RC2: Mimmo Palano

RC2: The GNSS is a primary technique, not a dataset. Please correct. The use of "raw GNSS data" is misleading, when speaking on velocity field. Usually, such a term is referred to RINEX GNSS data. Please check the term.

AC: Thank you for identifying this inconsistency. The use of terms has been standardized. P5L5, P14L22, P14L25: "the raw GNSS data (RINEX)" and P2L5 the incorrect terms have been replaced by "The GPS velocities".

RC2: I suggest to expand the first paragraph of introduction by explaining that crustal deformation at various temporal and areal scales are measured on volcanic areas also (see for instance Kilauea and Etna). In doing this you can also improve the discussion on the applicability of your approach on volcanic areas.

AC: As suggested, we added mentions to volcanic studies in the introduction (P1L22) and the conclusion (P15L21) to expend the scope of our analyses.

RC2: A table reporting velocity field both in ITRF2014 and the local reference frame should be added as supplementary material.

AC: Thank you, indeed this essential table has been forgotten. It is now present in the Supplement Materials.

RC2: Figures are of good quality; however, they need some small corrections. Please add a "north symbol" and a km scale to the figures. Moreover, all the figures reporting the local seismicity contain an error on the legend.

AC: Indeed, it lacks a character, thank you. The figures have been modified. Orientation and scale were added in Figure 1.

RC1: Anonymous

RC1: 0) This study approaches the problem through a combination of cluster analysis (which replaces observed velocities with the dominant velocity for a local cluster (or so I understand)) and Gaussian smoothing. The resulting velocities are then used to infer spatial gradients and define strain rates. The results look a bit puzzling with there being a number of significant elevated strain rate zones at places where they were unexpected (except for the Alps and Pyrenees). I am very concerned that the clustering approach, instead of having revealed systematic strain rate signals that were buried in the original data, has actually created signals that weren't there. The study also presents vertical rates but that analysis seems a bit disjointed from the rest of the paper.

AC: Several of the following comments are related to a misunderstanding regarding the usage of clustered velocities in the strain rate computations. We may not have been clear enough on this point in the original manuscript, and we understand how this misunderstanding might have led the reviewer to question some of our results.

In practice, the application of clustering has not biased the analysis of deformation rates because they are totally independent. Clustering only provides a velocity field and no strain rates are derived from
clustering. The fact that smoothing and clustering velocity fields reveal the same patterns is therefore a very good thing. This is the main idea of this study: from 2 completely independent methods we can extract the same information regarding regional kinematics and deformation contained in a low and noisy velocities field.

As a first answer, we have added an author comment during the review phase to clarify this point: "We apply each method (clustering and smoothing) on the raw GPS velocities. The two methods are fully independent. The strain rate map is computed using the smoothing method only (based on the raw data), independently of the clustering analysis."

To clarify the manuscript and eliminate the risk of misunderstanding, we added this sentence: P7L21 "We apply each method (clustering and smoothing) on the GPS velocities. The two methods are fully independent. Clustering only provides a velocity field and no strain rate field. The strain rate map (Fig. 7) is computed using the smoothing method only (based on the GPS velocities), independently of the clustering analysis." Also we specified the titles of the sections. P8L7 "Clustering applied to GPS velocities" and P9L7 "Gaussian smoothing applied to GPS velocities".

RC1: I have many comments, listed below in descending order of approx. significance. Before I discuss those I want to point out that I was expected to see reference to the (Kreemer et al., 2018) paper. While the authors could in general do better with citing references (see comments below), that particular paper had the same aim as this study (to present a robust procedure to pull signal out of noisy data) but applied to intraplate North America. Perhaps the authors were unaware of that paper, and I strongly encourage them to check it out.

AC: Indeed, Kreemer et al. 2018 is similar to ours but we forgot to quote it, thank you for this remark. The methodology and results are similar even if the study areas and the geodynamic mechanisms involved are different. We added this reference in several places: P1L27 "The lengthening of time series and the increase in the number of stations makes it possible to better constrain deformation in the intraplate domains (e.g., Kreemer et al., 2018; Tarayoun et al., 2018)."
P7L5 "Other methods of detection of outliers exist (e.g., Kreemer et al., 2018)."
P15L15 "In North America, Kreemer et al. (2018) have shown that, to first order, geodetic deformation is not directly correlated to seismicity and that the link between long-term tectonic processes, transient processes (GIA), seismicity and geodetic deformation is not simple at the scale of the regional deformation (> 100 km)."

RC1: 1) While I don’t think I fully understand the clustering analysis, it seems to me that the resulting velocity field (Fig. 4a) is much more clustered than the original velocity field seen in Fig. 3a. My slight hesitation comes from the fact that a clear comparison is hard to make since the original data (Fig 2,3) is presented for a much larger geographic area (and a different scale) than the rest of the paper (see comment 8), which makes the observed velocities in the France area hard to see. Could the authors either reduce the area for Fig 2,3 or add a figure that shows observed velocities for the same geographic area as the other figures?

AC: You are absolutely right, thank you.
For clarity, we modified Figure 2 to show the extent of the network used, Figure 3 has been cropped and Figure B show the entire velocity field. In Figure 3, there are now 3 elements:
- in black, the horizontal velocities associated with their 95% uncertainties,
- in brown the horizontal velocities whose uncertainty is larger than 0.3 mm/yr (for which the uncertainties are not represented for graphic reasons),
- in red, the horizontal velocities of the stations identified as outliers.

RC1: In any case, Fig 4a is ultimately being used as input to the Gaussian smoothing, and it has various curious traits.

AC: This remark is linked to the misunderstanding addressed in point n° 0 (the clustered velocities are not used in the Gaussian smoothing).

RC1: Is it still in the same “France reference frame” as the data? If so, the fact that there is a dominant eastward component to most velocities suggests that the clustering changed the essential characteristic of the velocity field in this frame. How come? Obviously this velocity field is not in a new “France reference frame”, because then that eastward motion should not be there. While the reference frame of the velocity field ultimately doesn’t matter (because the purpose is to investigate strain rates, which are reference frame independent (although see comment 5), this seemingly change in reference frame by the cluster analysis points to a possible problem with the clustering analysis. Secondly, from Fig 4a it is clear that the clustering analysis broke up the velocity field in domains and that there are rather discrete boundaries between these domains. Some of the main features in the strain rate field (Fig 7a) are directly related to these cluster boundaries; the NS zone in Aquitaine Basin, the NW trending zone in the Paris Basin, the NS zone in northernmost France, and the three related zones in Eastern France: the EW compressional zone in NE France, the EW extensional zone in eastern France and the NS compressional zone that connects them.

AC: This remark includes several points:
  a) The velocity fields seem to highlight a systematic movement towards the East that questions the definition of reference frame.
  b) This effect would be a clustering bias.
  c) This, and other clustering effects, would be at the origin of several deformation zones highlighted.

Reply to points b) and c):
(as a reminder, the analyzes (clustering and smoothing) are totally independent, see point n° 0).
The two velocity fields (Fig. 4a and 6a) highlight the same eastward trend in western France, which eliminates the hypothesis of a potential bias due to the clustering method. Furthermore, these apparent eastward motions cannot result in regional (ca. 100-200 km scale) deformation patterns as shown on the strain rate map, which is based on smoothing only and has no link with clustering. In addition, the clustering method produces, by definition, strong edges in the velocity field that could be due to the station spatial distribution. In our analysis of regional deformation, we are careful to not interpret these potential biases due to the network configuration.
It is worth noting that the clustering method is not new and has been applied to GPS velocities in the last decades or so. We added a couple of references to present this (Savage and Simpson 2013; Ozdemir and Karslioglu, 2019).

Reply to point a):
Indeed, both clustering and Gaussian velocity fields (Fig. 4a and 6a) show a systematic movement towards the E-NE. The Gaussian smoothing method, from which deformation rates are derived, is based on the assumption of a flat Earth. The presence of a residual rotation can theoretically bias the estimation of strain rates. However, the deformations from the velocity field before subtraction of the rotational movement are similar to those presented here. The differences between the 2 estimates yield a value of 0.12 x 10^-9 yr^-1 for the 95th percentile. This means that even if the entire rotational movement remains present, the associated deformation is much lower (one order of
magnitude) than our detection level. We can therefore consider that the hypothetical presence of
the rotation does not lead to significant bias in the determination of deformation rates.
Although it does not bias the estimation of deformation rates, this movement must be explained. Its
origin is linked on one hand to the stations used to define the rotational movement (stations of more
than 7 years) and on the other hand to the fact that the stations of less than 7 years undergo a
strong correction coming from the stack. Indeed, in the stack (Fig. A), we observe that in the last 7
years the trend slope shows a significant changes, notably because of the 2 changes of IGS frame in
2011 and 2012. The use of REPRO2 in a future calculation may allow overcoming these offsets and
reduce the correction brought to the series of less than 7 years.
NB: Such analysis requires much more details that are beyond the scope of this manuscript, further
information can be found the C. Masson Ph.D. thesis (manuscript to be deposited in the HAL archive
in late 2019).

RC1: 2) I'll leave it up to the authors to find out what may be wrong with the clustering analysis, but
I have two immediate suggestions that may further exemplify problems with the clustering: a) show
the (vectorial) difference between the original velocities and those obtained from clustering.

RC1: Right now the authors only show the difference between the velocities from the clustering and
those from the subsequent smoothing (Fig. 8) and they don't show them vectorially, which is
important.

AC: These vector differences have been added in Appendix and are mentioned in the manuscript
(P11, L11). These maps confirm what is shown on Figs. 8 (differences in scalar amplitude), which
indicate that the clustering does not show significant regional biases.

RC1: b) derive a strain rate model from the Gaussian smoothing but based instead on the original
horizontal velocities. I expect many differences.
While the authors may argue that those differences point to the clustering pulling out spatially
coherent strain rate signals, I would argue that the clustering seemingly creates signals that are
inconsistent with the original data.

AC: These remarks are linked to the misunderstanding addressed in point n° 0.

RC1: 3) Because of the concerns expressed above, I have little confidence in the validity of the
observed strain rate features and the discussion thereof (Section 4 and 5). Part of the discussion is
the comparison with seismicity. The authors indeed find no or confusing correlation (which the
authors call “surprising”). The relationship between intraplate deformation and seismicity is a hot
science topic, and I am worried that the general discussion on this topic does not benefit from
comparisons being made on the basis of a strain rate model that has some serious problems. The
authors also don’t offer a good explanation for the various strain rate features in eastern France
(except the Alps); I suggest this is because there isn’t any good tectonic explanation and that these
features are modeling artifacts.

AC: This remark is linked to the misunderstanding addressed in point n° 0. Considering that the
misunderstanding has been resolved, the reviewer points out that few interpretations have been
made for the East of France. Indeed, we can develop the interpretation of the results in the East of
France. Unlike the reviewer, we think that these results can have tectonic explanations. To clarify
this point we added these elements to the Discussion:
P14L1 "These results are consistent with those reported in other geodetic studies (Sanchez et al.,
2018)."
P14L14 "For the regions of the Vosges and Jura, the analysis of focal mechanisms provides results compatible with our geodesic deformations (Plenefisch et al., 1997, Maurer et al., 1997, Sue et al., 1999 and 2007). The compatibility suggests a tectonic origin of this deformation."

We would also like to point out that deeper analyses of our geodetic results in each area would require a lot more space than available in a SE manuscript. The main point of our study is to highlight the new applications and methods, hopefully triggering more complete analyses in the future. Some of the deformation patterns identified here might, in time, prove out to be incorrect, but this is part of the research process and should not deter the publication of new analyses and results. P2L18 "These interpretations are preliminary and for several regions a specific study is necessary."

RC1: 4) The authors don't question their results because they have faith in their uncertainties which they derived from a synthetic test in which strain rate model was inferred when observed velocities were nominally set to zero (but velocity uncertainties were kept). This may be a good test, as it shows how data uncertainty and network geometry map into model uncertainties. The clustering approach may also work well when velocities are set to zero, as it would be hard to make clusters out of such data. The clustering may however fail when it starts to determine median velocities from actual velocities.

AC: It is quite difficult to address this comment.

Concerning the last point, the clustering analysis does not depend on the velocity amplitudes because it is essentially driven by the station coordinates to derive geographical groups (as explained in the manuscript). Thus, the tests with zero velocities are representative of the real velocity analysis.

We would like to point out that we don't "have faith in the uncertainties". We propose a detailed analysis of uncertainties and resolution (much more detailed than most geodetic deformation studies). This analysis yields standard errors and detection levels that we use to define which parts of our results are significant and which are not. Our interpretation of what is significant is not subjective but factual (providing our computations and results are correct).

RC1: 5) I am quite confused by the strain rate estimation as part the Gaussian smoothing. Here are the reasons: a) it appears this is done on a flat-Earth approximation, which is may be ok, but given that this study tries to infer very small strain rates it is worth investigating what magnitude of error a flat-Earth approximation would introduce over a fully spherical treatment.

AC: The answer to this remark is in point 1a.

RC1: b) equation (3) is quite similar to equation B2 of (Mazzotti et al., 2011 which they reference, but some curious differences exist: in the current study the azimuthal weighting function is missing (why?), and the velocity in the latter half of both components is here given as that of a station and in Mazzotti et al as that of the grid point (the latter appears correct).

AC: The azimuthal weighting is not used here because this feature is not very robust and results in additional complexities in the analysis, with little effect in the end.

Concerning the grid point, we tried to clarify the equation to point out it could apply to a grid or only given point. This was not clear and we corrected this to limit to a grid analysis (as used here).
RC1: c) In general, I am puzzled how the strain rate field is parameterized as being the product of distance and velocity, because strain rate is ultimately related to velocity divided by distance. This explanation was missing in Mazzotti et al as well and I would suggest deriving and/or explaining this better.

AC: The fact that the distance comes as a multiplication is because of the derivative of the Gaussian exponential. It is a straight derivative, which we do not think requires a detailed presentation. However, if necessary, we can add it in a Supplementary Material. We will comply with the editor's opinion on this point.

RC1: d) the velocities contain a translation/rotation (which is particularly a problem in light of the reference frame problem discussed in comment 1). The way it reads now is that any rotation gets mapped into strain rate. Please clarify.

AC: The answer to this remark is in point 1a (the Flat Earth bias is not significant, one order of magnitude smaller than the signal).

RC1: e) Is there any fundamental difference between this method and the VISR method of (Shen et al., 2015) or even the SSPX method of (Cardozo & Allmendinger, 2009)?

AC: SSPX uses a similar method. Discussing the differences between our approach and the numerous other methods that exist (beyond SSPX and VISR) is beyond the scope of our manuscript.

RC1: 6) For the outlier detection, some questions came up: a) it is not mentioned, but are the detected outliers the red vectors in Fig 3a?

AC: The legend of the figure was indeed not clear and has been modified (see point n° 1).

RC1: b) How many of the added campaign velocities are identified as outliers? It seems like a lot. Is it still worth including those?

AC: There was a misunderstanding because of the legend of the figure (see point n° 1). The identification of outliers was made only on permanent stations and horizontal components. We added a clarification P6L23: "The statistical outlier detections are applied only on the horizontal velocities of permanent stations because vertical velocities show too much variability for robust results. Campaign stations are not included because of their large associated uncertainties."

RC1: c) I don't understand line 22-23 (page 6) "Stations for which DM is greater than the network 95% confidence interval are considered as outliers and rejected". Does this mean that the outlier detection is based on distance as well? Why?

AC: There was a misunderstanding: it is not a spatial distance but a statistical call. We added a clarification P7L1: "The term distance ($D_M$) does not refer to a spatial distance but to a statistical distance between each station variables and the barycentre of the multidimensional space formed by the network variables."

RC1: d) Note that Kreemer et al. (2018) also introduced an algorithm to identify outliers.

AC: Indeed, and the comparison of the results will be very interesting. We added this suggestion P7L5: "Other methods of detection of outliers exist (e.g., Kreemer et al., 2018)."
RC1: e) To test the “robustness” of the presented strain rate model one would need to show that the model is not affected by outlier data (if that is what was indeed meant with the model being “robust”). I understand why they flagged outliers, but to proof robustness they should also show a model that was based on data that included outlier velocities. Ideally the resulting model would be mostly the same.

AC: We added this figure on Supplementary Materials. In text P10L14 "(The smoothed horizontal strain rate fields but without excluding outliers is presented in Figure E)."

RC1: 7) the vertical velocities are also subjected to the clustering analysis and subsequent smoothing. The results are only sporadically mentioned in the discussion, which makes one wonder about that part of the presented data in light of this study's goals. There have been other recent attempts to obtain a "smooth" vertical velocity field (either as a continuous grid and/or by "despeckling" the original rates, as is done here). Examples are: (Hammond et al., 2016; Husson et al., 2018; Serpelloni et al., 2013) The authors should consider discussing and/or comparing the various approaches.

AC: We discuss our vertical velocities, to a first order, but choose to focus on horizontal signal that we deem more interesting / novel. A more detailed analysis of the vertical results and comparisons with others studies would be interesting, but would likely require a specific study and manuscript.

RC1: 8) It is not clear why the authors present data over an area much larger than the ultimate study area. The study and most figures are focused on greater France but Figs. 2 and 3 show a much larger area, which notably includes a lot of data in Italy. Why is this presented if it isn't used? Does the number of stations mentioned in the text include those in Italy? If yes, I would find that misleading. While I understand that the authors would want to add a little buffer to the area show in most figures, the current presentation is confusing and doesn't allow for a good comparison between data and model in the actual study area.

AC: This remark was considered and addressed in points 1 and 6. And an explanation of the number of stations used has been added. P2L20: "The calculation was extended to a wider area than the frame considered in the rest of this study. Thus 313 stations mainly in Italy and Spain do not appear on France centered maps. Table S1 shows the velocities of all stations used in the calculation."

RC1: 9) In the introduction (line 21-22) of page 1, some studies of intraplate strain rate are mentioned (Canada, India). It would be better if the mentioned studies would be previous attempts to model intraplate strain rates in the same area, which are currently not even mentioned, particularly (Tesauro et al., 2006).

AC: Indeed, we did not mention Tesauro et al. (2006) because we preferred to cite more recent studies. The study of Tesauro et al. (2006) is carried out on only 8 years of GPS data and with a rather heterogeneous network of stations. Despite the quality of this study and the results compatible with ours, we have privileged recent geodetic studies.

We now added this reference:
P2L11 "Indeed, they are often considered as a domain without significant deformation except in its bordering mountain ranges, the Alps (e.g., Houlié et al., 2018; Brockmann et al., 2012; Tesauro et al., 2006) and the Pyrenees (e.g., Neres et al., 2018; Rigo et al., 2015)."
RC1: 10) Abstract, first sentence. Authors say “we use dense geodetic networks and large GPS datasets”. What is the distinction between these two? They seem the same.

AC: Exactly, we replaced these sentences (P1L6) with "We use two decades of data from a dense geodetic network to extract regionally coherent velocities and deformation rates in France and neighboring Western Europe."

RC1: 11) The paper uses the word "technics" twice. Ironically, the English language uses the French word: "techniques". Please correct.

AC: Thank you for identifying these errors, we corrected them.

RC1: 12) The details on the GPS data analysis do not mention the minimum duration of the considered time-series. Is it 2.5 years? If not, what it it? If less, why?

AC: We have clarified this point. (P2L23) "The time series cover time spans from 1.5 to 19 years with an average duration of 7 years."

RC1: 13) page 3, line 11: “only a small percentage of stations is associated with reliable equipment logs”. I suppose this hinges on the word “reliable” but I would have thought that the majority of the stations would have logs.

AC: To clarify this point, we have reformulated this sentence. (P3L13) "Because many stations are associated with incomplete equipment logs that could provide position offset dates, the dates of potential offsets are automatically detected according to the method described in Masson et al. (2019)."

RC1: 14) page 3, line 15-16. Here the bias is mentioned of undetected jumps on velocities (I think) but only for long time-series (>8 years). How about short(er) time-spans?

AC: To answer this question, we developed the sentences about the results obtained by Masson et al., 2019. (P3L18) "Overall, using this method, results in horizontal (resp. vertical) velocity biases are smaller than 0.2 mm yr\(^{-1}\) (resp. 0.5 mm yr\(^{-1}\)) at 95\% confidence levels for series longer than 8 years. For series with duration between 4.5 and 8 years and no offset, the velocity biases are smaller than 0.3 mm yr\(^{-1}\) (horizontal and vertical) at 95\% confidence levels and, if at least one offset is present, the velocity biases are 0.6 mm yr\(^{-1}\) (resp. 1.3 mm yr\(^{-1}\)). For the shortest series (less than 4.5 years), the velocity biases are larger than 1.0 mm yr\(^{-1}\) (Masson et al., 2019)."

RC1: 15) Was the common-mode also removed from the campaign data. It should be, but wasn't explicitly mentioned.

AC: This point has been clarified. (P5L24) "Since the data are sporadic (a few points every 4–10 years), it is impossible to model annual and semi-annual seasonal signals, detect offsets and estimate noise characteristics by spectral analysis. No common-mode has been removed from the campaign data as the effect is not significant (Tarayoun et al., 2018)."

RC1: 16) page 7. the authors say that a spatial scale of 100-200 km corresponds to the interseismic deformation on a (vertical?) fault with a seismogenic thickness of 10-25. Of course, that would totally depend on the slip rate (and the precision in the data), so I think it would be better to omit this statement.
AC: No, the spatial scale of the interseismic loading does not depend on the slip rate, only on the locking depth (cf. eq. 1 in Savage and Bufford, 1973). The detectability of such signal does depend on the slip rate, but the point here is that the spatial scale. But to simplify, this statement has been removed, thank you. (P7L21)

RC1: 17) what are the orange colored points in Fig 4a and Fig 6a?

AC: Sorry for the misunderstanding. The brown vectors correspond to those whose amplitude is lower than the detection levels determined by the synthetic data. The captions of Figures 4a and 6a have been clarified.

RC1: 18) With the chance of sounding like a curmudgeon; the last author’s contribution is solely in the realm of GPS data processing. Does that warrant authorship? (Note that this comment is not affecting my assessment of this paper)

AC: We understand the remark, however Erik Doerflinger participated several months in the smooth running of the calculation. We would like to leave him in the list of co-authors to also value the work of technical staff. We will comply with the editor’s opinion on this point.
Extracting small deformation beyond individual station precision from dense GNSS networks in France and Western Europe

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Abstract. We use two decades of data from a dense geodetic network to extract regionally coherent velocities and deformation rates in France and neighboring Western Europe. This analysis is combined with statistical tests on synthetic data to quantify the deformation detection thresholds and significance levels. By combining two distinct methods, Gaussian smoothing and k-means clustering, we extract horizontal deformations with a 95% confidence level ca. 0.1–0.2 mm yr⁻¹ (ca. 0.5–1 x 10⁻⁹ yr⁻¹) on spatial scales of 100–200 km or more. From these analyses, we show that the regionally average velocity and strain rate fields are statistically significant in most of our study area. The first order deformation signal in France and neighboring Western Europe is a belt of N-S to NE-SW shortening ca. 0.2–0.4 mm yr⁻¹ (1–2 x 10⁻⁹ yr⁻¹) in central and eastern France. In addition to this large-scale signal, patterns of orogen-normal extension are observed in the Alps and the Pyrenees, but methodological biases, mainly related to GPS solution combinations, limit the spatial resolution and preclude associations with specific geological structures. The patterns of deformation in western France show either tantalizing correlation (Brittany) or anti-correlation (Aquitaine Basin) with the seismicity. Overall, more detailed analyses are required to address the possible origin of these signals and the potential role of aseismic deformation.

1 Introduction

The Global Navigation Satellite System (GNSS) is a primary dataset to study present-day crustal deformation, for example through the computation of strain rate tensors, in active tectonics areas (e.g., Indonesia or Greece; Gunawan et al., 2019; Chousianitis et al., 2015) and in very low deformation areas (e.g., Eastern Canada or India; Tarayoun et al., 2018; Banerjee et al., 2008), as well in volcanic areas (e.g., Etna; Palano et al., 2010). However, the analysis of regional and local deformation is commonly restricted by several factors, such as the precision of individual GNSS velocities, the presence of non-tectonic transient signals or the methods used to compute strain rates on different spatial scales (e.g., Cardozo et al., 2009; Zhu et al., 2011; Carafa and Bird, 2016). In particular, the precision of individual GNSS velocities is a strong limitation in intraplate regions, where the amplitude of the tectonic signal is of the same order of magnitude as the measurement uncertainties (e.g., Calais and Stein, 2009; Tarayoun et al., 2018). The lengthening of time series and the increase in the number of stations makes it possible to better constrain deformation in the intraplate domains (e.g., Kreemer et al., 2018; Tarayoun et al., 2018).
In this study, we evaluate the ability to extract regionally coherent and statistically significant information on the present-day deformation rates in France and neighboring Western Europe from GNSS networks. This analysis is performed in several stages. (1) We first compute a consistent velocity dataset based on GPS (Global Positioning System) signals for over 900 stations, using statistical semi-automatic techniques for time series processing (in particular offset and outlier detections). (2) The GPS velocities are analyzed using two independent methods (k-means clustering and Gaussian smoothing) in order to extract coherent velocities and deformations on spatial scales of 100–200 km. (3) We perform Monte Carlo and Bootstrap sampling analyses on the original GPS velocities and on synthetic velocity data to estimate the detection threshold and the significance level of the computed velocity and strain rate fields.

Our study is focused on France and neighboring Western Europe since they represent an ideal location for testing these methodological developments. Indeed, they are often considered as a domain without significant deformation except in its bordering mountain ranges, the Alps (e.g., Houlié et al., 2018; Brockmann et al., 2012; Tesauro et al., 2006) and the Pyrenees (e.g., Neres et al., 2018; Rigo et al., 2015). The Alps and Pyrenees have a high level of seismic activity (Fig. 1), allowing us to study how it relates to the GPS deformation rates, both in spatial distribution and style. The rest of France experiences a low to moderate diffuse seismicity in many regions (Cara et al., 2015; Fig. 1) suggesting that it undergoes a small but non-zero present-day deformation. We show that, in most of our study area, horizontal deformation rates can be estimated from GPS data with a 95% confidence level ca. 0.1–0.2 mm yr\(^{-1}\) (ca. 0.5–1 x 10\(^{-9}\) yr\(^{-1}\)) on a spatial scale of 100–200 km or more. We discuss the relationship between the observed deformation and regional seismicity and neotectonic indicators. These interpretations are preliminary and for several regions a specific and in-depth study is necessary.

2 GPS networks and data analysis

We process data of 987 GNSS stations over a period ranging from 1998 to the end of 2016. The calculation was extended to a wider area than the frame considered in the rest of this study. Thus 313 stations mainly in Italy and Spain do not appear on France centered maps. Table S1 shows the velocities of all stations used in the calculation. The time series cover time spans from 1.5 to 19 years with an average duration of 7 years. All stations have not been installed under the same conditions and the same goals (geodetic, cadastral, etc.). About a quarter of the stations are installed and maintained by private networks, for which we do not have all the information on the site monumentation or history of equipment changes. Figure 2 shows the distribution of these stations and identifies the additional campaign stations and Swiss stations combined to the main dataset (Section 2.4).

For data processing, we use the Precise Point Positioning (PPP) software developed by the Canadian Geodetic Survey of Natural Resources Canada (CSRS-PPP v1.05) (Héroux and Kouba, 2001). Optimum processing parameters and options to compute 24 h-average daily positions are defined by Nguyen et al (2016), following International GNSS Service (IGS) products and recommendations (Kouba et al., 2009; Dow et al., 2009). We use the IGS Final Products for satellite orbits and clocks, satellite and ground antenna absolute phase center mapping, and Earth rotation parameters. We also use standard
models for tropospheric delay corrections (VMF1, Boehm et al 2006) and solid Earth and ocean tide loading corrections (FES 2004, Lyard et al., 2006).

2.1 Time series analysis

Daily position time series are modeled with a constant velocity, annual and semi-annual periodic motions, instantaneous offsets, and random colored noise:

\[ x(t) = vt + A_1 \sin(\omega_1 t + \phi_1) + A_2 \sin(\omega_2 t + \phi_2) + C_i H(t, T_i) + \epsilon \]  

where \( x \) is the daily position, \( t \) is the time, \( v \) is the velocity, \( A_1, \omega_1 \) and \( \phi_1 \) are the amplitudes, periods and phases of the annual and semi-annual motions, \( C_i \) and \( T_i \) are the amplitude and date of the \( i^{th} \) offset (with \( H \) the Heaviside function) and \( \epsilon \) is the residual. To jointly estimate these parameters (except for the noise parameter), we use a linear least-square inversion of the model (Eq. 1).

Because many stations are associated with incomplete equipment logs that could provide position offset dates, the dates of potential offsets are automatically detected according to the method described in Masson et al. (2019). Their statistical analysis shows that this method compares favorably with most automatic and manual detection methods (Gazeaux et al., 2013), with an average detection level of about 52% vs. about 20% of false positives. Overall, using this method results in horizontal (resp. vertical) velocity biases are smaller than 0.2 mm yr\(^{-1}\) (resp. 0.5 mm yr\(^{-1}\)) at 95% confidence levels for series longer than 8 years. For series with duration between 4.5 and 8 years and no offset, the velocity biases are smaller than 0.3 mm yr\(^{-1}\) (horizontal and vertical) at 95% confidence levels and, if at least one offset is present, the velocity biases are 0.6 mm yr\(^{-1}\) (resp. 1.3 mm yr\(^{-1}\)). For the shortest series (less than 4.5 years), the velocity biases are larger than 1.0 mm yr\(^{-1}\) (Masson et al., 2019).

We calculate the velocity standard errors using Williams et al. (2003) generic expression for colored noise with a non-integer spectral index. The spectral index and amplitude of the colored noise are estimated using a least-square inversion of the residual (\( \epsilon \), eq. 1) spectrum limited to periods between 1/12 and T/2 years (with T the length of the time series). This simple approach only provides a first-order estimation of the noise parameters and velocity standard errors (compared to a more complex non-linear method, such as maximum likelihood). In agreement with other recent studies (Santamaria-Gomez et al., 2011; Nguyen et al., 2016), we observe that the spectral indices vary from -0.8 to -0.4, indicating a combination of white and flicker noise. Using synthetic time series analyses, Masson et al. (2019) show that the simple “least-square spectrum” approach yields estimations of velocity standard errors that are reasonable for series with a spectral index smaller than -0.6 but that are underestimated for series with a spectral index greater than -0.4. The latter corresponds to only 18% of our data, allowing us to have confidence in the calculated velocity standard errors.
2.2 Common-mode spatial filtering

In order to identify and correct for non-tectonic transient signals and noise common to the whole network, we define a common-mode correction (Wdowinski et al., 1997) by stacking the residual time series of 31 stations with near-complete data and durations greater than 17 years. Such a correction typically allows adjusting for network-wide biases such as systematic orbit and clock issues due to the IGS combination process, or potential large-scale environmental loads. On average, the application of the common-mode correction to all stations reduces the daily dispersion on the North, East and Up components from 1.94 mm to 1.36 mm (-30%), 2.49 mm to 2.07 mm (-17%) and 4.54 mm to 4.12 mm (-9%) respectively. The stacked time series show a decrease in dispersion of the North and East components between 1998 and 2002 (cf. Fig. S1 in the Supplement), which is likely related to improvements in IGS satellite ephemerids and reference frame definition (Griffiths, 2019). The latter can be observed on the North, East and Up components directly at or shortly after the transitions to IGS08 and IGB08 reference frames (cf. Fig. S1 in the Supplement).

Pluri-annual signals with amplitudes of 1–5 mm over periods of 2–5 yr are evidenced in the North, East and Up components (e.g., 2008–2011). Similarly, residual annual and semi-annual signals are also detected despite the integration of these periodic motions in the time series model (eq. 1). These residual signals indicate the presence of coherent phenomena operating over large geographical scales (100s km) with varying durations, regularities and cyclicities. Longer series are required to confirm the presence of decadal or pluri-decadal (periods 10–15 years) signals, which could impact the estimations of long-term velocities.

2.3 Reference Frame

After PPP processing and the application of the regional common-mode correction, daily positions and velocities are in an informal reference frame tied to the IGS satellite orbits and clocks (IGb08). In order to analyze the relative motions and deformations in France and conterminous Western Europe, we rotate the velocities in a local frame, first using the Eurasia-ITRF2014 rotation defined by the ITRF2014 (Atamimi et al., 2016), then by minimizing the residual velocities of 200 stations distributed evenly over our region of interest and with time series duration greater than 7 years (Fig. 2).

In this “France-centered” reference frame, two regional-scale systematic motions are detected in the velocity field (cf. Fig. S2 in the Supplement). In northwestern Spain, a northward motion of ca. 0.1–0.3 mm yr$^{-1}$ may be associated with the clockwise rotation of Iberia relative to Eurasia described by Palano et al (2015) and Neres et al., (2016). This motion is not observed in the northeastern part of Spain, likely reflecting the location of the rotation pole and the specific dynamics of the Pyrenees (see Section 5.2). In northern Italy, the northern motion increasing eastward from 0 to ca. 3 mm yr$^{-1}$ is compatible with the counterclockwise rotation of the Adria microplate relative to Eurasia, with a rotation pole located in the Po plain (Battaglia et al., 2004; Farolfi et al., 2015). These tectonic movements are beyond the scope of our study.
2.4 Network densification

In order to densify the velocity field, we integrate data from additional networks (including campaign data) that were either processed or analyzed with a different procedure from the main dataset.

2.4.1 The Swiss network

Raw GNSS data (RINEX) are not available for Swiss stations, leading us to directly combine the processed velocities (http://pnac.swisstopo.admin.ch/restxt/) with ours. We perform a six-parameter Helmert transformation (rotation and translation rates without scale) to minimize the residual velocities at the 58 sites common to the two datasets. Post-transformation statistics indicate an average agreement for the common sites of 0.15, 0.13, and 0.37 mm yr\(^{-1}\) in the North, East and Up components. The Swiss velocities include both campaign and permanent station velocities, for which the uncertainties are estimated with an unspecified method (Brockmann et al., 2012). These uncertainties are much lower than ours, requiring a first-order scaling to homogenize the two datasets. By comparing the distributions of uncertainties of the 58 common sites between the two solutions, we estimate a multiplication factor 24 for the North and East components and 20 for the Up component, to adjust the distribution of Swiss uncertainties to ours. This simple scaling yields a good first-order agreement of the two distributions (based on the 10, 50, and 90 quantiles), but detailed analysis still points out residuals issues that affect the interpretation of the combined field (see Section 5.3).

2.4.2 Campaign data

For the French Alps, we include campaign data from sites measured for at least 48h during surveys in 1998, 2004, 2015, 2017 and 2018. The characteristics of the shortest and longest time series are 14 years with 2 surveys and 21 years with 5 surveys. In 1998 and 2004, measurements were made on tripods, while since 2015 the sites have been modified to use anchored mast in order to optimize installation stability and antenna height measurement. We use the same data processing for 24-h daily positions as for permanent stations but the time series analysis is different. Since the data are sporadic (a few points every 4–10 years), it is impossible to model annual and semi-annual seasonal signals, detect offsets and estimate noise characteristics by spectral analysis. No common-mode has been removed from the campaign data as the effect is not significant (Tarayoun et al., 2018). A careful re-analysis of the antenna heights and RINEX data allows us to estimate a long-term velocity (including daily position weighting by the measurement duration) for 29 sites in the French Alps (Fig. 2).

In the Pyrenees, campaign data extend from 1992 to 2017, but because of the relatively low quality of satellite orbits and clocks in the early and mid 1990s (Griffiths, 2019), data before 1996 cannot be included in the PPP processing, which represents ca. 20% of the campaign sites. To avoid this problem, we process the 75 Pyrenees campaign sites with the GAMIT/GLOBK software (Herring et al. 2009) following the strategy defined by Rigo et al. (2015) to process Pyrenean GPS data from 1992 to 2010. Given the early measurement dates, few continuous GPS sites are available to provide the reference frame stabilization. We identify 17 permanent sites with data back to 1995, in common with our PPP solution.
allowing a combination of the two velocity fields. These sites are unevenly distributed, with three-quarters located northeast of the Pyrenees within a few 100s km, leading to potential reference biases that are discussed in the velocity field interpretation (see Section 5.2).

Because of their sporadic and sparse point density, campaign time series are not amenable to noise model estimation and computation of formal uncertainties. There is no standard method for estimating campaign velocity uncertainty, but most of them rely on scaling based on the nearby continuous GNSS sites (Tarayoun et al., 2018; Beavan et al., 2016; Reilinger et al., 2006). In this study, we use synthetic time series constructed from permanent-station parameters (Masson et al., 2019) to generate synthetic campaign time series with the Alps and Pyrenees campaign characteristics (dates and number of surveys). We generate datasets with 2–7 campaigns of 3 days for a variety of time spans. The deviations of the estimated velocities (compared to the true velocity set to 0 mm yr$^{-1}$) are used to estimate statistical standard errors on the campaign data. For time series longer than 15 years with more than 2 surveys, the average horizontal velocity standard error is ca. 0.3 mm yr$^{-1}$. Longer durations and additional surveys reduce this standard error to ca. 0.2 mm yr$^{-1}$. We assign to each campaign site a velocity standard error accordingly to its campaign characteristics. This method yields identical uncertainties for sites of the same campaigns, thus neglecting inter-site variability, but it provides the most consistent campaign uncertainties compared with the permanent data, allowing for the most efficient integration of the two datasets.

### 2.5 Statistical detection of outliers

GNSS sites can be affected by non-linear signals related to site conditions (e.g., monument instability, changes in site conditions) or transient local phenomena (e.g., resource extraction). It is necessary to identify and exclude these stations from velocity solutions aiming at a tectonic and geodynamic study. To do so, we use two statistical methods based on geographical coherence considering that stations with a velocity significantly different from its neighbors is not representative of a tectonic movement (at least on the 100-km scale that we consider here). The statistical outlier detections are applied only on the horizontal velocities of permanent stations because vertical velocities show too much variability for robust results. Campaign stations are not included because of their large associated uncertainties.

First, a regression tree analysis (Breiman et al., 1984) is used to divide the network into an un-prescribed set of rectangular regions presenting the minimum dispersion of the station variables (longitude, latitude, and North and East velocities weighted by their standard errors). For all regions, we calculate the velocity range and then we determine the median of all ranges. Regions with a range larger than the overall median are subject to an outlier rejection. For each of those, sites with velocities outside of the \((Q_1 - 1.5 \times IQR, Q_3 + 1.5 \times IQR)\) range are rejected, where \(IQR\) is the interquartile range, and \(Q_1\) and \(Q_3\) are the first and third quartiles (Tukey, 1977).

Second, outlier stations are detected according to the Mahalanobis distance criteria. Mahalanobis distances \((D_M)\) are computed for the whole network using each station variables (longitude, latitude, and North and East velocities) to define the barycentre, covariance, and 95% confidence interval of the multidimensional space formed by the network variables.
(Mahalanobis, 1936). The term distance ($D_M$) does not refer to a spatial distance but to a statistical distance between each station variables and the barycentre of the multidimensional space formed by the network variables. Stations for which $D_M$ is greater than the network 95% confidence interval are considered as outliers and rejected.

Of the initial 1163 permanent stations, 180 stations are rejected as outliers. This outlier population has velocity statistics ($Q_1$, median and $Q_3$) three times larger than the remaining station population. Other methods of detection of outliers exist (e.g., Kreemer et al., 2018). The final velocity field is shown in Figure 3. The station spatial density over France and immediately neighboring regions is on average $8.0 \times 10^4$ site/km$^2$ (i.e., ca. 25 sites within a radius of 100 km), with differences between the regions (Fig. 2). Some regions such as the Paris Basin have a high density of stations ($10.5 \times 10^4$ site/km$^2$) while others have a lower density of stations, such as the Aquitaine Basin ($6.3 \times 10^4$ site/km$^2$). The integration of campaign stations has different impacts on the density in the French Alps and Pyrenees (Fig. 2). In the former, the density of stations is above the network average with and without the campaign data ($12.6 \times 10^4$ vs. $11.2 \times 10^4$ site/km$^2$). On the contrary in the Pyrenees, the density is significantly below the national average without the campaign stations ($5.0 \times 10^4$ site/km$^2$). The resolution of the spatial coherence analysis on velocities may be lower in areas with low density of stations than in areas with high density of stations.

**3 Extraction of coherent regional velocities**

In our local “France-centered” reference frame, individual station velocities and uncertainties tend to be of the same order of magnitude (Fig. 3), precluding a detailed interpretation of the kinematics and deformation. We use two independent statistical approaches (clustering and spatial smoothing) to extract spatially coherent information on the present-day deformation at a spatial scale of 100–200 km. To a first order, this distance represents the expected scale of tectonic deformation in France and neighboring regions. It corresponds to the average width of the major tectonic systems (French Alps, Pyrenees, South Armorican Shear Zone, etc.). We apply each method (clustering and smoothing) on the GPS velocities. The two methods are fully independent. Clustering only provides a velocity field and no strain rate field. The strain rate map (Fig. 7a) is computed using the smoothing method only (based on the GPS velocities), independently of the clustering analysis.

The smoothing and clustering methods are tuned to extract coherent signals on geographical domains at this spatial scale by minimizing local noise without losing the regional signal. The robustness of the results is estimated with two independent approaches:

- We use synthetic data to estimate each method detection level. The synthetic dataset corresponds to random velocities derived from the combination of a null long-term velocity, annual and semi-annual sinusoids, position offsets and colored noise (eq. 1), with all parameters based on our GPS data characteristics (cf. Masson et al., 2019 for details). Thus, this dataset corresponds to null velocity and strain rate fields with additional noise representative of our actual GPS data. Synthetic and actual data are compared after processing by the clustering or smoothing methods to estimate their respective detection levels.
We estimate statistical standard errors on the velocities and strain rates calculated with the clustering or smoothing methods using a simple Monte Carlo and Bootstrap resampling of the original GPS velocities on the basis of their standard errors (Monte Carlo) and regional distribution (Bootstrap). Hereafter, the smoothed or clustered velocities and strain rates are given as the mean and 95% confidence interval (CI95) of the Monte Carlo / Bootstrap samples. Using 95% confidence intervals (rather than the more common standard errors) yields a strict definition of significant vs. not significant signals, which should be nuanced in cases of values close to the limits.

3.1 Clustering applied to GPS velocities

Clustering is a parametric unsupervised learning method and has been used in GNSS analyses to perform geographical groupings of stations with optimum velocity consistency (Savage et al., 2013 and 2018; Liu et al., 2015; Ozdemir et al., 2019). Several methods of clustering exist; here we use the k-means method (Hartigan and Wong, 1979) whose advantage is that the formed groups do not have a predefined geometry or size and allow for abrupt changes so to adapt to local geometries. In order to extract spatial coherence in the velocity field, we define clusters using station coordinates (longitude and latitude) and horizontal (north and east) or vertical velocities; vertical velocities are treated independently because of their large dispersions and uncertainties. The variables are not normalized, in order to ensure first-order geographical clustering with secondary adjustments based on the velocity variability.

The analysis takes place in four steps: 1) choice of random clusters (based on a predefined initial number); 2) minimization of the Euclidian distances between the cluster centroids and the different observations; 3) shift of the initial centroids to the mean of the groups; 4) minimization of the Euclidian distances according to new centroids from an increase of the cluster number and modifications of their boundaries. The last three steps are repeated until convergence to the predefined final number of clusters and no observation changes clusters. At the end of the process, each GNSS station is attributed a velocity that corresponds to its final cluster median.

We run the algorithm 50000 times in order to take into account three stochastic aspects of the computation:

- The choice of the final number of clusters is crucial as it controls the average cluster size (geographical extent and number of stations). In order to average velocities over 100–200 km spatial scale, we vary the final number of clusters between 75 and 200 (uniform distribution), resulting in a mean cluster area of $27.5 \times 10^3$ km$^2$ (i.e., scale ca. 166 km), with variations of a factor of 2–3 in the cluster sizes. A larger number of clusters (smaller spatial scale) leads to strong variability and incoherence of the final velocities.
- The random choice of initial clusters results in variability in the final results. We take advantage of this effect to improve the statistics of the results by varying the initial number of clusters between 1 and the final number divided by 2 (uniform distribution).
- In order to account for each station specific velocity uncertainty, we redefine its velocity using a random draw in a normal distribution defined by its velocity mean and standard deviation. Thus, sites with high uncertainties have a large variability and less weight in the overall cluster analysis.

For each station, the final velocity is defined as the median, with the associated 95% confidence interval, of the 50000 computations. The clustered horizontal and vertical velocities are presented on Figures 4 and 5a. The comparison of clustered velocities based on the actual GPS data and on the synthetic dataset indicates a detection level for the horizontal velocities of 0.12 mm yr$^{-1}$ (cf. Fig. S3.1 in the Supplement). Only 10% of the stations are associated with a clustered velocity
below this detection level (Fig. 4a). Vertical velocities are not analyzed with the synthetic comparison because of their high dispersion and spatial noise. Their interpretation is thus subject to caution.

Coherent horizontal patterns are observed with velocities *ca. 0.1–0.4 mm yr⁻¹* (Fig. 4a). Associated 95% confidence intervals are mostly *ca. 0.1–0.2 mm yr⁻¹*, except in the Pyrenees, Alps and Paris Basin where they reach 0.4–0.5 mm yr⁻¹ (Fig. 4b). The vertical velocities are associated with larger *CL₉₅ ca. 0.4–0.8 mm yr⁻¹*. The only significant vertical patterns (Fig. 5a) are the subsidence in the Paris Basin (*ca. 0.5–1 mm yr⁻¹*) and uplift in the Western and Central Alps (*ca. 0.5–2 mm yr⁻¹*).

### 3.2 Gaussian smoothing applied to GPS velocities

Smoothing is a standard technique for data interpolation, filtering and noise reduction. It allows the extraction of a continuous field, minimizing small-scale noise and precluding abrupt spatial changes. We use a Gaussian smoothing function to compute at any point in space a smoothed velocity \( V_{gi} \) based on all GPS velocities weighted according to their standard errors and their distance to the computation point (after Mazzotti et al., 2011):

\[
V_{gi} = \frac{\sum_{n=1}^{N} \frac{G_n V_n}{\sigma_n^2}}{W_i} \tag{2}
\]

with

\[
G_n = e^{-\log(2) \frac{\Delta_n^2}{r_g^2}}
\]

\[
W_i = \sum_{n=1}^{N} \frac{G_n}{\sigma_n^2}
\]

where \( i \) is the velocity component (North, East or Up), \( r_g \) is the smoothing length (half-width of the Gaussian function), \( V_n \) and \( \sigma_n \) are the velocity and standard error of the GPS station \( n \), and \( \Delta_n \) is the distance to the GPS station \( n \). The spatial derivative of the Gaussian function can be used to compute the smoothed horizontal strain rate tensor \( \dot{\varepsilon}_s \) at the same location:
The smoothed velocity and horizontal strain rate fields, and associated 95% confidence intervals, are presented in Figures 5b, 6 and 7. (The smoothed horizontal strain rate fields but without excluding outliers is presented in Figure S5 in the Supplement.) Horizontal strain rates are expressed in terms of “maximum strain rate”:

\[ \varepsilon_{\text{max}} = \max(|e_1|, |e_2|, |e_1 + e_2|) \]  

(4)

where \( e_1 \) and \( e_2 \) are the principal components of the strain rate tensor. The comparison of the smoothed velocities and strain rates based on the actual GPS data with those based on the synthetic dataset (cf. Figs. S3.2 and S3.3 in the Supplement) indicates detection levels of 0.04 mm yr\(^{-1}\) for the horizontal velocities and 0.35 x 10\(^{-9}\) yr\(^{-1}\) for the horizontal strain rates. Less than 5% of the results are below the detection level (Figs. 6a and 7a), similar to the clustering analysis.

Coherent patterns are observed with horizontal (resp. vertical) velocities ca. 0.1–0.4 mm yr\(^{-1}\) (0.2–1.6 mm yr\(^{-1}\)), similar to a first order to those obtained with the clustering method (Figs. 4 vs. 6 and Fig. 5). Statistical 95% confidence intervals on the horizontal velocities and strain rates are respectively ca. 0.05–0.1 mm yr\(^{-1}\) and ca. 0.7–0.9 x 10\(^{-9}\) yr\(^{-1}\), indicating that more than two-thirds of the velocities and strain rates are statistically significant (Figs. 6 and 7).
3.3 Coherence of clustering and Gaussian smoothing results

To first order, the clustered and smoothed velocity fields show a striking agreement in both the horizontal components (Figs. 4a and 6a) and the vertical components (Fig. 5). In order to better characterize the coherence of the two velocity fields, and its potential regional variability, we compute the difference between the two methods for each velocity component (North, East and Up). The dispersion of the North and East differences (cf. Fig. S6 in the Supplement) illustrates the consistency of the two methods: 28% of the differences are smaller than 0.05 mm yr\(^{-1}\) and 60% are smaller than 0.10 mm yr\(^{-1}\). In Figure 8, we identify the areas where the horizontal velocity differences are larger than 0.1 mm yr\(^{-1}\): the westernmost part of Brittany, parts of the Paris Basin, most of the Western Alps (especially near the France-Swiss-Italy borders) and the Pyrenees and their northern foreland. For these areas, the interpretations of the velocity fields must be carried out with caution. These velocity differences at the level of 0.1–0.3 mm yr\(^{-1}\) can be related to either abrupt spatial variations in the actual velocity and deformation patterns, or biases and limitations in one or both methods. Figure S7 in the Supplement shows vector differences between the two methods and the differences between the two velocity fields and the GPS velocities and confirms what is shown on Figure 8.

4 Large-scale deformation patterns

The analysis of the deformation in France and conterminous regions can be guided using the uncertainty levels described in section 3. To a first order, we consider as “well resolved” areas of 100–200-km scale or more within which (1) the GNSS station density is similar to or larger than the network average, (2) the clustered and smoothed velocities are consistent at 0.1 mm yr\(^{-1}\) or better. In contrast, areas where one of the criteria is not satisfied are considered less well constrained. These correspond roughly to the region northeast of the France-Belgium-Germany border (very low station density), the center and northwest of the Paris Basin, most of the Alps and northwestern Italy, and the Spain-Pyrenees region south of about 44° N (Fig. 8). The last three are discussed in more details in section 5.

Most of central, northern and western France is associated with coherent clustered and smoothed velocities resolved at ca. 0.1 mm yr\(^{-1}\). There, the first order and most important deformation signal is that, relative to the “France-centered” reference, western and central France are characterized by eastward to northeastward motions of 0.1–0.2 mm yr\(^{-1}\), whereas northeastern France shows 0–0.2 mm yr\(^{-1}\) southward to southwestward velocities (Figs. 4 and 6). The resulting overall deformation pattern corresponds to a belt of N-S to NE-SW shortening of \((1–2) \times 10^{-5}\) yr\(^{-1}\) in central and eastern France (Fig. 7).

In details, this first-order kinematic pattern is associated with regional variability, with extension in the Armorican Massif and a complex strain rate pattern in the Aquitaine Basin. In more details, from West to East:

- The western Armorican Massif is associated with a small E-W extension rate \((0.4–0.8 \times 10^{-5}\) yr\(^{-1}\), \(CI_{EL} = 1.0–1.2 \times 10^{-5}\) yr\(^{-1}\) subject to caution because of the high uncertainty. The smoothed and clustered velocities differ, likely due to the network configuration (lack of stations on three sides of the peninsula), precluding a more detailed spatial analysis. In the eastern part, the extension rotates to a N-S direction with similar rates and slightly lower uncertainties \((0.3–0.7 \times 10^{-5}\) yr\(^{-1}\), \(CI_{NS} = 0.6–0.8 \times 10^{-5}\) yr\(^{-1}\)). Smoothed and clustered vertical velocities reveal a
low generalized subsidence (-0.2 mm yr⁻¹, $C_{\text{LS}} \approx 0.1$ mm yr⁻¹ and -0.3 mm yr⁻¹, $C_{\text{LS}} \approx 0.3$ mm yr⁻¹, respectively). The overall extension is roughly compatible with the deformation and stress analyses from focal mechanisms that indicate NE-SW extension in Brittany (Mazabraud et al., 2004).

- To the south, the Aquitaine Basin shows a complex pattern of high strain rates ($1.5 - 2 \times 10^{-9}$ yr⁻¹) with N-S shortening in the northwest, E-W shortening in the southwest in the Pyrenees foreland, and E-W extension in the east at the border with the Massif Central (Fig. 7). All rates are statistically significant, but the low density of GNSS stations in the east strongly limits the validity of the E-W extension pattern. Both smoothed and clustered vertical velocities show a barely significant small subsidence (-0.15 mm yr⁻¹, $C_{\text{LS}} \approx 0.1$ mm yr⁻¹ and -0.3 mm yr⁻¹, $C_{\text{LS}} \approx 0.4$ mm yr⁻¹, respectively). The strong and spatially varying strain rates are surprising in light of the low seismicity (Fig. 1) and very few indications of active tectonics (Baize et al., 2013; Jomard et al., 2017). Peculiar hydrological loading is not reflected in the time series annual or pluri-annual signals.

- To the east, the large-scale pattern of E-W to NE-SW shortening is observed in the Massif Central ($0.8 - 1.0 \times 10^{-9}$ yr⁻¹, $C_{\text{LS}} = 0.5 - 0.7 \times 10^{-9}$ yr⁻¹), associated with near-zero vertical velocities, and in northeastern France, including strong shortening rates ($2 - 3 \times 10^{-9}$ yr⁻¹) rotating from E-W in the Bresse to N-S in the Upper Rhine Graben (Fig. 7). There, clustered velocities show a small subsidence (-0.4 mm yr⁻¹, $C_{\text{LS}} \approx 0.6$ mm yr⁻¹) not present in the smoothed velocities, indicating either a small-scale signal (< 10 km) or noise in the original data. This deformation pattern is discussed in more detail in section 5.3.

Finally, Corsica presents a coherent, near-rigid northward motion relative to the continent, similar between the smoothing and clustering methods at 0.4 mm yr⁻¹ ($C_{\text{LS}} = 0.1$ mm yr⁻¹), that may be related to the present-day tectonics of the Apennine-Tyrrhenian system (Figs. 4 and 6). This northern motion creates a domain of significant NNW-SSE shortening of $2.0 \times 10^{-9}$ yr⁻¹ ($C_{\text{LS}} \approx 0.2 \times 10^{-9}$ yr⁻¹) north of Corsica (Fig. 7), compatible with the tectonic and seismicity observations along the Ligure Margin (Larroque et al., 2012, 2016).

5 Regions with complex velocity and deformation patterns

Complex velocity and deformation patterns require more careful analysis in three specific regions: the Paris Basin, the Pyrenees and the Western Alps (associated with the Upper Rhine Graben). The first is associated with a very low seismicity, unlike the other two that are the most seismically active area of Western Europe.

5.1 The Paris Basin

For 20% of the stations in the Paris Basin, the differences between the clustered and smoothed velocities are between 0.1 and 0.3 mm yr⁻¹ (Fig. 8), but there is a general consistency in the spatial variations of the velocity directions: from west to east, ENE to NE for smoothing, Fig. 6a, and NE to SSE for clustering, Fig. 4a. The spatial variations are by definition sharper for the clustering results. These result in a significant NE-SW shortening ($0.8 \times 10^{-9}$ yr⁻¹, $C_{\text{LS}} \approx 0.6 \times 10^{-9}$ yr⁻¹), part of the large-scale shortening belt (section 4), without seismicity and with very few identified active faults (Fig. 1). Smoothed and clustered vertical velocities show a generalized subsidence (-0.3 mm yr⁻¹, $C_{\text{LS}} \approx 0.1$ mm yr⁻¹ and -0.5 mm yr⁻¹, $C_{\text{LS}} \approx 0.7$ mm yr⁻¹, respectively) with however a potential small area of uplift around Paris for the clustered velocities (0.35 mm yr⁻¹, $C_{\text{LS}} \approx 0.6$ mm yr⁻¹). The amplitudes of seasonal signals are more important than the national median (+29% for the annual
signals in E and +48% in U) suggesting that hydrological processes or natural resource extraction may contribute to the observed deformation.

5.2. Pyrenees

Most of the GNSS sites in the Pyrenees are campaign sites with large uncertainties. For about 50% of the stations, the differences between the smoothed and clustered velocities are between 0.1 and 0.4 mm yr⁻¹, but the orientations are similar (Fig. 4a and 6a). These differences may be due to the fact that most of the sites have been surveyed only twice with the first survey in the mid 1990s, when the satellite orbits and clocks were of lower quality, and the permanent GPS network was very sparse providing only few common stations for the solution combination (see Section 2.4.2). As a result, the campaign velocities are associated with large standard errors, leading to a low weight in the smoothing results.

Despite these differences, a first-order pattern of N-S extension is clearly visible in both the clustered and smoothed velocities (between 0.2 and 0.4 mm yr⁻¹). The extension rate decreases from west (1.5 × 10⁻⁹ yr⁻¹, C₁ₑ ≈ 0.8 × 10⁻⁹ yr⁻¹) to east (1.0 × 10⁻⁹ yr⁻¹, Cₑ ≈ 0.8 × 10⁻⁹ yr⁻¹), with an associated rotation of the extension direction from NNE-SSW to N-S (Fig. 9). Most vertical velocities are not significant, except in the eastern region with a value barely significant of 0.18 mm yr⁻¹, Cᵥ ≈ 0.2 mm yr⁻¹ for the smoothed velocities.

The seismicity of the Pyrenees is heterogeneously distributed along the orogen (Chevrot et al., 2011; Calvet et al., 2013). It is diffuse in the east and more focused in the west along the North Pyrenean Fault system (Fig. 9). In the central part of Pyrenees, the GPS-based extension zone extends over a wider area than the seismicity, but remains located within the northern and southern limits of the Pyrenean orogen. This difference in the spatial distribution of the seismicity, orogen topography, and GPS extension may be attributed to three potential causes:

1. Actual present-day deformation only takes place within the zone of high seismicity and our GPS analysis does not allow such a fine localization because of the limits in the smoothing and cluster spatial scales (100-200 km, see Section 3).
2. The location of the current seismicity does not reflect the location of the deformation on a longer time scale, which is in contrast, captured by GPS data. This would indicate potential large earthquakes outside present-day seismicity zone.
3. The deformation measured by GPS at the surface reflects a deeper aseismic deformation centered on the orogen center / highest topography, and not only the crustal seismic deformation.

5.3. The Alps and the Upper Rhine Graben

In the Alps, for 28% of the stations the differences between the clustering and smoothing methods are between 0.1 and 0.5 mm yr⁻¹, but the velocities have consistent directions. Roughly northward velocities of 0.2–0.4 mm yr⁻¹ in the Swiss Alps and nearby Jura (Fig. 4a and 6a) result in significant N-S extension ca. 2.1 × 10⁻⁹ yr⁻¹ near and south of the Swiss-Italy border, and N-S shortening ca. 1.8 × 10⁻⁹ yr⁻¹ in the Vosges - Upper Rhine Graben - Black Forest region. The region in between (most of Switzerland) is associated with low deformation (Fig. 7). The western foreland of the Alps (Saône Valley, the Jura and Rhone Valley) is mainly characterized by E-W shortening (ca. 0.8–2 × 10⁻⁹ yr⁻¹), in relation with the eastward motion of
the Massif Central and central France (see Section 4). These results are consistent with those reported in other geodetic studies (Sanchez et al., 2018). The central and southern parts of the Western Alps show a transition from N-S extension to strike-slip and E-W extension in the south, associated with the 0.2–0.4 mm yr\(^{-1}\) eastward motion in southeastern-most France and the western Po Plain (Figs. 4a and 6a). To a first order, these deformation patterns in the French Alps are consistent with those observed in Walpersdorf et al. (2018), although our strain rate amplitudes are on average 2–3 time smaller, potentially due to the lower number of stations and spatial coverage used in Walpersdorf et al. (2018).

The vertical velocities (Fig 5) have the same large-scale pattern in the two methods, with a maximum of uplift in the northern French and Swiss Alps (ca. 1.5–2 mm yr\(^{-1}\)) decreasing to near-zero (± 0.5 mm yr\(^{-1}\)) in the Southern Alps, the Rhone valley, the Po Plain and the Jura. This pattern is consistent with that derived from previous GPS data analysis and combinations with leveling data (Nocquet et al., 2016; Sternai et al., 2018). A more detailed analysis of the transition from relatively fast uplift to near-zero (or small subsidence) rates is restricted by the limits of the smoothing and clustering methods, as well as the low precision of individual stations.

The seismicity is distributed over the whole Alpine system (Figs. 1 and 10), with a concentration of epicenters in the southwest of Switzerland (Deichmann et al., 2012). For the regions of the Vosges and Jura, the analysis of focal mechanisms provides results compatible with our geodetic deformations (Plenefisch et al. al., 1997, Maurer et al., 1997, Sue et al., 1999 and 2007). The compatibility suggests a tectonic origin of this deformation. The GPS-derived N-S extension near the Swiss-Italy-French borders is compatible with the earthquake focal mechanism analysis of Delacou et al., 2004, but the peak of deformation is located south of the seismicity concentration in a region of relatively low activity (Fig. 10). The location of the maximal extension depends on how the uncertainties from the Swiss velocity field are scaled when combined with our solution. If the weight of the Swiss velocities is reduced, the maximum extension is shifted 50 km northward, near the Switzerland-Italy border at a location consistent with the seismicity. This issue points out the importance of consistent processing and uncertainty analysis of all raw GNSS data (RINEX). In addition, the region of Aosta is devoid of stations in our analysis, leading to an additional source of uncertainty on the precise localization of the maximum deformation. If the GPS-seismicity localization difference proves to be real, it may the expression of deformation not only accommodated by seismicity or of a lack of large earthquakes in the high strain rate area.

6. Conclusions

The application of semi-automatic statistical methods allows us to evaluate the potential of dense networks and large GNSS datasets to extract spatially coherent and significant deformation rates in France and conterminous Western Europe. In particular, the combination of spatial smoothing and clustering approaches on more than 900 GPS velocities results, for the first time, in the definition of horizontal velocity and strain rate fields with a 95% confidence level ca. 0.1–0.2 mm yr\(^{-1}\) (ca. 0.5–1 x 10\(^{-9}\) yr\(^{-1}\)) on spatial scales of 100–200 km or more (Figs. 4b, 6b, 7b). In most of the study area, the calculated
velocity and strain rate patterns are just at or above the 95% significant level. Based on this analysis, several conclusions can be drawn:

- The first order and most important deformation signal in France and neighboring Western Europe is a belt of N-S to NE-SW shortening (ca. 0.2–0.4 mm yr\(^{-1}\) (1–2 × 10\(^{-5}\) yr\(^{-1}\)) in central and eastern France.
- We observe orogen-normal (radial) extension (ca. 1–2 × 10\(^{-5}\) yr\(^{-1}\)) in the Western Alps and the Pyrenees, associated with radial shortening in the Western Alps foreland, compatible with previous studies (e.g., Rigo et al., 2015; Walpersdorf et al., 2018).
- In addition, several areas (Aquitaine Basin, Brittany, Bresse) present unexpected high deformation rates, some of them anti-correlated with the local level of seismicity.
- The only significant vertical velocity patterns are the subsidence in the Paris Basin (ca. 0.5–1 mm yr\(^{-1}\)) and uplift in the Western and Central Alps (ca. 0.5–2 mm yr\(^{-1}\)).

These results open questions about the origin and the time scales of these deformations, as well as their relationship with seismicity and the potential for significant aseismic deformation in France and Western Europe. In particular, these small velocity and deformations signals may relate to a variety of non-tectonic forces, such as Glacial Isostatic Adjustment or hydrological loading, operating from a local (100–200 km) to a continental scale. In North America, Kreemer et al. (2018) have shown that, to first order, geodetic deformation is not directly correlated to seismicity and that the link between long-term tectonic processes, transient processes (GIA), seismicity and geodetic deformation is not simple at the scale of the regional deformation (> 100 km).

In addition to these observations, our methodological developments highlight two conclusions regarding the potential of future more detailed analyses:

- The station density is critical to eliminate outliers and extract spatially coherent deformation signals in very low deformation areas such as intraplate domains and volcanic areas. Non-geodetic networks and campaign data, although of potentially lower resolution compared to permanent geodetic stations, can provide important densification.
- A consistent processing of the raw GNSS data (RINEX) and position time series is essential to extract significant deformation. Our results for the Western Alps are currently limited by the post-processing combination of velocity solutions that result in uncertainties of ca. 50 km in the peak of the extension pattern.

Finally, the combination of mathematical techniques for extracting spatially coherent signals can provide confidence, or point out limitations, in the observed deformation patterns beyond the application of simple standard error estimations.

Data Availability
The data providers file shows all the sources used to obtain the data present in this study. The time series analyses were performed using R (R Core Team, 2016). Maps were done with GMT5 (Wessel et al., 2011).

Author contributions.
CM, ED and PV processed the GPS data. CM and SM developed the analysis methods. CM did the statistical analyses. CM, SM, and PV interpreted the results and wrote the article.

Competing interests.
The authors declare that they have no conflict of interest.

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