea and Mediterranean. Three slices of the obtained 3D density model based on joint inversion of the residual gravity and topography constrained by the tomography based initial model are shown in Fig. 8. The calculated density anomalies range from -35 to 50 kg/m³ (Figs. 8A-C) and the final model significantly differs from the initial density model (~~Figs Fig. 7B8D–DF~~). Compared to the large-scale model of the whole Middle East, the present results clearly show the fragmentation of the upper mantle in Egypt. The central part and the Qattara Depression are characterized by an increased density of the mantle, which extends to the Mediterranean maximum at a depth of 100 km (Fig. ~~7B8D~~). At greater depths, the central Egyptian maximum extends to the southeast (Figs ~~7C8E, DF~~). The negative anomaly is localized over the Red Sea and some surroundings at the boundary of the Western Desert and Nubian Shield and limited to a depth of ~150 km, disappearing at greater depths. The local positive anomaly corresponds to the Sinai Massif (Figs ~~7B8E, CF~~).

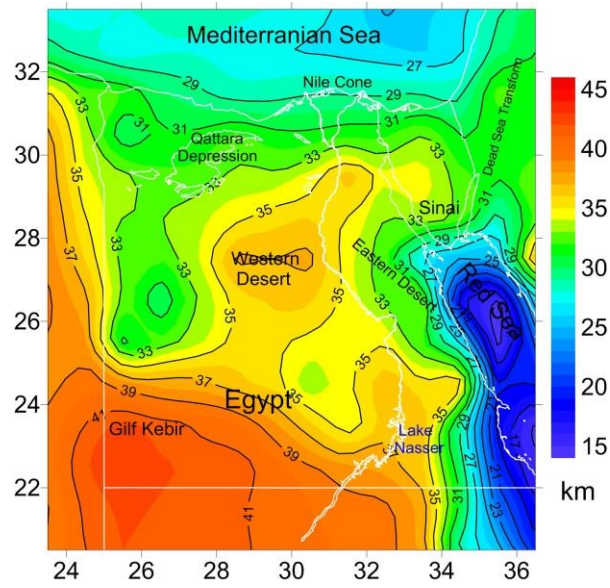


Fig. 7. The new Moho map corrected in the joint inversion of the residual gravity and residual topography.

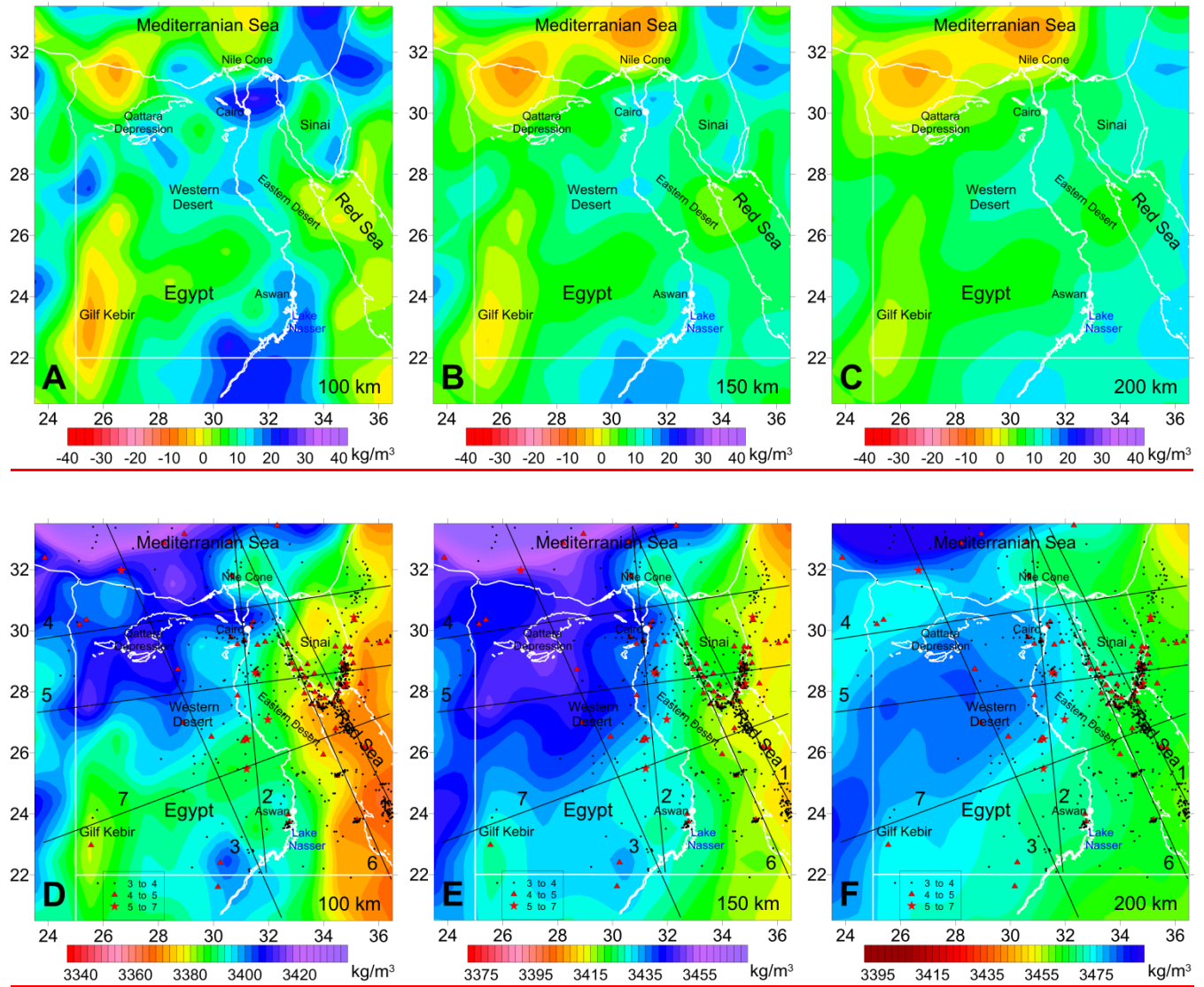


Figure 78. Results of the inversion. **(A)**: ~~Corrected Moho Map~~; **(B-C-D)**: ~~calculated density perturbations to the initial model (Fig. 5)~~ calculated density variations at the depths 100, 150 and 200 km. **(D-E-F)**: final density variations at the same depth. Black lines show location of the profiles in Fig. 8-9 are shown in the map D. Black dots, red triangles and stars show seismicity of Egypt (magnitudes > 3).

5 Discussion

5.1 Fragmentation of the lithosphere in Egypt based on its density structure

We further discuss seven ~~vertical 2D sections~~ ~~profiles~~ ~~along the profiles~~ ~~shown~~ ~~showing density variations relative to the reference model~~ ~~in~~ (Figs. 89, 10). Because the vertical resolution is limited to 35–50 km ~~according to the model setup~~, the anomaly in the crust might be smeared to the uppermost layer of the mantle (> 50 km), especially in offshore areas with thin crust.

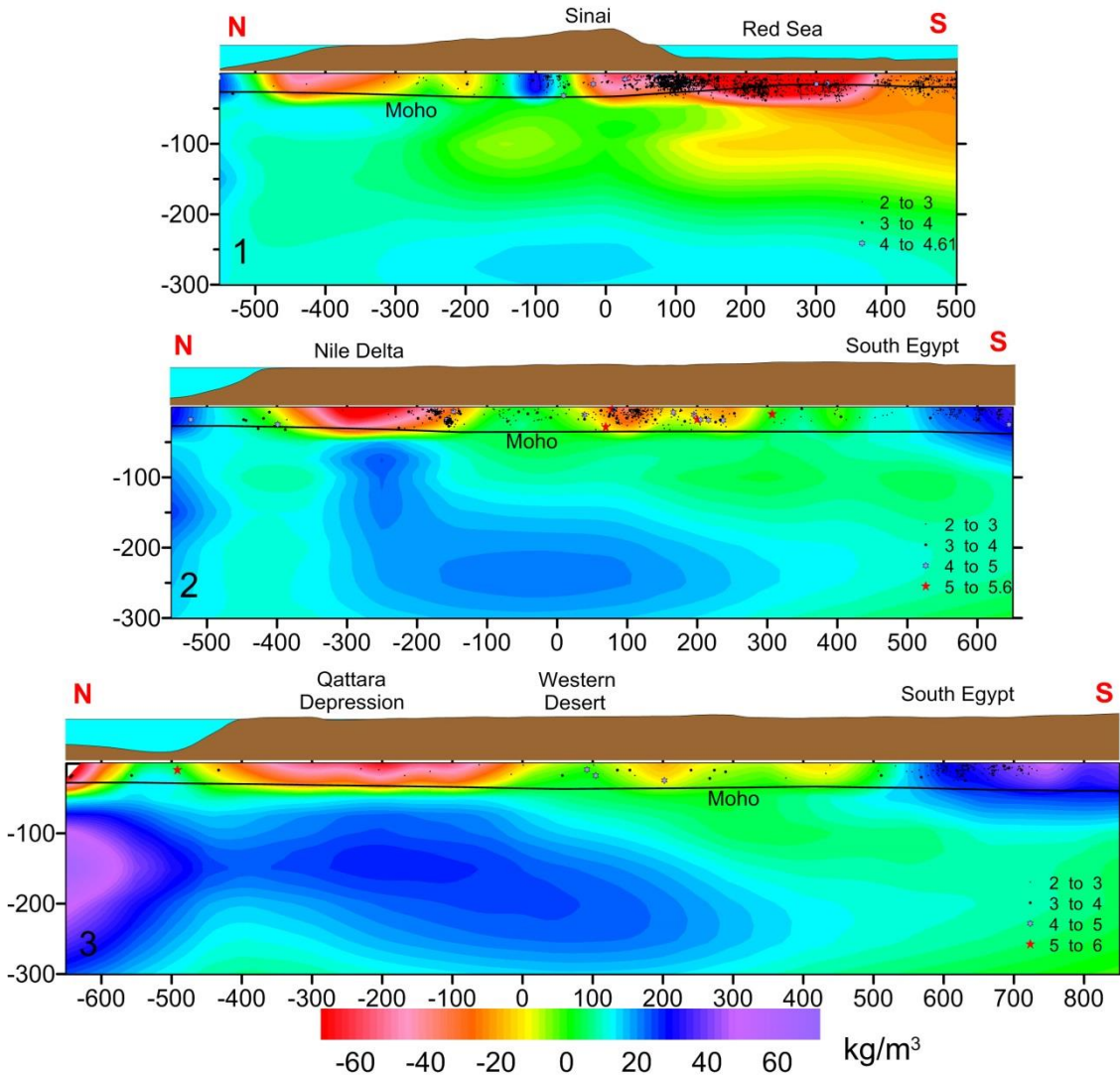


Figure 89. Density anomalies relative to the reference model (Table 1) along selected profiles. Sections-Profiles 1-3, Fig. 7D8D-F. Black dots indicate the hypocentres of the earthquakes projected on to the cross-sections profiles (ENSN earthquake Catalogues).

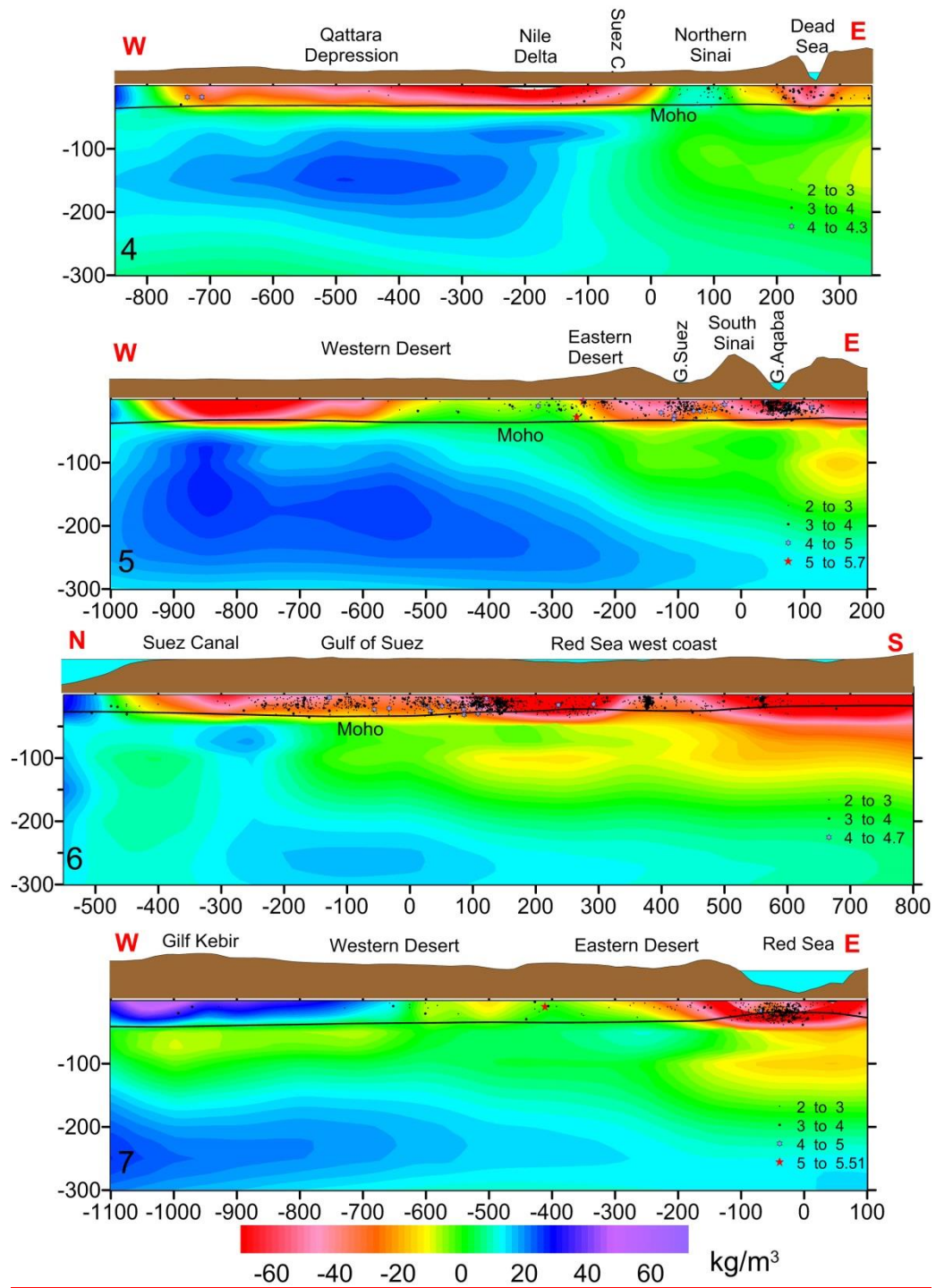


Figure 8-10(continue). Density anomalies along selected profiles(4-7), Fig. 7D8D-E. Notations are as in Fig. 9.

The negative density anomaly under the North Red Sea is limited to the uppermost mantle as shown in [section profile 1](#) (Fig. [89](#)), agrees with previous conclusions with respect to the passive origin of the extension in this area (e.g., Bosworth, 2015). This anomaly does not continue to Sinai, which is characterized by ~~neutral or zero or~~ slightly ~~positive~~ ~~increased densities~~ [density anomalies](#) in the upper mantle. The seismicity is mainly localized in the crust, which is characterized by an extremely low relative density likely related to the weak layer that is prone to strong deformations, resulting in seismic events. It is also clear that most of the earthquakes are of low magnitude and their hypocenters are concentrated in the crust and confined to the Red Sea Rift. This might be related to the shallow Moho Discontinuity, which is characterized by high temperature and low-density [mantle material underneath](#). Therefore, the stress is not accumulated for a long time. The continuous release of the stress thus generates permanent seismicity characterized by shallow depths and low magnitudes.

The distribution of anomalous density and seismicity from the Nile Delta to South Egypt is clearly indicated in [section profile 2](#) (Fig. [89](#)). It is well known that the Nile Delta is characterized by very low seismic activity compared to the surrounding area (Fig. 1). The constructed density model can provide some explanation for this phenomenon. It is clear from Fig. [8-9](#) ([section profile 2](#)) that this area corresponds to a dense and likely strong mantle lithosphere extending to the bottom of the crust. It has been demonstrated that seismicity occurs at the boundaries of rigid lithospheric blocks in similar situations (Tesauro et al., 2015). In the case of the Nile Delta, the weak crust easily accommodates relatively small deformations, which in contrast to the Red Sea are limited by the strong lithosphere beneath.

The Qattara Depression is also characterized by the high-density lithosphere overlain with relatively low-density crust (Fig. [89](#), [section profile 3](#)). The high-density zone in the mantle deepens to the North and is localized at depths of 200–250 km in Middle Egypt. In the east, the high-density lithosphere extends to the Suez Line (Fig. [810](#), [section profile 4](#)), which clearly marks the boundary between the strong lithosphere in Western Egypt and the weaker lithosphere in the east. This result agrees with estimations of the effective elastic thickness of the lithosphere based on the cross-spectral analysis of the gravity field (Chen et al, 2015). The seismicity behaviour at the edge of the high-density lithosphere block is similar to that at the southern border of the Nile Delta (Fig. [89](#), [section profile 2](#)). Further to the south, the transition between different lithosphere blocks is smoother; the high-density lithosphere gradually deepens from the Western Desert to Sinai (Fig. [810](#), [section profile 5](#)).

The crustal and mantle structure along the Suez Canal and Gulf of Suez is shown in [section profile 6](#) (Fig. [810](#)). One of the vital problems discussed for these structures is the cessation of the opening of the Gulf of Suez Rift. It is observed that the boundary between the Gulf and Isthmus of Suez corresponds to the boundary between the lithospheric blocks with different densities (Fig. [810](#), [section profile 6](#)). The high-density block in the south-eastern Mediterranean located to the north of the Suez Canal and Gulf of Suez might terminate the prolongation of the Gulf of Suez Rift further to the north. It also manifests

the significant decrease of seismicity in the Suez Isthmus and further to the north. Therefore, the stronger lithosphere in the north might prevent the continuation of the Gulf of Suez opening as was initially proposed by (Steckler & ten Brink, 1986).

The high-density block is observed in the area of Gilf El Kebir in southwestern Egypt, as indicated in section profile 7 of Fig. 810, with no associated seismicity revealing the stability of this region which is characterized by Paleozoic outcrop. This anomaly is already observed in the initial seismic tomography model; therefore it is likely related to relatively low temperatures. A low-density anomaly likely related to high thermal regime can be observed in the North Red Sea associated with high earthquake activity (Section Profile 7, Fig. 810). The lithosphere structure becomes asymmetric across the Northern Red Sea Rift, which corresponds to the asymmetric pattern of the seismicity relative to the central axis of the North Red Sea. The intensive seismicity is concentrated on the western side, where the lithosphere is weakened at a depth of 100 km (section profile 7, Fig. 810). Further to the north, the seismicity pattern is divided into two branches (Fig.2). The Red Sea Zone continues in the direction towards the Gulf of Suez (Fig. 1). Another branch extends along the Dead Sea Transform Fault, which is also characterized by high seismic activity. To conclude, the seismicity asymmetrically tends to the west of the North Red Sea Rift, possibly because the opening of the North Red Sea Rift is directed W–N–W to the Gulf of Suez, which is associated with the weakened lithosphere.

15 **5.2 Isostatic gravity anomalies and their relation to seismicity.**

The local isostatic anomalies image upper crust density heterogeneities, which are not included in the initial model, in particular not completely compensated in local isostasy sense but rather supported by the rigid lithosphere. They can be generated by various processes (e.g., mantle intrusions of mantle batholiths in the upper crust, faulting, and subduction) and could be associated with significant stresses in the lithosphere. Therefore, isostatic anomalies of the gravity field are often used to study active seismic areas (e.g., Assumpção and Sacek, 2013; Sobiesiak et al., 2007). However, the feasibility of this approach strongly depends on the isostatic model which was used to calculate the isostatic anomalies. The standard simple models (Airy and Pratt) that are based on the observed topography and don't adequately describe -often differ from- the real density structure of the crust and upper mantle, which can cause artificial anomalies (e.g., Kaban 2016b). Therefore, it is important to take into account as much as possible actual information about the crustal structure in the study area, which can be obtained from other geophysical and geological methods. In our approach, we intend to separate the gravity anomalies, which are chiefly related to the density inhomogeneities in the crust, which are not compensated in both ways: via density heterogeneity of the lithosphere or dynamically from the mantle. Therefore, the residual anomalies not adjusted in the inversion represent a large scale part of the isostatic anomalies, which might be responsible for the stress concentration and seismicity.

30 The isostatic anomalies, which are analyzed in this study, are compiled in the following way. First, we use the residual part of the mantle gravity anomalies (Fig. 6a), which is not fit in the inversion. This is a long-wavelength field (the resolution is

1x1 degree corresponding to degree/order 180), which is characterized by small amplitudes ($\pm 10 \times 10^{-5} \text{ m/s}^2$, mGal). This field has been complemented by the local part of the isostatic anomalies, which were computed in the previous study for a high-resolution grid (Kaban et al., 2016b). The total isostatic anomalies are shown in Fig. 911. Their resolution corresponds to the resolution of the initial gravity field model EIGEN-6c4 (max 10x10 km).

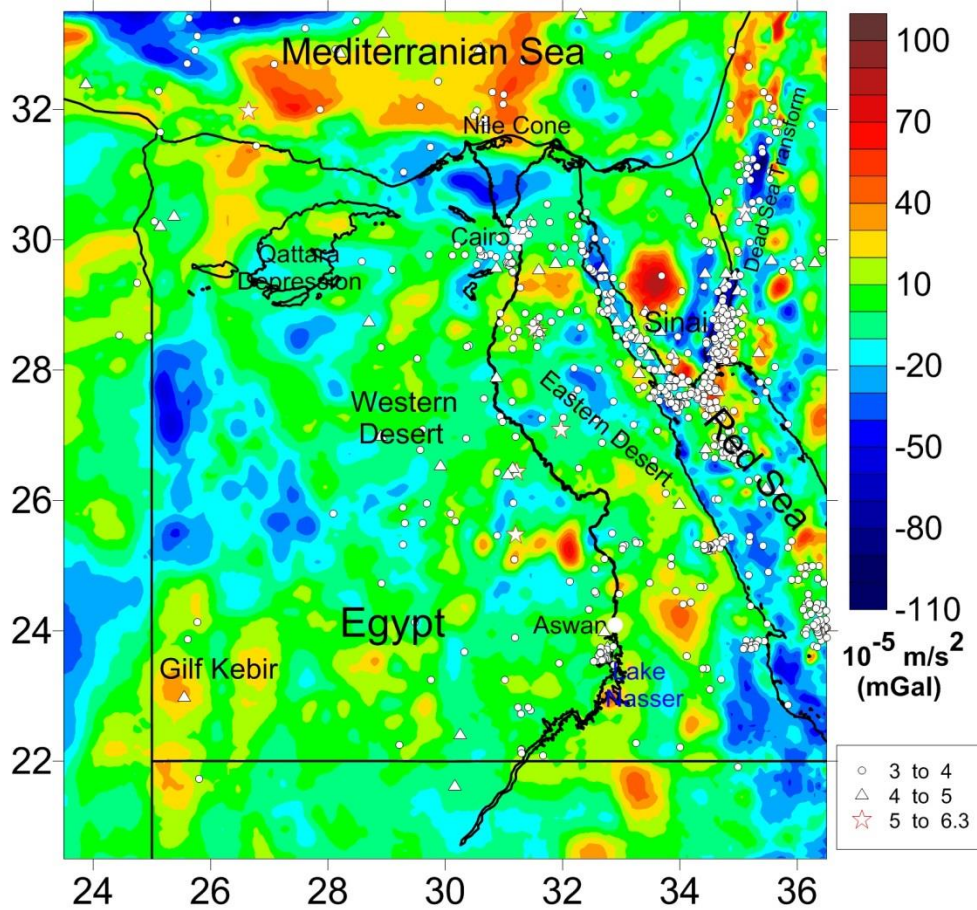


Figure 911. Isostatic anomalies of the gravity field and seismicity. Earthquakes are shown with for $M \leq 3$ are half-transparent to prevent masking of the isostatic anomalies.

The isostatic anomalies demonstrate very diverse patterns in Egypt and its surroundings. The strongest variations ($\pm 90 \times 10^{-5} \text{ m/s}^2$, mGal) are found in the south-eastern part along the Red Sea and Sinai Peninsula (Fig. 911). Sinai is bounded by linear anomalies parallel to the Gulf of Suez and Aqaba Gulf, which are clearly associated with high levels of seismicity.

The whole Sinai Peninsula is divided into several parts with different patterns of the isostatic anomalies. The central block with very high anomalies up to $100 \times 10^{-5} \text{ m/s}^2$ (mGal) demonstrates very low seismic activity. It is divided from the southern part by a narrow high-amplitude negative anomaly (Fig. 911). The relatively strong earthquakes (M.3) tend to occur in zones with high gradients of the isostatic anomalies (Figs. 11 and 12A). This tendency persists to the west over the Nile Valley and Eastern Desert. The seismicity in the Red Sea is also concentrated in the high-gradient zones. This certainly concerns only a part of the earthquakes; ~~there are many other factors controlling seismicity~~ earthquakes are also generated by the deformations related to plate motions, but the general tendency is clear.

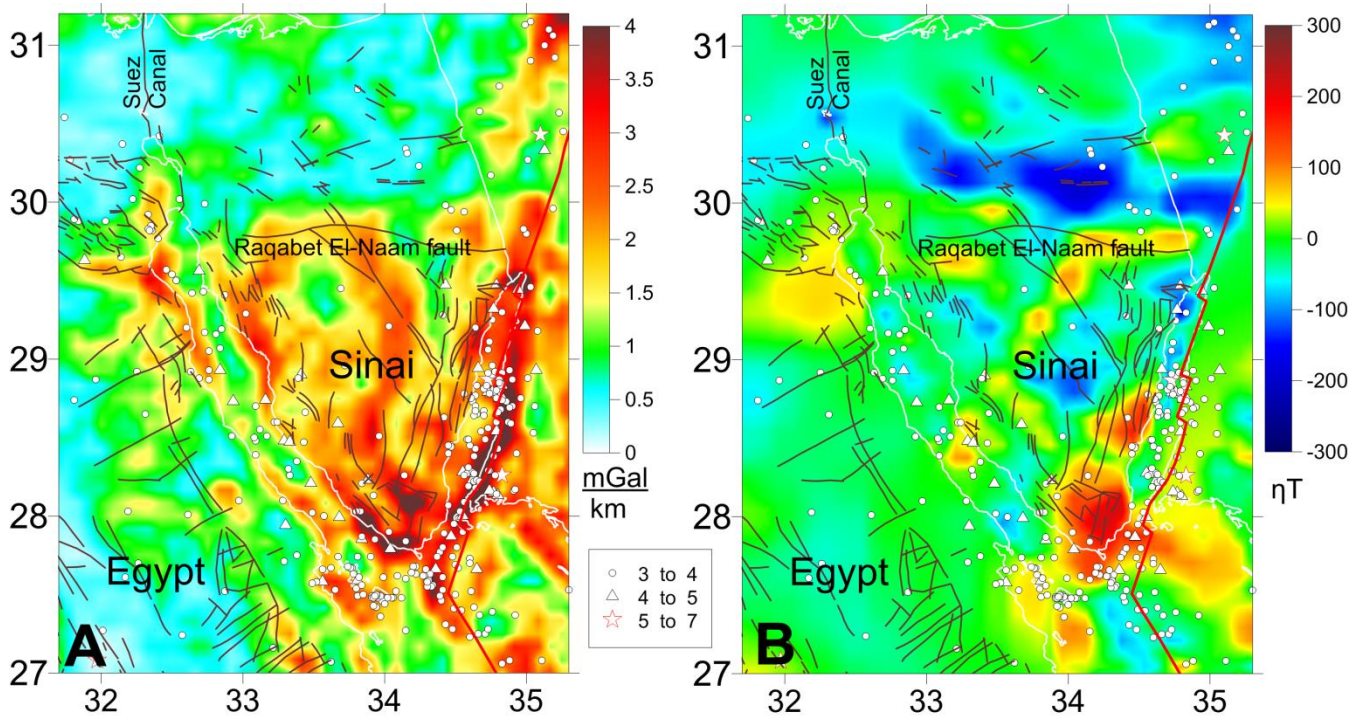


Fig. 12. (A) Maximal values of the horizontal gradients of the isostatic anomalies (filtered $\lambda > 25$ km to remove small-scale variations); (B) Magnetic anomalies (Maus et al., 2007).

The broad negative anomalies in the western part of the area and over the Qattara Depression likely indicate the increased thickness of the low-density upper crust with no seismic activity associated. In the same way, the broad negative anomaly over the Nile Delta indicates that the density of sediments is slightly overestimated in the initial model. The high amplitude isostatic anomalies in the Mediterranean might be related to the subduction of the African lithosphere under Eurasia.

5 We found some relationship between the isostatic anomalies (with their gradients) and magnetic anomalies (Fig. 12B). The E-W Raqabet El-Naam fault in the Central Sinai represents a fundamental boundary, which clearly marks changes of the isostatic gravity anomalies and magnetic field patterns and also changes of the seismicity (Fig. 12). The area to the south represents a high-gradient zone (both in magnetic and isostatic gravity anomalies), which is characterized by the increased seismic activity. The near circular positive magnetic anomaly in the south well corresponds to the positive isostatic anomaly pattern. This block is characterized by the uplifted basement and bounded by a swarm of earthquakes.

6 Conclusions

10 A joint analysis of the new satellite-terrestrial model of the gravity field, and the recent data on the crustal structure and tomography model was performed to create an integrative model of the crust and upper mantle and to investigate the relationship between the isostatic state of the lithosphere and seismicity. The following conclusions can be drawn.

1. This study reveals a distinct fragmentation of the lithosphere of Egypt into several blocks which are characterized by different properties.
2. The central area and the Qattara Depression are characterized by an increased density of the mantle, which extends to the Mediterranean maximum at a depth of 100 km. At the same time, the crystalline crust in this area demonstrates low average seismic velocities and density, which might indicate an increased thickness of the relatively low-density upper crust.
15
3. The central Egyptian maximum of the upper mantle density extends to the southeast in the mid–upper mantle and is localized at depths of ~170–270 km. The same trend is found in W–E direction; however, it is limited by the western part of the Eastern Desert.
4. In the northeastern part of Egypt, the high-density lithosphere is bounded by the Gulf of Suez, which marks the transition
20 between the typically strong and cold plate and the weakened lithosphere.
5. The Sinai Microplate is characterized, on average, by the normal density of the upper mantle; however, smaller-scale features cannot be resolved at these depths because they are already smoothed out in the gravity field. In contrast, the upper crust, which is imaged by the isostatic anomalies, demonstrates large density variations. The central block has a strong maximum, which should correspond to the strong and dense crust.
- 25 6. The density structure of the lithosphere is closely related to the seismicity distribution. The low seismicity in the Nile Delta and Suez Canal might be related to the increased strength of the lithosphere, which is associated with densification due to low temperatures. It prevents strong deformations; the weak crust accommodates insignificant strains. In the same way,

the increased strength of the lithosphere in the Suez Isthmus and further to the north prevents the Suez Gulf from opening further.

7. The negative mantle anomaly in the North Red Sea is limited to the uppermost mantle, which confirms the passive origin of this structure. The low-density and likely weak upper crust and uppermost layer of the mantle are characterized by high seismic activity.

8. The density structure of the lithosphere in the northern Red Sea is asymmetric; the western side is characterized by low densities at a depth of ~100 km, which likely corresponds to the hot weakened layer. Most earthquakes are of low magnitudes at shallow depths and are located to the west of the axial depression of the Red Sea Rift. Thus, earthquakes are confined to the crust and uppermost mantle, where the low strength provokes stress release.

9. The continuation of the Suez Rift further to the north might be blocked by the strong lithosphere in the northern direction.

10. We found a correlation between the variations of the isostatic anomalies and seismicity. High-amplitude and localized isostatic anomalies generally correspond to areas with high seismic activity. This tendency is especially visible in Sinai, which is bounded by strong linear isostatic anomalies with a corresponding increase of seismic activity. Less pronounced but still visible, this relationship extends to the west including the Nile Valley and Western Desert and to the North Red Sea.

15 **Data availability**

The gravity data are available from the International Centre for Global Earth Models (ICGEM) (<http://icgem.gfz-potsdam.de/home>). The tomography model of Schaeffer and Lebedev (2013) is available from the website of the author (<https://andrewjschaeffer.wordpress.com/tomography/sl2013sv/>). The data on the crustal structure are available by contacting the corresponding authors.

20 **Author contribution**

MKK and SEK conceived the study. MKK carried out the gravity data analysis and construction of the 3D density model. SEK and NAA carried out the analysis of seismicity and its relation to the lithosphere density distribution and isostatic anomalies. MKK, SEK and NAA contributed to interpretation of the results and conclusions and wrote the manuscript.

Competing financial interests

25 The authors declare no competing financial interests.

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