An automated fracture trace detection technique using the complex shearlet transform

Rahul Prabhakaran^{1,2}, Pierre-Olivier Bruna¹, Giovanni Bertotti¹, and David Smeulders² ¹Department of Geoscience and Engineering, Delft University of Technology, Delft, the Netherlands ²Department of Mechanical Engineering, Eindhoven University of Technology, the Netherlands **Correspondence:** Rahul Prabhakaran (r.prabhakaran@tudelft.nl / r.prabhakaran@tue.nl)

Abstract. Representing fractures explicitly using a discrete fracture network (DFN) approach is often necessary to model the complex physics that govern thermo-hydro-mechanical-chemical processes (THMC) in porous media. DFNs find applications in modelling geothermal heat recovery, hydrocarbon exploitation, and groundwater flow. It is advantageous to construct DFNs from photogrammetry of fractured outcrop analogues as the DFNs would capture realistic, fracture network properties. Recent

- 5 advances in drone photogrammetry have greatly simplified the process of acquiring outcrop images, and there is a remarkable increase in the volume of image data that can be routinely generated. However, manually digitizing fracture traces is tedious and inevitably subject to interpreter bias. Additionally, variations in interpretation style can result in different fracture network geometries, which, may then influence modelling results depending on the use-case of the fracture study. In this paper, an automated fracture trace detection technique is introduced. The method consists of ridge detection using the complex shearlet
- 10 transform coupled with post-processing algorithms that threshold, skeletonize, and vectorize fracture traces. The technique is applied to the task of automatic trace extraction at varying scales of rock discontinuities, ranging from 10^{0} - 10^{2} m. We present automatic trace extraction results from three different fractured outcrop settings. The results indicate that the automated approach enables extraction of fracture patterns at a volume beyond what is manually feasible. Comparative analysis of automatically extracted results with manual interpretations demonstrates that the method can eliminate the subjectivity that is
- 15 typically associated with manual interpretation. The proposed method augments the process of characterizing rock fractures from outcrops.

1 Introduction

NFR-Naturally fractured reservoir (NFR) modelling requires an explicit definition of fracture network geometry to accurately capture the effects of fractures on the overall reservoir behaviour. The National Research Council (1996) suggested the idea

20 of using geologically realistic outcrop fracture patterns to guide subsurface fracture modelling. In recent work, the use of deterministic DFNs discrete fracture networks (DFNs) based on trace digitization from photogrammetry of outcrop analogues was investigated by Bisdom et al. (2017) and Aljuboori et al. (2015) for reservoir fluid flow simulation and well testing. Outcrop derived DFNs encapsulate 2D fracture network properties at a scale that cannot be characterized using either standard surface approaches (scanlines and satellite imagery) or subsurface techniques (seismic imaging/borehole imagery/core sampling). Ukar et al. (2019) suggested a comprehensive set of protocols to select fractured outcrops that are representative of the subsurface. Stochastic and geomechanical DFNs are alternatives to outcrop derived DFNs for fractured reservoir modeling. Stochastically generated DFNs have the disadvantage that they cannot replicate the spatial organization of fracture network patterns observed in nature (Thovert et al., 2017). Geomechanically derived DFNs are based on the physics of fracture prop-

- 5 agation (for e.g. Olson et al., 2009; Thomas et al., 2018) and can reproduce realistic fracture patterns provided the complex paleostress field and paleo rock properties are known; however, they are also computationally intensive and hence have limited applicability. A carefully chosen fractured outcrop that is relatively free of noise (fractures resulting from exhumation and weathering and not too much hidden by vegetation) may be used to interpret realistic fracture networks which are geometrical inputs used in simulating various subsurface THMC thermo-hydro-mechanical-chemical (THMC) processes.
- 10

15

Recent advances in Unmanned Aerial Vehicles (UAVs) and stereo-photogrammetry has dramatically simplified the acquisition of georeferenced datasets of fractured outcrop images (for e.g. Bemis et al., 2014; Harwin and Lucieer, 2012; Turner et al., 2012). Photogrammetry using the Structure from Motion (SfM) principle is a relatively inexpensive and rapid technique by which 3D outcrop models are built by identifying, extracting, and positioning common points in georeferenced outcrop images (Donovan and Lebaron, 2009). Images are captured using a camera-equipped UAV that is capable of following pre-programmed flight missions where flight path, altitude, velocity, and overlap are specified. The images undergo further processing steps that include generating sparse point clouds of common points, aligning the images, generating dense point clouds (3D representation of outcrop geometry), and generating meshed surfaces (Bisdom et al., 2017). Interpreting fractures on the image orthomosaics with conventional Geographic Information System (GIS) software completes the outcrop-based DEE workform

20 DFN workflow.

Manually interpreting fractures is time-consuming and forms a bottleneck in an outcrop-based DFN workflow. A manual interpretation has a fair degree of associated subjectivity, and interpreter bias may take the form of specific scales of features being inadvertently omitted or deliberately ignored (Bond et al., 2007; Scheiber et al., 2015). Manual interpretation also suffers

- 25 from a lack of repeatability owing to the level of expertise of the interpreter, and the interpretation criteria followed (Hillier et al., 2015; Sander et al., 1997). Reproducibility may not be guaranteed even with the same interpreter in multiple trials (Mabee et al., 1994). According to Bond et al. (2015), quantifying the magnitude and impact of subjective uncertainty is difficult. Long et al. (2018) conducted a study on variability of fracture interpretation in which geologists with varying levels of expertise interpreted a single image. They found considerable variation in fracture topology, orientation, intensity, and length distributions
- 30 in the interpretations. Andrews et al. (2019) made a detailed quantification of subjective bias in scanlined-based fracture data collection and suggested protocols to manage bias. Another study by Peacock et al. (2019) delved into the reasons for bias and the resulting implications for modelling. Given the amount of data generated in short UAV flight missions, man-hours spent in interpretation, and the need to de-bias interpretation as much as possible, automatic feature detection techniques may be considered. Automated approaches can speed up the process, improve accuracy, and exploit the acquired data to the fullest

possible extent.

In this paper, we introduce an automated method to extract digitized fracture traces from images of fractured rocks. The method utilizes the complex shearlet transform measure to extract fracture ridge realizations from images. Post-processing im-

- 5 age analysis algorithms are coupled with the ridge extraction process to vectorize fracture traces in an automated manner. The complex shearlet transform was introduced by Reisenhofer, 2014; King et al., 2015 and Reisenhofer (2014) and King et al. (2015) and applied to problems such as detecting coastlines from Synthetic Aperture Radar (SAR) images (King et al., 2015) and propagating flame fronts from planar laser-induced fluorescence (PLIF) images (Reisenhofer et al., 2016). We present automatic fracture extraction results from drone images of two carbonate outcrops (Parmelan, France and Brejões, Brazil) and station
- 10 scale images of igneous dyke swarms.

2 Background

2.1 Review of Automated and Semi-Automated Fracture Detection Approaches

Rapid digitization of geological features from photogrammetry is challenging owing to issues like spatially varying image resolution, inadequate exposure, the presence of shadows due to effects of topography on illumination conditions, and chro-

- 15 matic variations of essential features. False positives are non-geological features (such as trees, shrubbery, and human-made structures) that are detected using semi-automated / automated approaches (Vasuki et al., 2014). Removal of false positives is time-consuming. On the other hand, essential features that are not detected at all (referred to as false negatives) by an algorithm, further complicates the task of automated feature extraction. Automated methods, in general, detect more features than what is present in the image (Abdullah et al., 2013). In this section, we review some approaches for automatic fracture detection based
- 20 on the class of algorithm used.

Automated fracture detection utilizing higher dimensional data such as point clouds, DEMs and DTMs digital elevation models (DEMs) and digital terrain models (DTMs) have an advantage in that depth variations are captured and can be used to extract features. Thiele et al. (2017) presented an approach based on a least cost function algorithm applicable to orthophotographs of jointed fracture sets and 3D point cloud data. Masoud and Koike (2017) introduced a software package to detect lineaments from composite grids derived from gravity, magnetic, DEMs, and satellite imagery. Bonetto et al. (2015) and Bonetto et al. (2017) presented semi-automatic approaches that extract lineaments from Digital Terrain Models DTMs utilizing the curvature of geological features. Hashim et al. (2013) presented an edge detection and line linking method using Enhanced Thematic Mapping (ETM).

Colorimetry of an image can be used to detect features. By partitioning features in the image, e.g., matrix rock as lighter shades of gray and fractures as darker shades of gray, fracture pixels may be extracted separately from matrix rock using pixel values. Vasuki et al. (2017) developed an interactive color based image segmentation tool using superpixels (Ren and Malik,

³⁰

2003) which are groupings of pixels that are perceptually similar.

Edge detection techniques identify points in images where sharp changes in image intensity occur. Some of commonly used edge detection techniques in image processing are Canny, Sobel, Prewitt, Robert, Kuwahara, and Laplacian of Gaussian filters.

- 5 Alternatively, edges may be detected using methods that are invariant to contrast and illumination in images. Phase symmetry and phase congruency algorithms (Kovesi, 1999, 2000) fall under this category. Phase symmetry is an edge detection technique that is invariant to local signal strength. The method works identifies the axis of a feature by isolating pixels symmetric along profiles that are sampled from all orientations except parallel to the feature. The axes of symmetry are regions where frequency components either approach a maximum or minimum. The phase congruency method is another edge detection method that
- 10 detects features by identifying points where Fourier components are maximally in phase. This approach is also invariant to the magnitude of the signal. The property of invariance enables the identification of structures within the image even in the presence of noise. Vasuki et al. (2014) utilized an edge detection algorithm using the phase congruency principle coupled with a multi-stage linking algorithm for detection of fault maps.
- The Hough transform (Duda and Hart, 1972) is another technique that has been used to detect lineaments in images. The Hough transform identifies pixels in binary images that are likely to represent rock fractures using a voting procedure. Each pixel in a binary image is represented as a sinusoidal curve in a 2D parametric space (or a Hough space). The voting procedure accumulates a vote for each curve in the parametric space corresponding to each non-zero pixel in the binary image. The curves with the highest votes are selected as probable fractures since they correspond to the largest number of non-zero pixels. Results
- 20 by Callatay (2016) using the Hough transform for fracture detection report the following limitations. Firstly, the detection is limited to a given fracture orientation set owing to the definition of the Hough transform parameter space. Secondly, the issues of false positive detection and discontinuities persisted. The method is also limited by the fact that it needs a binarized image to start.
- The development of wavelet theory in the field of harmonic analysis have led to applications in edge detection (Daubechies, 1992; Heil et al., 2006). Mallat and Hwang (1992) proposed wavelet-based approaches for edge detection. Wavelet-based methods differ from gradient-based edge detection methods that searches for local maxima of the absolute value of the gradient. Felsberg and Sommer (2001) introduced monogenic wavelets for the purpose. Tu et al. (2005) considered the use of magnitude response of complex wavelet transforms. Wavelets, owing to their isotropic properties, cannot extract curve-like features due
- 30 to the lack of directional information (Labate et al., 2005). A number of wavelet-based approaches that have been proposed to overcome this lack of directional information such as curvelets (Candès and Donoho, 2005), ridgelets (Candès and Guo, 2002), contourlets (Do and Vetterli, 2005), bandlets (Le Pennec and Mallat, 2005), wedgelets (Donoho, 1999), shearlets (Guo et al., 2005), and band-limited shearlets (Yi et al., 2009).

2.2 The Complex Shearlet Transform

Shearlets were introduced by Labate et al. (2005) as a new class of multidimensional representation systems to overcome the shortcoming of wavelets by applying dilation, shear transformation and translation operations to wavelet generating functions. Shearlets are hence very similar to wavelets except that isotropic dilation of wavelets is replaced with anisotropic dilation

5 and shearing(see Fig. A1a, Fig. A1b)... Shearlets have a number of properties that make them better suited to handle sparse, geometric features in multidimensional data compared to traditional wavelets (Kutyniok and Labate, 2012).

The complex shearlet transform is a complex-valued generalization of the shearlet transform that was developed by Labate et al. (2005) to handle geometric structures in 2D data. Reisenhofer (2014) and King et al. (2015) proposed the idea of creating

- 10 complex shearlets by modifying the shearlet construction so that real parts of the generating function are even-symmetric and imaginary parts of the generating function is odd-symmetric. They used the Hilbert transform to convert an even-symmetric function into an odd-symmetric function and vice versa. The complex shearlet measure for ridge and edge detection implemented in Reisenhofer (2014); King et al. (2015) and Reisenhofer et al. (2016) merged the ideas of phase congruency and complex shearlets.
- 15

The complex shearlet measure first introduced by Reisenhofer (2014) and improved by King et al. (2015) was used for applications like coastline detection King et al. (2015), flame front detection Reisenhofer et al. (2016), and feature extraction from terrestrial LIDAR inside tunnels Bolkas et al. (2018). Karbalaali et al. (2018) used the complex shearlet transform for channel edge detection from synthetic and real seismic slices. Reisenhofer et al. (2016) presented a comprehensive comparison

20 of CoShREM with Cannycomplex shearlet based feature detection compared with conventional edge detectors such as Canny (Canny, 1986), Sobel (Sobel and Feldman, 1973), Sobel, phase congruency (Kovesi, 1999), and another shearlet based edge detector Yi et al. (2009) (Yi et al., 2009). Bolkas et al. (2018) also makes made specific comparisons between the performance of Canny, Sobel, Prewitt (Prewitt, 1970) edge detection methods versus space-frequency transform methods such as wavelets, contourlets, and shearlets. A detailed overview of the complex shearlet transform is provided in Appendix. A for the interested reader.

3 Methods

3.1 The Automatic Detection Process

The automated fracture trace detection method that we present has five main steps (see Fig. 1). The first step of the method uses the Complex Shearlet-Based Ridge and Edge Measure (CoShREM), a MATLAB implementation by Reisenhofer et al. (2016).

30 The first step, namely the ridge detection, is dependent on a number of input parameters tabulated in Table 1 and Table 2. Equation (A28) gives the expression for the ridge measure. An optimal set of deterministic parameter values which can extract features on all scales is not known a priori. Therefore, we vary the input parameters corresponding to the construction of the shearlet system and the ridge detection parameters within user-defined ranges to compute multiple ridge realizations. A ridge ensemble map is obtained by superposing the ridge images and normalizing. A user-defined threshold is then applied to the intensity values of the normalized ride ensemble image to extract a highly probable, binarized, ridge network. The threshold is set by a visual comparison of the input image with the extracted ridges. The range for each parameter in Table 1 and Table 2

- 5 is ascertained by first testing the effect of variation of each parameter with respect to a chosen base case image. This approach to automated detection captures features of multiple scales and highlights regions of uncertain feature extraction within the image. An example of a fractured image and the effect of parameter variation on ridges that are detected is depicted in Fig.2. The sample represents Mesoproterozoic sandstone from the Tomkinson Province, Northern Territory, Australia.
- 10 The second step is the segmentation of the detected ridges using Otsu thresholding (Otsu, 1979). This operation removes small, disconnected, and isolated ridge pixel clusters. The third step is a skeletonization procedure where clusters of pixels representing the segmented ridges are thinned into single pixel representations. For intersecting fractures, the skeletonization procedure preserves the topology of the fracture network by recognizing and splitting the frame at the branch point. This step ensures that in subsequent DFN representation, there is no further effort expended in manually connecting the detected seg-15 ments.

The fourth step involves piecewise linear polyline fitting to the skeletonized clusters. By default, our code attempts to fit polylines rather than lines to the pixel clusters. Polyline fitting retains geologically realistic, veering and curvature of fractures in the vectorized result. The fifth step is a line simplification procedure applied to the piecewise linear polyline clusters. A large number of polyline points would increase the size of vectorized files; hence, we use the Douglas-Peucker line simplification algorithm (Douglas and Peucker, 1973). The algorithm simplifies a piecewise linear polyline into one which has fewer segments. The number of polyline points assigned to each skeletonized cluster is set constant in the code, but this may be modified to be a linear function of the cluster size measured in pixels. If the image is georeferenced or the image scale is known, the code georeferences the simplified polylines and writes to a vectorized shapefile format.

The DFN in the vectorized shapefile format may now be used for any application that requires explicit fracture network geometry. An example of a fractured Posidonia shale micro CT (computed tomography) image slice from Dwarkasing (2016) (see Fig. 3) illustrates the effects of each of the steps involved.

30 3.2 Shearlet parameter selection

To decide upon the shearlet parameter space to generate multiple ridge realizations, we chose one sample image (see Fig. 4a). Base case parameters are chosen based on recommendations underlined in Reisenhofer et al. (2016) for shearlet construction and ridge detection and these are tabulated in Table 3. The use of these results in the overlay depicted in Fig. 4b. As can be observed from visual inspection of the overlay of the detected ridges over the original image, the automatic method can extract

²⁵

a large number of fractures. However, there are still some false positives (features detected on the trees and inside the large karstic cavities) and false negatives (undetected small scale fractures).

To select the parameter ranges, we vary parameters with respect to the base case ridge image, thereby generating mul-5 tiple ridge images. We use the structural similarity measure (SSIM) (Wang et al., 2004) to quantify the difference between the base case ridge image and other ridge images. SSIM Structural similarity (SSIM) is a measure commonly used in image quality assessment that returns one value as a measure of similarity between two images, where one image is the reference image(Wang et al., 2004). The SSIM is calculated for each ridge realization image corresponding to each parameter with respect to the base case ridge image. The SSIM for variation in scaling offset, anisotropy scaling α , Mexican hat wavelet support

- 10 (Gaussian support scales with wavelet support), minimum contrast, scales per octave and number of shear levels are depicted in Fig. A3 according to the range of parameters in Table 4. From the analysis of the effects of parameters, we decided to vary the shearlet construction parameters so that we have 70 shearlet systems (see Table A1 for the parameters used to construct the 70 shearlet systems).
- 15 The total number of stochastic runs for the ridge detection is the number of combinations of shearlet systems and ridge specification parameters. Using such an approach, a probability map of detected features may be obtained based on which cut off thresholds can be defined to remove false positives. The result of such a stochastic run with 1050 realizations is depicted in Fig. 4. From this result, the utility of the method is evident wherein the features that are obscured by shadows and the shrubbery has a low strength signal which can then be filtered away thus reducing the number of false positives. Another advantage is that both large scale and fine features are captured which may not be possible using a single set of shearlet parameters.

4 Results

4.1 Trace Extraction Results from Parmelan, France

4.1.1 Geological setting of the Parmelan plateau

We tested the automated fracture extraction method on an example from a carbonate outcrop from the Parmelan plateau in
the Bornes Massif, France. The Bornes Massif is a northern subalpine chain in the western French Alps. The method was applied on a photogrammetric orthomosaic derived from a 3D outcrop model. The outcrop model was built from source photos acquired using a DJI Phantom 4 UAV. Processing of the drone images and generating the orthomosaic was done using AgiSoft PhotoScan Professional (Version 1.2.6) (2016*) software. The Parmelan Anticline in France (see Fig. 5) is situated in the frontal part of the Bornes Massif and consists of Upper Jurassic to Cretaceous rocks of the European passive margin 30 (Huggenberger and Wildi, 1991; Gidon, 1996, 1998; Berio et al., 2018).

This NE – SW trending anticline consists of a wide, flat crestal plateau bounded by steeply dipping limbs. Carbonates form the roof of a kilometre- scale box fold formed during the Alpine orogeny (Bellahsen et al., 2014). On the crestal plateau, a 1.7 km by 2.3 km large pavement of flat-lying shallow-water carbonates is exceptionally well exposed. The Parmelan outcrop is a good example of fracture patterns formed in a fold-and-thrust setting. We applied the automatic fracture detection technique on

an orthomosaic that has been stitched together from drone photogrammetry over six different drone missions over the Parmelan.
 The combined extent of the six orthomosaics is depicted in Fig. 6a, and the areal extent of each orthomosaic is depicted in Fig. 6b.

4.1.2 Automatic extraction results on the Parmelan orthomosaic

Considering memory requirements and for faster computation, the image domain was divided into georeferenced sub-tiles using the Grid Splitter plugin in QGIS software. Visual filtering was carried out to remove tiles that did not have exposed rock, had a large degree of shrubbery, and which were at the orthomosaic edges where image resolution is poor. A total of 1000 tiles were chosen for the automated interpretation process. The areal extent of the orthomosaic covered 0.589 km², and this region is depicted in Fig. 6. The region covered by the tiles amounts to 0.379 km² and this is shown as an overlay of the selected tiles in Fig. 7a.

15

An ensemble of 1050 ridges was computed using a set of shearlet parameters. A threshold for the ridge intensity was chosen to filter out the false positives. The threshold was determined by a visual examination of the overlay of detected ridges over the original images. The subsequent post-processing steps yielded features in each tile. These were geo-referenced and stitched back into a single vectorized file representation. Around 3 million features were extracted from the Parmelan orthomosaic.
20 The P₂₁ fracture intensity was computed using the box-counting method by dividing the tile into a 25 x 25 regular grid. The P₂₁ fracture intensity plot highlights the spatial variation of fracturing over the Parmelan plateau (see Fig. 7b). The vectorized fracture shape files along with the Parmelan basemap are presented as a public dataset (see Prabhakaran et al., 2019a).

4.1.3 Comparison with Manual Interpretation

To compare results of the automated approach to a manual interpretation, we chose a sub-region within the Parmelan ortho-25 mosaic. The selected subregion depicted in Fig. 8a consists of a 24 m x 24 m tile of the Parmelan orthomosaic. The image indicates fractures that seem to be isolated, without a well-connected topology, and which are predominantly aligned along an NW-SE direction. The fracturing intensity is variable across the tile. The contrast between fractures and the host rock fabric is intensified by the karstification of the fractures, which can be attributed to weathering and dissolution. Fig. 8b depicts an overlay of the automatically interpreted fractures overlain over the original tile. A total of 2910 features was extracted in this

30 tile. This example highlights some of the technical challenges associated with automated fracture trace detection. Shrubbery is present in the image which obscures certain relevant features. The north-western corner of the image is blurred since it forms the extent of the orthomosaic. The image also depicts open cavities or blobs, which could be the result of localized weathering. The effect of the cavities on the feature extraction is that only an edge is detected. Overall the fracture extraction efficiency is quite dependent on the resolution and quality of images. In the case of the Parmelan data acquisition, the UAV was flown at an altitude of 50-70 metres above the pavement; therefore, features such as closed veins, slightly open fractures, and micro fractures are below

- 5 the resolution of the drone camera. A higher image resolution is necessary to extract such features. In our specific case study, good lighting and exposure during the UAV flight mission prevented shadows from obscuring the imagery. Fig. 8c depicts a manually performed interpretation at a zoom level of 1:2000 on the raster image with a total of 341 features. P₂₁ fracture intensity comparisons of both automatic and manual traces are shown in Fig. 8d and Fig. 8e. The difference between the automatic and manual interpretation highlights the inclination of the interpreter to neglect small scale features. Based on
- 10 geological experience and prior knowledge of the field area, there is a tendency to interpret and link together disconnected features from the original raster image.

4.2 Trace Extraction Results from Brejões, Brazil

4.2.1 Geological setting of the Brejões Pavement

The second case study for the automated extraction method is a carbonate outcrop from the Irecê Basin, Central Bahia, Brazil
(see Fig. 9a, Fig. 9b). The Irecê Basin is located within the northern region of the São Francisco Craton. The Brejões pavement study area is within the Irecê Basin and consists of Neoproterozoic platform carbonates of the Salitre Formation (750-650 Ma). The Neoproterozoic cover was affected by the Brasiliano Orogeny (750-540 Ma) in two separate folding events resulting in fold belts around edges of the São Francisco Craton (Ennes-Silva et al., 2016). The Brejões pavement UAV imagery that we used for our analysis was acquired by Boersma et al. (2019). The orthomosaic covers an area of 0.81 km² and consists of fractured, black oolitic limestones that correspond to Unit A1 of the Salitre stratigraphy (Guimarães et al., 2011).

4.2.2 Automatic extraction results on the Brejões orthomosaic

The Brejões orthomosaic is split into 222 tiles for the analysis and this region is shown in Fig. 9bc. The Brejões example has a different fracturing style than the Parmelan and consists of an intricate pattern of multi-scale conjugate fractures. The shearlet combinations utilized in the case of the Parmelan was insufficient to capture this variation in scales. Specifically, in the Brejões case, the large scale features were not captured. A visual inspection of the ridges was necessary to identify the shearlet combinations that amplified the large scale features. The contribution of these ridges was increased (factor of 8) in the ridge ensemble to highlight these large deformation features. Fig. 9d depicts the P₂₁ fracturing intensity computed using the box-counting method by dividing each tile into a 25 x 25 regular grid. The vectorized fracture shape files along with the Brejões basemap are presented as a public datastet (see Prabhakaran et al., 2019b).

4.2.3 Comparison with Manual Interpretation

The automatically extracted features from the Brejões image data was compared with manual interpretations performed by and obtained from Boersma et al. (2019) at seven stations. The automatic interpretations were trimmed to the peripheries of the manual interpretations for a fair comparison between both the vectorizations. The location of these stations alongside the

5 automatic versus manual interpretations are shown in Fig.10. A few observations can be made from the comparison. Firstly, similar to the Parmelan case, the interpreter picks a lesser number of features. Secondly, there is a tendency to extend fractures across image regions where there is no real evidence of rock displacementfailure. Thirdly, there is an inconsistency in specifying the connecting topologies between the interpreted traces.

In some stations (see Mid #2, Mid #3 and North in Fig.10), the automated interpretation suffers from a large number of false positives. A close examination indicates that the presence of shadows and eroded, undulating topography of the rocks are the main reasons for these false positives. In the Brejões case, the drone was flown at around 10.00 AM, and hence the exposure of

the outcrop face was not optimal. The inclined illumination enhances shadows on the rugged topography, which are then seen as false positives in the automatic interpretation. False positives due to shrubbery are minimal in the station regions considered.

4.3 Benchmarking with data from Thiele et al. (2017)

- 15 We further tested the automated trace detection on a recently published case study from Thiele et al. (2017). The images selected are orthophotographs of two 10 x 10 m areas from Bingie Bingie Point, New South Wales, Australia (see Fig. 12a and Fig. 13a). The exposed rocks are Cretaceous to Paleogene dykes, intruding diorites, and tonalities cross-cut by joint sets (Thiele et al. 2017). The images are complex as they contain both open and closed fractures of different scales, distributed between multiple lithological layers. The images also contain water, shadows, and debris, which makes it even more challenging. We
- 20 chose this dataset to benchmark the quality of our results with those presented using the semi-automatic cost function based trace mapping approach of Thiele et al. (2017).

The variation in fracture scales implied that similar to Brejões, a different set of shearlet combinations were needed. We generated 2700 ridge realizations which were used to construct a normalized ridge ensemble map for both images (see Fig. 12b and Fig. 13b). A simple, non-linear sigmoid function was applied to the normalized ridge intensity to enhance ridge strength (see Fig. 12c and Fig. 13c) and a threshold was chosen based on visual comparison with the source image to yield highly probable, binarized ridge images (see Fig. 12d and Fig. 13.d). The subsequent workflow steps, as described in Sect. 3.1 were followed to obtain vectorized traces (see Fig. 12e and Fig. 13e). The vectorized traces were used to render assisted interpretations depicted in Fig. 12f and Fig. 13f which are comparable in quality to the manual assisted interpretation of Thiele et al. (2017).

30

In the published results of Thiele et al. (2017), assisted interpretations of both areas are achieved in 37 minutes and 34 minutes, respectively. We can report better performances of 27 and 32 minutes for the same areas. The time does not include computing of the ridge realizations. Once the high probability trace map was generated, the subsequent steps of the automated

detection workflow took around 3 minutes. The remainder of the time was used to perfect the assisted interpretation. The postprocessing tasks performed in this second step were the removal of false positives owing to shadows, water, and debris and joining of segments which were disjointed due to poor resolution within the image. Though we have performed a benchmarking exercise with the data from Thiele et al. (2017) and also compared our results with manual interpretation, it would be useful

5 to compare with more manual interpretations to further validate the accuracy of the technique. Such comparison, however, can be done only on networks which are either limited in their spatial extent or in the number of features interpreted. For large orthomosaics, a benchmarking exercise can be challenging as few manually rendered datasets are comparable in network size.

5 Discussion

20

Extraction of fracture traces from photogrammetric data is a necessary processing step to construct DFN representations.
DFNs created using fracture patterns that are directly extracted from rock images, are advantageous as they honour the spatial architecture of fracture networks. Automated extraction methods reduce the human component in data processing, and we have achieved this using the complex shearlet transform ridge detection method accompanied by post-processing steps. The complex shearlet method can detect both edges as well as ridges in fractured rock images. We find that the ridge measure works very well for extraction of fractures, and we use the ridge measure in all our case studies. Though the method performs very

15 well and can extract much more traces than is possible manually while reducing interpreter bias, there are some issues which need to be mentioned. In this section, we detail some areas where there is scope for further development and also describe some potential applications of the method.

- Detection of large cavities and false positives

- Both the Parmelan and Brejões pavements exhibit karstification with the Parmelan containing many more collapsed karstic regions. The presence of such low-aspect ratio discontinuities are quite rare in siliciclastic and volcanic outcrops but can prove problematic in carbonate outcrops where karstification is severe. Both the ridge and edge measures would fail in identifying such blobs or would at best, extract the periphery of the cavity. In recent work by Reisenhofer and King (2019), blob detection measures have been developed within the shearlet framework and could potentially solve this issue.
- Another issue is the effect of undulating topography and shrubbery in generating false positives. False positives generally appear when there is shrubbery, shadows, very rugged terrain, and non-fracture bedding planes. In the case of the Parmelan, the use of multiple ridges was successful in suppressing the false positives owing to shrubbery. However, in Brejões, false positives due to underbrush were more difficult to suppress because they shared the same scale as that of the fractures. In Brejões shrubbery was also present within some of the wider fractures causing false negatives. In such cases, manual interference is necessary to either mask the regions of shrubbery before the automatic extraction or to remove (or connect) the vectorized traces after the automated extraction. Additionally, carbonate outcrops are prone to widespread erosion owing to exposure to meteoric water from precipitation cycles and air corrosion. Geomorphological features owing to these erosive processes may also play a role in generation of false positives.

- Optimization of processing

A significant difference in fracture scales within the same image can prove problematic for the method. In such a case, a vast number of ridge detection runs would be needed to construct a ridge ensemble that takes into account all scales of discontinuities and yields a satisfactory result. When such variation is localized and easily recognizable, the image could be segmented into regions that correspond to varying fracture intensities and processed separately. In the Brejões, this difference in fracture scales was ubiquitous throughout the exposure and more pronounced than the Parmelan. Using visual comparison with the original image, the effect of ridges resulting from certain shearlet parameter combinations was enhanced, so that the ridge ensemble is improved. In Brejões, it was the large scale features that needed to be strengthened. Since these steps need manual intervention, a more comprehensive way of arriving at the optimal shearlet combination is desirable. An algorithm that automatically optimizes for shearlet parameters corresponding to each individual scale of fracture is worthy of attention.

- Relationship between extractable P₂₁, drone flying altitude, and camera resolution

From the P_{21} analysis on the Parmelan and the Brejões automatically extracted fractures, the maximum value P_{21} was around eight m⁻¹. The same drone model was used in both cases (DJI Phantom 4), and the flying altitude was also similar (between 40 and 70 metres). Although such a conjecture needs further verification, there could be a relation between the resolution of imagery and maximum extractable fracture intensity. Often flight altitudes are chosen by drone pilots depending upon considerations such as local topography, weather conditions, and presence of impediments (such as trees, electricity poles, and telecommunications towers). A detailed analysis of the relation between flying altitude (and consequently image resolution) and extracted fracture intensity could provide drone pilots with insights and guidelines for UAV-based outcrop analysis. The ideal flying resolution to identify features of interest may be ascertained by carrying out a series of acquisitions at a location where ground truth is known.

- Generating data for fractured reservoir modelling workflows

Fractured reservoir characterization workflows in the oil and gas industry have traditionally used stochastic techniques that attempt to extrapolate averaged fracture statistics (either from borehole imagery, core data, or outcrop analysis) to reservoir volumes. The use of Multiple Point Statistics (MPS) for fracture network generation was highlighted by Bruna et al. (2019) as an alternative approach to DFN modelling. MPS uses training images of realistic fracture networks to learn patterns and then generate non-stationary fractured reservoir models. Our <u>Corrected for false positives</u> and noise, the automated method can quickly produce accurate, geologically realistic, and unbiased training images that can feed into the MPS workflow. Since our method can extract large scale fracture networks (millions of features from sub- square kilometre regions), it is also well suited to provide training data for deep learning workflows. Recently, the use of Generative Adversarial Networks (GANs) for geological modelling at the reservoir scale was proposed by <u>Dupont et al. (2018); Zhang et al. (2019)</u> <u>Dupont et al. (2018), Zhang et al. (2019)</u> as an alternative to conventional geostatistics, MPS, and object-based modelling. GANs form a subset of deep learning architectures that are used for

15

20

25

generative modelling (Goodfellow et al., 2014). GANs that are trained on realistic data can then generate geologically realistic, non-stationary models.

6 Conclusions

This paper presents a method to automatically detect and digitize fracture traces from images of rock fractures using the complex shearlet transform. The technique replaces the task of manually interpreting fractures, which is time-consuming, prone to interpreter bias, and which suffers from a lack of repeatability. The case studies that are presented highlight the utility of the complex shearlet based measure for automatically detecting fracture traces from 2D images. The automatic trace detection method combines the complex shearlet ridge measure with a series of post-processing steps that include image segmentation, skeletonization, polyline fitting, and polyline simplification. We tested the method at different scales of rock displacement, at outcrop scale (~ 10² m) and station-scale (< 10 m), using two orthomosaics reconstructed from drone photogrammetry and two rock pavement images. We have considered carbonate and igneous rock lithologies in the case studies. Using the method, we have extracted millions of 2D features from outcrop-scale drone orthophotos. The processing time of the technique depends upon the intensity of fracturing and the complexity of the fracture networks contained within the image. The automatic trace extraction results are quantitatively compared with manually interpreted fractures on selected sub-samples of the image domain

15 using fracture trace density metrics. The automated technique is capable of extracting a much larger number of features, with a marked reduction in bias. The method outlined in this paper greatly simplifies the process of generating deterministic, outcrop-based DFNs. The automatically extracted, fracture patterns can be used by structural geologists to link deformation features to tectonic history and by geomodellers in sub-surface NFR modelling.

Code and data availability.

20 . MATLAB code that was used to generate the results in this manuscript is available on Github https://github.com/rahulprabhakaran/Automatic-Fracture-Detection-Code (see Prabhakaran 2019)

. Fracture and image data correponding to the Parmelan and Brejões outcrops are available at the 4TU Centre for Research Data repository (https://researchdata.4tu.nl/en/)

- Fracture Network Patterns from the Brejões Outcrop, Irecê Basin, Brazil (see Prabhakaran et al. 2019a)
- 25 Fracture Network Patterns from the Parmelan Anticline, France (see Prabhakaran et al. 2019b)

Appendix A: Overview of the Complex Shearlet Transform

A1 The Continuous Shearlet System

A shearlet generating function consists of an anisotropic scaling matrix and a shear matrix. Let the shearlet generating function be:

5
$$\psi \in L^2(\mathbb{R}^2)$$
 (A1)

The admissibility criteria for the shearlet generating function is :

$$\int_{R^2} \frac{\left|\hat{\psi}(\xi_1\xi_2)\right|^2}{{\xi_1}^2} d\xi_2 d\xi_1 < \infty$$
(A2)

where $\hat{\psi}$ is the 2D fourier transform of ψ .

10 A shearlet satisfying Eq.A2 is an admissible shearlet or a continuous shearlet (Kutyniok and Labate, 2012). The admissibility condition implies that a reconstruction formula exists for the associated continuous shearlet transform. In order to achieve an optimally sparse approximation of an image that possesses anisotropic singularities, the analysing elements must consist of waveforms that range over several scales, orientations, and locations with the ability to become very elongated. To this end, a combination of a scaling operator to generate elements at different scales, an orthogonal operator to change orientations, and a 15 translation operator to displace elements over the 2D plane, is used. The scaling matrix A_a is defined as (Labate et al., 2005):

$$A_a = \begin{pmatrix} a & 0\\ 0 & a^{\alpha} \end{pmatrix}, \ \alpha \ \in [0, 1]$$

25

The value of α controls the degree of anisotropy. (For more information on the anisotropy scaling molecules or α –molecules 20 see Grohs et al. 2016.) The scaling matrix is parabolic when $\alpha = \frac{1}{2}$.

An orthogonal transformation to change the orientations of waveforms. Rotation operators are not preferred as they destroy the structure of the integer lattice Z^2 whenever the rotation angle is different from $0, \pm \frac{\pi}{2}, \pm \pi, \pm \frac{3\pi}{2}$. Changes in the structure of integer lattice is problematic when transitioning from continuum to digital setting. Hence, a shearing transformation is used where the anisotropic shearing transformation matrix S_s are defined as:

$$S_s = \begin{pmatrix} 1 & s \\ 0 & 1 \end{pmatrix}$$
 where the parameters $a \in \mathbb{R}^+, s \in \mathbb{R}$

The shearing matrix S_s preserves the structure of the integer grid for any $s \in \mathbb{N}$. The shearing matrix parametrizes orientations using the variable s associated with slopes rather than angles and leaves the integer lattice invariant, provided s is an A shearlet system is defined as (Kutyniok and Labate, 2012):

$$SH(\psi) = \left\{ \psi_{a,s,t} = a^{-3/4} \psi \left(A_a^{-1} S_s^{-1} \left(\cdot - t \right) \right) a \in \mathbb{R}^+, s \in \mathbb{R}, t \in \mathbb{R}^2 \right\}$$
(A3)

5 where $(\cdot - t)$ denotes the translation by a point *t*.

The corresponding shearlet transform for mapping a function $f \in L^2(\mathbb{R}^2)$ into coefficients, $SH_{\psi} f(a, s, t)$ specified by scaling a, shearing s and translation t is given by:

$$f \to SH_{\psi} f(a,s,t) = f, \ \psi_{a,s,t} \tag{A4}$$

A2 Cone Adapted Continuous Shearlet Systems

- 10 Equation A4 renders horizontal shearlets elongated at very fine scales, which is problematic in digital implementations. Because the shearing operator can range over a non-bounded interval, directions are not treated uniformly. To overcome this drawback of shearing, the cone adapted shearlet system was introduced in which the frequency plane is split into a horizontal and vertical cone that restricts the shear parameter to bounded intervals (see Fig. A2 a). Dividing the frequency plane in such a manner ensures uniform treatment of directions (Guo et al., 2005; Kutyniok and Labate, 2012). A cone adapted shearlet system can be
- 15 tiled by further division of the frequency domain. Such a tiling configuration (see Fig.A2 b) ensures that all directions are treated "almost equally" (Kutyniok and Labate, 2012). There is still small, but controllable bias in the coordinate axes directions). The cone adapted shearlet systems can therefore be expressed as the union of a horizontal cone, a vertical cone, and a low-frequency centre component. The frequency plane is thus split into four horizontal and vertical cones with a low-frequency square region in the centre. The low-frequency region is given by the relation (Kutyniok and Labate, 2012):

20
$$\mathcal{R} = \{(\xi_1, \xi_1) : |\xi_1|, |\xi_2| \le 1\}$$
 (A5)

Inside each cone, the shearing variable s is only allowed to vary over a finite range. This produces elements with uniformly distributed orientations. The union of the generating functions for the horizontal cones $\psi \in L^2(\mathbb{R}^2)$, vertical cones $\tilde{\psi} \in L^2(\mathbb{R}^2)$ and for the square low frequency region $\varphi \in L^2(\mathbb{R}^2)$ is expressed as (Kutyniok and Labate, 2012):

$$SH(\varphi,\psi,\tilde{\psi}) = \Phi(\varphi) \cup \Psi(\psi) \cup \tilde{\Psi}(\tilde{\psi})$$
(A6)

25 where

$$\Phi\left(\varphi\right) = \left\{\varphi_t = \varphi\left(\cdot - t\right) : t \in \mathbb{R}^2\right\};\tag{A7}$$

$$\tilde{\Psi}(\psi) = \left\{ \tilde{\psi}_{a,s,t} = a^{-\frac{3}{4}} \tilde{\psi}\left(\tilde{A}_a^{-1} S_s^{-1} \left(\cdot - t\right)\right) : a \in (0,1], |s| \le 1 + a^{\frac{1}{2}}, t \in \mathbb{R}^2 \right\};$$
(A8)

$$\tilde{\Psi}(\psi) = \left\{ \tilde{\psi}_{a,s,t} = a^{-\frac{3}{4}} \tilde{\psi} \left(\tilde{A}_a^{-1} S_s^{-1} (\cdot - t) \right) \colon a \in (0,1], |s| \le 1 + a^{\frac{1}{2}}, t \in \mathbb{R}^2 \right\}.$$
(A9)

Scaling matrix for vertical cones, \tilde{A}_a is expressed as:

$$\tilde{A}_a = \begin{pmatrix} a^{\alpha} & 0\\ 0 & a \end{pmatrix} \tag{A10}$$

The cone adapted continuous shearlet transform is expressed as the mapping:

5
$$f \to SH_{\varphi,\psi,\tilde{\psi}} f(t',(a,s,t),(\tilde{a},\tilde{s},\tilde{t})) = \left(f, \varphi_{t'}, f, \psi_{a,s,t}, f, \tilde{\psi}_{\tilde{a},\tilde{s},\tilde{t}}\right)$$
 (A11)

A3 The Discrete Cone Adapted Shearlet System

A discrete version of the cone adapted shearlet system may be defined with scaling parameter j, shearing parameter k, and translation parameter m for a sampling factor of $c = (c_1, c_2) \in (\mathbb{R}_+)^2$. Similar to Eq.A6 this is a union of the generating functions for vertical, horizontal, and low frequency central region.

10
$$SH(\varphi,\psi,\bar{\psi};c) = \Phi(\varphi;c_1) \cup \Psi(\psi;c) \cup \bar{\Psi}(\bar{\psi};c)$$
 (A12)

$$\Phi(\varphi;c_1) = \left\{\varphi_m = \varphi(\cdot - c_1m) : m\epsilon\mathbb{Z}^2\right\};\tag{A13}$$

$$\Psi(\psi;c) = \left\{ \psi_{j,k,m} = 2^{\frac{3}{4}j} \psi(S_k A_{2^j} \cdot -M_c m) : \ j \ge 0, |k| \le \left\lceil 2^{\frac{j}{2}} \right\rceil, \ m \in \mathbb{Z}^2 \right\};$$
(A14)

15

$$\tilde{\Psi}\left(\tilde{\psi};c\right) = \left\{\tilde{\psi}_{j,k,m} = 2^{\frac{3}{4}j}\tilde{\psi}\left(S_k{}^T\tilde{A}_{2^j} \cdot -\tilde{M}_c m\right): \ j \ge 0, |k| \le \left\lceil 2^{\frac{j}{2}} \right\rceil, \ m \in \mathbb{Z}^2\right\};$$
with $M_c = \begin{bmatrix} c_1 & 0\\ 0 & c_2 \end{bmatrix}; \ \tilde{M}_c = \begin{bmatrix} c_2 & 0\\ 0 & c_1 \end{bmatrix}; (M_c \text{ and } \tilde{M}_c \text{ are sampling matrices for horizontal and vertical cones})$
(A15)

20 $A_{2^j} = \begin{bmatrix} 2^j & 0 \\ 0 & 2^{j/2} \end{bmatrix}$; $\tilde{A}_{2^j} = \begin{bmatrix} 2^{j/2} & 0 \\ 0 & 2^j \end{bmatrix}$; $(A_{2^j} \text{ and } \tilde{A}_{2^j} \text{ are dyadic scaling matrices for horizontal and vertical cones})$

$$S_k = \begin{bmatrix} 1 & k \\ 0 & 1 \end{bmatrix}$$
 (shearing matrix).

25

The discrete cone adapted shearlet transform associated with ϕ , ψ and $\tilde{\psi}$ is given by the mapping,

$$f \to SH_{\varphi,\psi,\tilde{\psi}} f\left(m',(j,k,m),(\tilde{j},\tilde{k},\tilde{m}) = \left(f, \varphi_{m'},f, \psi_{j,k,m},f, \tilde{\psi}_{\tilde{j},\tilde{k},\tilde{m}}\right).$$
(A16)

A4 The Complex Discrete Cone Adapted Shearlet System

Taking the complex valued wavelet of a real valued even symmetric wavelet generator $\psi^{even} \in L^2(\mathbb{R}^2)$, using the Hilbert transform operator (\mathcal{H}), a complex valued shearlet generator is obtained (from Reisenhofer, 2014; King et al., 2015)

$$\psi^c = \psi^{even} + i \,\psi^{\underline{even}\,odd}.\tag{A17}$$

5 The complex valued function can be written in terms of a Hilbert transform pair of an even-symmetric real valued shearlet and an odd-symmetric real valued shearlet: (from Reisenhofer, 2014; King et al., 2015)

$$\psi^c = \psi^{even} + i \mathcal{H}\psi^{even}. \tag{A18}$$

The Hilbert transform operator is written as,

$$\mathcal{H}(f)(t) = \lim_{a \to \infty} \int_{-a}^{a} \frac{f(\tau)}{t - \tau} d\tau.$$
(A19)

10 The discrete cone adapted complex shearlet system is given as (Reisenhofer, 2014; King et al., 2015):

$$SH(\varphi,\psi,\tilde{\psi};c) = \Phi(\varphi;c_1) \cup \Psi(\psi;c) \cup \tilde{\Psi}(\tilde{\psi};c)$$
(A20)

and

$$SH^{c}(\varphi,\psi,\tilde{\psi};c) = \Phi(\varphi;c_{1}) \cup \Psi^{c}(\psi;c) \cup \tilde{\Psi^{c}}(\tilde{\psi};c)$$
(A21)

where,

15
$$\Phi(\varphi;c_1) = \left\{\varphi_t = \varphi(\cdot - c_1 m) : m \in \mathbb{Z}^2\right\},\tag{A22}$$

$$\Psi^{c}(\psi;c) = \left\{ \psi^{c}_{j,k,m} = \psi^{c}_{j,k,m} + i \left(\mathcal{H}_{(1,0)} \mathbf{T} \; \psi \right)_{j,k,m} : \; j \ge 0, |k| \le \lceil 2^{\frac{j}{2}} \rceil, \; m \in \mathbb{Z}^{2} \right\},\tag{A23}$$

$$\tilde{\Psi}^{c}\left(\tilde{\psi};c\right) = \left\{\tilde{\psi}^{c}_{j,k,m} = \tilde{\psi}^{c}_{j,k,m} + i\left(\mathcal{H}_{(0,1)}\mathrm{T}\;\tilde{\psi}\right)_{j,k,m} : \; j \ge 0, |k| \le \lceil 2^{\frac{j}{2}} \rceil, \; m \in \mathbb{Z}^{2}\right\}.$$
(A24)

Correspondingly the discrete complex cone adapted shearlet transform is given by the mapping,

$$f \to SH^{c}_{\varphi,\psi,\tilde{\psi}} f\left(m',(j,k,m),(\tilde{j},\tilde{k},\tilde{m})\right) = \left(f, \varphi_{m'},f, \psi^{c}_{j,k,m},f, \tilde{\psi}^{c}_{\tilde{j},\tilde{k},\tilde{m}}\right).$$
(A25)

20

(A26)

A5 Edge and Ridge Detection using the Complex Shearlet Transform

The behavior of the coefficients of the even symmetric and odd symmetric shearlets can be used to detect edges and ridges. An edge measure for an image $f \in L^2(\mathbb{R}^2)$, a location $x \in \mathbb{R}^2$ and a shear parameter s is given as (Reisenhofer, 2014; King et al., 2015),

$$E_{\psi}(f,x,s) = \frac{\left|\sum_{a \in A} Im\left(f,\psi^{c}_{a,s,x}\right)\right| - \sum_{a \in A} \left|Re\left(f,\psi^{c}_{a,s,x}\right)\right|}{\left|A\right|max_{a \in A}\left|Im(f,\psi^{c}_{a,s,x})\right| + \varepsilon},\tag{A27}$$

where A ⊂ ℝ⁺ is a set of scaling parameters, ψ is a real valued symmetric shearlet and ε prevents division by zero. The complex shearlet based edge measure can give approximations of the tangential directions of an edge. A line measure or ridge
measure is obtained by interchanging the role of the even symmetric and odd symmetric shearlets (Reisenhofer, 2014; King et al., 2015),

$$L_{\psi}(f,x,s) = \frac{\left|\sum_{a \in A} Re\left(f,\psi^{c}{}_{a,s,x}\right)\right| - \sum_{a \in A} \left|Im\left(f,\psi^{c}{}_{a,s,x}\right)\right|}{\left|A\left|max_{a \in A}\left|Re(f,\psi^{c}{}_{a,s,x})\right| + \varepsilon}\right|\right|}.$$
(A28)

15 Both the edge and ridge measures given above are inspired from the phase congruency measure of Kovesi (2000). The edge and ridge measures are almost contrast invariant.

Author contributions. RP developed model code, performed the automatic extraction on all case studies, participated in data acquisition during the Parmelan fieldwork, and wrote the manuscript. P-OB took the lead role in data acquisition of the Parmelan dataset, carried out processing of the drone imagery, assisted in generating artwork, and provided manual fracture interpretations. GB took part in the data acquisition at the Brejões outcrop and provided knowledge and expertise about the regional geology of the Irecê Basin. GB and DS provided expertise and supervision concerning the development of the workflow and writing of the manuscript.

5

Competing interests. The authors would like to declare that there was no competing interests involved.

Acknowledgements. ENI Exploration is thanked for partial funding of the Ph.D. project of the first author, for the financing accorded to the fieldwork carried out in Parmelan, France and for permission to use the Parmelan photogrammetric data to test the automatic trace detection method. The authors would like to accord their special gratitude to Marco Meda (ENI Exploration) for his gracious hospitality and coordination of the SEFRAC consortium meetings held at Milano and for the stimulating discussions. Thanks are also due to Silvia

- 10 and coordination of the SEFRAC consortium meetings held at Milano and for the stimulating discussions. Thanks are also due to Silvia Mittempergher (University of Milano Bicocca), Fabrizio Storti, Fabrizio Balsamo, and Luigi Berio (University of Parma) for their company and the interesting discussions during the Parmelan expedition. Quinten Boersma (Delft University of Technology) is thanked for making available the Brejões orthomosaic and the manual fracture interpretations. The authors would like to thank Shell Exploration and Agência Nacional do Petróleo, Gás Natural e Biocombustíveis (ANP) for funding the field expedition to the Brejões outcrop in which Quinten
- 15 Boersma and Giovanni Bertotti participated. The collaboration and scientific inputs of Hilario Bezerra (Universidade Federal do Rio Grande do Norte) during the data acquisition campaign in Brazil is graciously acknowledged.

References

- Abdullah, A., Nassr, S., and Ghaleeb, A.: Landsat ETM-7 for Lineament Mapping Using Automatic Extraction Technique in the SW Part of Taiz Area, Yemen, Global Journal of Human-Social Science Research (B), 13 (3), 35–38, 2013.
- AgiSoft PhotoScan Professional (Version 1.2.6): PhotoScan Professional (Version 1.2.6) Retrieved from http://www.agisoft.com/downloads/installer/, 2016*.
- Aljuboori, F., Corbett, P. W. M., Bisdom, K., Bertotti, G., and Geiger, S.: Using Outcrop Data for Geological Well Test Modelling in Fractured Reservoirs, in: 77th EAGE Conference and Exhibition, Madrid, Spain, 1-5 June 2015, We-N118-01, https://doi.org/10.3997/2214-4609.201413037, 2015.
- Andrews, B., Roberts, J., ZK Shipton, S. B., Tartarello, M., and Johnson, G.: How do we see fractures? Quantifying subjective bias in fracture
 data collection. Solid Earth, 10(2), 487–516. https://doi.org/10.5194/se-10-487-2019. 2019.
- Bellahsen, N., Mouthereau, F., Boutoux, A., Bellanger, M., Lacombe, O., Jolivet, L., and Rolland, Y.: Collision kinematics in the western external Alps, Tectonics, 33 (6), 1055–1088, https://doi.org/10.1002/2013tc003453, 2014.
 - Bemis, S. P., Micklethwaite, S., Turner, D., James, M. R., Akciz, S., Thiele, S. T., and Bangash, H. A.: Ground-based and UAV-Based photogrammetry: A multi-scale, high-resolution mapping tool for structural geology and paleoseismology, Journal of Structural Geology,
- 15 69 (Part A), 163 178, https://doi.org/10.1016/j.jsg.2014.10.007, 2014.
- Berio, L., Balsamo, F., Mittempergher, S., Mozafari, M., Storti, F., Bistacchi, A., Bruna, P.-O., and Bertotti, G.: Deformation pattern in the thrust-related Parmelan Anticline (Bornes Massif, Subalpine Chains, Haute-Savoie, France): preliminary results, in: 20th EGU General Assembly, Vienna, Austria, 8–13 April 2018, 2018EGUGA..20.8923B, http://resolver.tudelft.nl/uuid: 259ea083-7bac-43d8-a4c5-34e79cc001e6, 2018.
- 20 Bisdom, K., Nick, H., and Bertotti, G.: An integrated workflow for stress and flow modelling using outcrop-derived discrete fracture networks, Computers & Geosciences, 103, 21 – 35, https://doi.org/10.1016/j.cageo.2017.02.019, 2017.
 - Boersma, Q., Prabhakaran, R., Bezerra, F. H., and Bertotti, G.: Linking natural fractures to karst cave development: a case study combining drone imagery, a natural cave network and numerical modelling, Petroleum Geoscience, https://doi.org/10.1144/petgeo2018-151, 2019.
 - Bolkas, D., Vazaios, I., Peidou, A., and Vlachopoulos, N.: Detection of Rock Discontinuity Traces Using Terrestrial LiDAR Data and Space-
- 25 Frequency Transforms, Geotechnical and Geological Engineering, 36 (3), 1745–1765, https://doi.org/10.1007/s10706-017-0430-6, 2018. Bond, C., Gibbs, A., Shipton, Z., and Jones, S.: What do you think this is?: "Conceptual uncertainty" In geoscience interpretation, GSA Today, 17 (11), 4–10, https://doi.org/10.1130/GSAT01711A.1, 2007.
 - Bond, C., Johnson, G., and Ellis, J.: Structural model creation: the impact of data type and creative space on geological reasoning and interpretation, Geological Society of London Special Publications, 421 (1), 83–97, https://doi.org/doi:10.1144/SP421.4, 2015.
- 30 Bonetto, S., Facello, A., Ferrero, A. M., and Umili, G.: A tool for semi-automatic linear feature detection based on DTM, Computers & Geosciences, 75, 1 – 12, https://doi.org/10.1016/j.cageo.2014.10.005, 2015.
 - Bonetto, S., Facello, A., and Gessica, U.: A New Application of Curvatool Semi-automatic Approach To Qualitatively Detect Geological Lineaments, Environmental and Engineering Geoscience, 23 (3), 179–190, https://doi.org/10.2113/gseegeosci.23.3.179, 2017.
- Bruna, P.-O., Straubhaar, J., Prabhakaran, R., Bertotti, G., Bisdom, K., Mariethoz, G., and Meda, M.: A new methodology to train fracture
 network simulation using multiple-point statistics, Solid Earth, 10 (2), 537–559, https://doi.org/10.5194/se-10-537-2019, 2019.
 - Callatay, G.: Hough Transform Application to Natural Fracture Networks: Detection, Characterization and Simulation, Master's thesis, Delft University of Technology, http://resolver.tudelft.nl/uuid:e7bea512-6b64-455c-961b-ceeff573c79c, 2016.

- Candès, E. J. and Donoho, D. L.: Continuous curvelet transform: I. Resolution of the wavefront set, Applied and Computational Harmonic Analysis, 19 (2), 162 197, https://doi.org/10.1016/j.acha.2005.02.003, 2005.
- Candès, E. J. and Guo, F.: New multiscale transforms, minimum total variation synthesis: applications to edge-preserving image reconstruction, Signal Processing, 82 (11), 1519–1543, https://doi.org/10.1016/S0165-1684(02)00300-6, 2002.
- 5 Canny, J.: A Computational Approach to Edge Detection, IEEE Transactions on Pattern Analysis and Machine Intelligence, PAMI-8 (6), 679 - 698, https://doi.org/10.1109/TPAMI.1986.4767851, 1986.
 - Daubechies, I.: Ten Lectures on Wavelets, CBMS-NSF Regional Conference Series in Applied Mathematics, Society for Industrial and Applied Mathematics, Philadelphia, USA, 1999 edn., https://doi.org/10.1137/1.9781611970104, 1992.

Do, M. N. and Vetterli, M.: The contourlet transform: an efficient directional multiresolution image representation, IEEE Transactions on Image Processing, 14 (12), 2091–2106, https://doi.org/10.1109/TIP.2005.859376, 2005.

- Donoho, D. L.: Wedgelets: Nearly Minimax Estimation of Edges, The Annals of Statistics, 27 (3), 859–897, http://www.jstor.org/stable/ 120143, 1999.
- Donovan, J. and Lebaron, A.: A Comparison of Photogrammetry And Laser Scanning For the Purpose of Automated Rock Mass Characterization, in: 43rd U.S. Rock Mechanics Symposium & 4th U.S. - Canada Rock Mechanics Symposium, 28 June-1 July 2009, Asheville,
- 15 North Carolina, USA, ARMA-09-122, https://www.onepetro.org/conference-paper/ARMA-09-122, 2009.
 - Douglas, D. and Peucker, T.: Algorithms for the Reduction of the Number of Points Required to Represent a Digitized Line or its Caricature, Cartographica: The International Journal for Geographic Information and Geovisualization, 10 (2), 112–122, https://doi.org/10.3138/FM57-6770-U75U-7727, 1973.

Duda, R. O. and Hart, P. E.: Use of the Hough Transformation to Detect Lines and Curves in Pictures, Communications of the ACM, 15 (1),

20 11–15, https://doi.org/10.1145/361237.361242, 1972.

10

Dupont, E., Zhang, T., Tilke, P., Liang, L., and Bailey, W.: Generating Realistic Geology Conditioned on Physical Measurements with Generative Adversarial Networks, in: 35th International Conference on Machine Learning, Stockholm, Sweden, 10 - 15 July 2018, 1802.03065, https://arxiv.org/abs/1802.03065v3, 2018.

Dwarkasing, A.: 3D Fracture Analyses of Various Rock Samples through X-Ray Micro-Tomography, Master's thesis, Delft University of

- 25 Technology, http://resolver.tudelft.nl/uuid:aefe6746-9788-4c93-ac4c-f80250e6a12c, 2016.
- Ennes-Silva, R. A., Bezerra, F. H. R., Nogueira, F. C. C., Balsamo, F., Klimchouk, A., Cazarin, C. L., and Auler, A. S.: Superposed folding and associated fracturing influence hypogene karst development in Neoproterozoic carbonates, São Francisco Craton, Brazil, Tectonophysics, 666, 244–259, https://doi.org/10.1016/j.tecto.2015.11.006, 2016.

Felsberg, M. and Sommer, G.: The Monogenic Signal, IEEE Transactions on Signal Processing, 49 (12), 3136-3144,

30 https://doi.org/10.1109/78.969520, 2001.

Gidon, M.: Vues nouvelles sur la structure des massifs des Bornes et des Bauges orientales, Géologie Alpine, 72, 35–39, http://geologie-alpine.ujf-grenoble.fr/articles/GA_1996_72_35_0.pdf, 1996.

Gidon, M.: Failles extensives antérieures au plissement dans les massifs subalpins: un exemple nouveau dans le massif des Bornes (France), Géologie Alpine, 74, 91–96, http://geologie-alpine.ujf-grenoble.fr/articles/GA_1998_74_91_0.pdf, 1998.

35 Goodfellow, I. J., Pouget-Abadie, J., Mirza, M., Xu, B., Warde-Farley, D., Ozair, S., Courville, A., and Bengio, Y.: Generative Adversarial Nets, in: Proceedings of the 27th International Conference on Neural Information Processing Systems - Volume 2, 08 - 13 December 2014, NIPS'14, pp. 2672–2680, MIT Press, Cambridge, MA, USA, http://dl.acm.org/citation.cfm?id=2969033.2969125, 2014.

- Grohs, P., Keiper, S., Kutyniok, G., and Schäfer, M.: Alpha-Molecules, Applied and Computational Harmonic Analysis, 41 (1), 297–336, https://doi.org/10.1016/j.acha.2015.10.009, 2016.
- Guimarães, J. T., Misi, A., Pedreira, A. J., and Dominguez, J. M. L.: The Bebedouro Formation, Una Group, Bahia (Brazil), The Geological Record of Neoproterozoic Glaciations, Geological Society, London, Memoirs, vol. 36, chap. 47, pp. 503-508, Geological Society of
- London, 2011 edn., https://doi.org/10.1144/M36.47, 2011. Guo, K., Kutyniok, G., and Labate, D.: Sparse multidimensional representation using anisotropic dilation and shear operators, in: Wavelets and Splines: Athens 2005, International Conference on "Interactions between Wavelets and Splines", 16-19 May 2005, Athens, Georgia, edited by Chen, G. and Lai, M.-J., pp. 189–201, Nashboro Press, 2006, 2005.

Harwin, S. and Lucieer, A.: Assessing the Accuracy of Georeferenced Point Clouds Produced via Multi-View Stereopsis from Unmanned Aerial Vehicle (UAV) Imagery, Remote Sensing, 4 (6), 1573–1599, https://doi.org/10.3390/rs4061573, 2012.

Hashim, M., Ahmad, S., Johari, M. A. M., and Pour, A. B.: Automatic lineament extraction in a heavily vegetated region using Landsat Enhanced Thematic Mapper (ETM+) imagery, Advances in Space Research, 51 (5), 874–890, https://doi.org/10.1016/j.asr.2012.10.004, 2013.

Heil, C., Walnut, D. F., and Daubechies, I.: Fundamental Papers in Wavelet Theory, Princeton University Press, Princeton, New Jersey, USA,

15 Princeton University Press, http://www.istor.org/stable/i.ctt7rt5v, 2006.

5

- Hillier, J., Smith, M., Armugam, R., Barr, I., Boston, C., Clark, C., Ely, J., Frankl, A., Greenwood, S., Gosselin, L., Hättestrand, C., Hogan, K., Hughes, A., Livingstone, S., Lovell, H., McHenry, M., Munoz, Y., Pellicer, X., Pellitero, R., Robb, C., Roberson, S., Ruther, D., Spagnolo, M., Standell, M., Stokes, C., Storrar, R., Tate, N., and Wooldridge, K.: Manual mapping of drumlins in synthetic landscapes to assess operator effectiveness, Journal of Maps, 11(5), 719-729, https://doi.org/10.1080/17445647.2014.957251, 2015.
- Huggenberger, P. and Wildi, W.: La tectonique du massif des Bornes (Chaînes Subalpines, Haute-Savoie, France), Eclogae Geologicae 20 Helvetiae, 84 (1), 125–149, https://doi.org/https://doi.org/10.5169/seals-166766, 1991.
 - Karbalaali, H., Javaherian, A., Dahlke, S., Reisenhofer, R., and Torabi, S.: Seismic channel edge detection using 3D shearlets-a study on synthetic and real channelised 3D seismic data, Geophysical Prospecting, 66 (7), 1272–1289, https://doi.org/10.1111/1365-2478.12629, 2018.
- 25 King, E. J., Reisenhofer, R., Kiefer, J., Lim, W.-Q., Li, Z., and Heygster, G.: Shearlet-based edge detection: flame fronts and tidal flats, in: Applications of Digital Image Processing XXXVIII, SPIE Optical Engineering + Applications, 2015, San Diego, California, United States, edited by Tescher, A. G., no. 959905 in Proc. SPIE, 9599, https://doi.org/10.1117/12.2188652, 2015.
 - Kovesi, P.: Image features from phase congruency, Videre: Journal of computer vision research, 1, 1-26, http://ftp.cs.rochester.edu/~brown/ Videre/001/articles/v1n3001.pdf, 1999.
- 30 Kovesi, P.: Phase Psychological congruency: А low-level image invariant, Research, 64 (2),136 - 148,https://doi.org/10.1007/s004260000024, 2000.
 - Kutyniok, G. and Labate, D., eds.: Shearlets Multiscale Analysis for Multivariate Data, Applied and Numerical Harmonic Analysis Book Series, Birkhäuser, Basel, Applied and Numerical Harmonic Analysis, Birkhäuser Basel, 2012 edn., https://doi.org/10.1007/978-0-8176-8316-0.2012.
- Labate, D., Lim, W.-Q., Kutyniok, G., and Weiss, G.: Sparse multidimensional representation using shearlets, in: Wavelets XI, Optics and 35 Photonics 2005, 31 July - 4 August 2005, San Diego, California, United States, 59140U, https://doi.org/10.1117/12.613494, 2005.
 - Le Pennec, E. and Mallat, S.: Sparse Geometric Image Representations with Bandelets, IEEE Transactions on Image Processing, 14 (4), 423-438, https://doi.org/10.1109/TIP.2005.843753, 2005.

- Long, J. J., Jones, R. R., and Daniels., S. E.: Reducing uncertainty in fracture modelling: assessing the sensitivity of inputs from outcrop analogues, in: The Geology of Fractured Reservoirs, 24-25 October 2018, The Geological Society of London, The Geological Society of London, oral Presentation, 2018.
- Mabee, S. B., Hardcastle, K. C., and Wise, D. U.: A Method of Collecting and Analyzing Lineaments for Regional-Scale Fractured-Bedrock Aquifer Studies, Groundwater, 32 (6), 884–894, https://doi.org/10.1111/j.1745-6584.1994.tb00928.x, 1994.
- Mallat, S. and Hwang, W. L.: Singularity detection and processing with wavelets, IEEE Transactions on Information Theory, 38 (2), 617–643, https://doi.org/10.1109/18.119727, 1992.
 - Masoud, A. and Koike, K.: Applicability of computer-aided comprehensive tool (LINDA: LINeament Detection and Analysis) and shaded digital elevation model for characterizing and interpreting morphotectonic features from lineaments, Computers & Geosciences, 106, 80, 100, https://doi.org/10.1016/j.aageo.2017.06.006.2017
- 10 89–100, https://doi.org/10.1016/j.cageo.2017.06.006, 2017.

- National Research Council: Rock Fractures and Fluid Flow: Contemporary Understanding and Applications, Washington, DC, The National Academies Press, Washington, DC, 1996 edn., https://doi.org/10.17226/2309, 1996.
- Olson, J. E., Laubach, S. E., and Lander, R. H.: Natural fracture characterization in tight gas sandstones: Integrating mechanics and diagenesis, AAPG Bulletin, 93 (11), 1535–1549, https://doi.org/10.1306/08110909100, 2009.
- 15 Otsu, N.: A Threshold Selection Method from Gray-Level Histograms, IEEE Transactions on Systems, Man, and Cybernetics, 9 (1), 62–66, https://doi.org/10.1109/TSMC.1979.4310076, 1979.
 - Peacock, D., Sanderson, D., Bastesen, E., Rotevatn, A., and Storstein, T.: Causes of bias and uncertainty in fracture network analysis, Norwegian Journal of Geology, 99(1), https://doi.org/10.17850/njg99-1-06, 2019.
 - Prabhakaran, R.: rahulprabhakaran/Automatic-Fracture-Detection- Code(supplement to Solid Earth Manuscript se-2019-104),
- 20 https://doi.org/10.5281/zenodo.3245452, 2019.
 - Prabhakaran, R., Boersma, Q., Bezerra, F., and Bertotti, G.: Fracture Network Patterns from the Brejões Outcrop, Irecê Basin, Brazil, 4TU Centre for Research Data. Dataset, https://doi.org/10.4121/uuid:67cde05c-9e99-4cc4-8cec-9f2666457d1f, 2019a.
 - Prabhakaran, R., Bruna, P.-O., Bertotti, G., Smeulders, D., and Meda, M.: Fracture Network Patterns from the Parmelan Anticline, France, 4TU Centre for Research Data. Dataset, https://doi.org/10.4121/uuid:3f5e255f-edf7-441f-89f2-1adc7ac2f7d1, 2019b.
- 25 Prewitt, J.: Object enhancement and extraction, in: Picture Processing and Psychopictorics, pp. 75–149, Academic Press, New York, 1970. Reisenhofer, R.: The complex shearlet transform and applications to image quality assessment, Master's thesis, Technical University of Berlin, 2014.
 - Reisenhofer, R. and King, E. J.: Edge, Ridge, and Blob Detection with Symmetric Molecules, SIAM Journal on Imaging Sciences, 12(4), 1585–1626, https://doi.org/10.1137/19M1240861, 2019.
- 30 Reisenhofer, R., Kiefer, J., and King, E. J.: Shearlet-based detection of flame fronts, Experiments in Fluids, 57, 41, https://doi.org/10.1007/s00348-016-2128-6, 2016.
 - Ren and Malik: Learning a classification model for segmentation, in: Proceedings Ninth IEEE International Conference on Computer Vision, pp. 10–17 vol.1, https://doi.org/10.1109/ICCV.2003.1238308, 2003.
- Sander, P., Minor, T. B., and Chesley, M. M.: Ground-Water Exploration Based on Lineament Analysis and Reproducibility Tests, Ground water, 35 (5), 888–894, https://doi.org/10.1111/j.1745-6584.1997.tb00157.x, 1997.
- Scheiber, T., Fredin, O., Viola, G., Jarna, A., Gasser, D., and Łapińska Viola, R.: Manual extraction of bedrock lineaments from highresolution LiDAR data: methodological bias and human perception, Geologiska Föreningen i Stockholm (GFF), 137 (4), 362–372, https://doi.org/10.1080/11035897.2015.1085434, 2015.

- Sobel, I. and Feldman, G.: A 3x3 isotropic gradient operator for image processing, presented at the Stanford Artificial Intelligence Project (SAIL) in 1968, pp. 271–272, John Wiley & Sons, 1973.
- Thiele, S. T., Grose, L., Samsu, A., Micklethwaite, S., Vollgger, S. A., and Cruden, A. R.: Rapid, semi-automatic fracture and contact mapping for point clouds, images and geophysical data, Solid Earth, 8 (6), 1241–1253, https://doi.org/10.5194/se-8-1241-2017, 2017.
- 5 Thomas, R. N., Paluszny, A., and Zimmerman, R. W.: Effect of Fracture Growth Velocity Exponent on Fluid Flow through Geomechanicallygrown 3D Fracture Networks, in: 2nd International Discrete Fracture Network Engineering Conference, 20-22 June 2018, Seattle, Washington, USA, ARMA-DFNE-18-0239, Seattle, Washington, USA, https://www.onepetro.org/conference-paper/ARMA-DFNE-18-0239, 2018.

Thovert, J.-F., Mourzenko, V., and Adler, P.: Percolation in three-dimensional fracture networks for arbitrary size and shape distributions, Physical Review E. 95 (4), 042 112, https://doi.org/10.1103/PhysRevE.95.042112, 2017.

- Tu, C.-L., Hwang, W.-L., and Ho, J.: Analysis of singularities from modulus maxima of complex wavelets, IEEE Transactions on Information Theory, 51 (3), 1049–1062, https://doi.org/10.1109/TIT.2004.842706, 2005.
- Turner, D., Lucieer, A., and Watson, C.: An Automated Technique for Generating Georectified Mosaics from Ultra-High Resolution Unmanned Aerial Vehicle (UAV) Imagery, Based on Structure from Motion (SfM) Point Clouds, Remote Sensing, 4 (5),
- 15 https://doi.org/10.3390/rs4051392, 2012.

- Ukar, E., Laubach, S. E., and Hooker, J. N.: Outcrops as guides to subsurface natural fractures: Example from the Nikanassin Formation tight-gas sandstone, Grande Cache, Alberta foothills, Canada, Marine and Petroleum Geology, 103, 255–275, http://www.sciencedirect. com/science/article/pii/S0264817219300492, 2019.
- Vasuki, Y., Holden, E.-J., Kovesi, P., and Micklethwaite, S.: Semi-automatic mapping of geological Structures using UAV-based photogram-
- 20 metric data: An image analysis approach, Computers & Geosciences, 69, 22–32, https://doi.org/10.1016/j.cageo.2014.04.012, 2014.
 Vasuki, Y., Holden, E.-J., Kovesi, P., and Micklethwaite, S.: An interactive image segmentation method for lithological boundary detection:
 A rapid mapping tool for geologists, Computers & Geosciences, 100, 27–40, https://doi.org/10.1016/j.cageo.2016.12.001, 2017.
 - Wang, Z., Bovik, A., Sheikh, H., and Simoncelli, E.: Image quality assessment: from error visibility to structural similarity, IEEE Transactions on Image Processing, 13 (4), 600–612, https://doi.org/10.1109/TIP.2003.819861, 2004.
- 25 Yi, S., Labate, D., Easley, G. R., and Krim, H.: A Shearlet Approach to Edge Analysis and Detection, IEEE Transactions on Image Processing, 18 (5), 929–941, https://doi.org/10.1109/TIP.2009.2013082, 2009.
 - Zhang, T., Tilke, P., Dupont, E., Zhu, L., Liang, L., and Bailey, W.: Generating Geologically Realistic 3D Reservoir Facies Models Using Deep Learning of Sedimentary Architecture with Generative Adversarial Networks, in: International Petroleum Technology Conference, 26-28 March 2019, Beijing, China, IPTC-19454-MS, International Petroleum Technology Conference, Beijing, China,
- 30 https://doi.org/10.2523/IPTC-19454-MS, 2019.



Figure 1. The Automated Fracture Trace Detection Workflow

The Automated Fracture Trace Detection Workflow



Figure 2. Effects of variation of parameters on extracted ridges using a fractured siliclastic example. The parameter that is varied, low (on left) and high (on right) is highlighted in blue within the table adjacent to each ridge image.



Figure 3. Illustration of the steps involved in the automatic fracture extraction using a 40 x 34 mm fractured shale core image (a) CT scan core image from Dwarkasing (2016) (b) Normalized ridge ensemble (c) Segmentation applied on the ridge ensemble (d) Skeletonization applied to the segmented ridge (e) Vectorized polylines fitted to the skeletonized clusters (f) Effect of line simplification applied to a single vectorized segment

Variation of the Structural Similarity Index of of base case ridges with shearlet and detection parameters (a) SSIM vs Anisotropy Exponent (b) SSIM vs MinContrast (c) SSIM vs Wavelet Effective Support (d) SSIM vs Scaling Offset (e) SSIM vs Scales / Octave (f) SSIM vs Shearlevels

Figure 4. Effect of multiple ridge realizations on a sample image from Parmelan Anticline, France (a) Base Case image used for testing the effect of multiple ridge realizations (b) Ridge map obtained using the base case shearlet parameters in Table. 3 (c) Overlay of ridges obtained using base case shearlet parameters over the test image (d) Normalized ridge intensity ensemble map obtained after 1050 ridge realizations using the parameters in Table. 4 (e) Threshold ridge intensity map that enhances features (f) Overlay of ridges using the threshold ridge intensities over the test image





Figure 5. Location of the Parmelan plateau in France within the Bornes Massif depicting drone flight base points for six drone missions



Figure 6. Drone photogrammetry coverage area from the Parmelan (a) Region within the Parmelan plateau highlighting the areal extent of the drone photogrammetric orthomosaics which are projected over the base map. Manually traced large scale faults are depicted in red. (b) Spatial extent of the drone coverage of each of the six UAV flight missions in different colours



Figure 7. Trace extraction results from the Parmelan (a) Selected tiles from the orthomosaic spatial extent are highlighted (b) Spatial variation of the fracture intensity depicted as a P₂₁ plot computed using the box counting method



Figure 8. Comparison between automatic and manual interpretation on a tile from the Parmelan (a) Tile from the Parmelan orthomosaic depicting intense fracturing with an organization along the NW-SE corridors (b) Overlay of fractures traced using the automatic detection method (c) Overlay of fractures manually traced for the tile at a zoom of 1:2000 (d) P_{21} Fracture intensity for automatic extracted fractures (e) P_{21} Fracture intensity for manually extracted fractures (f) Length weighted rose plot and cumulative trace length frequency distribution for the automated result (g) Length weighted rose plot and cumulative trace length frequency distribution for the manual result











Figure 11. Comparison of trace length weighted rose plots and cumulative trace length distributions for automatic and manual trace interpretations from Brejões outcrop stations



Figure 12. Comparison of Benchmark Image 1 (a) Bingie Area 21 from Thiele et al. (2017) (b) Normalized ridge map using complex shearlet automatic extraction (c) Threshold applied to the normalized ridges (d) Binarized ridges map (e) Vectorized automatic traces (f) Length weighted rose plot of the automatic interpreted traces (g) Cumulative frequency plot of the automatic interpreted traces (h) Assisted cleaned up trace map for Area 1 (i) Length weighted rose plot of the assisted traces (i) Cumulative frequency plot of the assisted traces (k) Assisted trace interpretation modified from Thiele et al. (2017) for comparison



Figure 13. Comparison of Benchmark Image 2 (a) Bingie Bingie Area 2 from Thiele et al. (2017) (b) Normalized ridge map using complex shearlet automatic extraction (c) Threshold applied to the normalized ridges (d) Binarized ridges map (e) Vectorized automatic traces (f) Length weighted rose plot of the automatic interpreted traces (g) Cumulative frequency plot of the automatic interpreted traces (h) Assisted cleaned up trace map for Area 2 (i) Length weighted rose plot of the assisted traces (i) Cumulative frequency plot of the assisted traces (k) Assisted trace interpretation modified from Thiele et al. (2017) for comparison

Parameter	er Description			
waveletEffSupp	Length of the effective support in pixels of the wavelet			
gaussianEffSupp	Length of the effective support in pixels of the Gaussian filter			
scalesPerOctave	Number of intermediate scales for each octave			
shearLevel	Number of differently oriented shearlets on each scale			
alpha	Degree of anisotropy introduced via scaling			
octaves	Number of octaves spanned by the shearlet system			

Shearlet system and detection parameters used to extract ridges for the base case **Base Case Parameters** waveletEffSupp 125 gaussianEffSup 63 scalesPerOctave 2 shearLevel 3 alpha 0.5 octaves 3.5 minContrast 10 detection negative ridges even/odd offset 1-

Table 2. Detection Parameters

Parameter	Description		
DetectionType	Specification of detection measure (edge/ridge)		
minContrast	Specification of the level of contrast for edge/ridge detection		
offset	Scaling offset between the even- and odd- symmetric shearlets		

Table 3. Shear	let system and	detection parameters us	ed to extract ridges	for the base case
~~~~			~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	

Base Case Parameters	
waveletEffSupp	125
gaussianEffSup	~~~~
scalesPerOctave	<u>63</u>
	2 ~
shearLevel	3
<u>alpha</u>	0.5
octaves.	3.5
minContrast	2. <u>.</u> ~
detection	10
	negative
	ridges
even/odd offset	1

## Table 4. Ensemble for Parameter Variation

Parameter	Values
waveletEffSupp	Original image size in pixels divided by 5, 8, 10, 12 and 15
gaussianEffSupp	Original image size in pixels divided by 5, 8, 10, 12 and 15
scalesPerOctave	1,2,3 and 4
shearLevel	2,3 and 4
alpha	0, 0.25, 0.5, 0.75, 1
minContrast	1, 5, 10, 15, 20
even/odd offset	0.001, 0.01, 0.1, 1, 2



Figure A1. (a). Isotropic elements capturing a discontinuity curve (b). Sheared, anisotropic elements capturing a discontinuity curve (modified from Kutyniok and Labate, 2012)



**Figure A2.** The cone adapted continuous shearlet system (a) Bias in directions is handled by dividing the frequency plane into 4 cones  $C_1$ ,  $C_2$ ,  $C_3$ ,  $C_4$  and a square low frequency box region in the centre  $\mathcal{R}$  (b) Trapezoidal shaped wedge tiling of the frequency induced domain induced by the shearlet transform (modified after Kutyniok and Labate 2012)



Figure A3. Variation of the Structural Similarity Index of of base case ridges with shearlet and detection parameters (a) SSIM vs Anisotropy Exponent (b) SSIM vs MinContrast (c) SSIM vs Wavelet Effective Support (d) SSIM vs Scaling Offset (e) SSIM vs Scales / Octave (f) SSIM vs Shearlevels

Shearlet System	waveletEffSupp	gaussianEffSupp	scalesPerOctave	shearLevel	scales	nShearlets	alpha
1	200	100	1	2	1	36	0
2	125	63	1	2	1	36	0
3	84	42	1	2	1	36	0
4	67	34	1	2	1	36	0
5	200	100	2	2	7	12	0
6	125	63	2	2	7	12	0
7	84	42	2	2	7	12	0
8	67	34	2	2	7	12	0
9	200	100	3	2	10.5	12	0
10	125	63	3	2	10.5	12	0
11	84	42	3	2	10.5	12	0
12	67	34 100	3	2	10.5	12	0
13	200	62	4	2	14	12	0
14	84	42	4	2	14	12	0
16	67	34	4	2	14	12	0
17	200	100	1	3	3.5	20	0
18	125	63	1	3	3.5	20	Õ
19	84	42	1	3	3.5	20	0
20	67	34	1	3	3.5	20	0
21	200	100	2	3	7	20	0
22	125	63	2	3	7	20	0
23	84	42	2	3	7	20	0
24	67	34	2	3	7	20	0
25	200	100	3	3	10.5	20	0
26	125	63	3	3	10.5	20	0
27	84	42	3	3	10.5	20	0
28	67	34	3	3	10.5	20	0
29	200	100	4	3	14	20	0
30	125	63	4	3	14	20	0
31	84	42	4	3	14	20	0
32	6/ 200	34 100	4	3	14	20	0
33 24	200	100	1	4	3.3 2.5	30 36	0
25	12J 94	42	1	4	2.5	30	0
35	64 67	42	1	4	3.5	36	0
30	200	100	2	4	7	36	0
38	125	63	2	4	7	36	0
39	84	42	2	4	7	36	0
40	67	34	2	4	7	36	Õ
41	200	100	3	4	10.5	36	0
42	125	63	3	4	10.5	36	0
43	84	42	3	4	10.5	36	0
44	67	34	3	4	10.5	36	0
45	200	100	4	4	14	36	0
46	125	63	4	4	14	36	0
47	84	42	4	4	14	36	0
48	67	34	4	4	14	36	0
49	200	100	1	2	3.5	12	0.5
50	125	63	1	2	3.5	12	0.5
51 52	84 67	42	1	2	5.5 2.5	12	0.5
52 52	200	54 100	1	2	3.3 7	12	0.5
55 54	200	63	2	2	7	12	0.5
55	84	42	$\frac{1}{2}$	$\frac{2}{2}$	7	12	0.5
56	67	34	2	2	7	12	0.5
57	200	100	3	$\frac{1}{2}$	10.5	12	0.5
58	125	63	3	2	10.5	12	0.5
59	84	42	3	2	10.5	12	0.5
60	67	34	3	2	10.5	12	0.5
61	200	100	4	2	14	12	0.5
62	125	63	4	2	14	12	0.5
63	84	42	4	2	14	12	0.5
64	67	34	4	2	14	12	0.5
65	200	100	1	3	3.5	20	0.5
66	125	63	1	3	3.5	20	0.5
67	84	42	1	3	3.5	20	0.5
68	67	34	1	3	3.5	20	0.5
69	200	100	2	3	7	20	0.5
/0	125	63	2	3	7	20	0.5