

1 **A review and evaluation of the methodology for digitising 2D** 2 **fracture networks and topographic lineaments in GIS**

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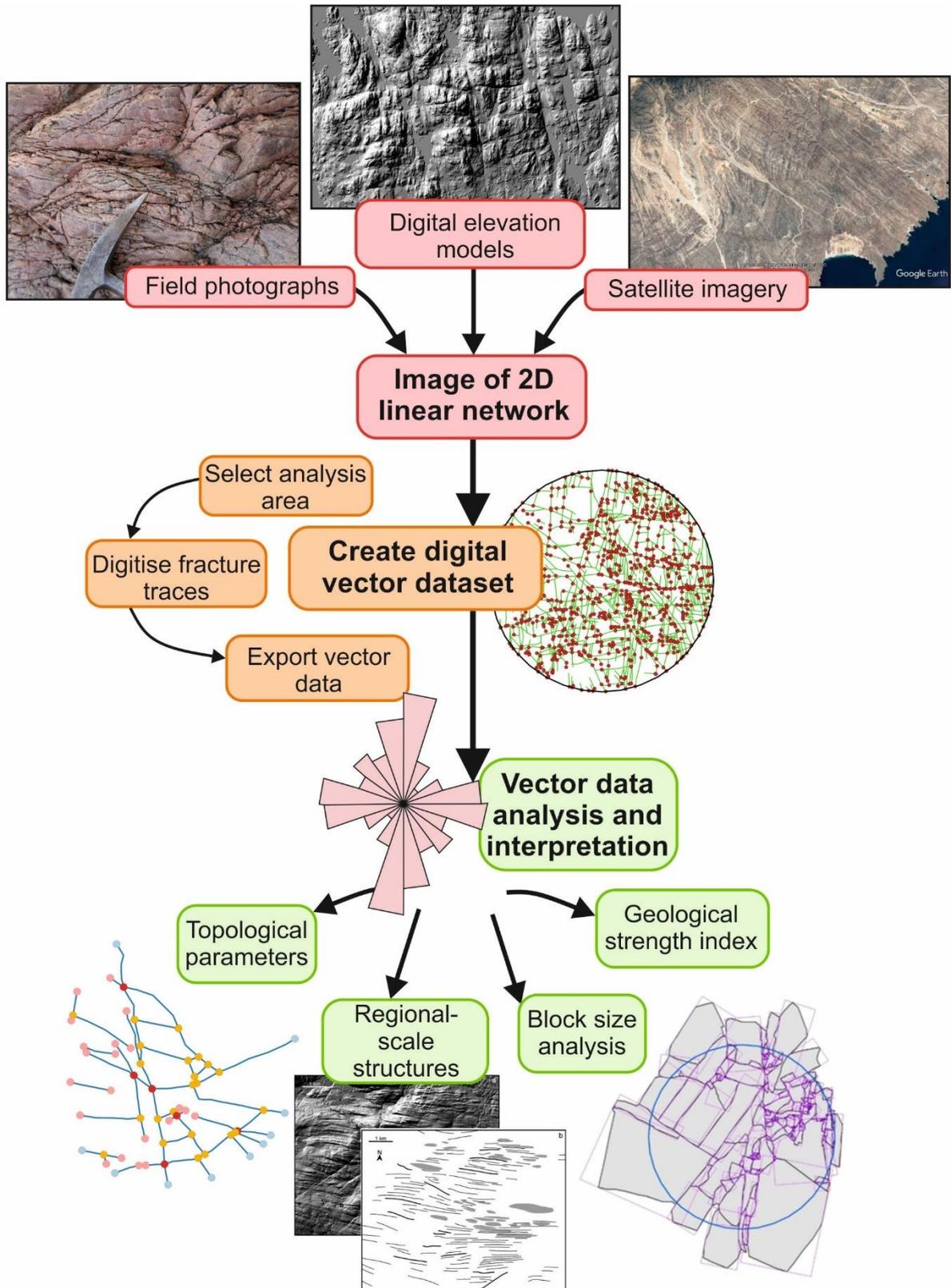
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6 **Abstract.** Understanding the impact of fracture networks on rock mass properties is an essential part of
7 a wide range of applications in geosciences, from understanding permeability of groundwater aquifers
8 and hydrocarbon reservoirs to erodibility properties and slope stability of rock masses for geotechnical
9 engineering. However, gathering high quality, oriented-fracture datasets in the field can be difficult and
10 time consuming, for example due to constraints on time or access (e.g. cliffs). Therefore, a method for
11 obtaining accurate, quantitative fracture data from photographs is a significant benefit. In this paper we
12 describe and evaluate the method for generating a series of digital fracture traces in GIS-environment,
13 in which spatial analysis of a fracture network can be carried out. The method is not meant to replace
14 the gathering of data in the field, but to be used in conjunction, and is well suited where fieldwork time
15 is limited, or where the section cannot be accessed directly. The basis of the method is the generation
16 of the vector dataset (shapefile) of a fracture network from a georeferenced photograph of an outcrop
17 in a GIS environment. From that shapefile, key parameters such as fracture density and orientation can
18 be calculated. Furthermore, in the GIS-environment more complex spatial calculations and graphical
19 plots can be carried out such as heat maps of fracture density. There are a number of advantages to
20 using a digital method for gathering fracture data including: time efficiency, generating large fracture
21 network datasets, flexibility during data gathering and consistency of data.

22 **1 Introduction**

23 Fractures are the main pathways of fluid flow in rocks, and exert a strong influence on rock mass
24 properties. The characterisation of fracture networks is an essential aspect of various applications in
25 earth science, for example to understand and predict the behaviour of fluid flow in groundwater aquifers
26 (Singhal and Gupta, 2010; Follin et al. 2014) and hydrocarbon reservoirs, and the erodibility and slope
27 stability of rock masses. Fracture network data are essential for assessing future sites of nuclear waste
28 repositories, predicting rock slope stability (Selby, 1982; Park et al., 2005) and understanding intact
29 rock strength for engineering of infrastructure (Hoek and Brown, 1997; Zhan et al., 2017; Ren et al.,
30 2017). For 2D fracture network analysis, there are a number fracture parameters that are widely used,
31 including orientation, spacing, length, density/intensity and various connectivity proxies (summarised
32 in Singhal and Gupta, 2010; Sanderson and Nixon, 2015; Peacock et al., 2016; Laubach et al., 2019).
33 In this paper, we present and evaluate a 2D digital fracture network analysis method that is commonly
34 in use in structural geology, and through numerous case studies we demonstrate the wider potential of

35 this method for other users, for example geotechnical engineers, groundwater modellers and
36 geomorphologists (Figure 1).



38 **Figure 1:** Flowchart providing an overview of the methodology used for digitising linear features, from preparing
39 an image, digitising the features to output of data. Digital elevation model examples are taken from Next
40 map © in Scotland, and the satellite image of Oman example is taken from Google Earth ©.

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42 Fracture networks can be characterised in different dimensions using a number of approaches. 1D
43 approaches include borehole fracture analysis and outcrop-based scanline surveys, typically represented
44 by the number of fractures per unit length, i.e. frequency. 1D approaches are relatively rapid, but cannot
45 directly constrain certain parameters such as fracture length and connectivity: if the fracture network is
46 anisotropic (which is commonly the case), the characterisation is biased by the orientation of the
47 scanline or the borehole ('orientation bias'; Singhal and Gupta, 2010; Zeeb et al. 2013b; Watkins et al.
48 2015b). 3D (really 2.5D) outcrop analysis using laser scanning provides a fuller analysis (e.g. Pless et
49 al., 2015) but requires expensive equipment and is time-consuming in its processing. Unmanned Aerial
50 Vehicles (UAVs) are used to generate high resolution images of an outcrop, with 3D information
51 generated with techniques such as structure from motion (SfM) photogrammetry (Vasuki et al., 2014).
52 True 3D characterisation is possible using CT scanning, but is restricted to very small samples (Voorn
53 et al. 2015). As a compromise, many studies employ a 2D approach. Normally, this uses some form of
54 characterisation within a circular window on a rock outcrop (Davies et al, 1996; Rohrbaugh et al. 2002;
55 Watkins et al. 2015a). Generally, for 2D analysis a circular scanline or window approach is taken. In
56 the former fractures intersecting the circular line are recorded, whereas in the latter fractures within the
57 window area are recorded. Circular scanline methods are more rapid than full 2D circular window
58 methods and have less length and orientation bias compared to 1D methods. A circular scanline can be
59 used to calculate proxies for fracture density and length based on the ratio of the types of trace
60 intersection (Mauldon et al. 2001). However, circular scanline methods lack the full analysis of a
61 complete 2D circular window approach. Connectivity within two-dimensional fracture networks was
62 parameterized by Manzocchi (2002), who characterised the different types of fracture intersections that
63 can be used to characterise fluid percolation potential. A complete understanding of the fluid flow
64 properties of a fracture network requires a broader understanding of 3D fracture network connectivity
65 factors, such as fracture fill and aperture (Laubach et al., 2019).

66 Field-based 2D fracture network analysis is commonly carried out by using a circular 'chalk line' on
67 an outcrop and measuring the fractures within the circular window. The benefit of the field-based
68 method is an accurate data set that includes a range of parameters from fracture geometry (Singhal and
69 Gupta, 2010) such as length and orientations, fracture network parameters (Singhal and Gupta, 2010)
70 such as density and spacing, network topology (Sanderson and Nixon, 2019) such as percolation
71 potential, and clustering and fracture character (Laubach et al., 2019) such as aperture and paragenesis
72 history. However, there are a number of limitations when gathering fracture network data in the field.
73 Firstly this can be very time consuming particularly when collecting large datasets across a large field

74 area. Secondly, some outcrops such as quarries or unstable cliffs may not be impractical or unsafe to
75 access for making fracture measurements. Thirdly, collecting fracture network data from larger fracture
76 networks of greater than 10 m can be challenging in the field, particularly when collecting fracture data
77 from an entire outcrop. Finally, more evolved modern fracture network analysis and modelling often
78 require a digital set of the fracture network traces.

79 The digital fracture trace method has been used for data collection in a range of structural geology
80 studies, including multiscale fracture network models (Strijker et al., 2012), the development of 3D
81 fracture models (Tavani et al., 2016; Menegoni et al., 2019) and developing discrete fracture networks
82 (DFNs) to model fluid flow (Bisdom et al., 2017). This methodology is used as the basis of data
83 generation in a broad range of structural studies, and this paper provides an evaluation of the method
84 that will be helpful to improve the quality of data collection.

85 Building on previous work (Krabbendam and Bradwell, 2014; Pless et al., 2015; Watkins et al., 2015a;
86 Krabbendam et al. 2016; Healy et al., 2017) we present and develop a method for capturing a 2D fracture
87 network as a digital (GIS) dataset from outcrop photographs. From this dataset, numerous key spatial
88 relationships and parameters can be calculated. The only equipment needed are a high-quality digital
89 camera, a measuring stick and GIS software (e.g. open source QGIS) for digitisation and analysis. This
90 method can also be applied to georeferenced (orthorectified) aerial photos, hillshaded DTMs and
91 satellite imagery for the characterisation of topographic lineaments. In addition, historic photos from
92 now-infilled excavations or quarries can be used, as long as the photos have a useable scale. The method
93 provides a relatively rapid and accessible way to generate accurate 2D fracture datasets and will be
94 beneficial for a wide range of users including engineering geologists and hydrogeologists.

95 **2 Digital 2D fracture analysis method**

96 The method in essence captures a set of digital traces (vectors) of a 2D linear feature network in a GIS
97 project from a georeferenced image. Here, we use open source GIS software (QGIS), making the
98 method accessible to all potential users. A number of open tools within QGIS can be used for more
99 advanced analysis of the digitised fracture network.

100 **2.1 Outcrop selection**

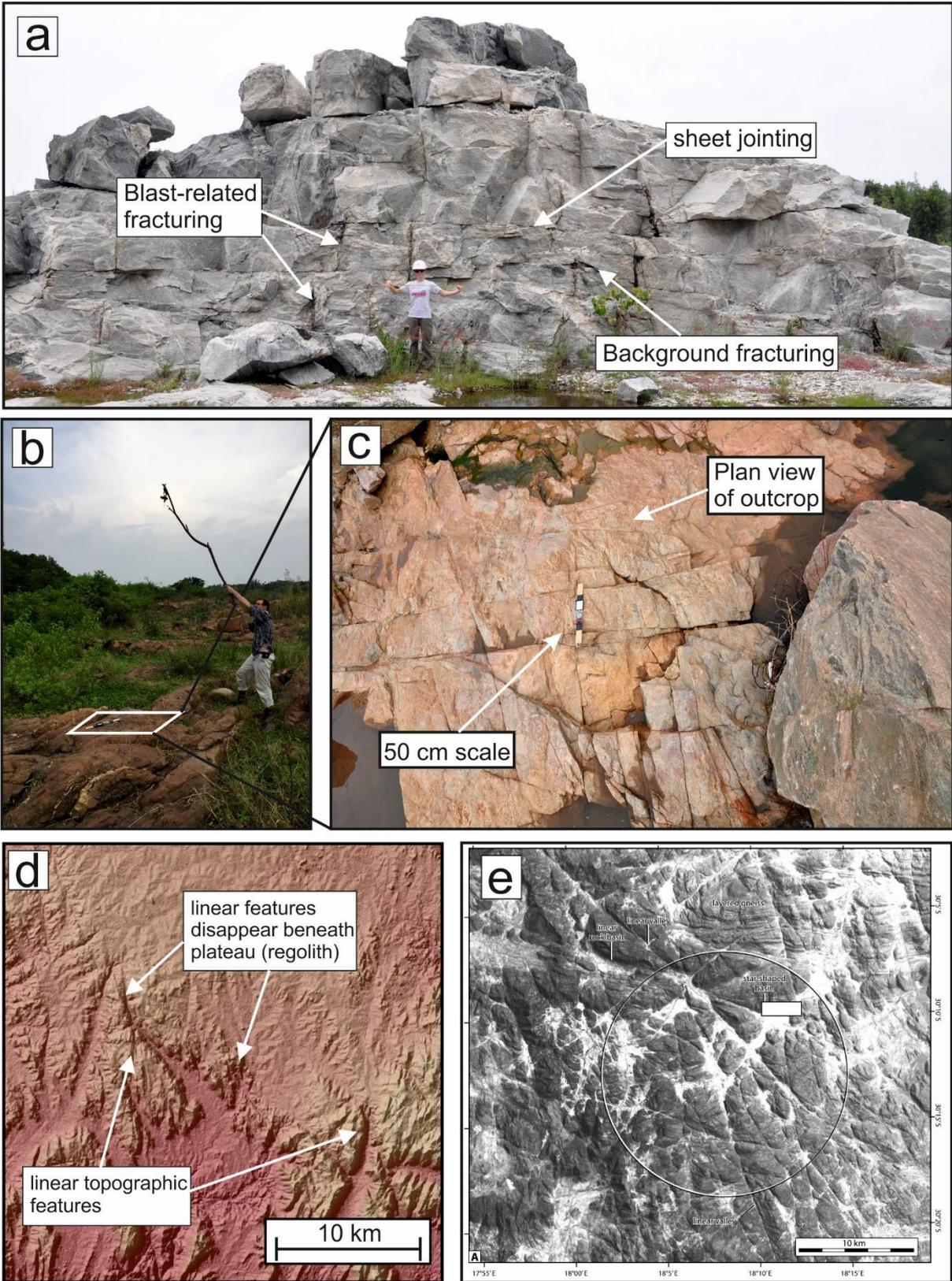
101 A suitable outcrop for digital fracture analysis must be first selected. Where spatial understanding of
102 the distribution or diversity of fracture characteristics in a region is an important element of study, the
103 implications of site selection choice on subsequent spatial analysis must also be considered. The outcrop
104 selected will depend on the nature of the study being undertaken and the type of fracture network
105 parameters required. It is important to consider whether the outcrop is representative of the rock mass
106 as a whole or whether multiple sites would better represent the diversity or distributions of fracture
107 characteristics. Outcrop selection has significant implications on the final results, i.e. whether the

108 outcrop is a proxy for wider-scale fracture network characteristics at depth or if it is the outcrop itself
109 that is being studied in isolation at the surface (Laubach et al 2019; Ukar et al 2019).

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111 **2.2 Outcrop image preparation**

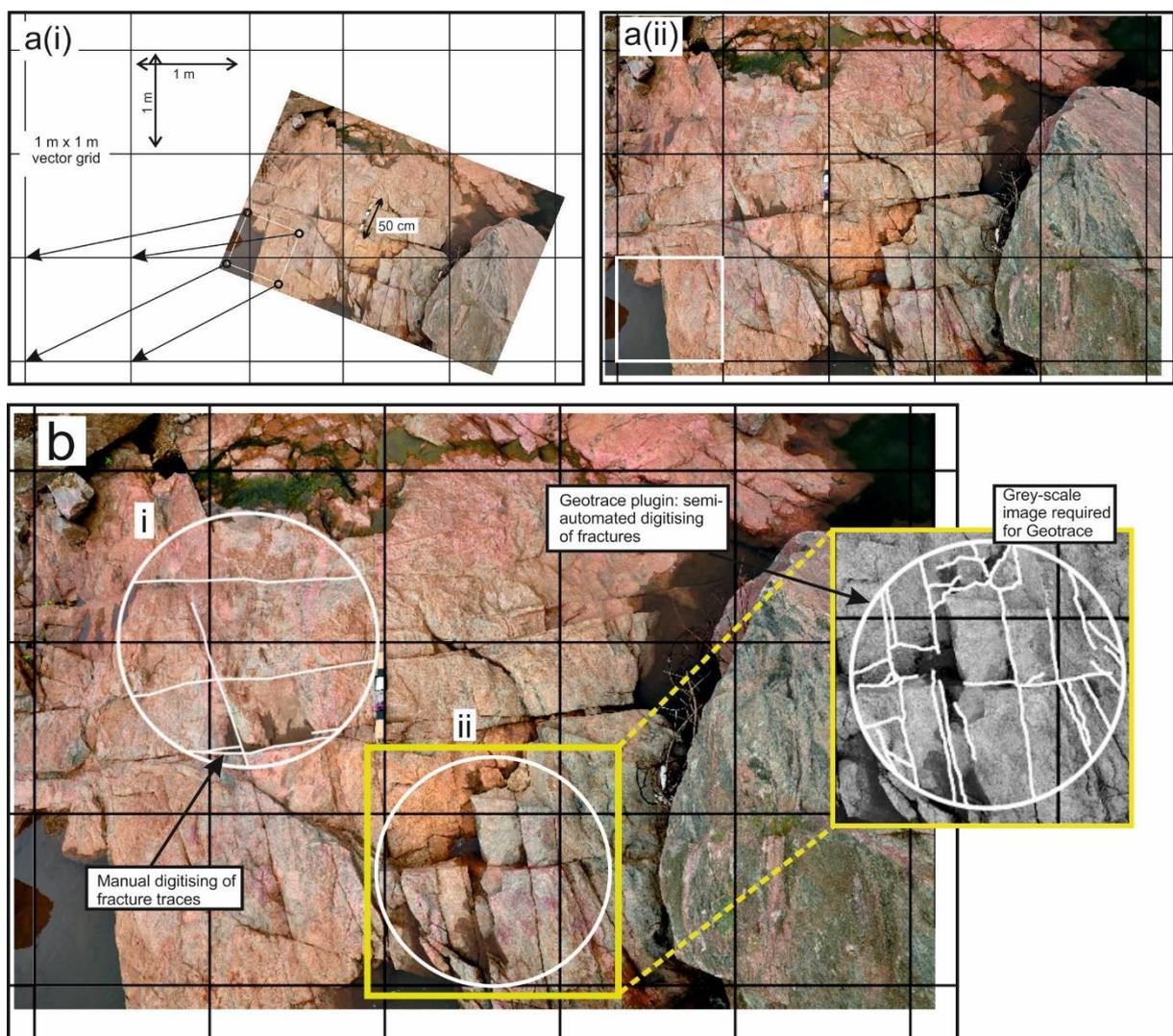
112 The first step is to prepare a suitable photograph or image of the outcrop to be analysed. The image can
113 be a photograph of a fracture network at outcrop of various scales from centimetres to 10s of metres. It
114 is important that the fractures can be clearly identified in the photograph, and that not too much of the
115 image is occupied by vegetation or broken ground (Figure 2a). It is important to include an accurate
116 and clearly identifiable scale; a strip of plywood with duct tape works very well. However, in some
117 dangerous outcrops (e.g. working quarries) this may be impractical and quarry machinery or other
118 features of known dimensions may be used as a scale in the photograph. The photograph should be
119 taken at right angles (or as much as possible) to the outcrop to minimise the issues created by a distortion
120 of the image. The camera should have a focal length of 35mm (analogue 35 mm equivalent) or longer,
121 to prevent further distortion. Horizontal outcrops should be photographed vertically to again minimise
122 the distortion of the fractures. Mounting the camera on a stick is useful to increase the distance and
123 capture a larger field of view (Figure 2b, c); or drones could also be used. For horizontal outcrops it is
124 convenient to orient the measuring stick accurately to the north, using a compass (Figure 2c), this will
125 help in capturing the correct orientations of the fractures.



126
 127 **Figure 2:** Examples of photographs and DEM images that can be used for digitising 2D linear features, including:
 128 (a-c) photographs of fracture networks of various scale from southern India and improvised methods for taking
 129 parallel photographs; (d) a DEM image from southern India of larger kilometre scale features that could also be
 130 digitised; and (e) an aerial photography from Namibia (adapted from Krabbendam and Bradwell, 2014).

132 **2.3 Georeferencing the images**

133 To aid robust georeferencing, the photograph needs to have a square of known size (e.g. 1 x 1 m)
134 embedded in it. This can be done by importing the photograph into a graphics software package (such
135 as Inkscape), and drawing a square based on the scale included in the original photograph (Figure 3).
136 The photograph with the embedded 1 x 1 m square is then imported into a new GIS project file. The
137 GIS project file needs a projection in metres; we recommend a Mercator projection, (such as
138 EPSG:3857). Within the GIS project, a ‘vector grid’ (fishnet grid) is created, with a grid extent that is
139 larger than the imported photograph and with a vertical and horizontal spacing of 1.0 m. Finally,
140 georeference the square on the photograph to a square on the fishnet grid, thus creating a georeferenced
141 photograph within the GIS project (Figure 3a).



142

143 **Figure 3:** Images showing (a (i-ii)) how to georeference an image to a fishnet grid (black) from a square of a
144 known scale (white); and (b) the tools available for digitising fractures in QGIS, including (i) a fully manual
145 method; and (ii) a semi-automatic method such as Geotrace.

146 **2.4 Using DEM, satellite and airphoto images**

147 DEMs (Digital Elevation Models) (and their hill-shaded derivatives), satellite images and
148 (orthorectified) aerial photographs commonly show good topographic lineaments that likely represent
149 fracture zones, or master joints (Fig. 2d,e). Such imagery if georeferenced can be used directly without
150 further preparation. It should be noted however that aerial photographs, DEMs and satellite images do
151 not directly show fracture traces, rather they show the topographic expression of these. Thus, fracture
152 density is likely to be underestimated, because fractures without topographic expression will not be
153 captured. Figure 2d is an example of a DEM image from southern India showing kilometre-scale 2D
154 topographic lineaments: in some parts lineaments are well developed, in other parts fracture zones have
155 no expression and presumably occur beneath a continuous layer of regolith. Furthermore, such imagery
156 is limited by the on-ground resolution, so that smaller-scale (smaller aperture) fractures may not appear.
157 Hill-shade DEM images, as well as satellite imagery and aerial photographs have the problem of bias
158 by a particular direction of illumination, so that lineaments of one orientation may be clearer than others.
159 For DEMs, hill-shades derivatives with different illumination direction can be made; for satellite
160 imagery, sometimes imagery taken at a different time of day are available. Lineaments in DEM images
161 also have the problem of illumination, which may result in bias depending on the orientation of the
162 lineament relative to the illumination orientation. Hence, for DEM-scale interpretations it is important
163 to take a multi-data type approach (e.g. geological maps and satellite images) to guide digitisation,
164 similar to that of Pless (2012).

165 **2.5 Data capture**

166 **2.5.1 Select analysis window**

167 Different 2D lineament analysis windows can be used with this method including line scanlines, areal
168 sampling and circular windows. For each of these methods a different shaped sample window is
169 required. For this create a line or polygon shapefile and digitise the area that is to be analysed. An
170 example is shown in Figure 3b as two circular windows, in white, digitised onto a photograph in GIS.
171 It is important to create a different id number for each shape that includes details of the photograph or
172 image that is being digitised.

173 **2.5.2 Digitise linear features**

174 This step aims to create a series of digital line traces from the georeferenced image. Create a new line
175 shapefile in the GIS project to hold the linear trace data. The shapefile needs to include an id column in
176 the attribute table so that the linear traces can be associated with a specific window and photograph.
177 Two methods can be used to create digital traces of the linear features. Firstly, the individual features
178 can be digitised manually in the GIS project, using the “add line features” tool. Alternatively, the plugin
179 tool “GeoTrace” can be used to semi-automate the digitising process. The GeoTrace plugin tool in

180 QGIS allows one to click on the start and end of each fracture and GeoTrace creates a line vector
181 between these points. For this method the photograph must be in grey scale, because the plugin follows
182 the linear feature based on low raster values and requires a sharp contrast between the feature and the
183 background. When digitising fracture traces it is important to only digitise in one orientation: if a
184 feature has multiple orientations along its length then multiple line segments should be digitised. Figure
185 3b is an example of both (i) manual digitisation and (ii) semi-automated digitisation with GeoTrace. In
186 both the manual and semi-automated methods, it is important that connecting fractures are properly
187 snapped against each other, and to the surrounding circular window.

188 A practical difficulty when analysing field outcrops will depend on whether the outcrop is natural or
189 anthropogenic. In a quarry or excavated section it can be challenging to distinguish natural joints from
190 those arising from quarrying processes, such as blast damage or drilling related fractures. Using field
191 observations, blast damage can be separated from natural joints (Figure 2a). Joints arising from blast
192 damage can easily be distinguished from natural joints as they do not fit with the overall fracture pattern
193 of the section, and are generally surrounded by small radiating fractures. The type of fractures digitised
194 will be depend on the study, and it is important to appreciate the wide range of processes causing
195 fractures that are dependent on the outcrop setting. Some basic initial observations in the field are
196 beneficial for making such distinctions at a later stage; hence, it is recommended that the outcrops that
197 are being analysed are always viewed in the field as well.

198 **2.6 Data output and further analysis**

199 The final step is to generate basic parameters and calculate dimensions from the digital traces of the
200 linear features. There are a number of different ways that the vector data can be analysed, which include:
201 1) using the field calculator in QGIS; 2) as an exported spreadsheet; or 3) using a programming language
202 such as Python or *R* to make calculations from the spreadsheet or directly from the shapefile.

203 Primary parameters can be calculated within the field calculator in the QGIS attribute table, including
204 length and orientation of individual fracture traces. The area of the circular window can also be
205 calculated in the attribute table using the field calculator. For further analysis, the attribute table
206 containing the primary fracture data (length, orientation and reference to the circular window) needs to
207 be exported as a spreadsheet, e.g. in CSV format. Fracture density (*D*) within the circular window can
208 now be calculated using total length of fractures (ΣL) within the area of the circular window (*A*),
209 following Singal & Gupta, (1999):

$$210 \quad D = \Sigma L/A \quad (\text{in m}^{-1}) \quad (1)$$

211 Fracture spacing (*S*) can be easily derived, as this is the reciprocal of fracture density, and is given by
212 (Singal & Gupta, 1999):

$$213 \quad S = A/\Sigma L \quad (\text{in m}). \quad (2)$$

214 Other parameters, that can be derived from the digitised fracture network include the number and
215 distribution of fracture intersections and block size. Fracture intersections (points) within the fracture
216 network can be created as a separate point shapefile with the ‘line intersection’ tool. The digitised
217 fracture traces can also be used to derive block size parameters, using the ‘polygonise’ tool to convert
218 the line vectors into polygons. As before, parameters such as area can be derived using the field
219 calculator in the attribute table and exported as a spreadsheet.

220 **3 Case studies**

221 Below we present a number of case studies that include fracture analysis for groundwater modelling;
222 quantifying rock mass properties for engineering geology; and block size distribution to understand
223 sediment erodibility that help demonstrate the potential broader uses of the digital GIS-based analysis
224 of fracture networks.

225 **3.1 Understanding fracture connectivity and permeability, southern India**

226 Characterisation of fracture networks is an important aspect of trying to understand local and regional-
227 scale aquifer properties such as connectivity and permeability. This type of understanding is particularly
228 relevant for groundwater studies in fractured ‘hard-rock’ aquifers, where fractures are the primary water
229 stores and pathways (e.g. Stober and Bucher, 2007; Singal and Gupta 2010). An example is given here
230 of the Peninsular Gneiss in the Cauvery Catchment in southern India. The groundwater properties of
231 the Cauvery Catchment has been an area of ongoing research (Maréchal et al 2006, Perrin et al 2011,
232 Collins et al. 2020) due to the spatial and temporal variability of groundwater availability and the impact
233 that this has on local communities. Two contrasting basement fracture networks can be identified
234 (Figure 4a-b): firstly, one massive gneiss with few fractures, dominated by a widely spaced ‘background
235 jointing’ and sheeting joints close to the surface, and secondly ‘fracture zones’ that are characterised by
236 a very dense fracture network.

237 Length-weighted rose plots show the variation in orientation of fractures (in a vertical section) in the
238 two identified domains. In the massive gneiss the fractures are generally orientated sub-horizontally,
239 with several short connecting vertical fractures. In contrast, fractures in the fracture zones are generally
240 orientated sub-vertically with short connecting sub-horizontal fractures. The fracture density in the
241 fracture zones is an order of magnitude higher than in the massive gneiss (Table 1). Using NetworkGT
242 (Nyberg et al., 2018), the fracture branches and nodes (intersections and fracture trace end-points) were
243 characterised based on the topology of the branch intersections (Sanderson and Nixon, 2015). The
244 massive gneiss is dominated by I-type nodes, whereas the fracture zones predominantly contain a
245 combination of Y- and X-type nodes (Figure 4a-b; for node types see Figure 4g) (Table 1). Heat maps
246 of intersection clustering from the massive gneiss versus a fracture zone illustrate the higher
247 connectivity of the fracture zones. To quantify the connectivity across the Cauvery catchment area the
248 connections per line and dimensionless intensity (a proxy for intensity that reflects average fracture

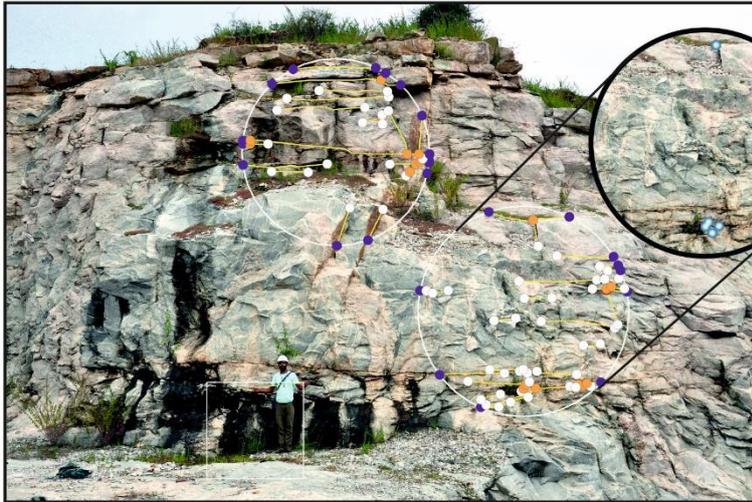
249 length) were calculated (following Sanderson and Nixon, 2015), (Table 1; Figure 4h). The connections,
 250 i.e the number of X- and Y-nodes, per line length, is an indication of the percolation potential of a
 251 fracture network (Sanderson and Nixon, 2018). The fracture zones have the highest connections per
 252 line length and dimensionless intensity, suggesting they have the highest potential connectivity. In
 253 contrast, the background gneiss has the lowest connections per line and intensity suggesting a relatively
 254 low potential connectivity. The coefficient of variation (Cv) is calculated by dividing the standard
 255 deviation of the fracture spacing by the mean fracture spacing (Gillespie et al., 1999; Watkins et al.,
 256 2015b) and is used to quantify the how clustered a fracture network is (Table 1) (Odling et al., 1999).
 257 The Cv ratios quantify the massive gneiss as generally having regularly-spaced fractures, while the
 258 fractures in the fracture zones are highly clustered (Table 1, Figure 4h).

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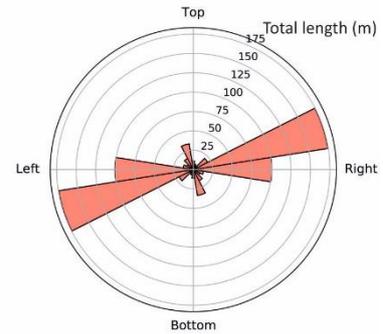
Rock type	Area (m ²)	Mean length (m)	2D density (m ⁻²)	I	U	X	Y	Dimensionless intensity	Connections per line	Coefficient of variation (Cv)
Fracture zone	4.6	0.2	17.8	157.0	61.0	121.0	517.0	3.3	3.8	1.4
Massive gneiss	15.0	0.6	1.4	41.0	10.0	1.0	11.0	0.8	0.9	0.2
Massive gneiss	11.9	1.0	1.9	19.0	15.0	0.0	10.0	1.9	1.4	0.6
Massive gneiss	26.8	0.5	3.9	136.0	32.0	18.0	157.0	2.0	2.4	0.8
Massive gneiss	8.5	0.3	8.8	130.0	40.0	38.0	204.0	2.7	2.9	1.3
Massive gneiss	137.8	2.9	0.7	21.0	10.0	6.0	23.0	1.9	2.6	0.9
Fracture zone	45.2	0.9	3.9	139.0	38.0	45.0	174.0	3.4	2.8	1.4
Fracture zone	38.5	1.7	1.6	139.0	38.0	45.0	174.0	2.6	2.8	1.3
Fracture zone	81.6	2.6	1.1	23.0	16.0	6.0	25.0	2.8	2.6	1.2
Massive gneiss	359.4	11.9	0.2	5.0	4.0	1.0	1.0	2.0	1.3	1.8
Massive gneiss	31.1	5.3	0.7	3.0	5.0	0.0	0.0	3.6	0.0	1.1
Fracture zone	9.2	1.5	1.4	4.0	6.0	0.0	6.0	2.1	2.4	0.7
Massive gneiss	13.3	2.1	0.9	2.0	8.0	0.0	2.0	1.9	2.0	0.5
Massive gneiss	10.5	1.9	0.9	2.0	5.0	2.0	1.0	1.7	4.0	0.7
Massive gneiss	119.6	2.1	0.8	41.0	12.0	4.0	27.0	1.6	1.8	0.4
Massive gneiss	95.4	2.3	1.0	29.0	19.0	5.0	30.0	2.4	2.4	0.5

260 **Table 1:** Summary fracture network statistics from the Peninsular Gneiss in the Cauvery Catchment,
 261 southern India.

(a) Digital fracture traces on massive gneiss

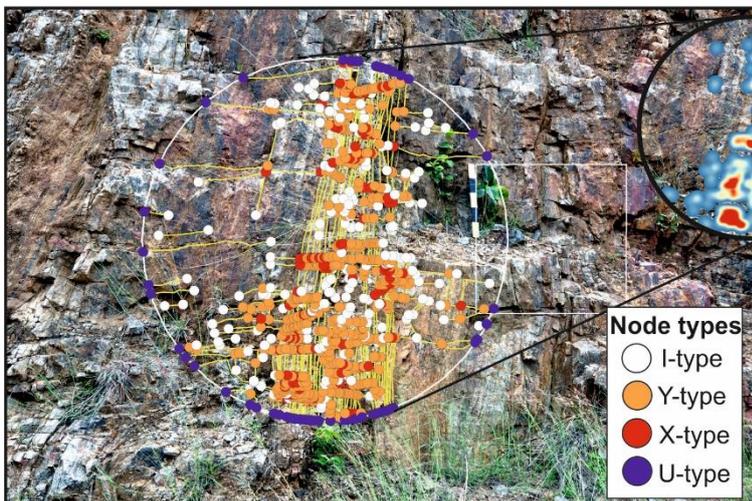


(c) Heat map of intersection density

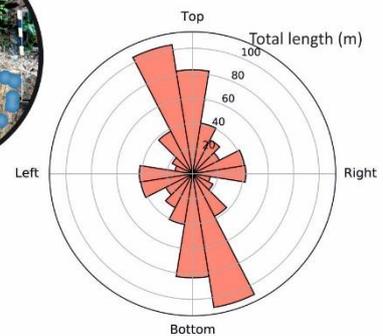


(e) Rose plot of fractures in background gneiss (n=176)

(b) Digital fracture traces from fracture zone

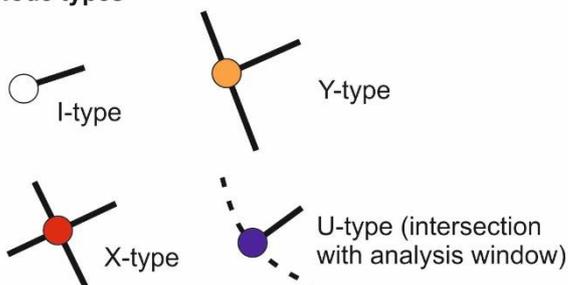


(d) Heat map of intersection density

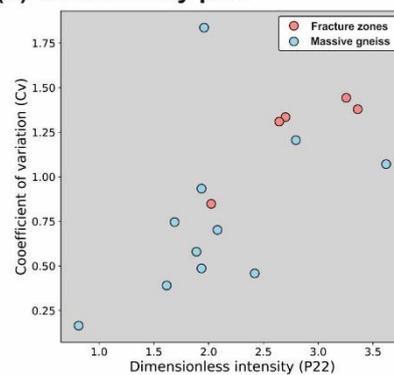


(f) Rose plot of fractures from fracture and shear zones (n=1104)

(g) Node types



(h) Connectivity plot



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Figure 4: Fracture analysis from the Peninsular Gneiss, South India, including: field photographs with digitised fracture branches and intersection types on (a) a massive gneiss example; and (b) from a fracture zone; (c-d) heat maps illustrate variations in fracture intersection density (massive gneiss: 0-5 nodes/m² and fracture zones: 0-18 nodes/m²); (e-f) length-weighted rose plots showing the variation in orientation of fractures traces in the background gneiss and fracture zones; (g) a schematic illustration of the various types of fracture connections (as defined by Manzocchi, 2002); (h) a plot of connections per line against dimensionless intensity (defined by Sanderson and Nixon, 2015) to show variations in connectivity.

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271 At the near-surface, the Peninsular Gneiss has a bimodal fracture density distribution with fracture
272 zones with high fracture density that make up a relatively small proportion of the bedrock, and the
273 majority of the crystalline basement containing a low-density fracture pattern. Connectivity proxies,
274 such as connections per line, indicate that the fracture zones have the highest potential permeability,
275 whereas the permeability potential of the background gneiss is highly variable but still significantly
276 lower.

277 In this case study, field time was limited and the digital method provided a quick and flexible way of
278 gathering fracture network data. It was possible to carry out a reconnaissance survey covering an area
279 over 30,000 km² and then retrospectively select the most suitable sites for fracture analysis. Key fracture
280 parameters such as fracture length, orientation and density, which impacts on aquifer characteristics
281 such as connectivity and permeability across the Peninsular Gneiss in the Cauvery River catchment,
282 where then calculated and used to constrain local and regional-scale groundwater models (Collins et al.
283 2020).

284 **3.2 Rock mass strength estimates (Geological Strength Index)**

285 Structural discontinuities are an important control on the engineering behaviour of a rock mass (Müller,
286 1974; Hoek 1983, Hoek & Brown 1997). Slopes, foundations and shallow underground excavations in
287 hard rock can be strongly be affected by the presence of discontinuities, for example, the intersection
288 of structural features can lead to falling and sliding of blocks or wedges from the surface.

289

290 In the last decade, rock mass classification systems have been applied extensively in engineering design
291 and construction (Liu, 2007). The Geological Strength Index (GSI) system provides a numerical
292 representation of the overall geotechnical properties of a rock mass, which is estimated using a standard
293 matrix chart and field observations of (a) the ‘blockiness’ of a rock mass and (b) the surface conditions
294 of any discontinuities. The GSI Index is based upon an assessment of the lithology, structure and
295 condition of discontinuity surfaces in the rock mass and it is estimated from visual examination of the
296 rock mass exposed in surface excavations such as roadcuts, in tunnel faces and in borehole core
297 (Marinos and Hoek, 2000). Both the ‘blockiness’ and surface conditions, however, are determined in a
298 qualitative and descriptive manner, which is subjective and dependent on the interpreter. Sönmez and
299 Ulusay (1999; 2002) suggested that the ‘blockiness’ or Structure Rating can be quantified by using the
300 Volumetric Joint (fracture) Count (J_v , in m⁻¹). This parameter is defined as the sum of the number of
301 joints per meter for each joint set present (Sönmez & Ulusay, 1999), and can be estimated by the
302 following expression:

303

$$304 \quad J_v = \frac{1}{s_1} + \frac{1}{s_2} + \dots + \frac{1}{s_n} \quad (3)$$

305

306 where S is the spacing of the joints in a set and n is the number of joint sets. The 2D fracture digitisation
307 method can clearly be applied to determine a more accurate representation of J_v from an image.

308

309 The procedure for quantifying rock mass strength parameters in jointed rocks is illustrated using
310 massive and fractured gneiss exposures in India (Figure 4). Using the qualitative method (Hoek, 1983)
311 the massive gneiss, with 'good' fracture surfaces, has a GSI index of 70-85 whereas the fractured gneiss,
312 with 'fair' fracture surfaces, has a GSI index of 30-45. To quantify this, the modified GSI methodology
313 after Sönmez & Ulusay (1999) is used. In this example, the massive gneiss has horizontal joint spacing
314 of 0.81 m (J1) and vertical joint spacing of 6.19 m (J2). The fractured gneiss has a horizontal joint
315 spacing of 0.17 m (J1) and vertical joint spacing of 0.08 m (J2). Thus, using equation 3, this gives a J_v
316 value of 1.4 for the massive gneiss and 17.7 for the fractured gneiss. Based on similar estimates of
317 roughness (5), weathering (3) and infill (6) the fracture surface condition rating (SCR) is 14 in both the
318 massive gneiss and the fracture zones. Finally, the GSI values calculated are *c.* 76 for the massive gneiss
319 and only *c.* 44 for the fractured gneiss, demonstrating an accurate representation of the rock mass
320 strength differences of the massive and fractured gneiss.

321 When determining rock mass strength properties the digital method can provide a fast, accurate and
322 consistent result. Understanding rock mass strength properties is relevant for both academic and
323 industry users, in both cases, available field time can often be limited. In addition, particularly in
324 industry there is likely to be multiple interpreters making rock mass strength estimates, and therefore
325 this method can help improve consistency in the results by undertaking analysis digitally.

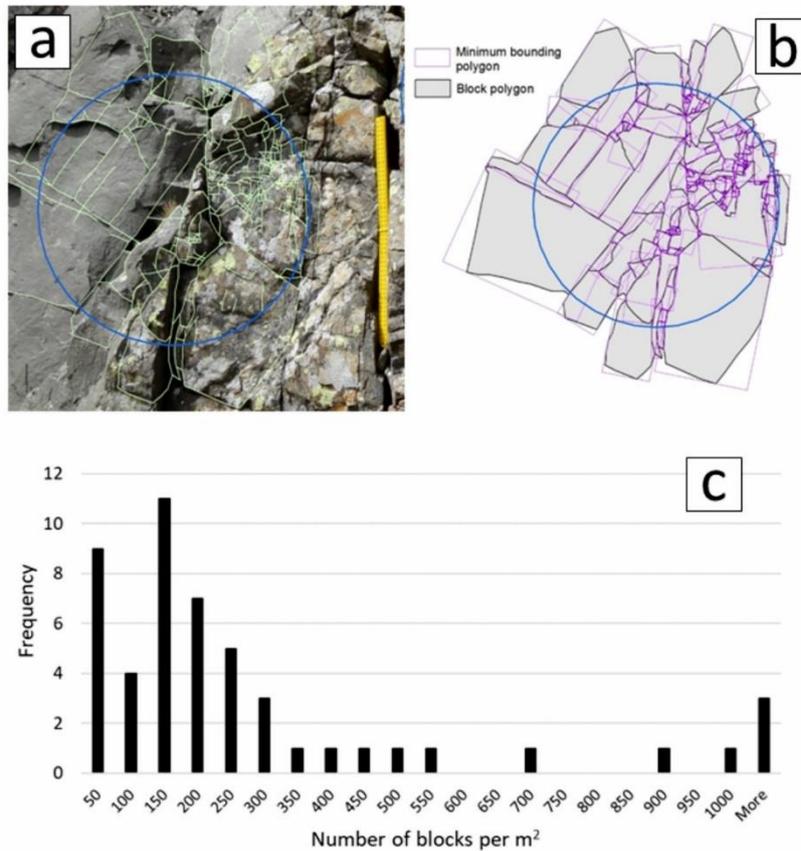
326

327 **3.3 Block size and rock erodibility, Southern Scotland**

328 Fracturing is a significant factor in the preconditioning of rock masses for erosion at the Earth's surface
329 (e.g. Roy et al., 2016; Clarke and Burbank, 2010). As well as influencing the volume of material
330 available for mobilisation and transport, fracturing of bedrock is a key control on the clast size
331 distribution of eroded material entering geomorphic systems from hillslopes, particularly in upland
332 landscapes (e.g. Sklar et al. 2016).

333 The 2D fracture digitisation method is here used to assess the spatial distribution of block-size and
334 fracture intensity of metasandstone of low metamorphic grade in the Southern Uplands, southern
335 Scotland. Block density can be expressed as blocks per square metre, which is easily derived from a
336 polygonised set of fracture traces. It should be noted that whether this 2D block size measure is
337 representative for the true 3D block size depends on the anisotropy of the fracture system and the
338 average block shape. Despite consistent bedrock type (metasandstone) across the study area, the
339 anisotropic fracture pattern gives rise to strong variations in block-size as shown by variation in the

340 number of blocks sampled per unit measuring area from <50 to >1000 blocks per m² (Figure 5). This
 341 data can help to quantify key controls on the influence of fracture intensity on block size, which may be
 342 used to inform modelling erosion and sediment movement within landscapes.



343
 344 **Figure 5.** Derivation of block-size metrics for Wacke sandstone in the Southern Uplands of Scotland. Field
 345 photograph of sandstone outcrop with fracture delineation (a), polygons for blocks sampled by the circular
 346 window (b), number of blocks sampled per m² for dataset of 50 measuring sites from the study area.

347
 348 For this study, a large amount of fracture and block data was required from several outcrops, and the
 349 digital method provided an accurate and efficient way for gathering large amounts of fracture and block
 350 size data. Due to the requirements of the study, photographs were taken close to the outcrop to improve
 351 the accuracy of digitisation (Figure 5a), resulting in a large and accurate dataset.

352 3.4 Case studies summary

353 The case studies presented here demonstrate the broad range of benefits of a digital method during both
 354 data collection and data analysis phases. The Cauvery Catchment case study demonstrates how the
 355 digital method provided flexibility to gather data while on a short reconnaissance-style field-campaign,
 356 with fracture data collected retrospectively from photographs taken at key localities. The digital dataset
 357 allows for further evolved quantitative and graphical data analysis, such as heat maps of fracture
 358 intersections to better understand connectivity. For engineering geology purposes, the digital method is

359 shown to provide a more accurate and consistent representation of the geological strength index (GSI)
360 of a rock mass. We build upon the well-used method for estimating GSI (Hoek, 1983; Sönmez &
361 Ulusay, 1999), to calculate a more accurate GSI based on fractures exposed in outcrop. Finally, the
362 block size and erodibility case study is used to demonstrate the benefits of being able to rapidly generate
363 a large digital dataset that would otherwise be impractical to gather in the field.

364 **4 Advantages and disadvantages**

365 The digital method described here is not meant to replace field-based data gathering but used in
366 conjunction, as it may be more suitable for different purposes. There are a number of advantages to
367 using a digital method for gathering fracture data including: speed of gathering data, creating large
368 datasets, flexibility in data gathering approach and consistency of data.

369 Gathering 2D fracture network data in the field can often be a time consuming processes and therefore
370 limits the amount of data that can be gathered during a field campaign. Using the digital methodology
371 allows for fracture network data to be quickly gathered in the office, allowing for more data to be
372 generated from an equivalent amount of time in the field. Field time can be used for detailed study of
373 the outcrop to improve the interpretation of fractures in the office and to gather other key data such as
374 aperture, fracture fill and 3D geometry's. The digital method allows for large, statistically significant
375 datasets to be quickly gathered during a short field campaign. Collecting the data after fieldwork with
376 a broader perspective provides an element of flexibility in terms of the selecting of outcrops for analysis,
377 the type and shape of the sample window and the amount of the data gathered. Finally, the digital
378 method has the potential to be used to improve the consistency and reliability of industry standards that
379 involve fracture networks, such as rock mass strength estimates (Section 3.2) by reducing collector bias
380 by standardising the data collection strategy.

381 For more evolved analysis of the fracture data the digital traces can be used in fracture analysis software
382 packages such as FracPaQ (Healy et al., 2017), NetworkGT (Nymberg et al., 2018), FraNEP (Zeeb et
383 al., 2013) and DigiFract (Hardebol and Bertotti 2013). These programmes can be used for wide range
384 of types of fracture analysis including topological analysis such as deducing node types, and plotting
385 fracture density heat maps illustrating density variations across a fracture zone.

386 There are limitations with capturing the data digitally. Firstly, capturing data in the field will always be
387 more reliable in terms of seeing the full extent of fractures: for example, fractures may be obscured by
388 vegetation making digitisation of traces more difficult than in the field (Andrews et al., 2019). Secondly,
389 field observations of the character of individual fractures such as roughness, aperture and any secondary
390 fills can be important observations made only in the field and useful when understanding rock mass
391 strength or permeability. It is also possible, of course, to digitise the fracture network, and then return
392 to the outcrop and augment the digital traces with further attribution that requires direct field observation
393 (e.g. fracture aperture, fracture fill); portable PC tablets are ideal for this purpose. Image scale can also

394 be an issue with this method, as smaller fractures can be harder to digitise from a from a single
395 photograph covering a large outcrop extent, therefore it is important to acquire photographs that cover
396 the appropriate scale of fractures, which will be dependent on the purpose of the study. Estimates of
397 fracture permeability and percolation when using topology alone represent the maximum potential and
398 does not account of closed fractures (Laubach et al., 2019). Additional observations such as aperture
399 and infilling are import for these types of studies.

400 Characterising the architecture of a fracture network is useful for understanding relative age history of
401 fracture sets, this can be significant when making larger scale interpretations particularly for fluid flow
402 modelling (Hancock 1985; Peacock et al 2018). Relative age relationships are best determined in the
403 field and can be challenging to gather digitally. It is important to appreciate the limitations of the
404 method, as it may not be suitable for all studies or may need supplementary field data.

405 **5 Conclusions**

406 The aim of this paper is to review and evaluate the methodology for digitising 2D fracture networks in
407 GIS, and make it more accessible to a broader range of users in both academia and industry. We present
408 a breakdown of the key steps in the methodology, which provides an understanding of how to avoid
409 error and improve the accuracy of the final dataset.

410 The digital method can be used to interpret traces of 2D linear features of a wide variety of scales from
411 the local metre-scale to the kilometre scale, including, fractures at outcrop scale to regional-scale
412 structural lineaments that are visible on aerial photographs or DEMs.

413 An important aspect of applied geosciences, such as hydrogeology and geotechnical engineering is the
414 accurate parameterisation of fracture networks in bedrock. The methodology that is commonly used is
415 a qualitative description and can be time consuming. The digital 2D fracture trace capture method is an
416 accurate and rapid way of quantifying 2D linear networks such as fracture zones using open access
417 software packages. It offers a robust, cost-effective methodology that can used in academy and industry
418 to gather accurate 2D fracture network data.

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424

425

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