

Dear Editorial Board,

We have addressed all the comments of the reviewers in a detailed point-by-point fashion. In our answer to the reviewers, we detail the modifications we made to the manuscript and answered to each of their comments. These answers are available publicly in the answer to the reviewers, which we posted as part of the interactive discussion. We therefore do not add a copy of these answers to our response here.

The rest of this document is organised as follows. The version of the manuscript represents the initial version, where what is shown in red symbolises parts of the manuscript which we removed/replaced. The second version is the revised version where what is shown in green marks what we have added. The third version is the comparison report where insertions (green), deletions (red) and replacements (purple) are highlighted.

Please do not hesitate to ask if you need further information.

Best regards,

The Authors

Integration of geological uncertainty into geophysical inversion by means of local gradient regularization

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Abstract. We introduce a workflow integrating geological uncertainty information in order to constrain gravity inversions. We test and apply this approach to data from the Yerrida Basin (Western Australia), where we focus on prospective greenstone belts beneath sedimentary cover. Geological uncertainty information is extracted from the results of a probabilistic geological modelling process using geological field data and their uncertainty as input. It is utilized to locally adjust the weights of a minimum-structure gradient-based regularization function constraining geophysical inversion. Our results demonstrate that this technique allows geophysical inversion to update the model preferentially in geologically less certain areas. It also indicates that inverted models are consistent with both the probabilistic geological model and geophysical data of the area, reducing interpretation uncertainty. The interpretation of inverted models finally reveals that the recovered greenstone belts may be shallower and thinner than previously thought.

1 Introduction

The integrated interpretation of multiple data types and disciplines in geophysical exploration is a powerful approach to mitigating the limitations inherent to each of the datasets. For instance, gravity data, which has poor horizontal resolution, can be integrated with seismic inversion to mitigate the poor lateral resolution of seismic inversion (Lelièvre et al., 2012). Likewise, geological modelling and geophysical inversions are routinely performed in the same area to obtain an subsurface model consistent with geological and geophysical measurements (Guillen et al., 2008; Lelièvre and Farquharson, 2016; Pears et al., 2017; Williams, 2008). When sufficient prior information is available, petrophysical constraints can be derived for inversion (Lelièvre et al., 2012; Paasche and Tronicke, 2007), and integrated with geological modelling to derive local constraints (Giraud et al., 2017). However, in exploration scenarios, this might be impractical as the available petrophysical information may be insufficient to allow us to derive such constraints (Dentith and Mudge, 2014). In such cases, when more than one

geophysical dataset is available, practitioners may rely on joint inversion using structural constraints (e.g., Gallardo and Meju, 2003; Haber and Oldenburg, 1997; Zhdanov et al., 2012).

Alternatively, when one of the datasets has a spatial resolution that is superior to the others, structural information can be transferred into the gradient regularization constraint for the inversion of the lesser resolving method(s), thus mitigating some of the challenges faced by joint inversion in such cases into what (Brown et al., 2012) termed guided inversion. This strategy has been applied in recent years using the interpretation of predominantly propagative data (e.g., seismics, ground-penetrating radar) to constrain the inversion of diffusive data (e.g., diffusive electromagnetic methods), see (Yan et al., 2017) and references reported therein. However, this avenue remains relatively unexplored to date.

In this article, we broaden the applications of guided inversion and explore the integration of non-geophysical information in inversion, such as geological uncertainty, into what we call uncertainty-guided inversion where we focus on the complementarity of information content between the datasets. We introduce a new technique that integrates local uncertainty information derived from probabilistic geological modelling in the inversion of potential field data, following recommendations of (Jessell et al., 2014, 2010; Lindsay et al., 2013; Lindsay et al., 2014; Wellmann et al., 2014, 2017). In contrast to (Giraud et al., 2016, 2017) who derives local petrophysical constraints from petrophysical measurements and geological modelling results, constraints used in uncertainty-guided inversion are based solely on the local conditioning of a gradient regularization function, thereby offering the possibility to integrate probabilistic geological modelling into geophysical inversion in the absence of sufficient petrophysical information. This conditioning relies on the calculation of local weights derived from prior geological information. In this study, we utilize a probabilistic geological model (PGM) (Pakyuz-Charrier et al., 2018) consisting of the observation probability of the different lithologies of the area in every model cell. More specifically, we utilize the information entropy (Shannon, 1948; Wellmann and Regenauer-Lieb, 2012), which measures geological uncertainty in probabilistic models. We calculate it in each model cell of the PGM to derive spatially varying weights applied to the gradient regularization function used during inversion.

The integration methodology we develop is similar in philosophy to (Brown et al., 2012; Guo et al., 2017; Wiik et al., 2015), who extract continuous structural information from seismic data to adjust the strength of the regularization term locally in order to promote specific structural features during electromagnetic inversion. However, our work differs from these authors in four main respects. Firstly, the geophysical problem we tackle is different in nature as we constrain potential field data in hard rock scenario instead of electromagnetic data in soft rock studies. Secondly, we use a metric encapsulating geological uncertainty derived from geological measurements, whereas, in contrast, previous studies use other geophysical attributes. Thirdly, we allow inversion to update the model preferably in the most uncertain parts of the geological model, instead of encouraging a certain degree of structural similarity between two geophysical inverse models. Finally, while previous work involve mostly 2D models, every step of our modelling is performed purely in 3D.

In this paper, we introduce the methodology and field application as follows. In the methodology Section, we first introduce the inversion and integration scheme and algorithm, and provide essential background information about probabilistic geological modelling. We then provide the essential background about information entropy before detailing its usage in inversion. In the ensuing section, we present a field application case focused on the Yerrida Basin (Western Australia), starting with the introduction of the geological context and modelling procedure. We then analyse the influence of local regularization conditioning on inverted models and demonstrate how it allows clearer and more reliable interpretation of the buried greenstone belts than when it is not utilized.

2 Modelling procedure

2.1 Inversion methodology

The inversion procedure we propose integrates spatially varying prior information to weight the regularization function locally (e.g., in each cell). It is implemented in an expanded version of the least-square inversion platform Tomofast-x (Martin et al., 2013, 2018), which offers the possibility to condition the regularization function (Tikhonov and Arsenin, 1977) of (Li and Oldenburg, 1996) locally using geological uncertainty. This is achieved by incorporating prior information into a structure-based regularization function in a fashion similar to (Brown et al., 2012; Wiik et al., 2015; Yan et al., 2017) by locally adjusting the related weight.

Solving the inversion problem regularized in this fashion consists of finding a model \mathbf{m} that minimizes the objective function θ given below:

$$\theta(\mathbf{d}, \mathbf{m}) = \underbrace{\|\mathbf{W}_d(\mathbf{d} - \mathbf{g}(\mathbf{m}))\|_2^2}_{\text{Data term}} + \underbrace{\|\mathbf{W}_m(\mathbf{m} - \mathbf{m}_p)\|_2^2}_{\text{Model term}} + \underbrace{\alpha\|\mathbf{W}_H\nabla\mathbf{m}\|_2^2}_{\text{Structural regularization term}}, \quad (1)$$

where \mathbf{d} relates to the geophysical measurements to be inverted, \mathbf{g} is the forward modelling operator; \mathbf{m} relates to the model being searched for, and \mathbf{m}_p is the prior model; \mathbf{W}_d , \mathbf{W}_m and \mathbf{W}_H are diagonal weighting matrices corresponding to data noise, model weighting and gradient regularization, respectively. The model term is a ridge regression constraint term (Hoerl and Kennard, 1970).

The structural regularization term in Eq. (1) enforces structural constraints during inversion. It is weighted locally by matrix \mathbf{W}_H , which can be derived from prior information (see Subsect. 2.3 for details). The positive free parameter α controls the overall weight of the regularization term; ∇ is the spatial gradient operator. Note that $\|\nabla\mathbf{m}\|_2$, estimates the amount of structure in inverted physical property model \mathbf{m} . Note that parts of the model where $\mathbf{W}_H = 0$ are excluded from the calculation of the structural regularization and can change freely to accommodate geophysical data.

2.2 Probabilistic geological modelling

Probabilistic geological modelling is performed using the Monte-Carlo Uncertainty Estimator (MCUE) method of (Pakyuz-Charrier et al., 2018), which is an uncertainty propagation method for 3D implicit geological modelling using geological rules and geological orientation measurements (foliation and interface) as inputs. The sampling algorithm perturbs orientation data by sampling probability distributions describing the uncertainty of orientation data to produce a series of unique altered models. Realizations that do not respect a series of geological rules are considered implausible and are rejected. Coupled to the 3D geological modelling engine of Geomodeller© (Calcagno et al., 2008), it produces a set of plausible geological models representing the geological model space (Lindsay et al., 2013b). The observation probabilities constituting the probabilistic geological model (PGM) are obtained, in each model cell, by calculating the relative observation frequencies of the different lithologies from the set of geological models. For the i^{th} model cell of a PGM containing L lithologies, vector $\boldsymbol{\psi}^i = [\psi_{k=1}^i, \dots, \psi_{k=L}^i]$ contains the observation probabilities of each lithology. As we show in the next subsection, the resulting PGM can be used to estimate uncertainty levels and as a source of prior information.

2.3 Utilisation of information entropy for local conditioning

Information entropy has recently been introduced in geological modelling by (Wellmann and Regenauer-Lieb, 2012) and is gaining popularity as a measure of uncertainty in probabilistic geological modelling (de la Varga et al., 2018; de la Varga and Wellmann, 2016; Lindsay et al., 2014; Lindsay et al., 2013; Pakyuz-Charrier et al., 2018; Schweizer et al., 2017; Thiele et al., 2016; Wellmann et al., 2017; Yamamoto et al., 2014). Quoting (Schweizer et al., 2017), information entropy “quantifies the amount of missing information and hence, the uncertainty at a discrete location”. For the i^{th} model-cell, it is given as (Shannon, 1948):

$$H^i = H(\boldsymbol{\psi}^i) = - \sum_{k=1}^L \psi_k^i \log(\psi_k^i). \quad (2)$$

Instead of using H directly, we calculate W_H utilising its normalized complementary, which reflects the degree of certainty across the model. Let us express W_H as follows, for the i^{th} model cell:

$$W_H^i = \frac{\max H - H^i}{\max H - \min H} \quad (3)$$

The consequence of Eq. (2) and 3 is that W_H is minimum at interfaces and in areas poorly constrained by geological information, and equal to unity in areas where the geology is well resolved. Consequently, the conditioning process attaches small weights to the structural term of Eq. (1) in uncertain cells, while consistently high values will be applied to the most geologically certain cells. As a result, it enables the inversion algorithm to favour nearly constant changes in the inverted model in contiguous certain groups of cells (e.g., where $W_H \rightarrow 1$) while relaxing the regularisation constraints in the most uncertain parts (e.g., where $W_H \rightarrow 0$).

For proof-of-concept validation, we simulated an idealized case study to assess the capability of inversion using W_H as per Eq. (3) to improve inversion results compared to the non-conditioned case (e.g., with W_H equal to the identity matrix). We tested the proposed methodology using synthetic geophysical data calculated from the structural geological model of the Mansfield area of (Pakyuz-Charrier et al., 2018), which we populated in the same fashion as (Giraud et al., 2017). The analysis of inverted models demonstrates the potential of the proposed inverse modelling scheme to ameliorate inversion results and to reduce interpretation uncertainty (see details in Appendix A). Importantly, in this synthetic case, local conditioning allows geophysical inversion to significantly improve the imaging of geologically uncertain areas. From the success of that theoretical proof-of-concept study, we are confident that our integration method can be tested here using real world data for field validation.

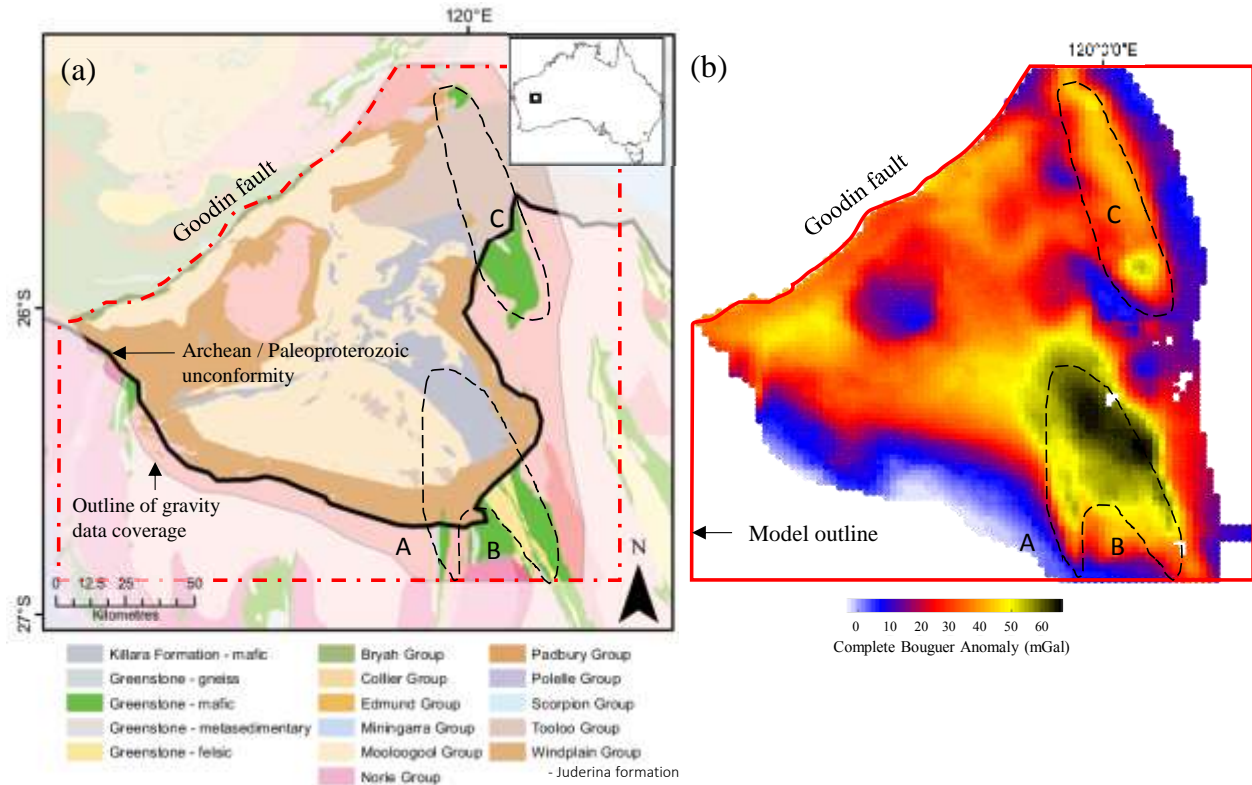
3 Field validation: Yerrida Basin case study

3.1 Geological context and geophysical survey setup

The Yerrida Basin is located in the southern part of the Capricorn Orogen, at the northern margin of the Yilgarn Craton in Western Australia (Fig. 1a), and extends approximately 150km N-S and 180 km E-W (Fig. 1b). The studied area is delimited in the northwest by the Goodin Fault, which represents a faulted contact between the Yerrida Basin and the Bryah-Padbury Basin. The structures of interest in this work are: Archean greenstone belts extending north-northwest that are unconformably overlain by Paleoproterozoic sedimentary rocks that form the Yerrida Basin. Features A and B (Fig. 1a and Fig. 1b) indicate the interpreted position of buried Wiluna Greenstone Belt. Where the Wiluna Greenstone Belt is exposed, it is host to base and precious metal mineralisation (Williams, 2009). With a relatively high positive density contrast (expected to be between 190 and 270 kg.m⁻³) to the Yilgarn Craton granite-gneiss host, mafic greenstone belts A, B, and C are suitable targets for gravity inversion. Interpretations from multiple studies in the region, e.g. (Johnson et al., 2013; Pirajno et al., 1998; Pirajno and Adamides, 2000; Pirajno and Occhipinti, 2000) were compiled while additional geological measurements acquired in 2015, 2016 and 2017 complemented legacy data (Occhipinti et al., 2017; Olierook et al., 2018). This allowed the revision of existing models and improved our understanding of the area. This, in turn, also highlights the challenges presented by the characterization of greenstone belts A, B and C, and that further geophysical analysis through constrained inversion is a useful pathway for reducing exploration risk.

Inverted geophysical data consists of ground surveys obtained from Geoscience Australia (<http://www.ga.gov.au/data-pubs>). Post-processing includes spherical-cap and terrain corrections and the removal of the regional trend to obtain the complete Bouguer anomaly, which we forward model following (Boulinger and Chouteau, 2001). As most data points were acquired 1 to 4 km apart, the dataset was resampled to match the geological model discretization, making up a total of 4882 measurement points. The model is discretized into $100 \times 100 \times 42$ cells of dimensions 2.335 km \times 1.875 km \times 1.0475 km, down to a depth

of 44 km, making up a total of 420000 cells. We utilize the integrated sensitivities technique of (Li and Oldenburg, 2000; Portniaguine and Zhdanov, 2002) to precondition the data term in Eq. (1) in order to balance the decreasing sensitivity of gravity field data with depth.



5

Figure 1. Geological context and geophysical data. (a) Geological map of the area and (b) complete Bouguer anomaly. The dashed lines delineate the possible sub-basin extent of the mafic greenstone belts A, B and C.

3.2 Geological modelling

10 Geological data consists of in-situ structural measurements (interfaces and foliations) and interpretation of aeromagnetic, airborne electromagnetic, Landsat 8 and ASTER data. Legacy data from the Geological Survey of Western Australia (Pirajno and Adamides, 2000) and CSIRO (Ley-Cooper et al., 2017) were used, to which about 600 data points and petrophysical measurements from recent geological field campaigns were added. Although the available petrophysical measurements are not used to derive petrophysical constraints because of the insufficient sampling of several of the modelled lithologies, they are a

15 useful source of information to populate geological models and for interpretation.

These datasets were used jointly to build a reference geological model for MCUE simulations, after which lithologies with similar density contrasts were merged and subsequently treated as a single rock type. Uncertainty related to structural

measurements was subsequently used as inputs to the MCUE perturbations (Pakyuz-Charrier et al., 2018) of the reference model to generate a collection of 500 accepted models. Information extracted from the PGM displayed in Fig. 2. Figure 2a shows the lithologies with the highest probability for each cell of the PGM. The associated W_H values used in inversion are shown in Fig. 2b. The starting model for inversion, which we also use as prior model m_p , is equal to the mean model of the 500 plausible models generated by MCUE, is shown in Fig. 2c.

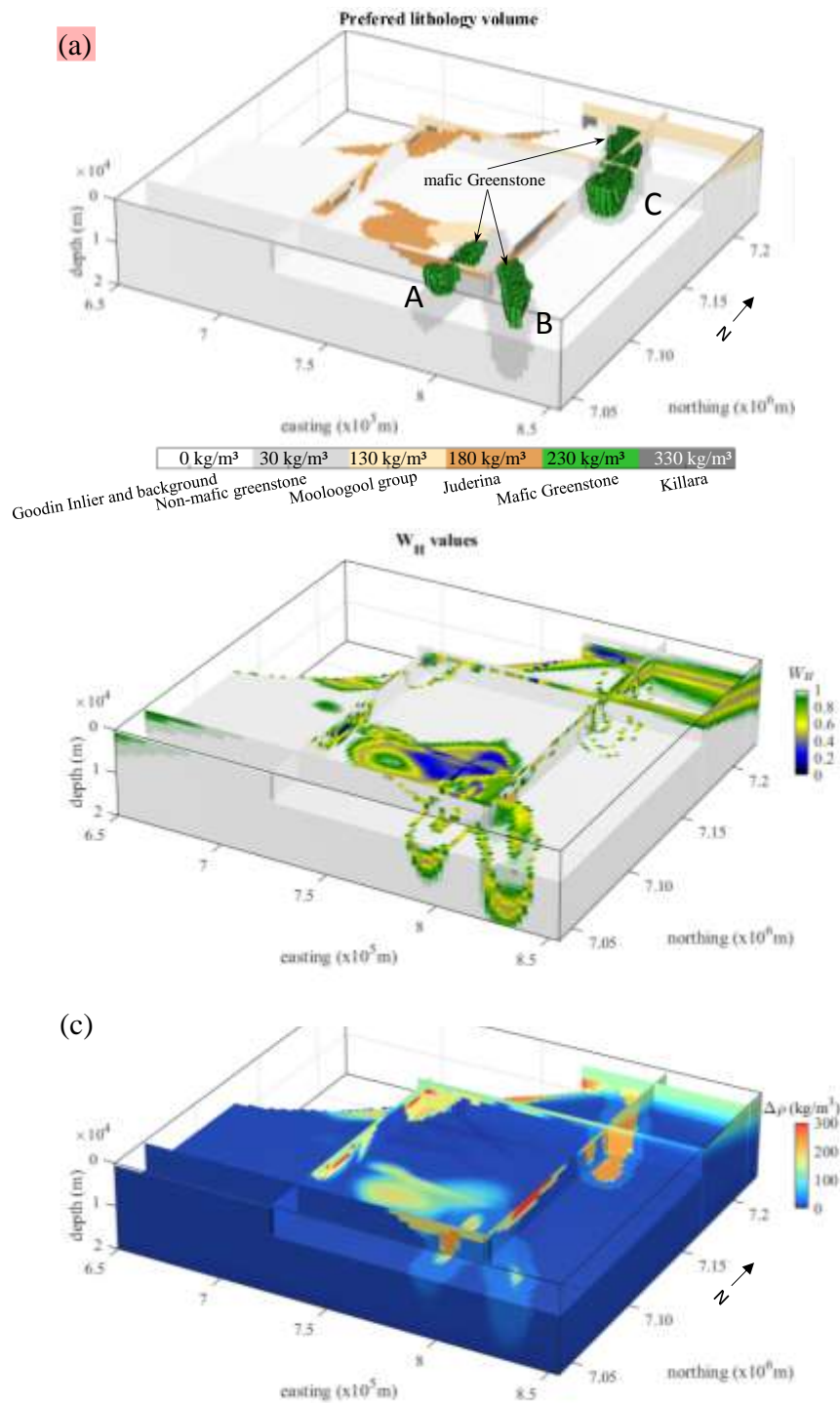


Figure 2. Geological modelling results. (a) Most probable lithology in each model cell (same colour code as in Fig. 1) (b) values used for local regularization conditioning, (c) and starting model derived from PGM and prior petrophysical information). In (a), “background” refers to all the lithologies that have a density contrast equal to 0 kg.m^{-3} .

3.3 Inversion results and analysis

Our analysis aims at determining the influence of the local conditioning of structural constraints on inversion through comparison with the non-conditioned case, all other things remaining constant.

3.3.1 Comparative analysis strategy

5 Prior to examination of the inverted models, we analyse geophysical data misfit after inversion for a fixed number of major iterations (100) of the least-square geophysical inverse solver superior to that needed for convergence of the inversion algorithm (~10 in this case). This enables us to ensure that the inversion results we compare produce, in our case, similar gravity anomalies. Our study of inverted models focuses on results obtained through usage of non-conditioned (Fig. 3a) and conditioned regularization function (Fig. 3b) using W_H (Fig. 2b). In addition to departures from the starting model, variations between the two cases are studied by visual comparison of Fig. 3a and Fig. 3b, through qualitative (Fig. 3c) and quantitative comparative analysis (Fig. 3d-e). Our interpretation of inversion results is complemented by metrics quantifying the differences between models. We give particular attention to model cells where the probability of mafic greenstone is superior to zero. For these cells, we classify lithologies by identifying cells with a density contrast corresponding to mafic greenstone.

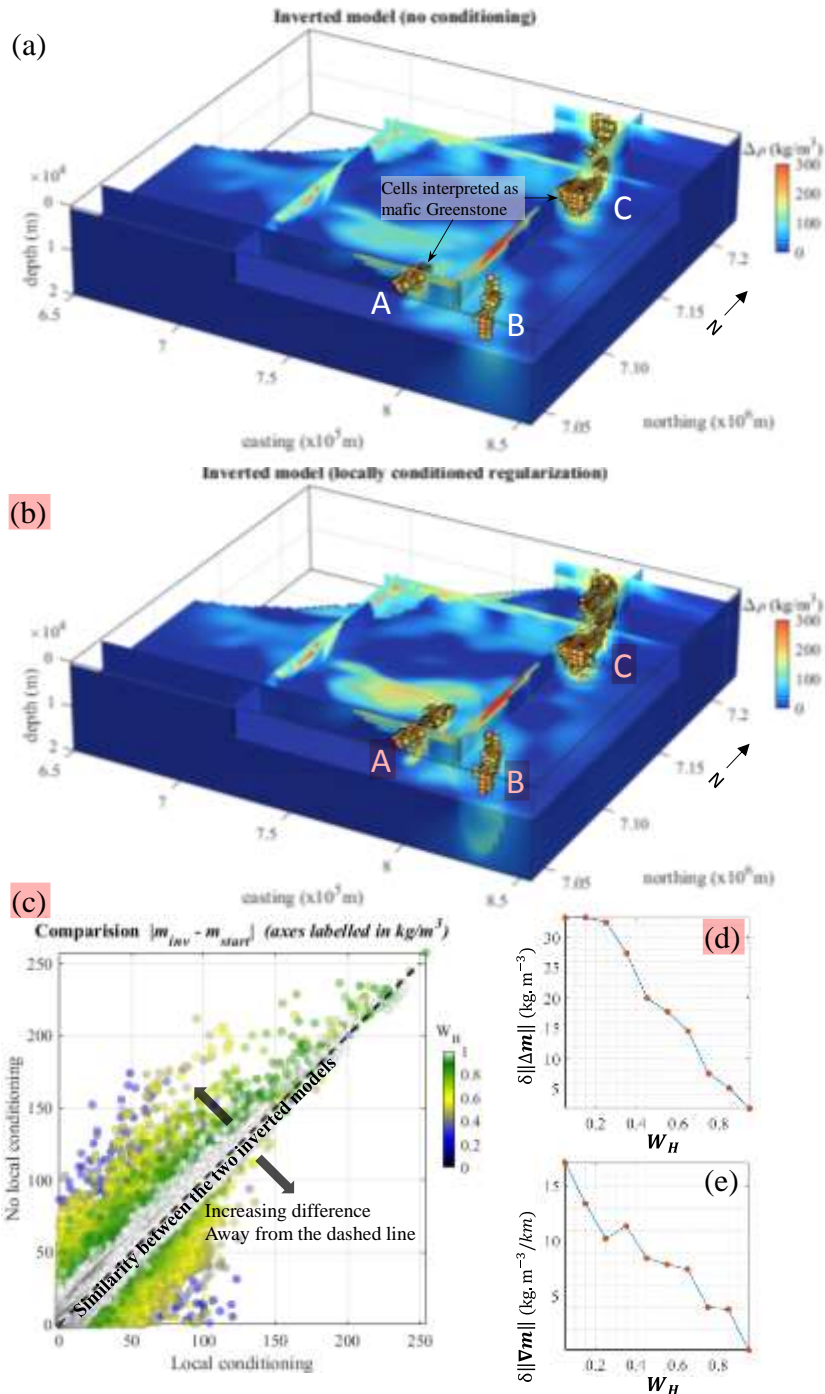
3.3.2 Results

15 Data root-mean-square (RMS) error decreases during inversion from 12.46 mGal to reach 1.59 mGal and 1.53 mGal for the non-conditioned and conditioned cases, respectively. The corresponding data misfit maps show a linear correlation coefficient of 0.999 (see details in Appendix A3 and Fig. A3). This similarity illustrates that, as in many other studies, most changes related to holistic data integration in geophysical inversion occur primarily in model space, hence reducing the effect of non-uniqueness (Abubakar et al., 2012; Brown et al., 2012; Demirel and Candansayar, 2017; Gallardo et al., 2012; Gallardo and Meju, 2004, 2007, 2011; Gao et al., 2012; Giraud et al., 2017; Guo et al., 2017; Heincke et al., 2017; Jardani et al., 2013; Juhonjuntti and Kamm, 2015; Molodtsov et al., 2013; Moorkamp et al., 2013; Rittgers et al., 2016; Sun and Li, 2016, 2017).

Qualitatively, comparison of Fig. 3a and Fig. 3b reveals that departures from the starting model (Fig. 2c) are more significant in the most geologically uncertain areas. Quantitatively, the RMS model update for cells characterized by $0 \leq W_H < 0.05$ (most uncertain group) is equal to 40.1 kg/m^3 and 51.5 kg/m^3 , for the non-conditioned and conditioned cases, respectively, whereas the same quantities are equal to 17.7 kg/m^3 and 16.9 kg/m^3 for the cells identified by $0.95 < W_H \leq 1$ (most certain group). This suggests that local regularization conditioning allows inversion to update the model preferentially in geologically uncertain areas. In turn, differences with the starting model in more geologically certain areas are reduced compared to the non-conditioned case. This effect of conditioning is corroborated by Fig. 3c where the longest distances to the dashed line, which represents equal model update for the two studied cases, occur in geologically uncertain areas. This also translates in higher difference between model updates of the two compare cases in Fig. 3d for lower values of W_H . In addition,

we observe that local conditioning produces stronger density contrasts in Fig. 3b in some of the areas where the conditioning values are higher in Fig. 2b. Furthermore, structures in the inverted model are easier to identify when local conditioning is used. It is confirmed by global roughness measures $\|\nabla\mathbf{m}\|_2$ equal to $3.4 (kg/m^3)/m$ and $4 (kg/m^3)/m$ for the non-conditioned and conditioned cases, respectively. More specifically, as shown by Fig. 3e, this difference arise in parts of the model associated with lower W_H , which characterize uncertain areas, including interfaces between lithologies.

The recovered greenstone belts are shown in Fig. 3a and Fig. 3b. In Fig. 3b, the extension of recovered mafic greenstone belts is significantly different than when geological uncertainty is not accounted for (Fig. 3a). In particular, belt A is significantly larger in Fig. 3b than in Fig. 3a ($2.4 \times 10^2 \text{ km}^3$ vs $4.6 \times 10^2 \text{ km}^3$). Similarly, the extent of belt C is increased overall (volume of $5.3 \times 10^2 \text{ km}^3$ vs $14 \times 10^2 \text{ km}^3$), while its different portions reconnect; the northern half is also significantly shallower and broader than in Fig. 2a and Fig. 3a. It appears that belt A remains thinner and shallower (Fig. 3b) than suggested by the preferred lithology volume (Fig. 2a). While similar geometries for belt B are recovered in Fig. 3a and Fig. 3b, they both differ from Fig. 2a as only the eastern part is preserved. Note that it is larger in Fig. 3b, with a volume 40% higher than in Fig. 3a. As discussed in the next subsection, these differences have a signification impact on the interpretation of inversions results and are important to understand the influence of local conditioning on inversion.



5 **Figure 3.** Comparison of inversion results. (a) inverted models with non-conditioned regularization weights, and (b) using local conditioning. (c) cross-plot between the corresponding absolute value of the update of the **starting** model, (d) difference in model updates $\delta\|\Delta m\| = \|m_{cond} - m_{nocond}\|_2$ as a function of values of W_H and (e) difference in model roughness $\delta\|\nabla m\| = \|\nabla m_{cond}\|_2 - \|\nabla m_{nocond}\|_2$ as a function of values of W_H . The model cells labelled A, B and C are interpreted as mafic greenstone belts. All voxels are coloured as a function of density contrast.

3.4 Interpretation

Note that, in contrast to the differences between inversion results highlighted above for belts A and C, differences between the inverted models in the north-eastern part of the model and the different interpretations of belt B (Fig. 3a and Fig. 3b) are small.

This shows that locally conditioned regularization does not enforce changes in the inverted model everywhere geological uncertainty is high as uncertainty is only a reflection of potential errors. Rather, this indicates that in such cases, the guiding effect of such regularization will be exerted provided that it does not prevent the data term in $\theta(\mathbf{d}, \mathbf{m})$ as per Eq. (1) from decreasing. This also confirms that geophysical data is the main driver of the model updates in geologically uncertain areas. Instead of smooth departures from the starting model to match geophysical data regardless of geological considerations, local regularization constraints allow inversion to account for the probabilistic geological modelling of the area and for geological uncertainty. It can therefore provide results that conform better to known geology.

In consequence, by confronting a probabilistic geological model encapsulating all MCUE realizations with geophysical measurements in an inversion scheme favouring model updates in the most geologically uncertain areas, inversion complements probabilistic geological modelling in that it guides and refines the interpretation of the geoscientific data in the area.

Geophysical inversion using geological uncertainty information (Fig. 2b) confirms the presence of high density anomalies that we interpret to be the mafic components of the greenstone as suggested by MCUE in several portions of the model. It also adjusts the outline and geometry of belts A, B and C to obtain a model honouring geological uncertainty information. In particular, mafic greenstone A and B may be smaller than the extent suggested by the PGM, and mafic greenstone C shallower than anticipated. Inversion results interpretation also reveal that greenstone B might be extended further to the east than indicated by the preferred lithology volume (Fig. 2a) and that greenstone C may be thinner in its central part.

4 Conclusions

We have introduced a new integration scheme for the inversion of gravity data that utilizes a measure of geological uncertainty to calculate locally-conditioned gradient regularization constraints. Contrarily to previous work, this approach enables the integration of probabilistic geological modeling in geophysical inversion in the absence of petrophysical information sufficient to the calculation of petrophysical constraints. It uses geophysical measurements to optimize the inverse problem by updating the physical property model preferably in geologically uncertain parts of the studied area during what we called *uncertainty-guided inversion*. This therefore partly mitigates inversion's non-uniqueness through the addition of constraints encouraging inversion to produce models that account for geological uncertainty across the entire inverted volume. We have demonstrated that it can be used collaboratively with geological modelling efficiently through field application in the Yerrida Basin. Inversion results show that our integration methodology has the capability to refine the recovered physical property model and interpretations in portions of the model where geological uncertainty is high. Another advantage of the proposed technique

pertains to its time and cost-effectiveness as our workflow utilizes the PGM resulting from geological modelling and requires the same parameterization as non-conditioned inversion.

In the Yerrida Basin study area, application of the proposed methodology provided the effective delineation of the greenstone belts by quantitatively integrating geological measurements and geophysical data. Our findings suggest that some of the greenstone belts covered by the basin might be shallower than previously anticipated and occupy smaller volumes. This is particularly pronounced in the North-East (belt C) where the resulting model is in agreement with the shallowest cases allowed by the PGM. Likewise, in the South (belt A), only the shallowest part of the mafic greenstone body can be resolved, while the south-eastern (belt B) greenstone belt appears to be limited in extension to the eastern part of the volume where it is the preferred lithology in the PGM. In such cases, this can also indicate that these greenstone bodies might be too thin to be imaged by gravity data. These results have implications for the geological knowledge of the southern Capricorn Orogen as they indicate reduced (compared to the preferred lithology volume) mafic greenstone volumes under the Yerrida Basin on one hand, and decreased cover thickness on the other hand, thereby opening the door to updates in the geological interpretation of the history of the Yerrida Basin and potential new undercover exploration prospects.

Future research include the utilization of local petrophysical constraints of (Giraud et al., 2017) in the uncertainty-guided inversion scheme we presented, as well as its application to weight the cross-gradient term of (Gallardo and Meju, 2003) in joint inversion schemes. With this last respect, uncertainty-guided inversion can be assisted in the most uncertain parts of the model by guided inversion (in the sense of Brown et al., 2012) or through cross-gradient joint inversion.

Code and data availability. Reference property models, inversion results and recovered models relating to the Yerrida Basin shown in this article are made available online: Jeremie Giraud, Mark Lindsay, and Vitaliy Ogarko, 2018, Yerrida Basin Geophysical Modeling - Input data and inverted models. (Version version 1.0) [Data set]. Zenodo. <http://doi.org/10.5281/zenodo.1238216>. Reference property models, inversion results and recovered models relating to the synthetic case from the Mansfield area shown in this article are made available online: Jeremie Giraud, Vitaliy Ogarko, and Evren Pakyuz-Charrier, 2018, Synthetic dataset for the testing of local conditioning of regularization function using geological uncertainty. (Version version 1.0) [Data set]. Zenodo. <http://doi.org/10.5281/zenodo.1238529>

Appendix A: proof-of-concept using synthetic case study

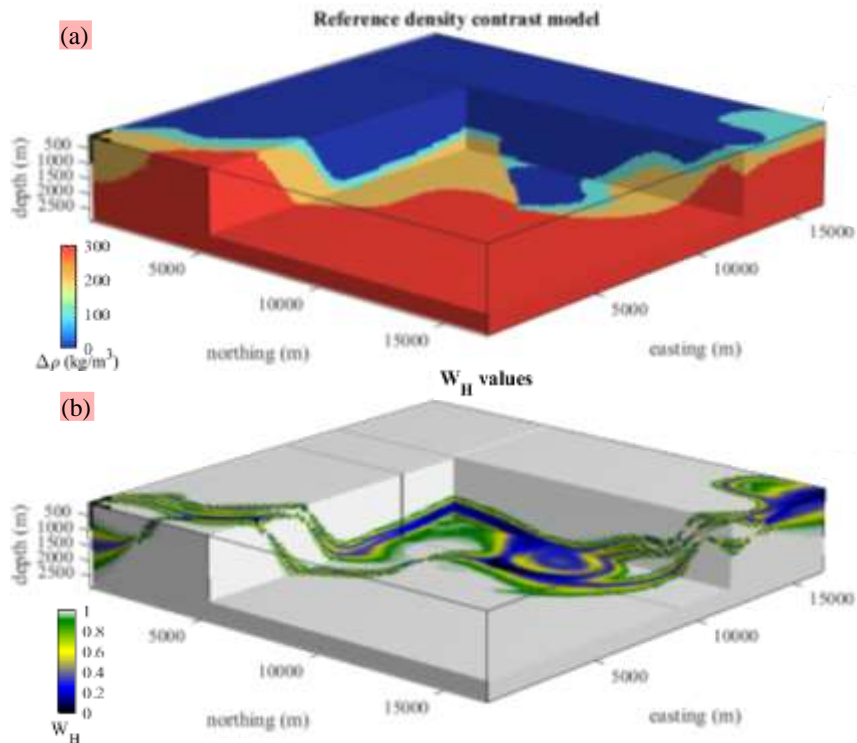
This Appendix introduces the proof-of-concept of the proposed method through an idealized case study illustrating the potential of the proposed inverse modelling scheme to ameliorate inversion results and to reduce interpretation uncertainty. We use the same 3D density contrast model as (Giraud et al., 2017), which is obtained using the structural framework and PGM of (Pakyuz-Charrier et al., 2018). The short presentation of the model below and the analysis of results provides essential information and support about the proof-of-concept of the methodology used in the paper.

A1 Synthetic survey setup

The 3D unperturbed geological model was generated from contact (interface points) and surface orientation (foliations) field measurements collected in the Mansfield area (Victoria, Australia). It presents a Carboniferous mudstone-sandstone basin oriented N170, abutting a faulted contact with a folded ultramafic basement to the South-West. Model complexity was artificially increased through the addition of a North-South fault and of a mafic intrusion.

The reference density contrast model (Fig. A4a) was obtained assigning density contrasts consistently with the structural setting of the unperturbed model, assuming a flat topography. Density contrasts of 0 and 100 kg.m⁻³ were assigned to the upper and lower basin lithotypes, respectively. Mafic rocks were assigned a density contrast of 200 kg.m⁻³ while the density contrast of the ultramafic basement was set to 300 kg.m⁻³.

MCUE perturbations of the reference model were performed using standard measurement uncertainty values recommended by metrological studies as reported by (Allmendinger et al., 2017; Novakova and Pavlis, 2017) generating a series of 300 models subsequently combined into a PGM. The resulting volume representing the W_H values calculated from this PGM in each cell of the model as per Eq. (3) is shown in Fig. A4b.



15 **Figure A4.** Reference model and W_H values used for local regularization conditioning. (a) Unperturbed reference model with density contrast value, (b) uncertainty values used for local regularization conditioning.

A2 Comparison of inversion results

To assess the impact of local conditioning of the regularization function, we compare inversions using non-conditioned (Fig. A5a) and locally conditioned (Fig. A5b) regularization function, respectively. Please note that, simulating the absence of prior petrophysical information, a homogenous starting model set to 0 kg.m^{-3} was used in both cases.

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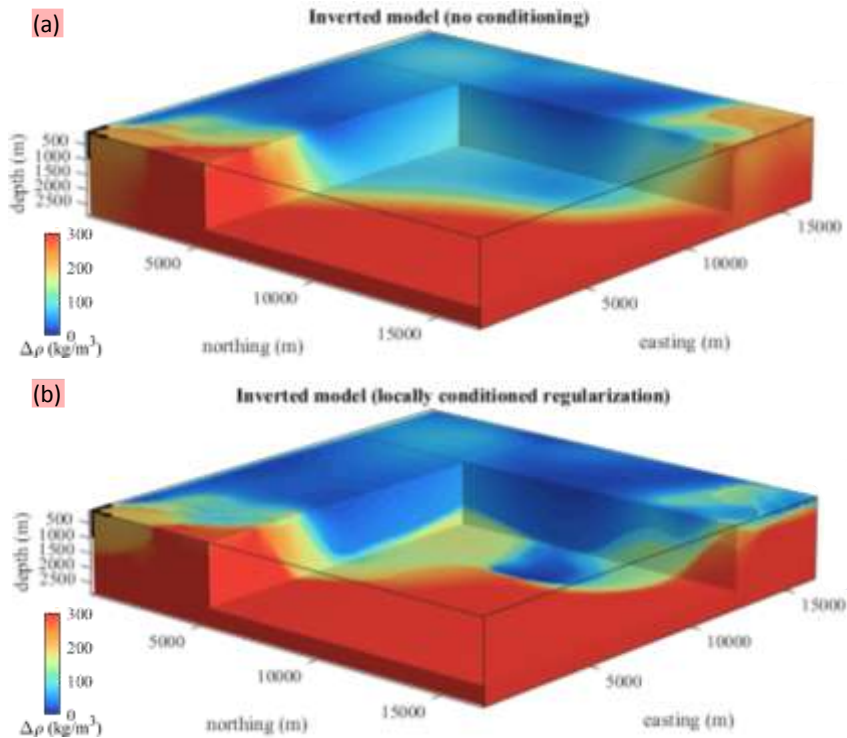


Figure A5. Comparison of inversion results. (a) Inverted models with non-conditioned regularization weights, and (b) using local conditioning.

Besides qualitative visual comparison of the models, we interpret inversion results through the commonly used model and data root-mean-square error (RMSE). We evaluate the geometrical similarity between inverted and true model through the Bravais-Pearson correlation (also often called ‘linear correlation coefficient’) between their gradients (Table A1).

Comparison of the reference model (Fig. A4a) with inversion results in Fig. A5a and Fig. A5b shows that while the structures in shallowest part of the model are well retrieved in both cases, it appears that they are considerably better recovered through usage of conditioned regularization overall (Fig. A5b). The guiding effect of W_H is visible in Fig. A5b where the main structures at depth follow the general features of the conditioning volume (Fig. A4b). Moreover, in order to minimize the conditioned regularization constraint simultaneously to data misfit, inversion was driven to accommodate inverted model values (Fig. A5b) such that they are closer to the causative model (Fig. A4a) than without conditioning (Fig. A5a). This leads

to reduced model RMSE on one hand, and data RMSE on the other hand (Table A1). This reduction in data RMSE can also be explained by the relaxation of the constraints in several portions of the model, thus increasing the degree of liberty to accommodate the model towards lower data misfit. Importantly, the Bravais-Pearson correlation between the inverted and reference model gradients is nearly three times higher when information from information entropy is used, which indicates that local conditioning of the regularization function also allows for significantly better retrieval of the causative bodies' (e.g., true model) structural features.

From these observations, we conclude that the application of the local conditioning scheme can fulfill the objectives of data integration in inversion as it is capable to recover models that are closer to the causative bodies and easier to interpret, while potentially providing reduced data misfit.

10 A3 Data misfit maps from inversion in the Yerrida Basin

Figure A6 below relates to the analysis of data misfit in Sect. 3 of the article through the plot of the data misfit maps for the non-conditioned and conditioned cases (Fig. A6d and Fig. A6h, respectively). It is complemented by the corresponding plots of starting (Fig. A6a and Fig. A6e), observed (Fig. A6b and Fig. A6f), and calculated data (Fig. A6c and Fig. A6g). Note that Fig. A6c and Fig. A6g show little visual differences, and that Fig. A6d and Fig. A6h exhibit similar features while showing limited coherent signal.

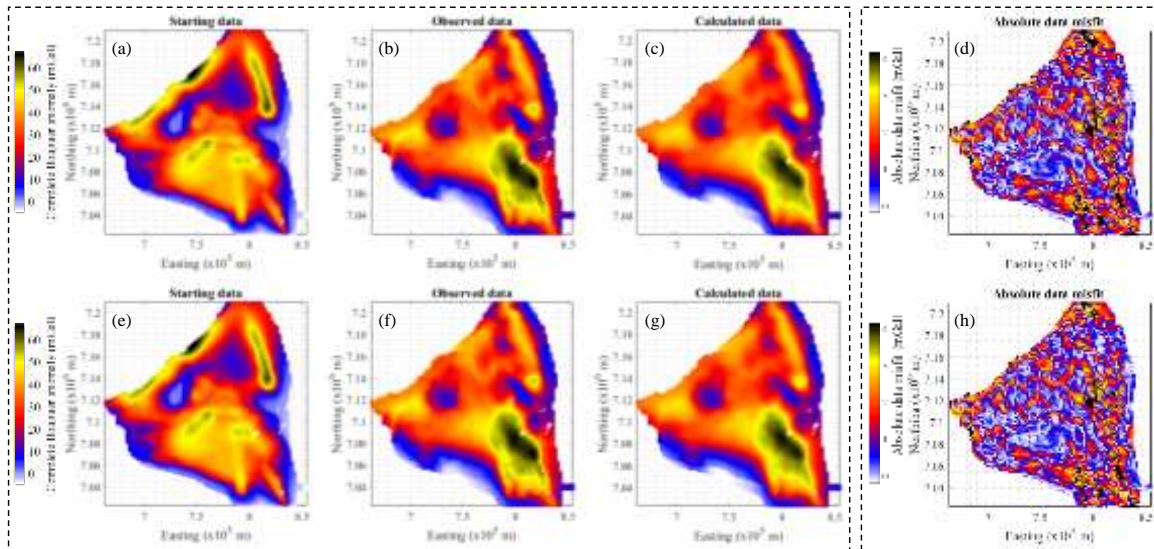


Figure A6. Comparison of input and output geophysical data. (a) and (e) show data calculated from the starting model, (b) and (f) input measurements, (c) and (g) data calculated from the inverted model, and (d) and (h) the absolute value of the difference of the misfit between the observed and calculated data. (a)-(d) (e.g., first line) and (e)-(h) (e.g., second line) correspond to the non-conditioned and conditioned cases, respectively.

Authors contribution. Jeremie Giraud performed the integrated inverse modelling of geophysical data for both the Mansfield synthetic study and the Yerrida Basin. He performed posterior analysis and interpretation of results and he is the main contributor to the writing of this article. Mark Lindsay acquired part of the geological field measurements from the Yerrida Basin and performed the geological modelling of the area. He participated in the writing of the geological setting subsection and he produced the geological map shown in Fig. 1a. Vitaliy Ogarko and Jeremie Giraud worked together on the implementation and testing of the proposed methodology in Tomofast-x, of which Vitaliy Ogarko, Roland Martin and Jeremie Giraud are the main developers. Mark Jessell has been involved in the validation of the methodology at the initial development stage and supervised the progress of the presented work. Roland Martin provided support at the initial stage of the inversion of gravity data from the Yerrida Basin. Evren Pakyuz-Charrier assisted Mark Lindsay with the utilisation of MCUE. All co-authors contributed to the final version of this article. Mark Lindsay and Vitaliy Ogarko were the most actively involved in the revision process of the drafts leading to this paper.

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10 **Table A1.** Indicators for comparison of inversion results in terms of model, data, and structure.

	Model RMSE (kg.m ⁻³)	Data RMSE (m.s ⁻²)	Bravais-Pearson correlation between gradients
Non-conditioned regularization	74.66	2.38*10 ⁻⁹	0.18
Locally conditioned regularization	53.05	7.44*10 ⁻¹⁰	0.53

Integration of geoscientific uncertainty into geophysical inversion by means of local gradient regularization

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Abstract. We introduce a workflow integrating geological modelling uncertainty information to constrain gravity inversions. We test and apply this approach to the Yerrida Basin (Western Australia), where we focus on prospective greenstone belts beneath sedimentary cover. Geological uncertainty information is extracted from the results of a probabilistic geological modelling process using geological field data and their inferred accuracy as inputs. The uncertainty information is utilized to locally adjust the weights of a minimum-structure gradient-based regularization function constraining geophysical inversion. Our results demonstrate that this technique allows geophysical inversion to update the model preferentially in geologically less certain areas. It also indicates that inverted models are consistent with both the probabilistic geological model and geophysical data of the area, reducing interpretation uncertainty. The interpretation of inverted models reveals that the recovered greenstone belts may be shallower and thinner than previously thought.

1 Introduction

The integrated interpretation of multiple data types and disciplines in geophysical exploration is a powerful approach to mitigating the limitations inherent to each of the datasets. For instance, gravity data, which has poor horizontal resolution, can be integrated with seismic inversion to mitigate the poor lateral resolution of seismic inversion (Lelièvre et al., 2012). Likewise, geological modelling and geophysical inversions are routinely performed in the same area to obtain a subsurface model consistent with geological and geophysical measurements (Guillen et al., 2008; Lelièvre and Farquharson, 2016; Pears et al., 2017; Williams, 2008). When sufficient prior information is available, petrophysical constraints can be used in inversion (Lelièvre et al., 2012; Paasche and Tronicke, 2007), and integrated with geological modelling to derive local constraints (Giraud et al., 2017). However, in exploration scenarios, this can be impractical as the available petrophysical information

may be insufficient to allow us to derive such constraints (Dentith and Mudge, 2014). In such cases, when more than one geophysical dataset is available, practitioners have relied on joint inversion using structural constraints (e.g., Gallardo and Meju, 2003; Haber and Oldenburg, 1997; Zhdanov et al., 2012). Alternatively, when one of the datasets has a spatial resolution that is superior to the others, structural information can be transferred into the gradient regularization constraint for the inversion of the lesser resolving method(s), thus mitigating some of the challenges faced by joint inversion in such cases into what has been called guided inversion (Brown et al., 2012). This strategy has been applied in recent years using the interpretation of predominantly propagative data (e.g., seismics, ground-penetrating radar) to constrain the inversion of diffusive data (e.g., diffusive electromagnetic methods), as reported by (Yan et al., 2017) and references reported therein. However, this avenue remains relatively underexplored to date.

10 In this article, we broaden the applications of guided inversion and explore the integration of non-geophysical information in inversion, such as geological uncertainty, into what we call uncertainty-guided inversion where we focus on the complementarity of information content between the datasets. We introduce a new technique that integrates local uncertainty information derived from probabilistic geological modelling in the inversion of potential field data, following recommendations of (Jessell et al., 2014, 2018, 2010, Lindsay et al., 2013a, 2014, Wellmann et al., 2014, 2017). In contrast to (Giraud et al., 2016, 2017) who derives local petrophysical constraints from petrophysical measurements and geological modelling results, constraints used in uncertainty-guided inversion are based solely on the local conditioning of a gradient regularization function, thereby offering the possibility to integrate probabilistic geological modelling into geophysical inversion in the absence of sufficient petrophysical information. Such conditioning relies on the calculation of local weights derived from prior geological information. In this study, we utilize a probabilistic geological model (PGM) (Pakyuz-Charrier et al., 2018b) consisting of the observation probability of the different lithologies of the area in every model cell. More specifically, we utilize the information entropy (Shannon, 1948; Wellmann and Regenauer-Lieb, 2012), which measures geological uncertainty in probabilistic models. We calculate it in each model cell of the PGM to derive spatially varying weights applied to the gradient regularization function used during inversion.

The integration methodology we develop is similar in philosophy to the work of Brown et al. (2012), Guo et al. (2017), and Wiik et al. (2015), who extract continuous structural information from seismic data to adjust the strength of the regularization term locally in order to promote specific structural features during electromagnetic inversion. However, our work differs from these authors in four main respects. Firstly, the geophysical problem we tackle is different in nature as we constrain potential field data in hard rock scenario instead of electromagnetic data in soft rock studies. Secondly, we use a metric encapsulating geological uncertainty derived from geological measurements, whereas, in contrast, previous studies use other geophysical attributes. Thirdly, we allow inversion to update the model preferably in the most uncertain parts of the geological model, instead of encouraging a certain degree of structural similarity between two geophysical inverse models. Finally, while some of the previous work involve mostly 2D models, every step of our modelling is performed purely in 3D.

In this paper, we introduce the methodology and field application as follows. In the methodology section, we first introduce the inversion and integration scheme, and provide essential background information about probabilistic geological modelling. We then provide the essential background about information entropy before detailing its usage in inversion. In the ensuing section, we investigate the applicability of the proposed technique using a realistic synthetic case study. Following this, we present a field application case focused on the Yerrida Basin (Western Australia), starting with the introduction of the geological context and modelling procedure. We then analyse the influence of local regularization conditioning on inverted models and demonstrate how it improves the clarity and improves the reliability of the interpretation of the buried greenstone belts.

2 Modelling procedure

2.1 Inversion methodology

The inversion procedure we propose integrates spatially varying prior information to weight the regularization function locally (e.g., in each cell). It is implemented in an expanded version of the least-square inversion platform Tomofast-x (Martin et al., 2013, 2018), which offers the possibility to condition the regularization function (Tikhonov and Arsenin, 1977) of (Li and Oldenburg, 1996) locally using geological uncertainty. This is achieved by incorporating prior information into a structure-based regularization function in a fashion similar to (Brown et al., 2012; Wiik et al., 2015; Yan et al., 2017) by locally adjusting the related weight.

Solving the inversion problem regularized in this fashion consists of finding a model \mathbf{m} that minimizes the objective function θ given below:

$$\theta(\mathbf{d}, \mathbf{m}) = \underbrace{\|\mathbf{W}_d(\mathbf{d} - \mathbf{g}(\mathbf{m}))\|_2^2}_{\text{Data term}} + \underbrace{\alpha_m \|\mathbf{W}_m(\mathbf{m} - \mathbf{m}_p)\|_2^2}_{\text{Model term}} + \underbrace{\alpha_H \|\mathbf{W}_H \nabla \mathbf{m}\|_2^2}_{\text{Structural regularization term}}, \quad (1)$$

where \mathbf{d} relates to the geophysical measurements to be inverted, \mathbf{g} is the forward modelling operator; \mathbf{m} relates to the model being searched for, and \mathbf{m}_p is the prior model; \mathbf{W}_d , \mathbf{W}_m and \mathbf{W}_H are diagonal weighting matrices corresponding to data noise, model weighting and gradient regularization, respectively. The model term is a ridge regression constraint term (Hoerl and Kennard, 1970).

The structural regularization term in Eq. (1) enforces structural constraints during inversion. It is weighted locally by matrix \mathbf{W}_H , which can be derived from prior information (see Subsect. 2.3 for details). The positive free parameters α_m and α_H control the overall weight of model and structural regularization terms; ∇ is the spatial gradient operator. Note that $\|\nabla \mathbf{m}\|_2$, estimates the amount of structure in inverted physical property model \mathbf{m} . Also note that parts of the model where $\mathbf{W}_H = 0$ are excluded from the calculation of the structural regularization and can change freely to accommodate geophysical data.

We utilize the integrated sensitivities technique of (Portniaguine and Zhdanov, 2002) to balance the decreasing sensitivity of gravity data with depth. We chose this technique because it offers the advantage of providing “equal sensitivity of the observed data to the cells located at different depths and at different horizontal positions” (Vatankhah and Renaut, 2017).

5 2.2 Probabilistic geological modelling

Probabilistic geological modelling is performed using the Monte-Carlo Uncertainty Estimator (MCUE) method of (Pakyuz-Charrier et al., 2018b, 2018a), which extends previous works from (Jessell et al., 2010; Lindsay et al., 2012; Wellmann et al., 2010). It is a 3D uncertainty propagation method for implicit geological modelling that uses geological rules and geological orientation measurements (foliation and interface of the geological units sampled at surface level or in borehole) as inputs. The sampling algorithm perturbs orientation data used to derive a reference model by sampling probability distributions describing the uncertainty of orientation data to produce a series of unique altered geological models. Realizations that do not respect a series of geological rules are considered implausible and are rejected. Coupled to the 3D geological modelling engine of Geomodeller© (Calcagno et al., 2008), it produces a set of plausible geological models honouring the geological input measurements that represent the geological model space (Lindsay et al., 2013b). The observation probabilities constituting the probabilistic geological model (PGM) are obtained, in each model cell, by calculating the relative observation frequencies of the different lithologies from the set of geological models. For the i^{th} model cell of a PGM containing L lithologies, vector $\boldsymbol{\psi}^i = [\psi_{k=1}^i, \dots, \psi_{k=L}^i]$ contains the observation probabilities of each lithology. As we show in the next subsection, the resulting PGM can be used to estimate uncertainty levels and as a source of prior information.

2.3 Utilisation of information entropy for local conditioning

Information entropy was introduced for geological modelling by Wellmann and Regenauer-Lieb (2012) and is gaining popularity as a measure of uncertainty in probabilistic geological modelling (de la Varga et al., 2018; de la Varga and Wellmann, 2016; Lindsay et al., 2014; Lindsay et al., 2013; Pakyuz-Charrier et al., 2018; Schweizer et al., 2017; Thiele et al., 2016; Wellmann et al., 2017; Yamamoto et al., 2014). Quoting (Schweizer et al., 2017), information entropy “quantifies the amount of missing information and hence, the uncertainty at a discrete location”. For the i^{th} model-cell, it is given as (Shannon, 1948):

$$H^i = H(\boldsymbol{\psi}^i) = - \sum_{k=1}^L \psi_k^i \log(\psi_k^i). \quad (2)$$

Fundamentally, geological uncertainty contained in H encapsulates information about possible locations of interfaces between units and areas where the geological data is insufficiently informative. Instead of using H directly, we calculate \mathbf{W}_H utilising

its normalized complementary, which reflects the degree of certainty across the model. Let us express W_H as follows, for the i^{th} model cell:

$$W_H^i = \frac{\max H - H^i}{\max H - \min H} \quad (3)$$

The consequence of Eq. (2) and 3 is that W_H is minimum at interfaces and in areas poorly constrained by geological information, and equal to unity in areas where the geology is well resolved. Consequently, the conditioning process attaches small weights to the structural term of Eq. (1) in uncertain cells, while consistently high values will be applied to the most geologically certain cells. As a result, it enables the inversion algorithm to favour nearly constant changes in the inverted model in contiguous certain groups of cells (e.g., where $W_H \rightarrow 1$) while relaxing the regularisation constraints in the most uncertain parts (e.g., where $W_H \rightarrow 0$).

3 Proof of concept: synthetic case study

This section introduces the proof of concept of the proposed method through an idealized case study illustrating the potential of the proposed inverse modelling scheme to ameliorate inversion results and to reduce interpretation uncertainty. We use the same 3D density contrast model as (Giraud et al., 2017), which is obtained by populating the structural framework of (Pakyuz-Charrier et al., 2018b). We simulate a series of PGM sought to represent expected values as well as possible extreme scenarii. The short presentation of the model below and the analysis of results provides essential information about the synthetic survey and shows the proof of concept of the methodology used in the paper.

3.1 Survey setup

The 3D unperturbed reference geological model was generated from contact (interface points) and surface orientation (foliations) field measurements collected in the Mansfield area (Victoria, Australia). It presents a Carboniferous mudstone-sandstone basin oriented N170, abutting a faulted contact with a folded ultramafic basement to the South-West. Model complexity was artificially increased through the addition of a North-South fault and of a mafic intrusion.

The true density contrast model (Figure 1a) was obtained assigning density contrasts consistently with the structural setting of the reference geological model, assuming a flat topography. Density contrasts of 0 and 100 kg.m⁻³ were assigned to the upper and lower basin lithotypes, respectively. Mafic rocks were assigned a density contrast of 200 kg.m⁻³ while the density contrast of the ultramafic basement was set to 300 kg.m⁻³.

MCUE perturbations of the reference geological model were first performed using standard measurement uncertainty values recommended by metrological studies as reported by (Allmendinger et al., 2017; Novakova and Pavlis, 2017). We generated a series of 300 models that were subsequently combined into a PGM. The resulting volume representing the W_H values calculated from this PGM in each cell of the model as per Eq. (3) is shown in Figure 1b.

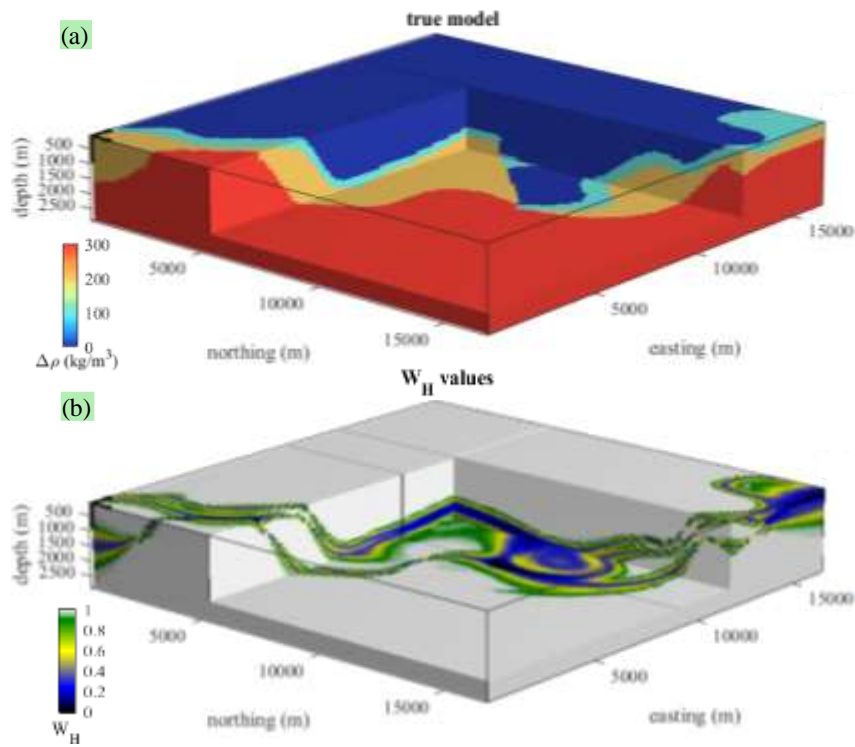


Figure 1. True density contrast model and W_H values used for local regularization conditioning. (a) Unperturbed reference model populated with density contrast values, (b) uncertainty values used for local regularization conditioning.

3.2 Locally constrained inversion: validation

- 5 To assess the impact of local conditioning of the regularization function onto inversion, we compare inversions using non-conditioned (Figure 2a) and locally conditioned (Figure 2b) regularization function, respectively. Please note that, simulating the absence of prior petrophysical information, a homogenous prior model set to 0 kg.m⁻³ was used in both cases.

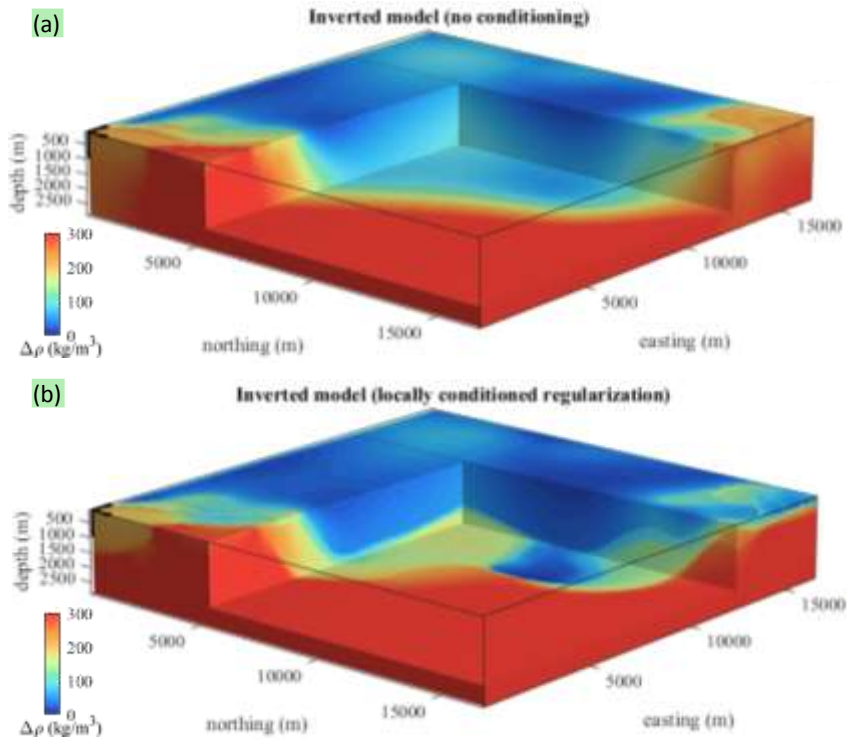


Figure 2. Comparison of inversion results. (a) Inverted models with non-conditioned regularization weights, and (b) using local conditioning.

Besides qualitative visual comparison of the models, we interpret inversion results (Figure 2) through the commonly used model and data root-mean-square error (RMSE), which correspond to the model and data terms calculated with weights and covariances set to unity. We evaluate the geometrical similarity between inverted and true model through the Bravais-Pearson correlation (also often called ‘linear correlation coefficient’) between their gradients (Table 1).

Comparison of the true model (Figure 1a) with inversion results in Figure 2a and Figure 2b shows that while the structures in shallowest part of the model are well retrieved in both cases, it appears that they are considerably better recovered through usage of conditioned regularization overall (Figure 2b). The guiding effect of W_H is visible in Figure 2b where the main structures at depth follow the general features of the conditioning volume (Figure 1b). Moreover, in order to minimize the conditioned regularization constraint simultaneously to data misfit, inversion was driven to accommodate inverted model values (Figure 2b) such that they are closer to the causative model (Figure 1a) than without conditioning (Figure 2a). This leads to reduced model RMSE on the one hand, and data RMSE on the other (Table 1). This reduction in data RMSE can also be explained by the relaxation of the constraints in several portions of the model, thus increasing the degree of liberty to accommodate the model towards lower data misfit. More importantly, the Bravais-Pearson correlation between the inverted and true model gradients is much higher when information from information entropy is used. This indicates that local

conditioning of the regularization function also allows for significantly better retrieval of the causative bodies' (e.g., the true model) structural features.

Please also note that we do not show the recovered geophysical measurements because visual differences between recovered and inverted measurements are minimal.

5

Table 1. Indicators for comparison of inversion results in terms of model, data, and structure.

	<i>Model RMSE (kg.m⁻³)</i>	<i>Data RMSE (m.s⁻²)</i>	<i>Correlation between gradients</i>
<i>Non-conditioned regularization</i>	74.66	2.38×10^{-9}	0.18
<i>Locally conditioned regularization</i>	53.05	7.44×10^{-10}	0.53

From these observations, we conclude that the application of the local conditioning scheme can fulfil the objectives of data integration in inversion as it allows inversion to recover models that are closer to the causative bodies and easier to interpret, while honouring geophysical data. Nevertheless, it remains important to test the methodology in cases where the uncertainty indicator W_H is biased and/or shows high geological uncertainty levels away from faults and contacts. A thorough analysis lying beyond the scope of this paper, the remainder of this section presents an elementary sensitivity analysis using a series of two W_H volumes representing distinct extreme scenarios.

10

3.3 Inversion constrained by biased geological uncertainty model

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In this subsection, we investigate the effect of inaccurate geological models and the propagation of the related uncertainty in inversion. For this purpose, we calculate a second PGM from MCUE perturbations in which we split the ultramafic basement into two independent units, without changing the density contrast values (Figure 3a). This results in the existence of a fictitious geological unit that is invisible to gravity data and presents no density contrast but which increases geological complexity and uncertainty (Figure 3b) (we further refer to it as 'ghost' geological unit). Notably, it increases geological uncertainty and smears interfaces that are well-constrained as per Figure 1. It also decreases W_H in large parts of the model where $W_H \rightarrow 1$ previously, thereby favouring model changes in these areas during inversion and encouraging it to place larger density contrast or interfaces in these areas.

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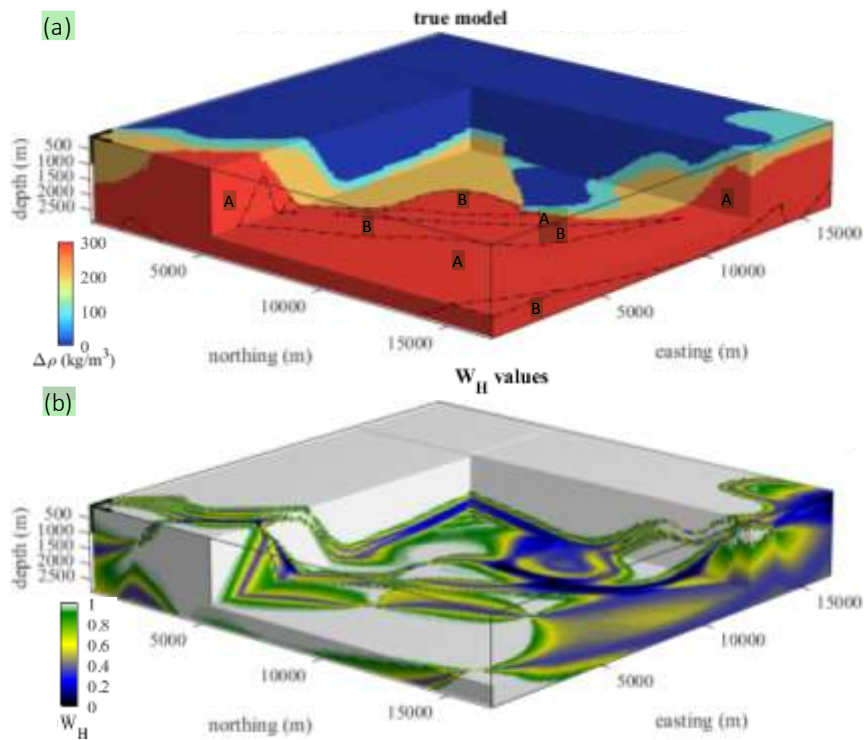


Figure 3. (a) true density contrast model with outline of the ‘ghost’ unit B (black dashed line), embedded in ultramafic unit A, and (b) local weights calculated from the PGM calculated using MCUE for model (a).

- 5 Comparison of the inverted models obtained without (Figure 4a) and with the ghost unit (Figure 4b) reveals that they exhibit broadly similar features except in the most geologically complex parts of the model as per Figure 1b, where differences are minor. This indicates that while geophysical inversion updates the prior density contrast model preferably in geologically uncertain regions, low values of W_H do not necessarily lead to the modelling of an interpretable interface by inversion. From the comparison of Figure 3b and Figure 4b, we can deduce that local conditioning as applied in this work does not necessarily
- 10 enforce strict structural similarity between the inverted model and the conditioning geological uncertainty volume.

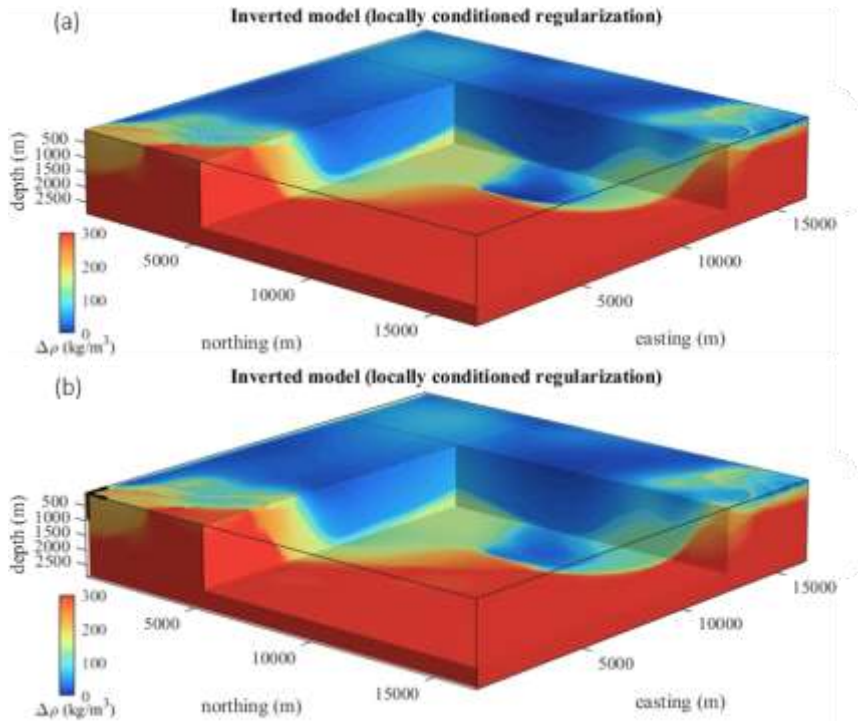


Figure 4. Comparison of inverted model using W_H derived from a PGM considering the ghost unit (b) and without it (a); (a) is the inverse model obtained without bias in the PGM as per Figure 2 and is shown here for comparison with (b).

3.4 Inversion constrained using exaggerated geological uncertainty

- 5 To complete this series of tests, we generated a third PGM showing exaggerated geological uncertainty. To this end, we used a half aperture 95% confidence interval of ~ 50 degrees for orientation data measurements in our MCUE simulations. This is far higher than for the rest of the MCUE simulations used in this paper. All other simulations (Subsect. 3.2 and 3.3) use a value of ~ 11 degrees, which is representative of realistic measurement uncertainty as proposed by recent metrological studies (Allmendinger et al., 2017; Cawood et al., 2017; Novakova and Pavlis, 2017). Figure 5 below shows the resulting W_H volume
- 10 (Figure 5a) and the inverted model obtained using it for local conditioning of the regularization constraint (Figure 5b).

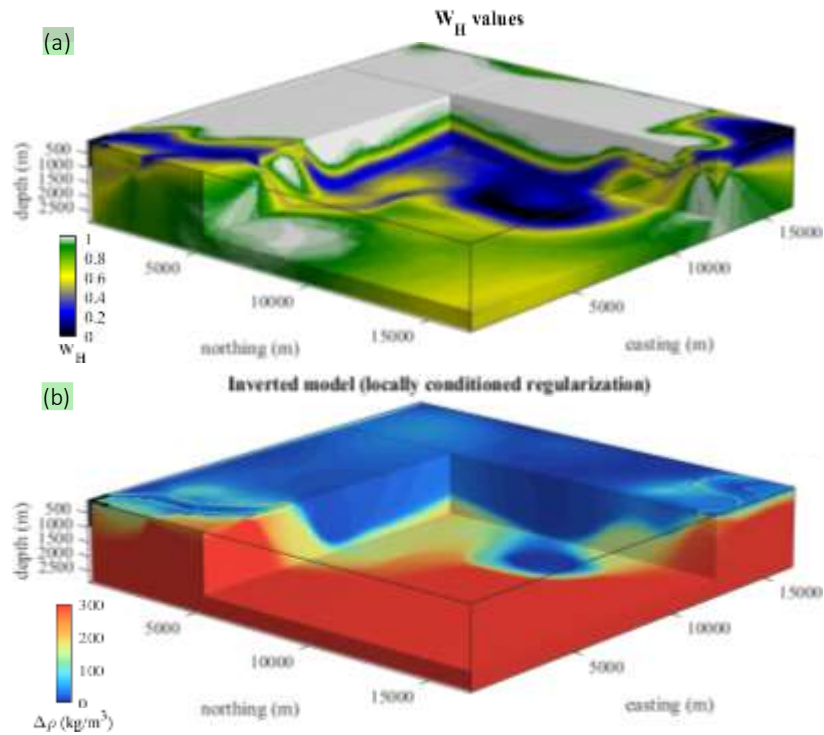


Figure 5. (a) Local weights W_H calculated from a PGM corresponding to exaggerated uncertainty in geological input measurements and (b) corresponding inverted density contrast model.

5 The features visible in Figure 5a reflect the high geological input measurement uncertainty. Geologically uncertain areas cover large portions of the volume and only the simplest geological structures (e.g., the basin) seem to be well constrained by geology. Areas of the model previously well constrained (Figure 1b) present varying degrees of uncertainty. This illustrates that, as can be expected, increasing geological input uncertainty translates in relaxing the guiding effect of local conditioning using W_H , which results in geophysical inversion being less strongly guided by geological information. As can be seen in Fig 10 4b, the inverted model obtained in this case shows structures that present weaker contrast around interfaces than when geological uncertainty is lower (Figure 2b). Importantly, however, most structures are well preserved and the overall model values for the different lithologies remain closer to the true model than for the non-conditioned case (Figure 2a). This indicates that even in high geological uncertainty scenarios, interpretation outcome may be largely more reliable when local regularisation is used.

15

The analysis and comparison of the results shown in this section demonstrates the potential of the proposed inverse modelling scheme to ameliorate inversion results and to reduce interpretation uncertainty. It also illustrates the capability of our methodology to deal with high or biased conditioning uncertainty estimates. In this synthetic case, local conditioning allows

geophysical inversion to significantly improve the imaging of geologically uncertain areas and to exploit complementarities between geological modelling and geophysical inversion. From the success of this proof of concept study, we are confident that our integration method can be tested here using real world data for field validation.

4 Field validation: Yerrida Basin case study

5 4.1 Geological context and geophysical survey setup

The Yerrida Basin is located in the southern part of the Capricorn Orogen, at the northern margin of the Yilgarn Craton in Western Australia (Figure 6a), and extends approximately 150km N-S and 180 km E-W (Figure 6b). The studied area is bounded in the northwest by the Goodin Fault, which represents a faulted contact between the Yerrida Basin and the Bryah-Padbury Basin. The structures of interest in this work are the Archean greenstone belts extending north-northwest that are unconformably overlain by Paleoproterozoic sedimentary rocks that form the Yerrida Basin. Features A and B (Figure 6a and Figure 6b) indicate the interpreted position of buried Wiluna Greenstone Belt. Where the Wiluna Greenstone Belt is exposed, it is host to base and precious metal mineralisation (Williams, 2009). With a relatively high positive density contrast (expected to be between 190 and 270 kg.m⁻³) to the Yilgarn Craton granite-gneiss host, mafic greenstone belts A, B, and C are suitable targets for gravity inversion. Interpretations from multiple studies in the region, e.g. (Johnson et al., 2013; Pirajno et al., 1998; Pirajno and Adamides, 2000; Pirajno and Occhipinti, 2000) were compiled while additional geological measurements acquired in 2015, 2016 and 2017 complemented legacy data (Occhipinti et al., 2017; Olierook et al., 2018). This allowed the revision of existing models and improved our understanding of the area. This, in turn, also highlights the challenges presented by the characterization of greenstone belts A, B and C, and that further geophysical analysis through constrained inversion is a useful pathway for reducing exploration risk.

20 Geophysical data consists of ground surveys obtained from Geoscience Australia (<http://www.ga.gov.au/data-pubs>). Post-processing includes spherical-cap and terrain corrections and the removal of the regional trend to obtain the complete Bouguer anomaly. As most data points were acquired 1 to 4 km apart, the dataset was resampled to match the geological model discretization, making up a total of 4882 measurement points. The model is discretized into 100 × 100 × 42 cells of dimensions 2.335 km × 1.875 km × 1.0475 km, down to a depth of 44 km, making up a total of 420000 cells.

25

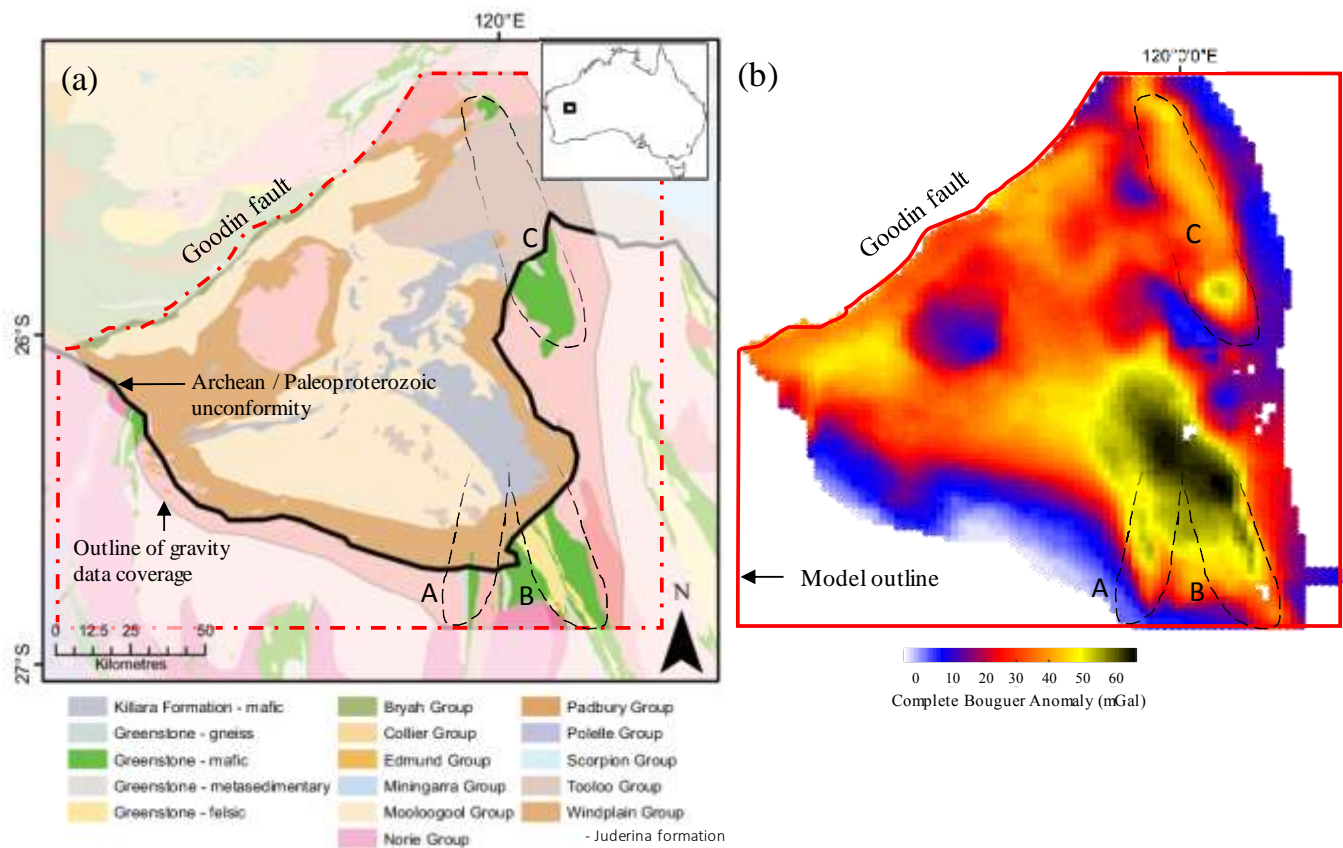


Figure 6. Geological context and geophysical data. (a) Geological map of the area and (b) complete Bouguer anomaly. The dashed lines delineate the possible sub-basin extent of the mafic greenstone belts A, B and C.

5 4.2 Geological modelling

Geological information consists of in-situ structural measurements (interfaces and foliations) and interpretation of aeromagnetic, airborne electromagnetic, Landsat 8 and ASTER hyperspectral data. Legacy data from the Geological Survey of Western Australia (Pirajno and Adamides, 2000) and CSIRO (Ley-Cooper et al., 2017) were used, to which about 600 surface geological and petrophysical measurements from recent geological field campaigns were added. Although the available petrophysical measurements were not used to derive petrophysical constraints because of the insufficient sampling of several of the modelled lithologies, they were a useful source of information to populate geological models and for interpretation. Remote-sensing data were used to test interpretations.

These datasets were used jointly to build a reference geological model reconciling the available geological information in Geomodeller.

Lithologies with similar density contrasts were merged and subsequently treated as a single rock type in MCUE simulations. Uncertainty related to structural measurements was subsequently used as inputs to the MCUE perturbations (Pakyuz-Charrier et al., 2018b) of the reference model to generate a collection of 500 accepted models. Information extracted from the PGM is displayed in Figure 7. Figure 7a shows the lithologies with the highest probability for each cell of the PGM. The associated W_H values used in inversion are shown in Figure 7b. The prior model for inversion m_p is equal to the mean model of the 500 plausible models generated by MCUE. It is shown in Figure 7c.

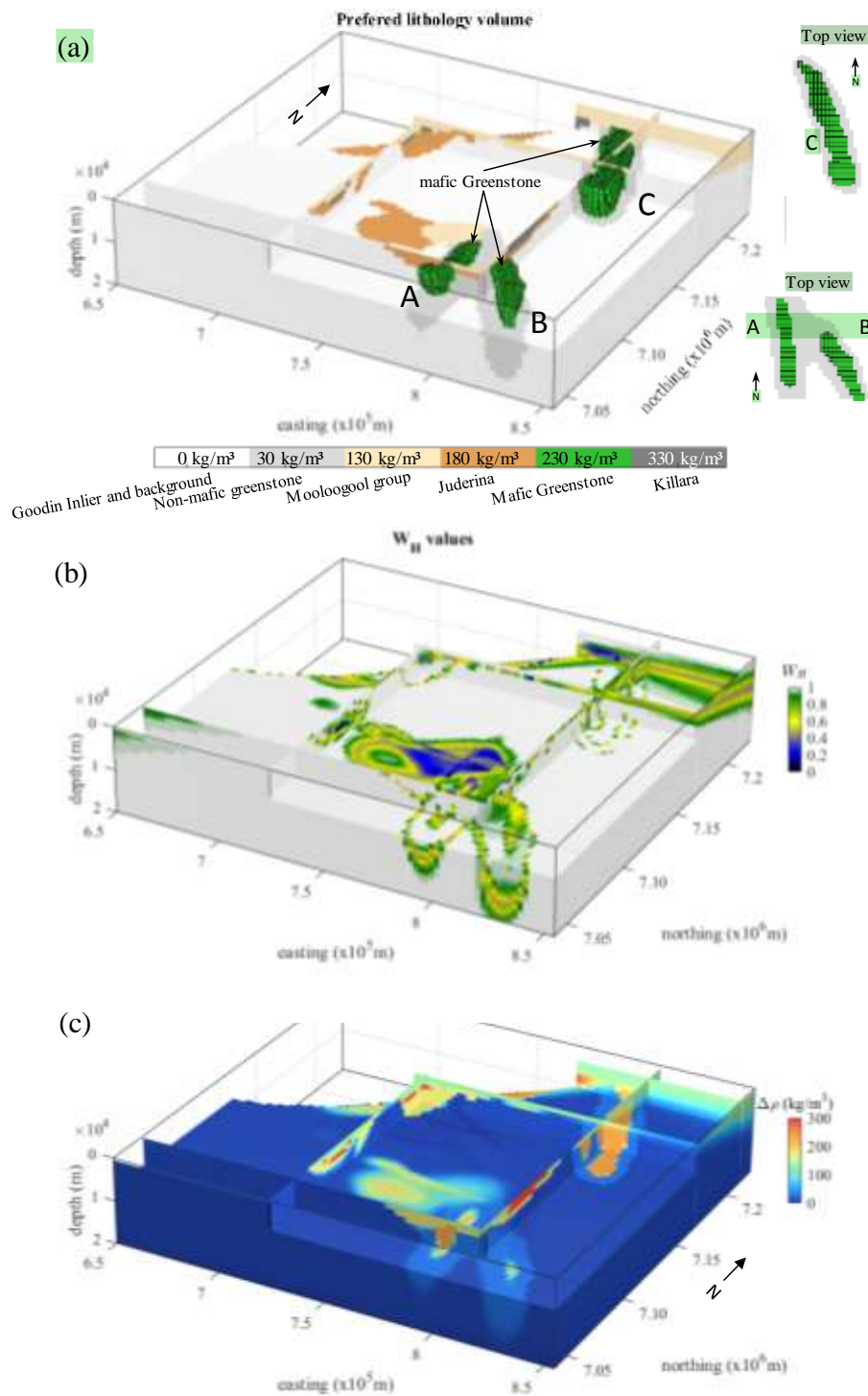


Figure 7. Geological modelling results. (a) Most probable lithology in each model cell (same colour code as in Figure 6) (b) values used for local regularization conditioning, (c) and prior model derived from PGM and prior petrophysical information). In (a), “background” refers to all the lithologies that have a density contrast equal to 0 kg.m⁻³.

4.3 Inversion results and analysis

The aim of our analysis is to assess the influence of the local conditioning of structural constraints on inversion through comparison with the non-conditioned case, all other things remaining constant.

4.3.1 Comparative analysis strategy

5 Prior to examination of the inverted models, we analyse geophysical data misfit after inversion. This enables us to ensure that the inversion results we compare produce, in our case, similar gravity anomalies. Our study of inverted models focuses on results obtained through usage of non-conditioned (Figure 8a) and conditioned regularization function (Figure 8b) using W_H (Figure 7b). In addition to departures from the prior model, variations between the two cases are studied by visual comparison of Figure 8a and Figure 7b, through qualitative (Figure 7c) and quantitative comparative analysis (Figure 7d-e). Our
10 interpretation of inversion results is complemented by metrics quantifying the differences between models. We give particular attention to model cells where the probability of mafic greenstone is larger than zero. For these cells, we classify lithologies by identifying cells with a density contrast corresponding to mafic greenstone.

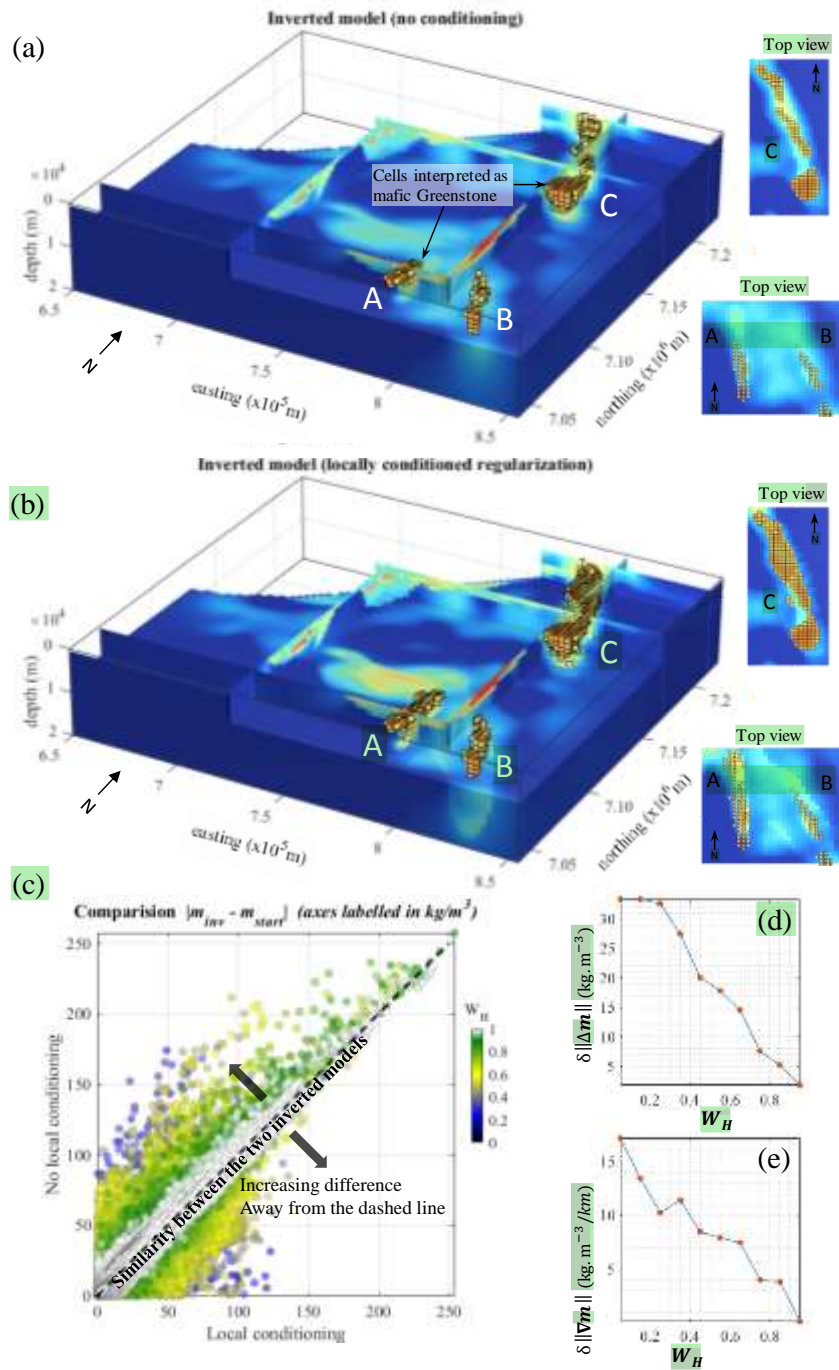
4.3.2 Results

Data root-mean-square (RMS) error decreases during inversion from 12.46 mGal to reach 1.59 mGal and 1.53 mGal for the
15 non-conditioned and conditioned cases, respectively. The corresponding data misfit maps show a linear correlation coefficient of 0.999 (see details in Appendix A). This similarity illustrates that, as in many other studies, most changes related to holistic data integration in geophysical inversion occur primarily in model space, hence reducing the effect of non-uniqueness (Abtahi
et al., 2016; Abubakar et al., 2012; Brown et al., 2012; Demirel and Candansayar, 2017; Gallardo et al., 2012; Gallardo and
Meju, 2004, 2007, 2011; Gao et al., 2012; Giraud et al., 2017; Guo et al., 2017; Heincke et al., 2017; Jardani et al., 2013;
20 Juhojuntti and Kamm, 2015; Kalscheuer et al., 2015; Molodtsov et al., 2013; Moorkamp et al., 2013; Rittgers et al., 2016; Sun
and Li, 2016, 2017).

Qualitatively, comparison of Figure 8a and Figure 8b reveals that departures from the prior model (Figure 7c) are more
significant in the most geologically uncertain areas. Quantitatively, the RMS model update for cells characterized by $0 \leq$
 $W_H < 0.05$ (most uncertain group) is equal to 40.1 kg/m^3 and 51.5 kg/m^3 , for the non-conditioned and conditioned cases,
25 respectively, whereas the same quantities are equal to 17.7 kg/m^3 and 16.9 kg/m^3 for the cells identified by $0.95 < W_H \leq$
1 (most certain group). This suggests that local regularization conditioning allows inversion to update the model preferentially
in geologically uncertain areas. In turn, differences with the prior model in more geologically certain areas are reduced
compared to the non-conditioned case. This effect of conditioning is corroborated by Figure 8c where the longest distances to
the dashed line, which represents equal model update for the two studied cases, occur in geologically uncertain areas. This also
30 translates in higher difference between model updates of the two cases in Figure 7d for lower values of W_H . In addition, we

observe that local conditioning produces stronger density contrasts in **Figure 8b** in some of the areas where the conditioning values are higher in **Figure 8b**. Furthermore, structures in the inverted model are easier to identify when local conditioning is used. It is confirmed by global roughness measures $\|\nabla\mathbf{m}\|_2$ equal to $3.4 (kg/m^3)/m$ and $4 (kg/m^3)/m$ for the non-conditioned and conditioned cases, respectively. More specifically, as shown by **Figure 7e**, this difference arise in parts of the model associated with lower W_H , which characterize uncertain areas, including interfaces between lithologies.

The recovered greenstone belts are shown in **Figure 8a** and **Figure 8b**. In **Figure 8b**, the extension of recovered mafic greenstone belts is significantly different than when geological uncertainty is not accounted for (**Figure 8a**). In particular, belt A is significantly larger in **Figure 8b** than in **Figure 8a** ($2.4 \times 10^2 \text{ km}^3$ vs $4.6 \times 10^2 \text{ km}^3$). Similarly, the extent of belt C is increased overall (volume of $5.3 \times 10^2 \text{ km}^3$ vs $14 \times 10^2 \text{ km}^3$), while its different portions reconnect; the northern half is also significantly shallower and broader than in **Figure 7a** and **Figure 8a**. It appears that belt A remains thinner and shallower (**Figure 8b**) than suggested by the preferred lithology volume (**Figure 7a**). While similar geometries for belt B are recovered in **Figure 8a** and **Figure 8b**, they both differ from **Figure 7a** as only the eastern part is preserved. Note that it is larger in **Figure 8b**, with a volume 40% higher than in **Figure 8a**. As discussed in the next subsection, these differences have a signification impact on the interpretation of inversions results and are important to understand the influence of local conditioning on inversion.



5 **Figure 8.** Comparison of inversion results. (a) inverted models with non-conditioned regularization weights, and (b) using local conditioning, (c) cross-plot between the corresponding absolute value of the update of the prior model, (d) difference in model updates $\delta \|\Delta \mathbf{m}\| = \|\mathbf{m}_{cond} - \mathbf{m}_{nocond}\|_2$ as a function of values of W_H and (e) difference in model roughness $\delta \|\mathbf{V} \mathbf{m}\| = \|\mathbf{V} \mathbf{m}_{cond}\|_2 - \|\mathbf{V} \mathbf{m}_{nocond}\|_2$ as a function of values of W_H . The model cells labelled A, B and C are interpreted as mafic greenstone belts. All voxels are coloured as a function of density contrast.

4.4 Interpretation

Note that, in contrast to the differences between inversion results highlighted above for belts A and C, there are only small differences between the inverted models in the north-eastern part of the model and the different interpretations of belt B (Figure 7a and Figure 7b). This shows that locally conditioned regularization does not enforce changes in the inverted model everywhere geological uncertainty is high as uncertainty is only a reflection of potential errors. Rather, this indicates that in such cases, the guiding effect of such regularization will be exerted on the condition that it does not prevent the data term in $\theta(\mathbf{d}, \mathbf{m})$ as per Eq. (1) from decreasing. This also confirms that geophysical data is the main driver of the model updates in geologically uncertain areas. Instead of smooth departures from the prior model to match geophysical data regardless of geological considerations, local regularization constraints allow inversion to account for the probabilistic geological modelling of the area and for geological uncertainty. It can therefore provide results that conform better to known geology.

In consequence, by confronting a probabilistic geological model encapsulating all MCUE realizations with geophysical measurements in an inversion scheme favouring model updates in the most geologically uncertain areas, inversion complements probabilistic geological modelling in that it guides and refines the interpretation of other geoscientific data in the area.

Geophysical inversion using geological uncertainty information (Figure 7b) confirms the presence of high density anomalies that we interpret to be the mafic components of the greenstone as suggested by MCUE in several portions of the model. It also adjusts the outline and geometry of belts A, B and C to obtain a model honouring geological uncertainty information. In particular, mafic greenstone belts A and B may be smaller than the extent suggested by the PGM, and mafic greenstone C shallower than anticipated. The interpretation of inversion results also reveal that greenstone B might extend further to the east than indicated by the preferred lithology volume (Figure 7a) and that greenstone C may be thinner in its central part.

5 Concluding remarks

We have introduced a new integration scheme for the inversion of gravity data that utilizes a measure of geological uncertainty to calculate locally-conditioned gradient regularization constraints. This approach enables the integration of probabilistic geological modeling in geophysical inversion in the absence of petrophysical information sufficient to the calculation of petrophysical constraints. It uses geophysical measurements to optimize the inverse problem by updating the physical property model preferably in geologically uncertain parts of the studied area during what we called *uncertainty-guided inversion*. This therefore partly mitigates the non-uniqueness of the inversion through the addition of constraints encouraging inversion to produce models that account for geological uncertainty across the entire inverted volume. We have demonstrated that it can be used collaboratively with geological modelling efficiently through field application in the Yerrida Basin. Inversion results show that our integration methodology has the capability to refine the recovered physical property model and interpretations in portions of the model where geological uncertainty is high. Another advantage of the proposed technique is that it is time

and cost-effective as our workflow utilizes the PGM resulting from standalone probabilistic geological modelling and requires the same parameterization as non-conditioned inversion.

In the Yerrida Basin study area, application of the proposed methodology provided the effective delineation of the greenstone belts by quantitatively integrating geological measurements and geophysical data. Our findings suggest that some of the greenstone belts covered by the basin might be shallower than previously anticipated and occupy smaller volumes. This is particularly pronounced in the North-East (belt C) where the resulting model is in agreement with the shallowest cases allowed by the PGM. Likewise, in the South (belt A), only the shallowest part of the mafic greenstone body can be resolved, while the south-eastern (belt B) greenstone belt appears to be limited in extension to the eastern part of the volume where it is the preferred lithology in the PGM. In such cases, this can also indicate that these greenstone bodies might be too thin to be imaged by gravity data. These results have implications for our knowledge of the southern Capricorn Orogen as they indicate reduced (compared to the preferred lithology volume) mafic greenstone volumes under the Yerrida Basin on one hand, and decreased cover thickness on the other hand, thereby opening the door to updates in the geological interpretation of geometry of the Yerrida Basin and potential new undercover exploration prospects.

The quantitative integration technique we presented reduces uncertainty and ambiguity compared to qualitative interpretation technique or single-discipline workflows. However, despite its robustness to misplaced interface (e.g., bias) or to high geological uncertainty (e.g., sparse or very uncertain geological input measurements) as shown in the synthetic case, interpreters need to bear in mind the specificities of the geophysical data inverted for (resolution of specific geometries, depth of investigation) and the shortcomings of geological modelling workflows. As for all geological modelling, MCUE is oblivious to geological units or faults that are not sampled by field geological measurements, which can lead to biases in final models due to, for instance, inclusions not be accounted for.

Current research comprises the development of sensitivity and resolution analyses in an effort to mitigate the risk of the model being affected by uncertainty sources not accounted for. Future research will include the utilization of local petrophysical constraints of (Giraud et al., 2017) in the uncertainty-guided inversion scheme we presented, as well as the utilisation of geological uncertainty to weight the cross-gradient term of (Gallardo and Meju, 2003) locally. With this last respect, uncertainty-guided inversion can be assisted in the most uncertain parts of the model by guided inversion (in the sense of Brown et al., 2012) or through cross-gradient joint inversion.

Code and data availability. True property models, inversion results and recovered models relating to the Yerrida Basin shown in this article are made available online: Jeremie Giraud, Mark Lindsay, and Vitaliy Ogarko, 2018, Yerrida Basin Geophysical Modeling - Input data and inverted models. (Version version 1.0) [Data set]. Zenodo. <http://doi.org/10.5281/zenodo.1238216>. True property models, inversion results and recovered models relating to the synthetic case from the Mansfield area shown in this article are made available online: Jeremie Giraud, Vitaliy Ogarko, and Evren Pakyuz-Charrier, 2018, Synthetic dataset for

the testing of local conditioning of regularization function using geological uncertainty. (Version version 1.0) [Data set]. Zenodo. <http://doi.org/10.5281/zenodo.1238529>

Appendix A: Data misfit maps from inversion in the Yerrida Basin

Figure A below relates to the analysis of data misfit in Sect. 4 of the article through the plot of the data misfit maps for the non-conditioned and conditioned cases (Fig. Ad and Fig. Ah, respectively). It is complemented by the corresponding plots of starting (Fig. Aa and Fig. Ae), observed (Fig. Ab and Fig. Af), and calculated data (Fig. Ac and Fig. Ah). Note that Fig. Ac and Fig. Ag show little visual differences, and that Fig. Ad and Fig. Ah exhibit similar features while showing limited coherent signal.

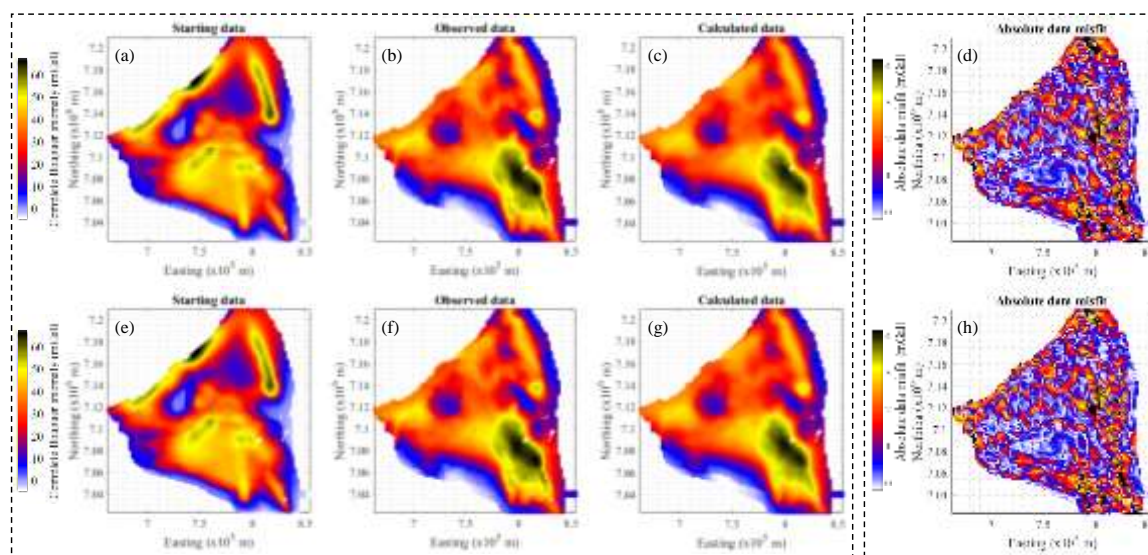


Figure A. Comparison of input and output geophysical data. (a) and (e) show data calculated from the prior model, (b) and (f) input measurements, (c) and (g) data calculated from the inverted model, and (d) and (f) the absolute value of the difference of the misfit between the observed and calculated data. (a)-(d) (i.e., first line) and (e)-(h) (i.e., second line) correspond to the non-conditioned and conditioned cases, respectively.

15 *Authors contribution.* Jeremie Giraud performed the integrated inverse modelling of geophysical data for both the Mansfield synthetic study and the Yerrida Basin. He performed posterior analysis and interpretation of results and he is the main contributor to the writing of this article. Mark Lindsay acquired part of the geological field measurements from the Yerrida Basin and performed the geological modelling of the area. He participated in the writing of the geological setting subsection and he produced the geological map shown in Figure 6a. Vitaliy Ogarko and Jeremie Giraud worked together on the implementation and testing of the proposed methodology in Tomofast-x, of which Vitaliy Ogarko, Roland Martin and Jeremie Giraud are the main developers. Mark Jessell has been involved in the validation of the methodology at the initial development

stage and supervised the progress of the presented work. Roland Martin provided support at the initial stage of the inversion of gravity data from the Yerrida Basin. Evren Pakyuz-Charrier assisted Mark Lindsay with the utilisation of MCUE. All co-authors contributed to the final version of this article. Mark Lindsay and Vitaliy Ogarko were the most actively involved in the revision process of the drafts leading to this paper.

5 **Competing interests.** The authors declare that they have no conflict of interest.

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Integration of geoscientific uncertainty into geophysical inversion by means of local gradient regularization

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Abstract. We introduce a workflow integrating geological modelling uncertainty information to constrain gravity inversions. We test and apply this approach to the Yerrida Basin (Western Australia), where we focus on prospective greenstone belts beneath sedimentary cover. Geological uncertainty information is extracted from the results of a probabilistic geological modelling process using geological field data and their inferred accuracy as inputs. The uncertainty information is utilized to locally adjust the weights of a minimum-structure gradient-based regularization function constraining geophysical inversion. Our results demonstrate that this technique allows geophysical inversion to update the model preferentially in geologically less certain areas. It also indicates that inverted models are consistent with both the probabilistic geological model and geophysical data of the area, reducing interpretation uncertainty. The interpretation of inverted models reveals that the recovered greenstone belts may be shallower and thinner than previously thought.

1 Introduction

The integrated interpretation of multiple data types and disciplines in geophysical exploration is a powerful approach to mitigating the limitations inherent to each of the datasets. For instance, gravity data, which has poor horizontal resolution, can be integrated with seismic inversion to mitigate the poor lateral resolution of seismic inversion (Lelièvre et al., 2012). Likewise, geological modelling and geophysical inversions are routinely performed in the same area to obtain a subsurface model consistent with geological and geophysical measurements (Guillen et al., 2008; Lelièvre and Farquharson, 2016; Pears et al., 2017; Williams, 2008). When sufficient prior information is available, petrophysical constraints can be used in inversion (Lelièvre et al., 2012; Paasche and Troncke, 2007), and integrated with geological modelling to derive local constraints (Giraud et al., 2017). However, in exploration scenarios, this can be impractical as the available petrophysical information

may be insufficient to allow us to derive such constraints (Dentith and Mudge, 2014). In such cases, when more than one geophysical dataset is available, practitioners have relied on joint inversion using structural constraints (e.g., Gallardo and Meju, 2003; Haber and Oldenburg, 1997; Zhdanov et al., 2012). Alternatively, when one of the datasets has a spatial resolution that is superior to the others, structural information can be transferred into the gradient regularization constraint for the inversion of the lesser resolving method(s), thus mitigating some of the challenges faced by joint inversion in such cases into what has been called guided inversion (Brown et al., 2012). This strategy has been applied in recent years using the interpretation of predominantly propagative data (e.g., seismics, ground-penetrating radar) to constrain the inversion of diffusive data (e.g., diffusive electromagnetic methods), as reported by (Yan et al., 2017) and references reported therein. However, this avenue remains relatively underexplored to date.

In this article, we broaden the applications of guided inversion and explore the integration of non-geophysical information in inversion, such as geological uncertainty, into what we call uncertainty-guided inversion where we focus on the complementarity of information content between the datasets. We introduce a new technique that integrates local uncertainty information derived from probabilistic geological modelling in the inversion of potential field data, following recommendations of (Jessell et al., 2014, 2018, 2010, Lindsay et al., 2013a, 2014, Wellmann et al., 2014, 2017). In contrast to (Giraud et al., 2016, 2017) who derives local petrophysical constraints from petrophysical measurements and geological modelling results, constraints used in uncertainty-guided inversion are based solely on the local conditioning of a gradient regularization function, thereby offering the possibility to integrate probabilistic geological modelling into geophysical inversion in the absence of sufficient petrophysical information. Such conditioning relies on the calculation of local weights derived from prior geological information. In this study, we utilize a probabilistic geological model (PGM) (Pakyuz-Charrier et al., 2018b) consisting of the observation probability of the different lithologies of the area in every model cell. More specifically, we utilize the information entropy (Shannon, 1948; Wellmann and Regenauer-Lieb, 2012), which measures geological uncertainty in probabilistic models. We calculate it in each model cell of the PGM to derive spatially varying weights applied to the gradient regularization function used during inversion.

The integration methodology we develop is similar in philosophy to the work of Brown et al. (2012), Guo et al. (2017), and Wiik et al. (2015), who extract continuous structural information from seismic data to adjust the strength of the regularization term locally in order to promote specific structural features during electromagnetic inversion. However, our work differs from these authors in four main respects. Firstly, the geophysical problem we tackle is different in nature as we constrain potential field data in hard rock scenario instead of electromagnetic data in soft rock studies. Secondly, we use a metric encapsulating geological uncertainty derived from geological measurements, whereas, in contrast, previous studies use other geophysical attributes. Thirdly, we allow inversion to update the model preferably in the most uncertain parts of the geological model, instead of encouraging a certain degree of structural similarity between two geophysical inverse models. Finally, while some of the previous work involve mostly 2D models, every step of our modelling is performed purely in 3D.

In this paper, we introduce the methodology and field application as follows. In the methodology section, we first introduce the inversion and integration scheme, and provide essential background information about probabilistic geological modelling. We then provide the essential background about information entropy before detailing its usage in inversion. In the ensuing section, we investigate the applicability of the proposed technique using a realistic synthetic case study. Following this, we present a field application case focused on the Yerrida Basin (Western Australia), starting with the introduction of the geological context and modelling procedure. We then analyse the influence of local regularization conditioning on inverted models and demonstrate how it improves the clarity and improves the reliability of the interpretation of the buried greenstone belts.

2 Modelling procedure

2.1 Inversion methodology

The inversion procedure we propose integrates spatially varying prior information to weight the regularization function locally (e.g., in each cell). It is implemented in an expanded version of the least-square inversion platform Tomofast-x (Martin et al., 2013, 2018), which offers the possibility to condition the regularization function (Tikhonov and Arsenin, 1977) of (Li and Oldenburg, 1996) locally using geological uncertainty. This is achieved by incorporating prior information into a structure-based regularization function in a fashion similar to (Brown et al., 2012; Wiik et al., 2015; Yan et al., 2017) by locally adjusting the related weight.

Solving the inversion problem regularized in this fashion consists of finding a model \mathbf{m} that minimizes the objective function θ given below:

$$\theta(\mathbf{d}, \mathbf{m}) = \underbrace{\|\mathbf{W}_d(\mathbf{d} - \mathbf{g}(\mathbf{m}))\|_2^2}_{\text{Data term}} + \alpha_m \underbrace{\|\mathbf{W}_m(\mathbf{m} - \mathbf{m}_p)\|_2^2}_{\text{Model term}} + \underbrace{\alpha_H \|\mathbf{W}_H \nabla \mathbf{m}\|_2^2}_{\text{Structural regularization term}}, \quad (1)$$

where \mathbf{d} relates to the geophysical measurements to be inverted, \mathbf{g} is the forward modelling operator; \mathbf{m} relates to the model being searched for, and \mathbf{m}_p is the prior model; \mathbf{W}_d , \mathbf{W}_m and \mathbf{W}_H are diagonal weighting matrices corresponding to data noise, model weighting and gradient regularization, respectively. The model term is a ridge regression constraint term (Hoerl and Kennard, 1970).

The structural regularization term in Eq. (1) enforces structural constraints during inversion. It is weighted locally by matrix \mathbf{W}_H , which can be derived from prior information (see Subsect. 2.3 for details). The positive free parameters α_m and α_H control the overall weight of model and structural regularization terms; ∇ is the spatial gradient operator. Note that $\|\nabla \mathbf{m}\|_2$ estimates the amount of structure in inverted physical property model \mathbf{m} . Also note that parts of the model where $\mathbf{W}_H = 0$ are excluded from the calculation of the structural regularization and can change freely to accommodate geophysical data.

We utilize the integrated sensitivities technique of (Portniaguine and Zhdanov, 2002) to balance the decreasing sensitivity of gravity data with depth. We chose this technique because it offers the advantage of providing “equal sensitivity of the observed data to the cells located at different depths and at different horizontal positions” (Vatankhah and Renaut, 2017).

5 2.2 Probabilistic geological modelling

Probabilistic geological modelling is performed using the Monte-Carlo Uncertainty Estimator (MCUE) method of (Pakyuz-Charrier et al., 2018b, 2018a), which extends previous works from (Jessell et al., 2010; Lindsay et al., 2012; Wellmann et al., 2010). It is a 3D uncertainty propagation method for implicit geological modelling that uses geological rules and geological orientation measurements (foliation and interface of the geological units sampled at surface level or in borehole) as inputs. The sampling algorithm perturbs orientation data used to derive a reference model by sampling probability distributions describing the uncertainty of orientation data to produce a series of unique altered geological models. Realizations that do not respect a series of geological rules are considered implausible and are rejected. Coupled to the 3D geological modelling engine of Geomodeller© (Calcagno et al., 2008), it produces a set of plausible geological models honouring the geological input measurements that represent the geological model space (Lindsay et al., 2013b). The observation probabilities constituting the probabilistic geological model (PGM) are obtained, in each model cell, by calculating the relative observation frequencies of the different lithologies from the set of geological models. For the i^{th} model cell of a PGM containing L lithologies, vector $\boldsymbol{\psi}^i = [\psi_{k=1}^i, \dots, \psi_{k=L}^i]$ contains the observation probabilities of each lithology. As we show in the next subsection, the resulting PGM can be used to estimate uncertainty levels and as a source of prior information.

2.3 Utilisation of information entropy for local conditioning

Information entropy was introduced for geological modelling by Wellmann and Regenauer-Lieb (2012) and is gaining popularity as a measure of uncertainty in probabilistic geological modelling (de la Varga et al., 2018; de la Varga and Wellmann, 2016; Lindsay et al., 2014; Lindsay et al., 2013; Pakyuz-Charrier et al., 2018; Schweizer et al., 2017; Thiele et al., 2016; Wellmann et al., 2017; Yamamoto et al., 2014). Quoting (Schweizer et al., 2017), information entropy “quantifies the amount of missing information and hence, the uncertainty at a discrete location”. For the i^{th} model-cell, it is given as (Shannon, 1948):

$$H^i = H(\boldsymbol{\psi}^i) = - \sum_{k=1}^L \psi_k^i \log(\psi_k^i). \quad (2)$$

Fundamentally, geological uncertainty contained in H encapsulates information about possible locations of interfaces between units and areas where the geological data is insufficiently informative. Instead of using H directly, we calculate \mathbf{W}_H utilising

its normalized complementary, which reflects the degree of certainty across the model. Let us express W_H as follows, for the i^{th} model cell:

$$W_H^i = \frac{\max H - H^i}{\max H - \min H} \quad (3)$$

The consequence of Eq. (2) and 3 is that W_H is minimum at interfaces and in areas poorly constrained by geological information, and equal to unity in areas where the geology is well resolved. Consequently, the conditioning process attaches small weights to the structural term of Eq. (1) in uncertain cells, while consistently high values will be applied to the most geologically certain cells. As a result, it enables the inversion algorithm to favour nearly constant changes in the inverted model in contiguous certain groups of cells (e.g., where $W_H \rightarrow 1$) while relaxing the regularisation constraints in the most uncertain parts (e.g., where $W_H \rightarrow 0$).

3 Proof of concept: synthetic case study

10 This section introduces the proof of concept of the proposed method through an idealized case study illustrating the potential of the proposed inverse modelling scheme to ameliorate inversion results and to reduce interpretation uncertainty. We use the same 3D density contrast model as (Giraud et al., 2017), which is obtained by populating the structural framework of (Pakyuz-Charrier et al., 2018b). We simulate a series of PGM sought to represent expected values as well as possible extreme scenarii. The short presentation of the model below and the analysis of results provides essential information about the synthetic survey and shows the proof of concept of the methodology used in the paper.

3.1 Survey setup

The 3D unperturbed reference geological model was generated from contact (interface points) and surface orientation (foliations) field measurements collected in the Mansfield area (Victoria, Australia). It presents a Carboniferous mudstone-sandstone basin oriented N170, abutting a faulted contact with a folded ultramafic basement to the South-West. Model complexity was artificially increased through the addition of a North-South fault and of a mafic intrusion.

The true density contrast model (Figure 1a) was obtained assigning density contrasts consistently with the structural setting of the reference geological model, assuming a flat topography. Density contrasts of 0 and 100 kg.m⁻³ were assigned to the upper and lower basin lithotypes, respectively. Mafic rocks were assigned a density contrast of 200 kg.m⁻³ while the density contrast of the ultramafic basement was set to 300 kg.m⁻³.

25 MCUE perturbations of the reference geological model were first performed using standard measurement uncertainty values recommended by metrological studies as reported by (Allmendinger et al., 2017; Novakova and Pavlis, 2017). We generated a series of 300 models that were subsequently combined into a PGM. The resulting volume representing the W_H values calculated from this PGM in each cell of the model as per Eq. (3) is shown in Figure 1b.

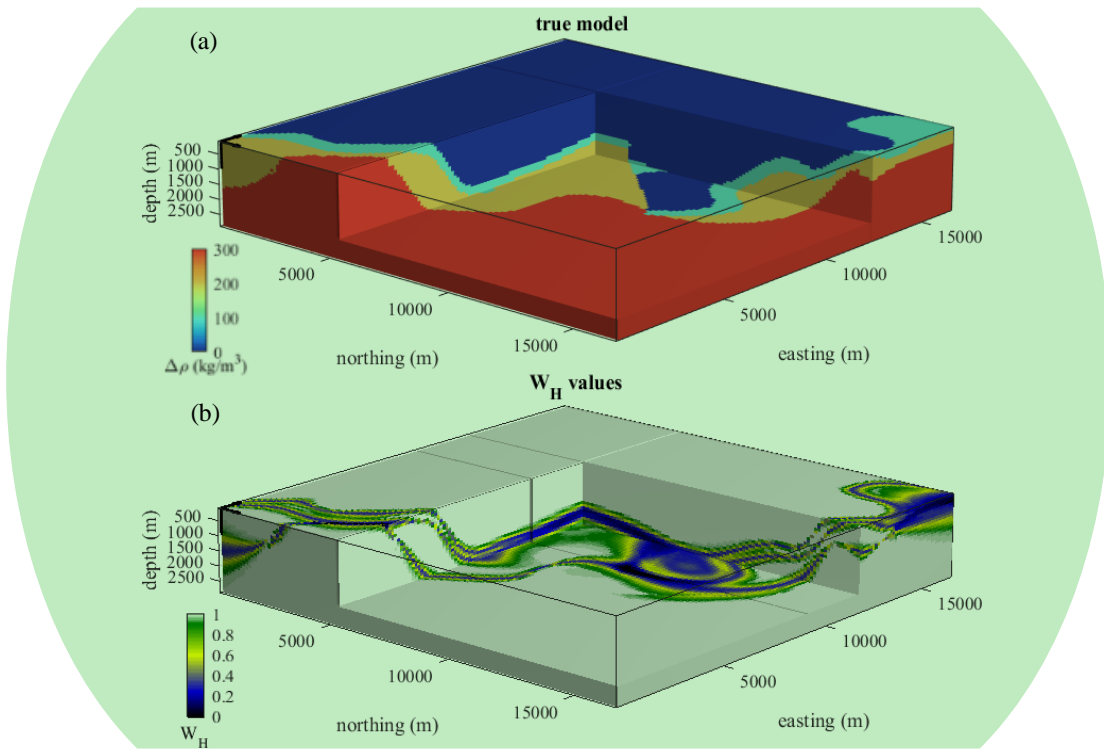


Figure 1. True density contrast model and W_H values used for local regularization conditioning. (a) Unperturbed reference model populated with density contrast values, (b) uncertainty values used for local regularization conditioning.

3.2 Locally constrained inversion: validation

- 5 To assess the impact of local conditioning of the regularization function onto inversion, we compare inversions using non-conditioned (Figure 2a) and locally conditioned (Figure 2b) regularization function, respectively. Please note that, simulating the absence of prior petrophysical information, a homogenous prior model set to 0 kg.m^{-3} was used in both cases.

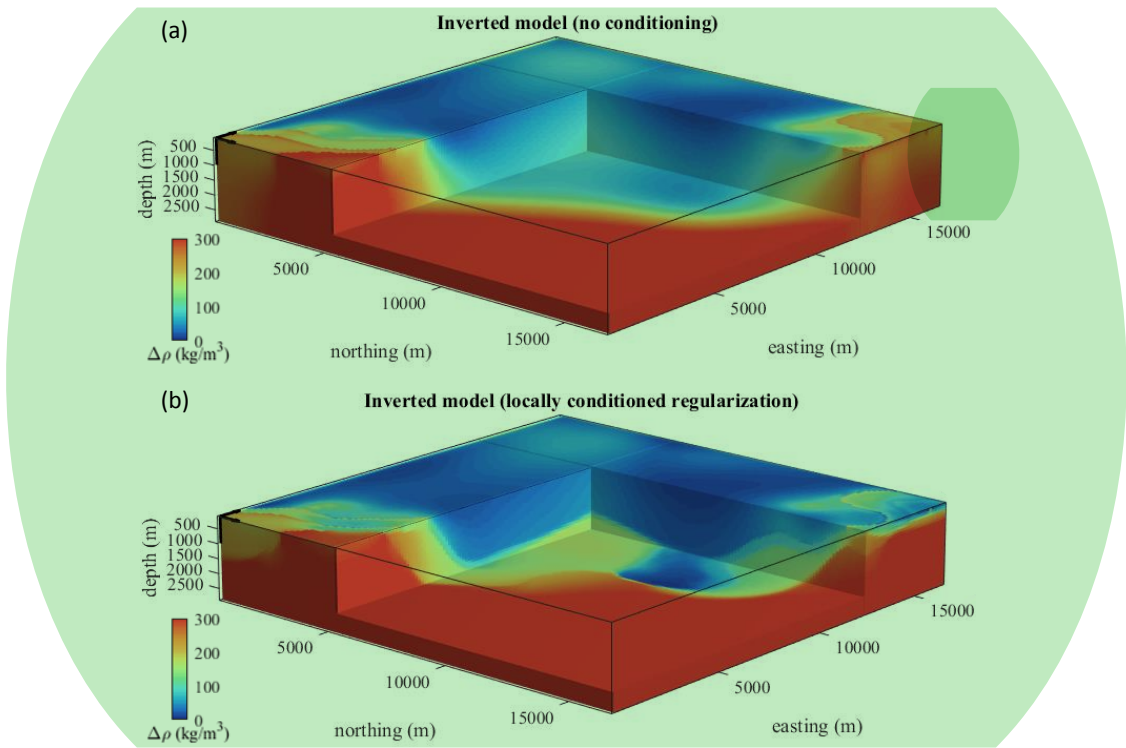


Figure 2. Comparison of inversion results. (a) Inverted models with non-conditioned regularization weights, and (b) using local conditioning.

Besides qualitative visual comparison of the models, we interpret inversion results (Figure 2) through the commonly used model and data root-mean-square error (RMSE), which correspond to the model and data terms calculated with weights and covariances set to unity. We evaluate the geometrical similarity between inverted and true model through the Bravais-Pearson correlation (also often called ‘linear correlation coefficient’) between their gradients (Table 1).

Comparison of the true model (Figure 1a) with inversion results in Figure 2a and Figure 2b shows that while the structures in shallowest part of the model are well retrieved in both cases, it appears that they are considerably better recovered through usage of conditioned regularization overall (Figure 2b). The guiding effect of W_H is visible in Figure 2b where the main structures at depth follow the general features of the conditioning volume (Figure 1b). Moreover, in order to minimize the conditioned regularization constraint simultaneously to data misfit, inversion was driven to accommodate inverted model values (Figure 2b) such that they are closer to the causative model (Figure 1a) than without conditioning (Figure 2a). This leads to reduced model RMSE on the one hand, and data RMSE on the other (Table 1). This reduction in data RMSE can also be explained by the relaxation of the constraints in several portions of the model, thus increasing the degree of liberty to accommodate the model towards lower data misfit. More importantly, the Bravais-Pearson correlation between the inverted and true model gradients is much higher when information from information entropy is used. This indicates that local

conditioning of the regularization function also allows for significantly better retrieval of the causative bodies' (e.g., the true model) structural features.

Please also note that we do not show the recovered geophysical measurements because visual differences between recovered and inverted measurements are minimal.

5

Table 1. Indicators for comparison of inversion results in terms of model, data, and structure.

	<i>Model RMSE (kg.m⁻³)</i>	<i>Data RMSE (m.s⁻²)</i>	<i>Correlation between gradients</i>
<i>Non-conditioned regularization</i>	74.66	2.38×10^{-9}	0.18
<i>Locally conditioned regularization</i>	53.05	7.44×10^{-10}	0.53

From these observations, we conclude that the application of the local conditioning scheme can fulfil the objectives of data integration in inversion as it allows inversion to recover models that are closer to the causative bodies and easier to interpret, while honouring geophysical data. Nevertheless, it remains important to test the methodology in cases where the uncertainty indicator W_H is biased and/or shows high geological uncertainty levels away from faults and contacts. A thorough analysis lying beyond the scope of this paper, the remainder of this section presents an elementary sensitivity analysis using a series of two W_H volumes representing distinct extreme scenarios.

10

3.3 Inversion constrained by biased geological uncertainty model

In this subsection, we investigate the effect of inaccurate geological models and the propagation of the related uncertainty in inversion. For this purpose, we calculate a second PGM from MCUE perturbations in which we split the ultramafic basement into two independent units, without changing the density contrast values (Figure 3a). This results in the existence of a fictitious geological unit that is invisible to gravity data and presents no density contrast but which increases geological complexity and uncertainty (Figure 3b) (we further refer to it as 'ghost' geological unit). Notably, it increases geological uncertainty and smears interfaces that are well-constrained as per Figure 1. It also decreases W_H in large parts of the model where $W_H \rightarrow 1$ previously, thereby favouring model changes in these areas during inversion and encouraging it to place larger density contrast or interfaces in these areas.

20

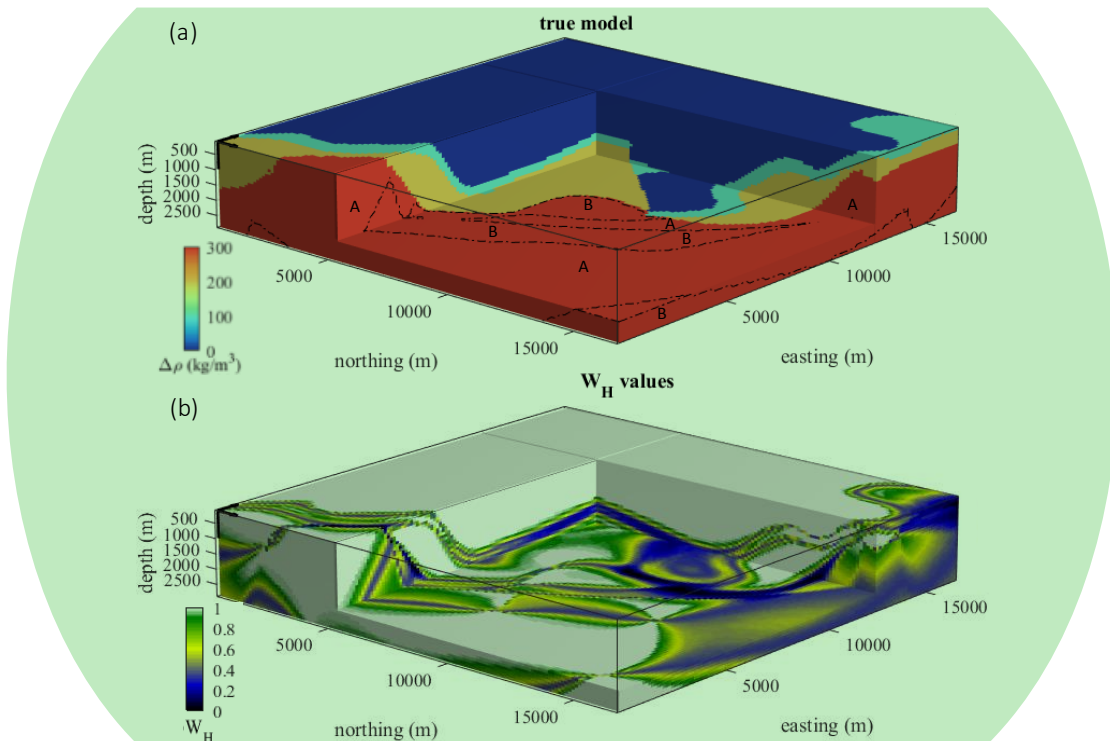


Figure 3. (a) true density contrast model with outline of the ‘ghost’ unit B (black dashed line), embedded in ultramafic unit A, and (b) local weights calculated from the PGM calculated using MCUE for model (a).

- 5 Comparison of the inverted models obtained without (Figure 4a) and with the ghost unit (Figure 4b) reveals that they exhibit broadly similar features except in the most geologically complex parts of the model as per Figure 1b, where differences are minor. This indicates that while geophysical inversion updates the prior density contrast model preferably in geologically uncertain regions, low values of W_H do not necessarily lead to the modelling of an interpretable interface by inversion. From the comparison of Figure 3b and Figure 4b, we can deduce that local conditioning as applied in this work does not necessarily
- 10 enforce strict structural similarity between the inverted model and the conditioning geological uncertainty volume.

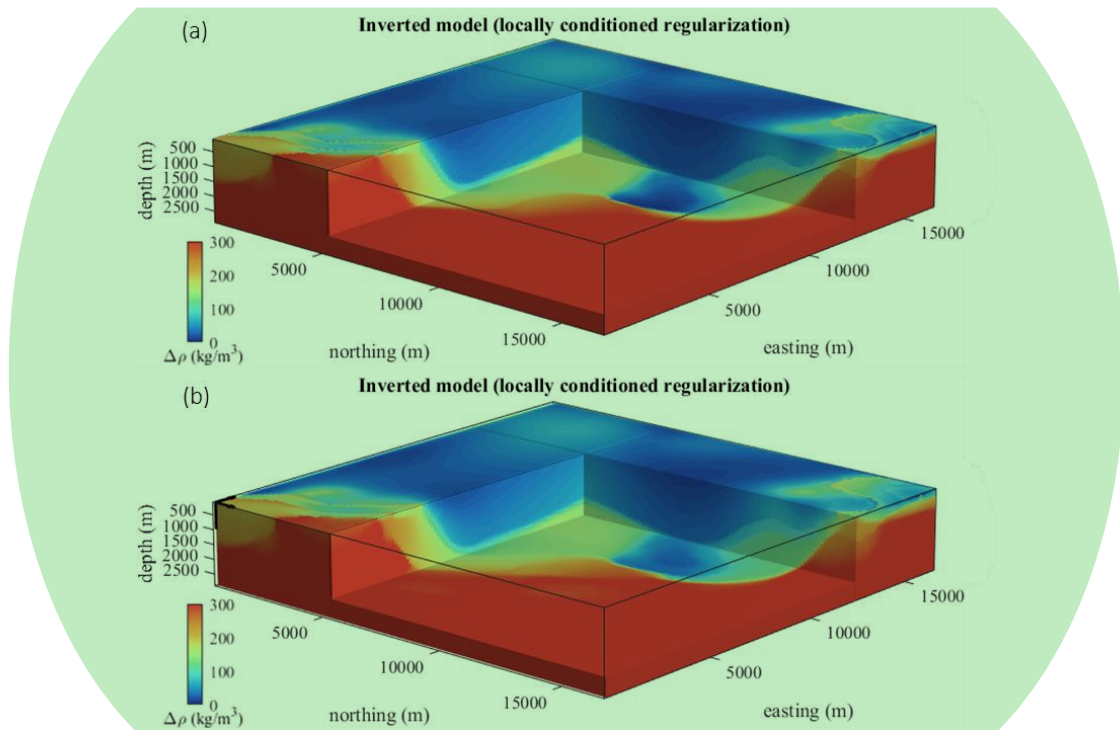


Figure 4. Comparison of inverted model using W_H derived from a PGM considering the ghost unit (b) and without it (a); (a) is the inverse model obtained without bias in the PGM as per Figure 2 and is shown here for comparison with (b).

3.4 Inversion constrained using exaggerated geological uncertainty

- 5 To complete this series of tests, we generated a third PGM showing exaggerated geological uncertainty. To this end, we used a half aperture 95% confidence interval of ~ 50 degrees for orientation data measurements in our MCUE simulations. This is far higher than for the rest of the MCUE simulations used in this paper. All other simulations (Subsect. 3.2 and 3.3) use a value of ~ 11 degrees, which is representative of realistic measurement uncertainty as proposed by recent metrological studies (Allmendinger et al., 2017; Cawood et al., 2017; Novakova and Pavlis, 2017). Figure 5 below shows the resulting W_H volume
- 10 (Figure 5a) and the inverted model obtained using it for local conditioning of the regularization constraint (Figure 5b).

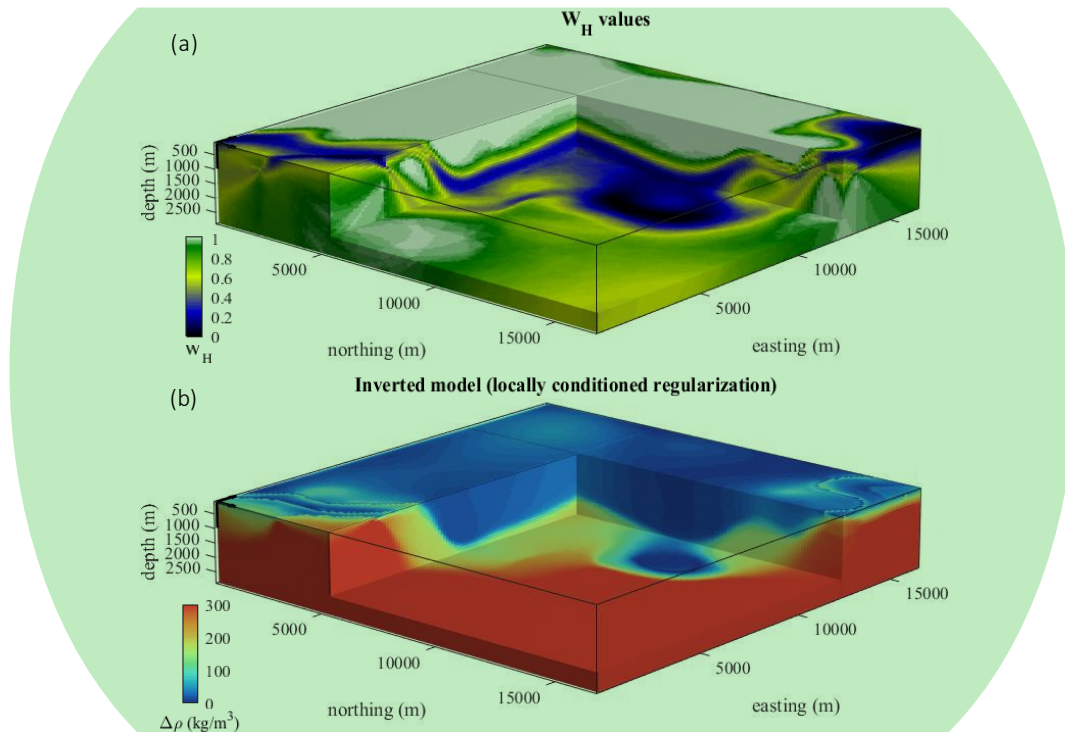


Figure 5. (a) Local weights W_H calculated from a PGM corresponding to exaggerated uncertainty in geological input measurements and (b) corresponding inverted density contrast model.

5 The features visible in Figure 5a reflect the high geological input measurement uncertainty. Geologically uncertain areas cover large portions of the volume and only the simplest geological structures (e.g., the basin) seem to be well constrained by geology. Areas of the model previously well constrained (Figure 1b) present varying degrees of uncertainty. This illustrates that, as can be expected, increasing geological input uncertainty translates in relaxing the guiding effect of local conditioning using W_H , which results in geophysical inversion being less strongly guided by geological information. As can be seen in Fig 10 4b, the inverted model obtained in this case shows structures that present weaker contrast around interfaces than when geological uncertainty is lower (Figure 2b). Importantly, however, most structures are well preserved and the overall model values for the different lithologies remain closer to the true model than for the non-conditioned case (Figure 2a). This indicates that even in high geological uncertainty scenarios, interpretation outcome may be largely more reliable when local regularisation is used.

15

The analysis and comparison of the results shown in this section demonstrates the potential of the proposed inverse modelling scheme to ameliorate inversion results and to reduce interpretation uncertainty. It also illustrates the capability of our methodology to deal with high or biased conditioning uncertainty estimates. In this synthetic case, local conditioning allows

geophysical inversion to significantly improve the imaging of geologically uncertain areas and to exploit complementarities between geological modelling and geophysical inversion. From the success of this proof of concept study, we are confident that our integration method can be tested here using real world data for field validation.

4 Field validation: Yerrida Basin case study

5 4.1 Geological context and geophysical survey setup

The Yerrida Basin is located in the southern part of the Capricorn Orogen, at the northern margin of the Yilgarn Craton in Western Australia (Figure 6a), and extends approximately 150km N-S and 180 km E-W (Figure 6b). The studied area is bounded in the northwest by the Goodin Fault, which represents a faulted contact between the Yerrida Basin and the Bryah-Padbury Basin. The structures of interest in this work are the Archean greenstone belts extending north-northwest that are unconformably overlain by Paleoproterozoic sedimentary rocks that form the Yerrida Basin. Features A and B (Figure 6a and Figure 6b) indicate the interpreted position of buried Wiluna Greenstone Belt. Where the Wiluna Greenstone Belt is exposed, it is host to base and precious metal mineralisation (Williams, 2009). With a relatively high positive density contrast (expected to be between 190 and 270 kg.m⁻³) to the Yilgarn Craton granite-gneiss host, mafic greenstone belts A, B, and C are suitable targets for gravity inversion. Interpretations from multiple studies in the region, e.g. (Johnson et al., 2013; Pirajno et al., 1998; Pirajno and Adamides, 2000; Pirajno and Occhipinti, 2000) were compiled while additional geological measurements acquired in 2015, 2016 and 2017 complemented legacy data (Occhipinti et al., 2017; Olierook et al., 2018). This allowed the revision of existing models and improved our understanding of the area. This, in turn, also highlights the challenges presented by the characterization of greenstone belts A, B and C, and that further geophysical analysis through constrained inversion is a useful pathway for reducing exploration risk.

20 Geophysical data consists of ground surveys obtained from Geoscience Australia (<http://www.ga.gov.au/data-pubs>). Post-processing includes spherical-cap and terrain corrections and the removal of the regional trend to obtain the complete Bouguer anomaly. As most data points were acquired 1 to 4 km apart, the dataset was resampled to match the geological model discretization, making up a total of 4882 measurement points. The model is discretized into 100 × 100 × 42 cells of dimensions 2.335 km × 1.875 km × 1.0475 km, down to a depth of 44 km, making up a total of 420000 cells.

25

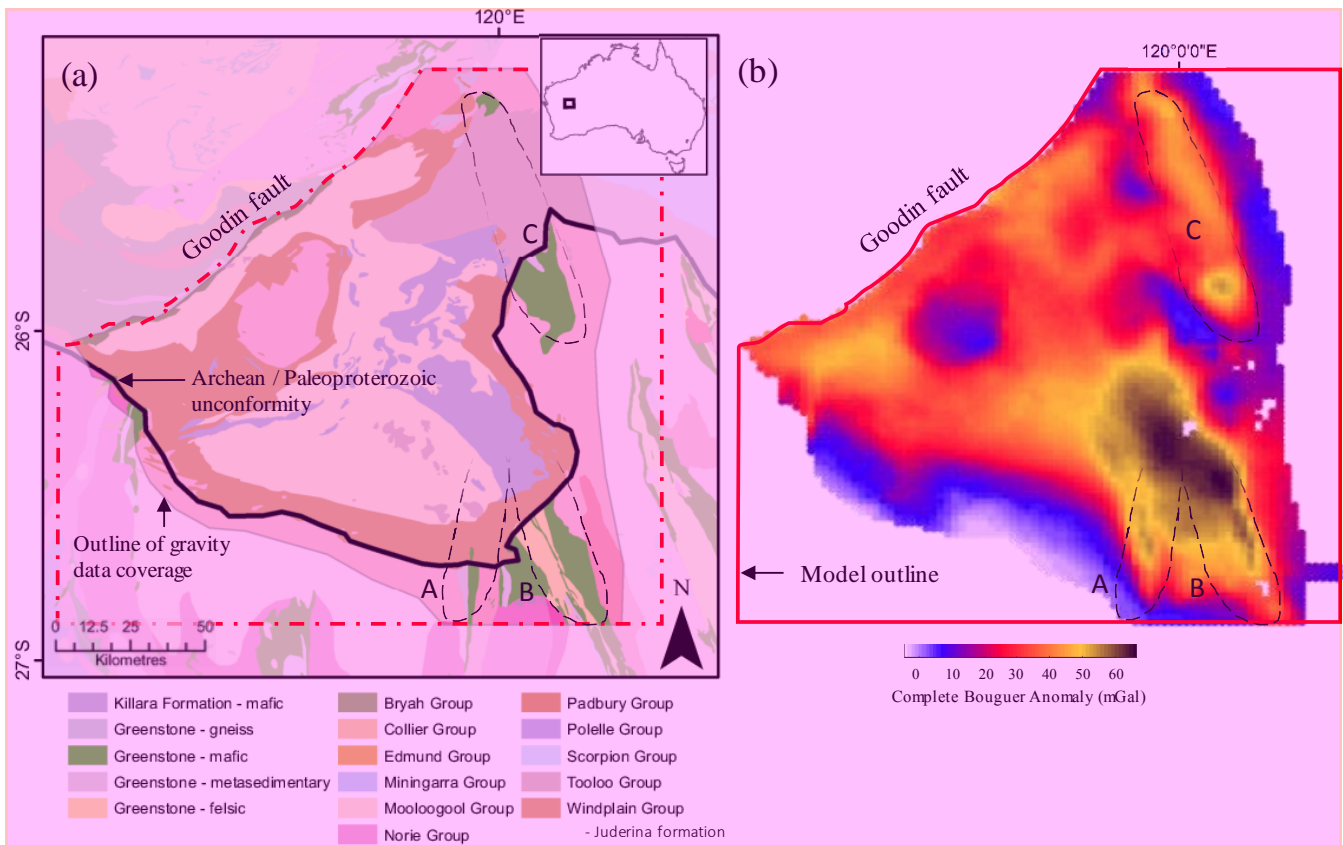


Figure 6. Geological context and geophysical data. (a) Geological map of the area and (b) complete Bouguer anomaly. The dashed lines delineate the possible sub-basin extent of the mafic greenstone belts A, B and C.

5 4.2 Geological modelling

Geological information consists of in-situ structural measurements (interfaces and foliations) and interpretation of aeromagnetic, airborne electromagnetic, Landsat 8 and ASTER hyperspectral data. Legacy data from the Geological Survey of Western Australia (Pirajno and Adamides, 2000) and CSIRO (Ley-Cooper et al., 2017) were used, to which about 600 surface geological and petrophysical measurements from recent geological field campaigns were added. Although the available petrophysical measurements were not used to derive petrophysical constraints because of the insufficient sampling of several of the modelled lithologies, they were a useful source of information to populate geological models and for interpretation. Remote-sensing data were used to test interpretations.

These datasets were used jointly to build a reference geological model reconciling the available geological information in Geomodeller.

Lithologies with similar density contrasts were merged and subsequently treated as a single rock type in MCUE simulations. Uncertainty related to structural measurements was subsequently used as inputs to the MCUE perturbations (Pakyuz-Charrier et al., 2018b) of the reference model to generate a collection of 500 accepted models. Information extracted from the PGM is displayed in Figure 7. Figure 7a shows the lithologies with the highest probability for each cell of the PGM. The associated W_H values used in inversion are shown in Figure 7b. The prior model for inversion m_p is equal to the mean model of the 500 plausible models generated by MCUE. It is shown in Figure 7c.

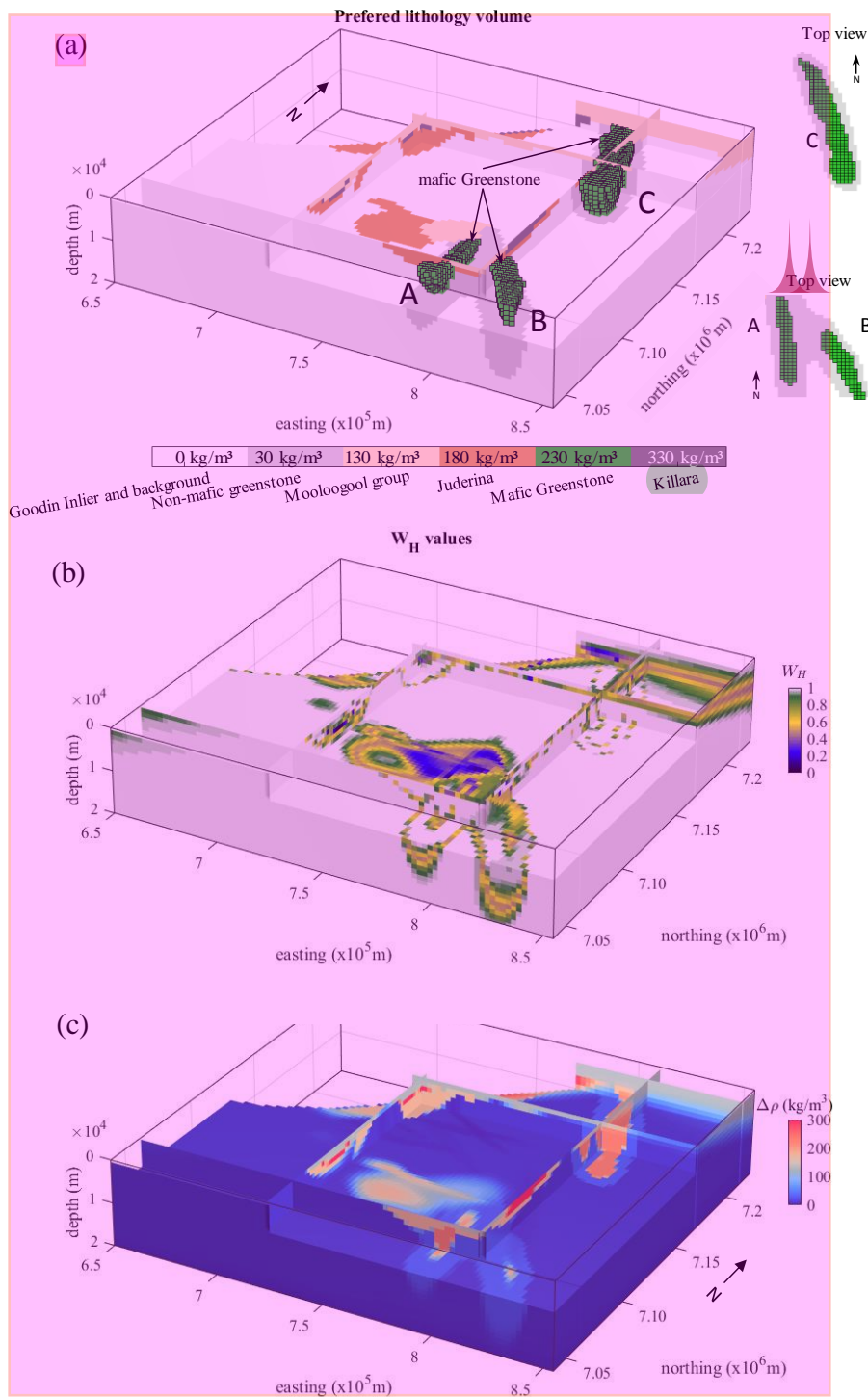


Figure 7. Geological modelling results. (a) Most probable lithology in each model cell (same colour code as in Figure 6) (b) values used for local regularization conditioning, (c) and prior model derived from PGM and prior petrophysical information). In (a), “background” refers to all the lithologies that have a density contrast equal to 0 kg/m^3 .

4.3 Inversion results and analysis

The aim of our analysis is to assess the influence of the local conditioning of structural constraints on inversion through comparison with the non-conditioned case, all other things remaining constant.

4.3.1 Comparative analysis strategy

5 Prior to examination of the inverted models, we analyse geophysical data misfit after inversion. This enables us to ensure that the inversion results we compare produce, in our case, similar gravity anomalies. Our study of inverted models focuses on results obtained through usage of non-conditioned (Figure 8a) and conditioned regularization function (Figure 8b) using W_H (Figure 7b). In addition to departures from the prior model, variations between the two cases are studied by visual comparison of Figure 8a and Figure 7b, through qualitative (Figure 7c) and quantitative comparative analysis (Figure 7d-e). Our
10 interpretation of inversion results is complemented by metrics quantifying the differences between models. We give particular attention to model cells where the probability of mafic greenstone is larger than zero. For these cells, we classify lithologies by identifying cells with a density contrast corresponding to mafic greenstone.

4.3.2 Results

Data root-mean-square (RMS) error decreases during inversion from 12.46 mGal to reach 1.59 mGal and 1.53 mGal for the
15 non-conditioned and conditioned cases, respectively. The corresponding data misfit maps show a linear correlation coefficient of 0.999 (see details in Appendix A). This similarity illustrates that, as in many other studies, most changes related to holistic data integration in geophysical inversion occur primarily in model space, hence reducing the effect of non-uniqueness (Abtahi et al., 2016; Abubakar et al., 2012; Brown et al., 2012; Demirel and Candansayar, 2017; Gallardo et al., 2012; Gallardo and Meju, 2004, 2007, 2011; Gao et al., 2012; Giraud et al., 2017; Guo et al., 2017; Heincke et al., 2017; Jardani et al., 2013;
20 Juhojuntti and Kamm, 2015; Kalscheuer et al., 2015; Molodtsov et al., 2013; Moorkamp et al., 2013; Rittgers et al., 2016; Sun and Li, 2016, 2017).

Qualitatively, comparison of Figure 8a and Figure 8b reveals that departures from the prior model (Figure 7c) are more significant in the most geologically uncertain areas. Quantitatively, the RMS model update for cells characterized by $0 \leq W_H < 0.05$ (most uncertain group) is equal to 40.1 kg/m^3 and 51.5 kg/m^3 , for the non-conditioned and conditioned cases,
25 respectively, whereas the same quantities are equal to 17.7 kg/m^3 and 16.9 kg/m^3 for the cells identified by $0.95 < W_H \leq 1$ (most certain group). This suggests that local regularization conditioning allows inversion to update the model preferentially in geologically uncertain areas. In turn, differences with the prior model in more geologically certain areas are reduced compared to the non-conditioned case. This effect of conditioning is corroborated by Figure 8c where the longest distances to the dashed line, which represents equal model update for the two studied cases, occur in geologically uncertain areas. This also
30 translates in higher difference between model updates of the two cases in Figure 7d for lower values of W_H . In addition, we

observe that local conditioning produces stronger density contrasts in Figure 8b in some of the areas where the conditioning values are higher in Figure 8b. Furthermore, structures in the inverted model are easier to identify when local conditioning is used. It is confirmed by global roughness measures $\|\nabla\mathbf{m}\|_2$ equal to $3.4 (kg/m^3)/m$ and $4 (kg/m^3)/m$ for the non-conditioned and conditioned cases, respectively. More specifically, as shown by Figure 7e, this difference arise in parts of the model associated with lower W_H , which characterize uncertain areas, including interfaces between lithologies.

The recovered greenstone belts are shown in Figure 8a and Figure 8b. In Figure 8b, the extension of recovered mafic greenstone belts is significantly different than when geological uncertainty is not accounted for (Figure 8a). In particular, belt A is significantly larger in Figure 8b than in Figure 8a ($2.4 \times 10^2 \text{ km}^3$ vs $4.6 \times 10^2 \text{ km}^3$). Similarly, the extent of belt C is increased overall (volume of $5.3 \times 10^2 \text{ km}^3$ vs $14 \times 10^2 \text{ km}^3$), while its different portions reconnect; the northern half is also significantly shallower and broader than in Figure 7a and Figure 8a. It appears that belt A remains thinner and shallower (Figure 8b) than suggested by the preferred lithology volume (Figure 7a). While similar geometries for belt B are recovered in Figure 8a and Figure 8b, they both differ from Figure 7a as only the eastern part is preserved. Note that it is larger in Figure 8b, with a volume 40% higher than in Figure 8a. As discussed in the next subsection, these differences have a signification impact on the interpretation of inversions results and are important to understand the influence of local conditioning on inversion.

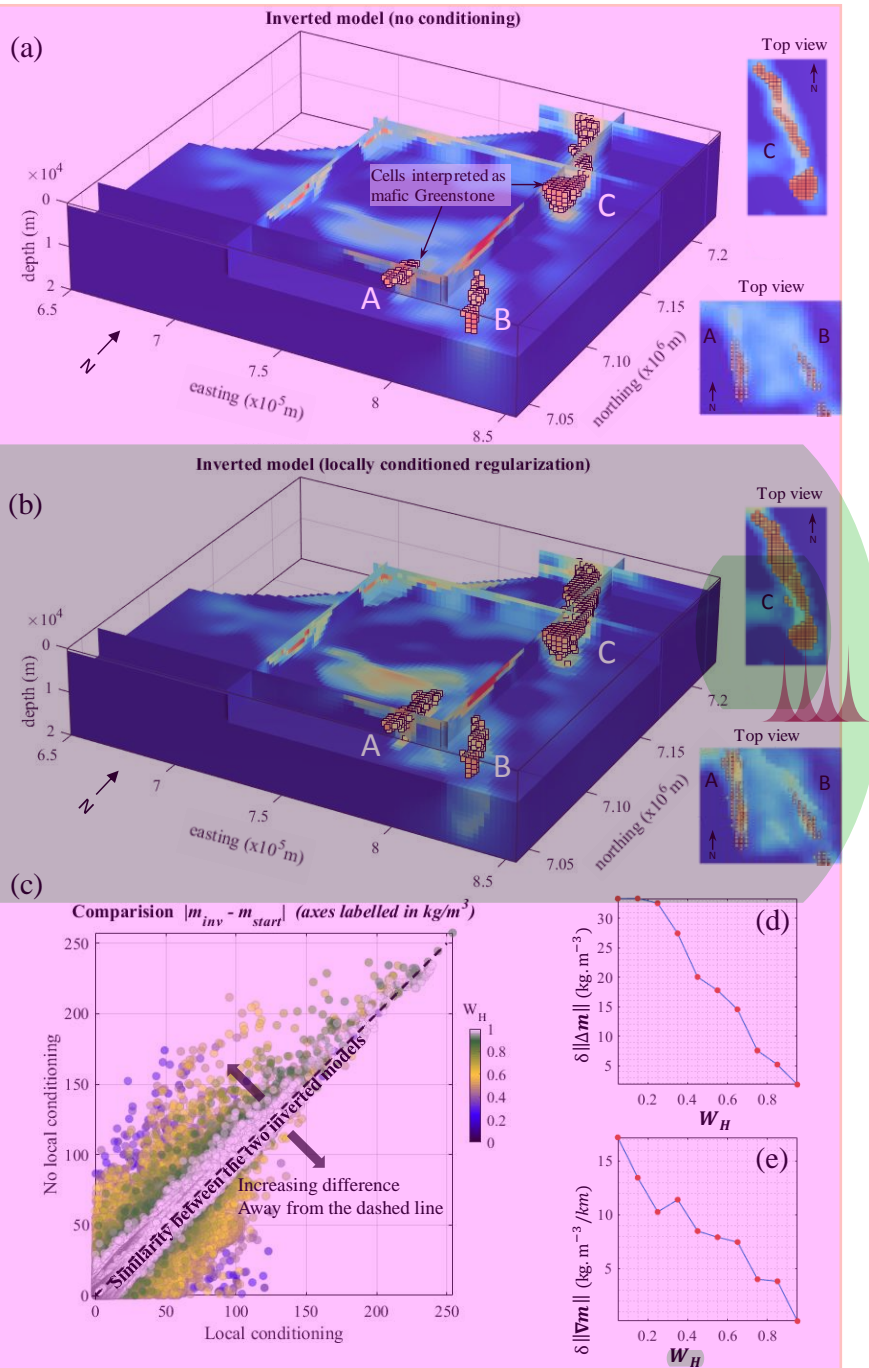


Figure 8. Comparison of inversion results. (a) inverted models with non-conditioned regularization weights, and (b) using local conditioning. (c) cross-plot between the corresponding absolute value of the update of the prior model, (d) difference in model updates $\delta \|\Delta m\| = \|m_{cond} - m_{nocond}\|_2$ as a function of values of W_H and (e) difference in model roughness $\delta \|\nabla m\| = \|\nabla m_{cond}\|_2 - \|\nabla m_{nocond}\|_2$ as a function of values of W_H . The model cells labelled A, B and C are interpreted as mafic greenstone belts. All voxels are coloured as a function of density contrast.

4.4 Interpretation

Note that, in contrast to the differences between inversion results highlighted above for belts A and C, there are only small differences between the inverted models in the north-eastern part of the model and the different interpretations of belt B (Figure 7a and Figure 7b). This shows that locally conditioned regularization does not enforce changes in the inverted model everywhere geological uncertainty is high as uncertainty is only a reflection of potential errors. Rather, this indicates that in such cases, the guiding effect of such regularization will be exerted on the condition that it does not prevent the data term in $\theta(\mathbf{d}, \mathbf{m})$ as per Eq. (1) from decreasing. This also confirms that geophysical data is the main driver of the model updates in geologically uncertain areas. Instead of smooth departures from the prior model to match geophysical data regardless of geological considerations, local regularization constraints allow inversion to account for the probabilistic geological modelling of the area and for geological uncertainty. It can therefore provide results that conform better to known geology. In consequence, by confronting a probabilistic geological model encapsulating all MCUE realizations with geophysical measurements in an inversion scheme favouring model updates in the most geologically uncertain areas, inversion complements probabilistic geological modelling in that it guides and refines the interpretation of other geoscientific data in the area.

Geophysical inversion using geological uncertainty information (Figure 7b) confirms the presence of high density anomalies that we interpret to be the mafic components of the greenstone as suggested by MCUE in several portions of the model. It also adjusts the outline and geometry of belts A, B and C to obtain a model honouring geological uncertainty information. In particular, mafic greenstone belts A and B may be smaller than the extent suggested by the PGM, and mafic greenstone C shallower than anticipated. The interpretation of inversion results also reveal that greenstone B might extend further to the east than indicated by the preferred lithology volume (Figure 7a) and that greenstone C may be thinner in its central part.

5 Concluding remarks

We have introduced a new integration scheme for the inversion of gravity data that utilizes a measure of geological uncertainty to calculate locally-conditioned gradient regularization constraints. This approach enables the integration of probabilistic geological modeling in geophysical inversion in the absence of petrophysical information sufficient to the calculation of petrophysical constraints. It uses geophysical measurements to optimize the inverse problem by updating the physical property model preferably in geologically uncertain parts of the studied area during what we called *uncertainty-guided inversion*. This therefore partly mitigates the non-uniqueness of the inversion through the addition of constraints encouraging inversion to produce models that account for geological uncertainty across the entire inverted volume. We have demonstrated that it can be used collaboratively with geological modelling efficiently through field application in the Yerrida Basin. Inversion results show that our integration methodology has the capability to refine the recovered physical property model and interpretations in portions of the model where geological uncertainty is high. Another advantage of the proposed technique is that it is time

and cost-effective as our workflow utilizes the PGM resulting from standalone probabilistic geological modelling and requires the same parameterization as non-conditioned inversion.

In the Yerrida Basin study area, application of the proposed methodology provided the effective delineation of the greenstone belts by quantitatively integrating geological measurements and geophysical data. Our findings suggest that some of the greenstone belts covered by the basin might be shallower than previously anticipated and occupy smaller volumes. This is particularly pronounced in the North-East (belt C) where the resulting model is in agreement with the shallowest cases allowed by the PGM. Likewise, in the South (belt A), only the shallowest part of the mafic greenstone body can be resolved, while the south-eastern (belt B) greenstone belt appears to be limited in extension to the eastern part of the volume where it is the preferred lithology in the PGM. In such cases, this can also indicate that these greenstone bodies might be too thin to be imaged by gravity data. These results have implications for our knowledge of the southern Capricorn Orogen as they indicate reduced (compared to the preferred lithology volume) mafic greenstone volumes under the Yerrida Basin on one hand, and decreased cover thickness on the other hand, thereby opening the door to updates in the geological interpretation of geometry of the Yerrida Basin and potential new undercover exploration prospects.

The quantitative integration technique we presented reduces uncertainty and ambiguity compared to qualitative interpretation technique or single-discipline workflows. However, despite its robustness to misplaced interface (e.g., bias) or to high geological uncertainty (e.g., sparse or very uncertain geological input measurements) as shown in the synthetic case, interpreters need to bear in mind the specificities of the geophysical data inverted for (resolution of specific geometries, depth of investigation) and the shortcomings of geological modelling workflows. As for all geological modelling, MCUE is oblivious to geological units or faults that are not sampled by field geological measurements, which can lead to biases in final models due to, for instance, inclusions not being accounted for.

Current research comprises the development of sensitivity and resolution analyses in an effort to mitigate the risk of the model being affected by uncertainty sources not accounted for. Future research will include the utilization of local petrophysical constraints of (Giraud et al., 2017) in the uncertainty-guided inversion scheme we presented, as well as the utilisation of geological uncertainty to weight the cross-gradient term of (Gallardo and Meju, 2003) locally. With this last respect, uncertainty-guided inversion can be assisted in the most uncertain parts of the model by guided inversion (in the sense of Brown et al., 2012) or through cross-gradient joint inversion.

Code and data availability. True property models, inversion results and recovered models relating to the Yerrida Basin shown in this article are made available online: Jeremie Giraud, Mark Lindsay, and Vitaliy Ogarko, 2018, Yerrida Basin Geophysical Modeling - Input data and inverted models. (Version version 1.0) [Data set]. Zenodo. <http://doi.org/10.5281/zenodo.1238216>. True property models, inversion results and recovered models relating to the synthetic case from the Mansfield area shown in this article are made available online: Jeremie Giraud, Vitaliy Ogarko, and Evren Pakyuz-Charrier, 2018, Synthetic dataset for

the testing of local conditioning of regularization function using geological uncertainty. (Version version 1.0) [Data set]. Zenodo. <http://doi.org/10.5281/zenodo.1238529>

Appendix A: Data misfit maps from inversion in the Yerrida Basin

Figure A below relates to the analysis of data misfit in Sect. 4 of the article through the plot of the data misfit maps for the non-conditioned and conditioned cases (Fig. Ad and Fig. Ah, respectively). It is complemented by the corresponding plots of starting (Fig. Aa and Fig. Ae), observed (Fig. Ab and Fig. Af), and calculated data (Fig. Ac and Fig. Ah). Note that Fig. Ac and Fig. Ag show little visual differences, and that Fig. Ad and Fig. Ah exhibit similar features while showing limited coherent signal.

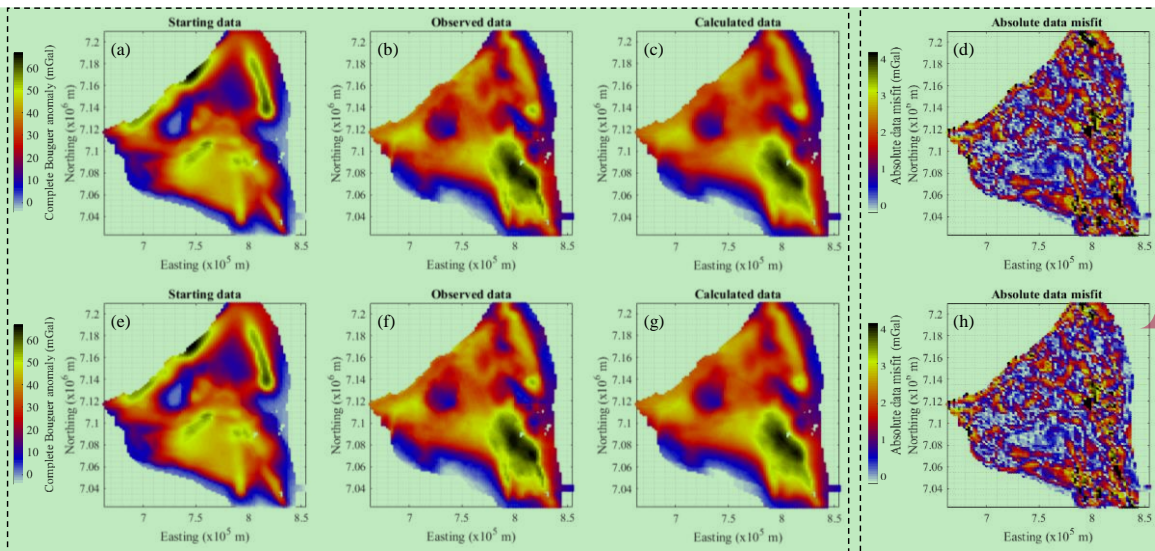


Figure A. Comparison of input and output geophysical data. (a) and (e) show data calculated from the prior model, (b) and (f) input measurements, (c) and (g) data calculated from the inverted model, and (d) and (f) the absolute value of the difference of the misfit between the observed and calculated data. (a)-(d) (i.e., first line) and (e)-(h) (i.e., second line) correspond to the non-conditioned and conditioned cases, respectively.

15 **Authors contribution.** Jeremie Giraud performed the integrated inverse modelling of geophysical data for both the Mansfield synthetic study and the Yerrida Basin. He performed posterior analysis and interpretation of results and he is the main contributor to the writing of this article. Mark Lindsay acquired part of the geological field measurements from the Yerrida Basin and performed the geological modelling of the area. He participated in the writing of the geological setting subsection and he produced the geological map shown in Figure 6a. Vitaliy Ogarko and Jeremie Giraud worked together on the implementation and testing of the proposed methodology in Tomofast-x, of which Vitaliy Ogarko, Roland Martin and Jeremie Giraud are the main developers. Mark Jessell has been involved in the validation of the methodology at the initial development

stage and supervised the progress of the presented work. Roland Martin provided support at the initial stage of the inversion of gravity data from the Yerrida Basin. Evren Pakyuz-Charrier assisted Mark Lindsay with the utilisation of MCUE. All co-authors contributed to the final version of this article. Mark Lindsay and Vitaliy Ogarko were the most actively involved in the revision process of the drafts leading to this paper.

5 *Competing interests.* The authors declare that they have no conflict of interest.

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