

# Gravity Effect of Alpine Slab Segments Based on Geophysical and Petrological Modelling

Maximilian Lowe<sup>1,2,3</sup>, Jörg Ebbing<sup>1</sup>, Amr El-Sharkawy<sup>1,4</sup>, Thomas Meier<sup>1</sup>

<sup>1</sup> Institute for Geosciences, Kiel University, Germany

<sup>2</sup> NERC British Antarctic Survey, Cambridge, United Kingdom

<sup>3</sup> School of geosciences, University of Edinburgh, United Kingdom

<sup>4</sup> National Research Institute of Astronomy and Geophysics (NRIAG), 11421, Helwan, Cairo, Egypt

Correspondence to Maximilian Lowe: maxwe32@bas.ac.uk

## Abstract

In this study, we present an estimate of the gravity signal of the slabs beneath the Alpine mountain belt. Estimates of the gravity effect of the subducting slabs are often omitted or simplified in crustal scale models. The related signal is here calculated for alternative slab configurations at near surface height and on a satellite altitude of 225 km.

We apply three different modelling approaches in order to estimate the gravity signal from the subducting slab segments, by: i) Direct conversion of upper mantle seismic velocities to density distribution, which are then forward calculated to obtain the gravity signal. ii) Definition of slab geometries based on seismic crustal thickness and high-resolution upper mantle tomography for two competing slab configurations. The geometries are then forward calculated by assigning a constant density contrast and slab thickness. iii) Accounting for compositional and thermal variations with depth within the predefined slab geometry.

Forward calculations predict a ~~positive~~ gravity signal of up to 40 mGal for the Alpine slab configuration. Significant differences in the gravity anomaly patterns are visible for different slab geometries in the near surface gravity field. However, different contributing slab segments are not easily separated, especially at satellite altitude. Our results demonstrate that future studies addressing the lithospheric structure of the Alps should have to account for the subducting slabs in order to provide a meaningful representation of the geodynamic complex Alpine area.

## Keywords:

Satellite gravity gradient, Alpine subduction, lithospheric and sub lithospheric structure, mantle composition, seismic tomography

## 1. Introduction

Interpretation of gravity anomalies can reveal information on the architecture and tectonic setting of the lithosphere (e.g. Zeyen, & Fernández, 1994; McKenzie & Fairhead, 1997; Holzrichter & Ebbing, 2006; Braitenberg, 2015; Spooner et al. 2019). For subduction zones, like the Andes, several studies have shown that the gravity effect of the subducting plates is significant and has to be considered in order to study the feedback between the subducting lithosphere and the overriding plate (Götze et al. 1994; Götze & Krause 2002; Tašárová 2007; Gutknecht et al. 2014; Götze & Pail 2018; Mahatsente 2019). ~~For Subducting~~ lithosphere ~~to~~

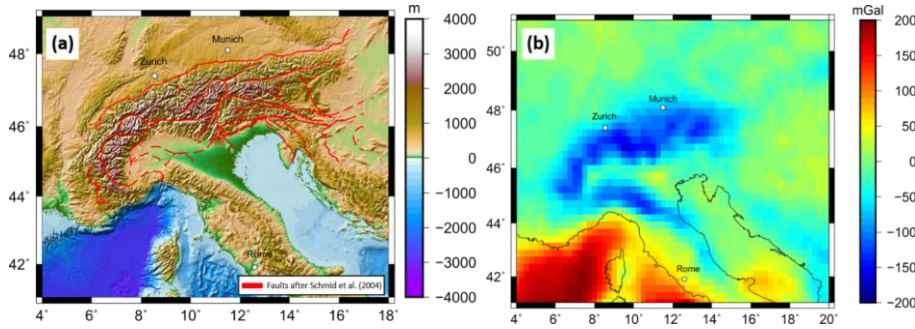
subduct, ~~has~~ a higher density than the surrounding mantle material at the same depth interval is  
 required, causing a negative buoyancy for the slab and therefore the slab is subducted into  
 earth's interior (e.g. Kincaid & Olson 1987; Ganguly et al. 2009). However, the gravitational  
 contribution of subducting material in the upper mantle to the gravity field has so far not been  
 systematically addressed for the Alpine system. In order to provide an assessment, the  
 magnitude of the gravity signal of such sub-crustal long wavelength features has to be estimated.  
 The Alpine mountain belt (Fig. 1a) is chosen for this sensitivity study because firstly a large  
 range of recent seismic ~~topography~~ tomography studies imaged subducting slab segments in  
 the Alpine region (e.g. Babuska et al., 1990; Lippitsch et al., 2003; Spakman & Wortel, 2004;  
 Mitterbauer et al. 2011; Karousová et al., 2013; Zhao et al., 2016; Kästle et al., 2018; El-  
 Sharkawy et al., 2020). Those different studies suggest different configurations of slab  
 segments (see section 1.1), allowing us to test how sensitive the gravity field is to varying  
 geometries of subducting slab segments. ~~Secondly, previous Alpine models addressing the~~  
~~Alpine gravity field have not considered any slab segments, rather they only account for the~~  
~~thickness of the lithosphere (e.g. Ebbing et al., 2006; Spooner et al., 2019; Tadiello and~~  
~~Braitenberg 2020).~~ Secondly, previous Alpine models addressing the Alpine gravity field have  
considered the subcrustal mantle inhomogeneities in form of lithosphere thickness (e.g. Ebbing  
et al., 2006; Spooner et al., 2019) or in form of mantle density variations (Tadiello and  
Braitenberg 2021), but without identifying the isolated effect of subducting slabs segments in  
the velocity or density variations. If the contribution of the slab is not considered, a significant  
~~part of the gravity field might be attributed to crustal thickness variations or intra-crustal~~  
~~sources.~~ If the contribution of the mantle density variations is not considered, a significant part  
of the gravity field might be attributed to crustal thickness variations or intra-crustal sources.  
 In addition, the Bouguer Anomaly of the Alps (Fig. 1b) shows no direct sign of subducting slabs  
 (in contrast to the Andes subduct zone) as the field is dominated by crustal thickness variations  
 (Ebbing et al., 2001, 2006). Therefore, forward modeling of the proposed slab geometries, as

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69 imaged by high-resolution tomographic studies, is necessary to separate the gravity signal  
 70 caused by the subducting slabs from the gravity anomaly field.



72 **Figure 1.** (a) Topography from ETOPO1 from Amante and Eakins (2009). Faults in red after Schmid et al. (2004). (b) Bouguer  
 73 Anomaly based on XGM 2019 (Zingerle et al., 2020) with a maximum spherical harmonics degree of 719 at a station height of  
 74 6040m above the ellipsoid, just above the surface of the Alps. Correction density for rock: 2670 kg/m<sup>3</sup> and for water: 1030  
 75 kg/m<sup>3</sup>.

76 We present three different approaches to model the gravity effect of the slab segments and  
 77 discuss the strengths and limitations of the applied methods. In the first approach, the alpine  
 78 sup-crustal density distribution is derived by converting seismic velocities to density. This  
 79 model is then forward calculated to estimate the gravity response. In the second approach, 3D  
 80 slab geometries are derived by evaluating seismic crustal thickness estimations and high-  
 81 resolution upper mantle tomographic models. Here, two competing slab configurations are  
 82 chosen. The predefined slab geometries are then forward calculated by assigning different  
 83 density contrasts and slab thicknesses. The third approach uses similar predefined slab  
 84 configurations as in the second approach, however, here we consider petrology, temperature,  
 85 and density variation. The gravity response is calculated for all three approaches at a near  
 86 surface height for the gravity disturbance and the gravity gradients at satellite altitude of 225  
 87 km.

### 88 1.1 Alpine setting

89 The formation and present geodynamics of the Alps are linked to long lasting tectonic  
 90 processes, including Adria-Europe continent-continent collision, subduction of oceanic and  
 91 continental lithosphere, the formation of crustal nappes as well as extensional and

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92 compressional processes (Frisch, 1979; Stampfli & Borel, 2002; Handy, et al., 2010, 2015).  
 93 The Adriatic microplate is a major driver of the present geodynamics in the Alpine region,  
 94 which is trapped between the converging major plates of Europe and Africa. Adria is moving  
 95 counterclockwise with respect to Europe, as seen by GPS observations (e.g. Nocquet and Calais,  
 96 2004; Vrabec and Fodor, 2006; Serpelloni et al., 2016) and is subducted beneath the Apennines  
 97 to the west as well as to the east beneath the Dinarides, while colliding with Eurasia in the Alps  
 98 to the north (e.g. Channel & Horvath, 1976; Dewey et al., 1989; Stampfli & Borel, 2002; Handy  
 99 et al., 2010; Le Breton et al., 2017). Subducting slab segments have been imaged by different  
 100 seismological body wave travel time tomographic studies as well as surface wave tomographic  
 101 studies within the Alpine upper mantle (e.g. Babuska et al., 1990; Lippitsch et al., 2003;  
 102 Spakman & Wortel, 2004; Mitterbauer et al. 2011; Karousová et al., 2013; Zhao et al., 2016;  
 103 Kästle et al., 2018; El-Sharkawy et al., 2020). However, the configuration of subducting slab  
 104 segments remains controversial. In the Western Alps, Lippitsch et al. (2003) propose a slab  
 105 break-off at about 100 km depth, which is in line with the findings of Beller et al. (2018), Kästle  
 106 et al. (2018) and El-Sharkawy et al. (2020). In contrast, a continuous subducting slab segment  
 107 in the Western Alps, down to at least 250 km depth, is imaged by a number of other tomographic  
 108 models (e.g. Koulakov et al., 2009; Zhao et al., 2016; Hua et al., 2017; Lyu et al., 2017).  
 109 A continuous subduction of Eurasia beneath the Central Alps down to at least 200 km depth is  
 110 imaged by different tomographic models (e.g. Lippitsch et al., 2003; Piromallo and  
 111 Morelli, 2003; Koulakov et al., 2009; Mitterbauer et al., 2011; Hua et al., 2017; Fichtner  
 112 et al., 2018; El-Sharkawy et al., 2020). A potential slab gap with an approximately size of 2° is  
 113 separating the subducting slab segments in the Central Alps to the Eastern Alps as imaged by  
 114 e.g. Lippitsch et al. (2003). The slab configuration and subduction direction in the Eastern Alps  
 115 remains unclear. According to the classical view, Eurasia is subducting beneath Adria in a  
 116 southward subduction (Hawkesworth et al., 1975; Lüschen et al., 2004; 2006). This idea was  
 117 challenged by Lippitsch et al. (2003), Schmid et al. (2004), Kissling et al. (2006), Handy et al.

(2015), and Hetenyi et al. (2018). Instead, slab break-off in the eastern Alps and a northward-dipping Adriatic slab in the easternmost Alps is suggested, leading to a switch of the slab polarity, as Adria is subducting beneath the European plate (Handy et al., 2015). The view that Adriatic and not Eurasian lithosphere is subducting northwards in the Eastern Alps has been opposed by Mitterbauer et al. (2011), as their model shows a northward dipping slab in the eastern most Alps connected to the European plate. In an early tomographic study, Babuska et al. (1990) proposed that both Eurasian and Adriatic lithosphere is subducting in the eastern Alps. In subsequent studies and interpretations this model was mentioned but northward subduction of Adria seems to be favoured (e.g. Karousov~~á~~<sup>a</sup> et al., 2013; Hetenyi et al., 2018). Recently, subduction of both Eurasian and Adriatic lithosphere in the eastern Alps down to about 150 km has been suggested by Kästle et al. (2020) and El-Sharkawy et al. (2020) based on surface wave studies. For a more in-depth comparison and discussion of tomographic Alpine models the reader is referred to e.g. Kästle et al. (2020).

## 2. Data

The Bouguer Anomaly (Fig. 1b) is based on the global model *XGM 2019* (Zingerle et al., ~~2019~~2020) developed for spherical harmonics up to degree 719, with a resolution of ~25 km (half wavelength). The XGM 2019 model is a global integrated gravity model, which includes satellite and terrestrial measurements. The ~~simple~~-Bouguer Anomaly is calculated from the Free-Air gravity disturbance with a correction density of 2670 kg/m<sup>3</sup> for topography, and a correction density for water of 1030 kg/m<sup>3</sup> for the offshore areas using Tesseroids (Uieda et al., 2016). For the tesseroids, we use the topography and bathymetry from ETOPO (Amante & Eakins, 2009), which was regridded at a regular grid with a grid space of 25 km to match the resolution of the XGM 2019 model for a maximum degree of 719. ~~We calculated the gravity contribution of the topography and bathymetry using Tesseroids and subtracting the signal proportion from the Free-Air Anomaly to obtain the Bouguer Anomaly. For the topography and~~

bathymetry information, we use ETOPO1 with a 1 arc minute resolution (Amante & Eakins, 2009), which was regrided at a regular grid with a grid space of 25 km to match the resolution of the XGM 2019 model for a maximum degree of 719. The gravity field is defined at a constant station height of 6040 m above the ellipsoid, just above the surface of the Alps. The resulting Bouguer Anomaly shows a gravity low in the order of -200 mGal over the high topography of the Alps, indicating an isostatic ~~compensation of the crustal thickening in response to~~ topography (e.g. Ebbing et al., 2006). Additionally, we calculate the ~~topographic correction~~ mass correction for the gravity gradients at a station height of 225 km representing the GOCE satellite altitude. The topographic corrected gravity gradients after Bouman et al. (2016) measured by the GOCE ESA satellite mission are presented in the appendix. For the definition of the slab geometry, we use crustal thickness estimates based on the receiver function study by Spada et al. (2013). The crustal thickness map was digitized and the Moho gap in the eastern Alps is filled by nearest neighbour interpolation. To avoid edge effects, surrounding areas are supplemented by the Moho depth model of the European plate by Grad et al. (2009), both data sets were merged using a cosine taper with a taper width of 2° using equation (1). The overlapping areas at the grid edges are distance weighted to obtain a smooth transition.

$$G_{new} = T(x, y) \cdot G_1(x, y) + (1 - T(x, y))G_2(x, y) \quad (1)$$

$$with: T(x, y) = \cos \frac{D \cdot \pi}{2 \cdot L}$$

$$with: G = \text{Grids}, T = \text{taper}, D = dx, L = \text{Taper length}$$

The merged Moho depth map is sampled at a regular grid with a cell size of 0.25° (Fig. 2) to be consisted with resolution of the topographic and gravity models.

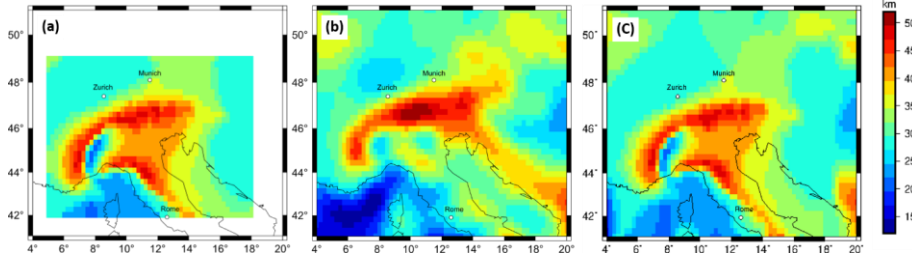


Figure 22 a) digitized *crustal thickness* Moho depth after Spada et al. (2013) with a  $0.25^\circ$  grid spacing, b) *crustal depth* Moho depth estimation after Grad et al. (2009) with a  $0.25^\circ$  grid spacing c) Merged *crustal thickness* Moho depth map from Spada et al. (2016) and Grad et al. (2009) with a grid resolution of  $0.25^\circ$  using a cosine taper with a  $2^\circ$  width.

For the upper mantle seismic velocity, the 3-D shear wave velocity model (MeRE2020) by El-Sharkawy et al., (2020) is used (Fig. 3). The model covers the upper mantle across the Alpine-Mediterranean area down to a depth of 300 km and absolute shear-wave velocities are given. In this study, relative shear-wave velocities in the depth range from 70 to 200 km are calculated with respect to a 1-D average shear wave velocity model, the background model is *described* *described* in El-Sharkawy et al., (2020). The upper limit of 70 km is introduced because i) we focus on the contribution of the slab segments removing therefore crustal information from the model ii) the tomography model MeRE2020 is not sensitive to shallow structures, as a result the slabs are not well recovered in depths shallower than 70 km iii) we want to ensure a uniform upper boundary. The lower boundary of 200 km is chosen based on clear images of the Alpine Slab segments to at least 200 km depth (with exception of the Western Alpine slab), as discussed in section 1, and the assumptions that depth larger than 200 km will have a negligible effect on the regional gravity field considered here.

The ambient noise tomography by Kästle et al. (2018) is used to define the geometry of the Western Alpine slab segment, hence we follow the idea of a slab-breakoff in the Western Alps at 100 km depth (Kästle et al., 2020) as suggested also by Lippitsch et al. (2003) and Beller et al. (2018). For the eastern Alps, we consider two alternative models. For the first hypothesis, the P-wave tomography by Lippitsch et al. (2003) is used, to define the Eastern Alpine slab segment. The second hypothesis is based on Kästle et al. (2020) and El-Sharkawy et al. (2020).

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188 It assumes southward subduction of a short Eurasian Slab as well as northward subduction of a  
 189 short Adriatic Slab in the eastern Alps. The slab configurations which are incorporated in the  
 190 Alpine density models are discussed in greater detail in section 4.1.

### 191 **3 Conversion of seismic velocities into density distribution**

192 Seismic velocity variations are dependent on temperature and pressure. Densities in the  
 193 subsurface are also temperature and pressure dependent. A conversion factor ( $\zeta$ ) can describe  
 194 the linear relation between seismic velocities variations and densities variation (e.g. Tiberi et al.  
 195 2001; Webb 2009). We convert seismic shear wave velocities from the tomographic model  
 196 MeRE2020 by El-Sharawy et al. (2020) in the depth range from 70 to 200 km, as discussed in  
 197 section 2, to obtain a density distribution of the upper mantle in the Alpine region based on a  
 198 conversion factor ( $\zeta$ ). The relationship between seismic velocities and densities is described in  
 199 equation (2), this assumption is a strong simplification of reality, but gives a first order  
 200 estimation of the expected relative density structure beneath the Alps.

$$201 \quad \rho_{rel} = [(Vsv_{abs} + \Delta\%)Vsv_{abs}(1 + \Delta\%) - Vsv_{abs}] \cdot \zeta = Vsv_{abs} \cdot \Delta\% \cdot \zeta \quad (2)$$

202 *with:  $Vsv_{abs}$  = absolute velocities from MeRE2020;*

203  *$\Delta\%$  = percentage ~~divagation~~ deviation from the MeRE2020 background model;*

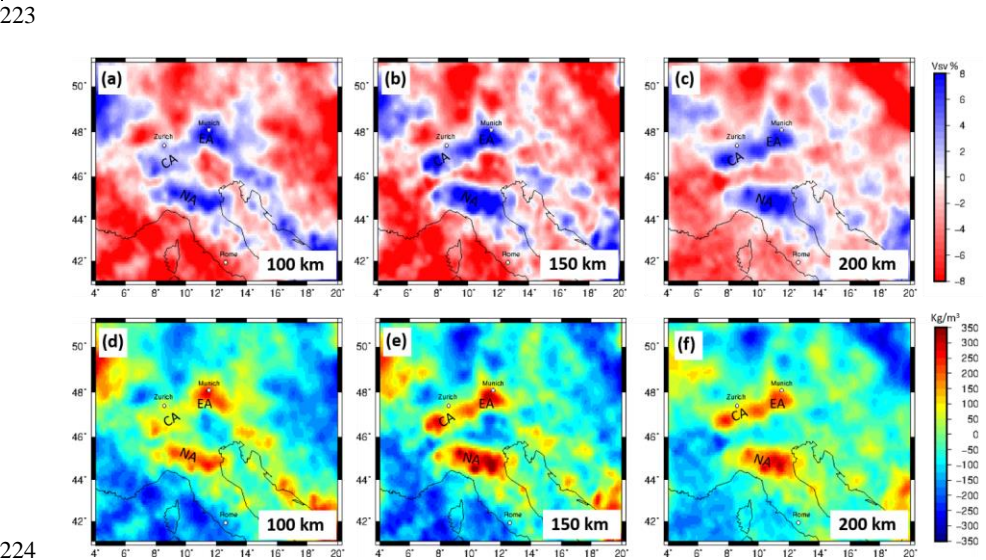
204  *$\zeta$  = conversion factor*

205 The result is strongly dependent on the chosen conversion factor. A range for conversion  
 206 factors has been proposed in the literature for different rock types ranging from 0.1 to 0.45 (e.g.  
 207 Isaac et al., 1989; Isaak, 1992; Karato, 1993; Kogan and McNutt, 1993; Vacher et al., 1998).

208 The relative shear-wave velocity distribution in a 3D domain from the tomography model  
 209 MeRE2020 from El-Sharkawy et al., (2020) is converted using a constant conversion factor ( $\zeta$ )  
 210 of 0.3. The converted relative density distribution varies between -240 and 350 kg/m<sup>3</sup>. High  
 211 correlations between the structural pattern in the converted density distribution and the relative  
 212 seismic velocities are observed (Fig. 3), the similarity in the structure pattern is expected due



to the linear relationship we introduced here. The converted 3D relative density distribution reflects the variation of seismic velocities in the Alpine lithosphere and therefore includes the heterogeneities of the subduction slab segments, as seen by the tomographic models (Fig 3). The relative density model is transferred into tesseroids with a horizontal expansion of  $0.2^\circ$  and a vertical expansion of 3 km. The Tesseroid model is forward calculated in order to estimate the gravity response of the converted density distribution of the Alpine lithosphere in the depth interval of 70 km to 200 km. No horizontal extensions of the mantle model are introduced because relative densities are used and therefore edge effects are not expected to be significant and would only affect the outer most degrees of the model. The slab segments are located central in the model far away from possible artifact due border effects.



**Figure 33.** (a)-(c) Depth slices of relative surface wave velocities ( $V_{sv}$ ) from MeRE2020 (El-Sharkawy et al., 2020). (d)-(f) converted relative density distribution in different depths based on a conversion factor ( $\zeta$ ) of 0.3. CA = Central Alpine Slab; EA = Eastern Alpine Slab; NA = Northern Apennine Slab

### 3.1 Results

In the forward calculated gravity field, a gravity high with a magnitude of  $\sim 40$  mGal is observed over the Alps (Fig. 4). That might be interpreted as relating to the proposed slab segments in the Northern Apennine and Alpine area. However, the gravity field (and gradients, see appendix)

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is dominated by anomalies outside the Alpine realm (Fig. 4), for instance in the Ligurian Sea and the Dinaride-Hellenide Orogen. Therefore, in the next step, we try to concentrate on the seismic anomalies in the Alpine realm that can be related to the slab segments.

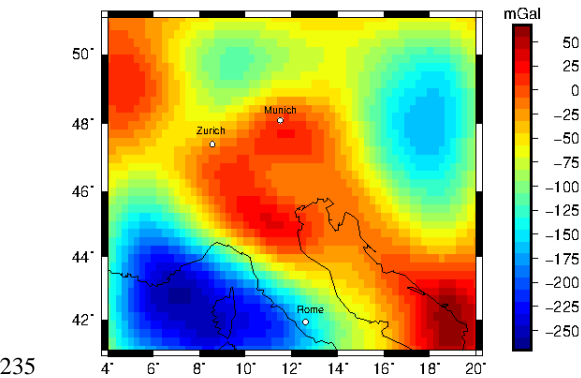


Figure 4: Forward calculated gravity signal from relative density distribution converted from relative seismic velocities using a conversion factor of 0.3 at a station height of 6040m.

#### 4 Slab models

To estimate the gravity contribution of independent slab segments we introduce different models for the subducting lithosphere. First, we use a set of models with simple constant density distribution in the slab, where the parameters, namely the density contrast and thickness of the slab segment is varied (approach 2). Secondly, we create a set of slab models accounting for compositional and thermal variations with depth (approach 3). Those models of approach 3 are created with the software package LitMod 3D (Fullea et al., 2009) and here the slabs are strictly vertical due to software limitations. ~~and~~ Slab models created within LitMod will be referred as LitMod models in the following. For all non-LitMod models, the gravity and gravity gradients are calculated using tesseroids, which are spherical prisms (Uieda et al., 2016).

##### 4.1 Slab modelling with constant density contrast and slab thickness

We define two alternative slab configurations based on crustal thickness model by Spada et al. (2013) and several different tomographic studies, see detailed description of the slab configurations below. At different depths, isolines are picked in the erustal-Moho depth map

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and tomographic images, defining the upper boundary of subducting slab segments. The isoline of the crust mantle boundary (Moho interface) is used as an onset of the slab to the crust and defines the upper boundary of the subduction slab segment. At upper mantle depth, increased seismic velocity anomalies in tomographic models beneath the Alps are interpreted as contrast between colder and therefore denser subducting material to the surrounding mantle material. At 100, 150, and 200 km depth, the upper boundary of the slab segment is defined at the 0% contour line of the relative seismic velocity, marking the transition from rocks with low velocity to high velocity rocks. The isolines at the Moho interface, 100 km, 150 km and 200 km depth are displayed upon the Alpine topography (Fig. 5 a-b) Vertical interpolation between the upper boundary isolines at different depths (Moho depth, 100, 150 and 200 km) define a continuous surface of the upper slab boundary. The lower boundary of the slabs and therefore the thickness of the slab segment is not picked based on seismic data but assumed to have constant thicknesses for simplifications. The thickness is varied for different models from 60 to 100 km depth.

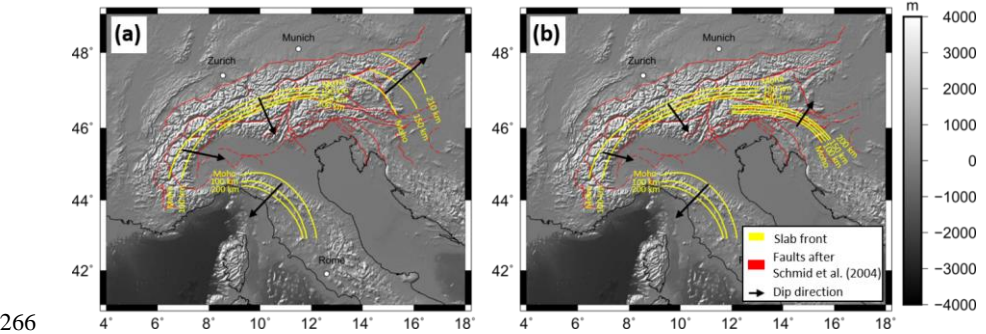


Figure 5. Defined isolines based on crustal thickness estimations and seismological tomography models for the upper slab boundary for (a) Configuration 1 and (b) Configuration 2. Black arrows indicate the subduction direction. In red the fault configuration after Schmid et al. (2004).

### 3.1.1 Alternative slab configurations

We define two different slab configurations. Configuration 1 (Fig. 5a) features a northeast subducting slab segment in the Eastern Alps based on Lippitsch et al. (2003). A Central Alpine slab segment is defined based on Lippitsch et al. (2003) and MeRE2020 (El-Sharkawy et al.,

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2020) subducting in south-southeast direction. The Eastern and Central Alpine slab segments are separated by a slab gap and show perpendicular subduction directions. The east-southeastward subducted slab segment in the Western Alps is defined using the tomographic model of Kästle et al. (2018), supporting the idea of slab break-off at about 100 km depth. Only attached slab segments are considered, ignoring potential mantle upwelling in the break off zone and neglecting the potentially remaining detached slab segment in larger depths. In addition, a southwest-subducting slab segment beneath the northern Apennines is considered down to about 200 km depth, as imaged by MeRE2020 (El-Sharkawy et al., 2020) because of its proximity to the western Alps.

Configuration 2 (Fig. 5b) considers a slab configuration mainly based on the interpretation of the MeRE2020 model (Fig. 3) by El-Sharkawy et al. (2020). In the Eastern Alps, both a short southward subducting Eurasian slab segment as well as a short northward subducting Adriatic slab are assumed. The Central and Western Alpine slab segments as well as the slab beneath the northern Apennines are identical to Configuration 1.

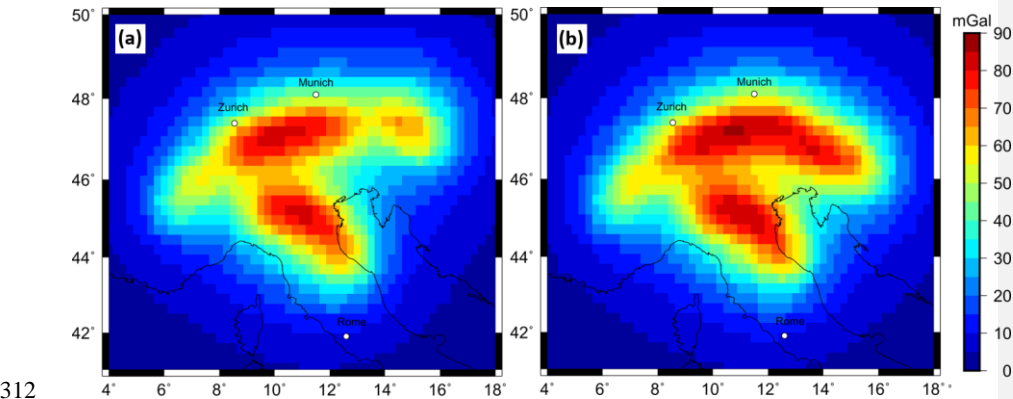
#### 4.1.2 Forward calculation

To estimate the gravity effect of the slab configurations, the geometries are discretized into tesserooids with a  $0.2^\circ$  extension in the horizontal domain and a vertical size of 20 km. The tesserooids range from 40 km to 200 km depth. First, a constant density contrast is assigned to the entire slab. We test density contrasts from  $20 \text{ kg/m}^3$  to  $80 \text{ kg/m}^3$ . The thickness of the Alpine slab is not well constrained. We test for three slab volumes by assigning three slab thicknesses, 60 km, 80 km and 100 km based on studies on other subducting slab segments (e.g. Wang et al., 2020). Due to the curved geometries of the proposed slab segments rectangular tesserooids with a horizontal expansion of  $0.2^\circ$  will either over- or under-estimate the volume of a subducting slab at the edges of the slab. The percentage volume share of each tesserooid to the slab geometry is calculated. The assigned density contrast of the tesserooids which does not lay fully within the slab geometry is decreased according to the percentage volume within the slab

300 geometry. Therefore, the density distribution correlates to the hypothetical slab positions and  
301 volumes in the Alpine subsurface without increasing the discretisation resolution of the  
302 tesseroïd model beyond the uncertainty of gravity measurements and seismic tomographies.  
303 The offset between the 40 km upper tesseroïd boundary to the slab onset at the crust in 44 km  
304 depth is corrected using the same process.

305 4.1.3 Results

306 Forward calculated slab models for predefined slab geometries of Configuration 1 and 2 with a  
307 constant density contrast of  $60 \text{ kg/m}^3$  and a constant thickness of 80 km result in a sharp gravity  
308 signal ranging from 70 mGal to 100 mGal (Fig. 6). Both models generate gravity signals in the  
309 order of magnitude of 70 mGal in the Central Alpine region as well as in the Apennine. The  
310 gravity signal in the Eastern Alps differ for the two hypotheses (Fig. 6 a, b). The Western Alpine  
311 slab segment shows the weakest signal in both models.



313 *Figure 66. Forward calculated gravity disturbance signal at a station height of 6040 m for predefined sub-crustal slab*  
314 *geometries with a content density contrast of  $60 \text{ kg/m}^3$  and a constant thickness of 80 km. (a) predefined slab configuration 1*  
315 *(b) predefined slab configuration 2.*

316 The gravity signal ranges from 30 to 110 mGal depending on the assigned density contrast and  
317 thickness for both slab geometry models (Fig. 7). The highest magnitude of forward calculated  
318 gravity signal is in the order of 110 mGal and is observed for a slab model with a density  
319 contrast of  $80 \text{ kg/m}^3$  and a constant slab thickness of 100 km, while the lowest signal is  
320 produced by a combination of  $20 \text{ kg/m}^3$  density contrast and a slab thickness of 60 km. Similar

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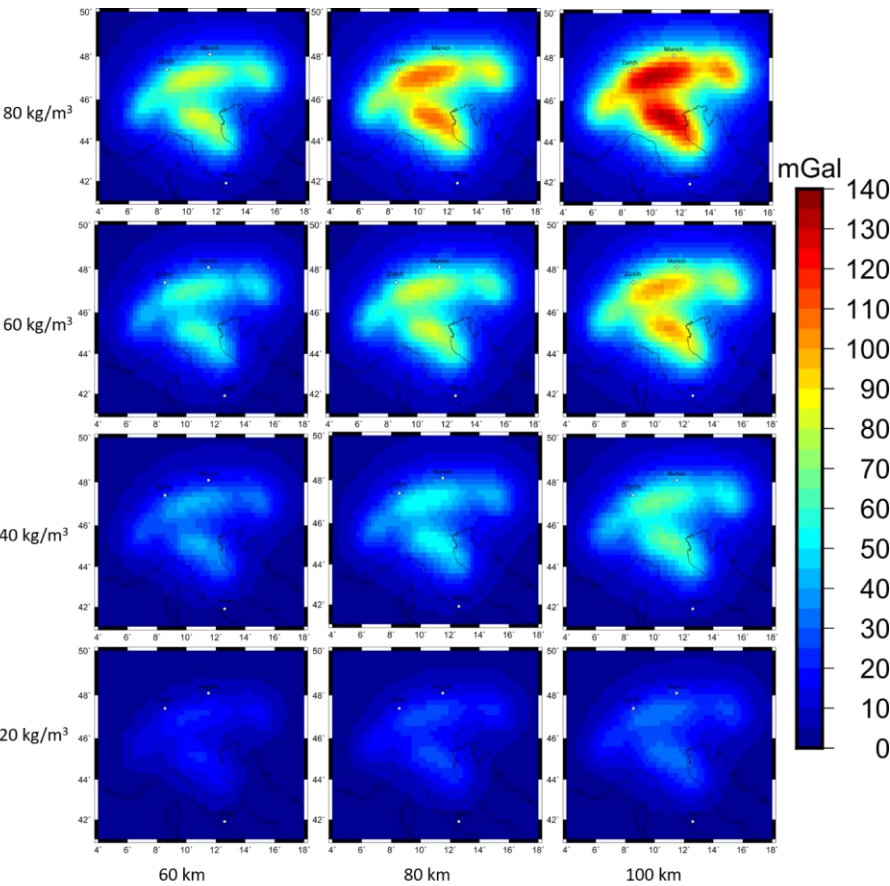
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321 gravity response is produced by different combinations of density contrast and volume. The  
 322 signal pattern is influenced by the predefined slab geometry, while the magnitude of the gravity  
 323 signal is depending on the density contrast and thickness (Fig. 7).



324  
 325 *Figure 7. Forward calculated gravity disturbance signal for 12 different combination of density contrast and slab thickness*  
 326 *for sub-crustal slab configuration 1 at a station height of 6040 m.*  
 327 Forward calculated gravity gradients at satellite height show the same dependency of signal  
 328 strength (see Appendix). The forward calculated gravity field of approach 2 differs significantly  
 329 from the forward calculated gravity field of the complete mantle density inhomogeneity of  
 330 approach 1 (Fig. 4), which only reaches a positive mantle effect of maximum 50 mGal.

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## 4.2 Geophysical and petrological modelling with LitMod

For modelling the Alpine slab segments taking temperature and pressure variations as well as composition of the lithosphere and sub lithosphere into account, the geophysical and petrological modelling software LitMod 3D is utilized (Fullea et al.,2009). LitMod 3-D is a finite difference code, which allows the modelling of lithospheric and sub lithospheric structures down to 400 km depth by solving the heat transfer, thermodynamical, rheological, geopotential, and isostasy equations (Afonso et al., 2008; Fullea et al., 2010).

A LitMod model consists of a set of crustal, lithospheric- and sub lithospheric layers characterized by their petrophysical and thermal properties, which are used as input data (Fullea et al., 2010). LitMod provides as an output i.e. the density -, temperature-, pressure- distribution as well as the forward calculated gravity disturbance and gravity gradients (Fullea et al. 2009). The assigned composition for the different layers is calculated using a LitMod subroutine which utilizes the Perple\_X algorithm of Connolly (2009). Perple\_X calculates in the LitMod implementation the specific bulk rock properties based on the six main lithospheric oxides ( $\text{SiO}_2$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{FeO}$ ,  $\text{CaO}$ ,  $\text{Na}_2\text{O}$ ) by minimizing Gibbs free energy equation. The Alpine lithosphere and sub lithosphere as well as the proposed slab segments are modelled using standard global lithospheric and sub lithospheric compositions to test the influence of compositional variations within the slab segments on the gravitational signal. Here, we use the so-called Tecton and Proterozoic type-composition (Table 1). Those compositions were chosen for a model with a homogeneous crust, lithosphere and sub-lithosphere, where the density changes as a function of temperature and pressure based on the assigned compositions. The different slab composition is introduced to test whether a compositional contrast, in addition to the expected thermal difference, results in a significant density contrast between the slab and the surrounding material.

**Table 11: Mineralogical composition for the lithospheric and sub lithospheric structure.**

Major Oxide Compositions	Aver. Tecton Gnt. SCLM <sup>a</sup>	Aver. Tecton Gnt. Peridotite <sup>a</sup>	Average Proterozoic Massif	PUM <sup>b</sup>	DMM <sup>c</sup>
SiO <sub>2</sub>	44.5	45	45.2	45	44.7
Al <sub>2</sub> O <sub>3</sub>	3.5	3.9	2	4.5	3.98
FeO	8	8.1	7.9	8.1	8.1
MgO	39.8	38.7	41.6	37.8	37.8
CaO	3.1	3.2	1.9	3.6	3.17
Na <sub>2</sub> O	0.26	0.24	0.13	0.36	0.13

<sup>a</sup> Classifications according to Griffin et al. (1999b), <sup>b</sup> McDonough & Sun (1995), <sup>c</sup> Workman & Hart (2005) DMM = Depleted mid-oceanic ridge basalt mantle, PUM = primitive upper mantle.

First, we create a reference model ( $M_0$ ) without a slab segment. This model contains topography from the ETOPO1 dataset (Amante and Eakins, 2009), the Moho depth from Spada et al. (2013) and Grad et al. (2009). The lithosphere asthenosphere boundary (LAB) is a required interface for the LitMod 3D to divide the model between the lithosphere and sub lithosphere and to assign compositions. We introduce a fixed technical LAB at a depth of 100 km throughout the model despite of the presence of slabs as the LAB is defined as the 1300°C isotherm. This set-up avoids that the isotherm follows the geometrical shape of the slab, which would lead to a location in unrealistic large depths (>200 km). In addition, we neglect the topography of the LAB for several reasons: i) the information of the lithospheric thickness in the Alpine forelands is sparse and under ongoing discussions, ii) the fixed depth value is based on thermal isostasy LAB estimations from Artemieva et al. (2019), which shows a LAB depth in the range of 80 to 120 km depth in the Alpine forelands. This technical LAB is used to parameterize the model and is not meant to represent the topography of the LAB. The modelled slab segments are extending vertically downwards.

Slab segments are introduced stepwise for the lithosphere and sub lithosphere domains into the model as well as thermal anomalies for the slab segment beneath the technical LAB, which

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describes the 1300°C isotherm (Table 2). Calculating the difference to the reference model ( $M_0$ ) allows to estimate the effect a slab segments has on the density, temperature distribution of the Alpine subsurface and therefore on the Alpine gravity field based on slab position, slab geometry and composition.

*Table 22: Different LitMod models and there incorporated lithospheric and sub lithospheric structures and compositions.*

Models	Slab geometries	Slab composition (mantle)	Mantle composition	Slab composition (sub lithosphere)	Sub lithosphere composition	Thermal anomaly within sub lithospheric slab
<b>M<sub>0</sub></b>	-	-	aver. Tecton Gnt.	-	PUM	-
<b>M<sub>1</sub></b>	Configuration 1	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	-	PUM	-
<b>M<sub>2</sub></b>	Configuration 2	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	-	PUM	-
<b>M<sub>3</sub></b>	Configuration 1	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	DMM	PUM	-100 °K
<b>M<sub>4</sub></b>	Configuration 2	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	DMM	PUM	-100 °K
<b>M<sub>5</sub></b>	Configuration 1	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	PUM	PUM	-
<b>M<sub>6</sub></b>	Configuration 1	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	DMM	PUM	-
<b>M<sub>7</sub></b>	Configuration 1	Aver. Tecton Gnt. Peridotite	aver. Tecton Gnt.	DMM	PUM	-200 °K
<b>M<sub>8</sub></b>	Configuration 2	Average Proterozoic Massif	aver. Tecton Gnt.	-	PUM	-

A positive density contrast between subducting material and the surrounding mantle material results in a negative buoyancy force. A density contrast is introduced into the LitMod model by a difference in composition between the subducting denser slab and the surrounding mantle (Fig. 9). Here, we use Tecton like compositions for the lithosphere and the subducting slab segments since the Alpine slab segments result from continent-continent collision (Tables 1 and 2). A later model features a Proterozoic slab composition ( $M_8$ ). Depleted mid-oceanic ridge basalt mantle (DMM) and primitive upper mantle (PUM) are used for the sub lithospheric domain. Additional to the density contrast within the sub lithosphere, a temperature anomaly of – 100 K is introduced for the sub lithospheric part. Later models include a variation of temperature anomalies ( $M_5$ ,  $M_6$ ,  $M_7$ ). Note those compositions are used as a first order test and

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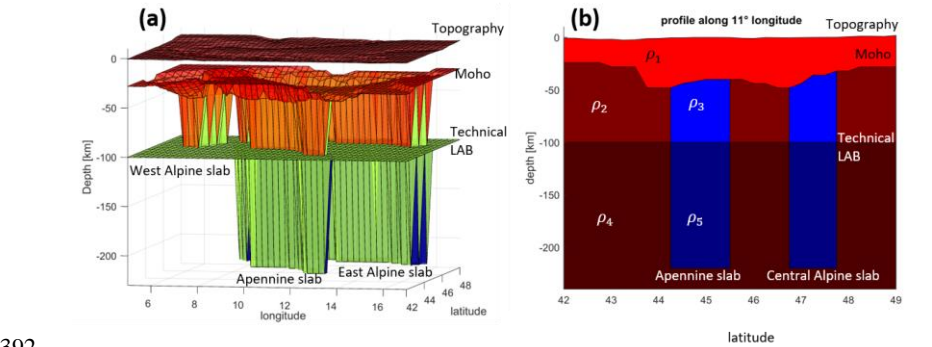
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389 serve as a starting point for synthetic slab models to illustrate the compositional and thermal  
 390 effect on the gravity signal by influencing the density distribution. They do not necessary  
 391 represent the compositional mantle environment in the Alpine region.



392  
 393 *Figure 88. (a) 3D model set up using LitMod 3D. Topography, Moho and LAB depth as well as the vertical incorporated slab*  
 394 *models are used as input layers with assigned petrophysical and thermal properties. (b) Profile along 11° longitude through a*  
 395 *LitMod model containing Topography, crustal and lithospheric thickness as well as a slab segment.  $\rho_{0-5}$  indicate*  
 396 *petrophysical and thermal property variations for each layer.*

#### 397 4.2.1 Results

398 The gravity signal of the predefined slab segments is forward calculated as well as the  
 399 background model without incorporation of slab segments. The residual between both forward  
 400 calculations gives the gravitational contribution of the slab segments, while other gravitational  
 401 effects, like the topography or crustal thickness variation and mantle variations outside the slab  
 402 are not considered.

403 A slab segment with an average Tecton Gnt. composition ( $M_1, M_2$ ) results in a slightly denser  
 404 material compared to the surrounding mantle ( $M_0$ ), while a slab segment with a Proterozoic  
 405 composition ( $M_3$ ) shows a less dense lithospheric structure compared to the reference model  
 406 ( $M_0$ ), this composition results in less dense slab segment, which would not be subducted due to  
 407 the positive buoyancy (Fig. 10). However, we aim to illustrate the effect composition has on  
 408 the density distribution within the slab and to the surrounding mantle and show the importance  
 409 of correct compositional information, therefore we focus on the difference in density contrast  
 410 between slab and surrounding mantle and neglecting the sign of the density contrast.

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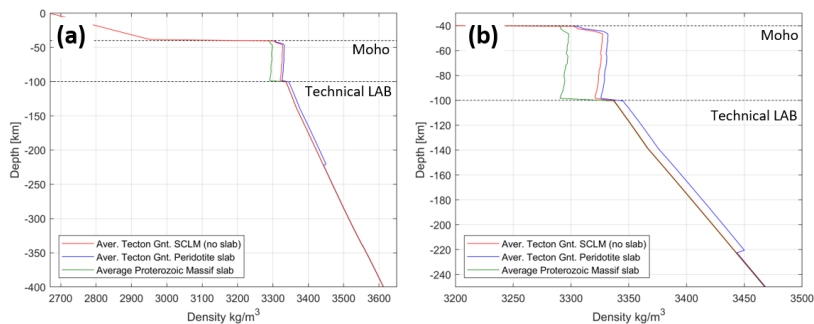


Figure 9a (a) density profile at 11° longitude and 45° latitude for the full vertical model space of 400 km depth. Density profiles for 3 different models ( $M_0$ ,  $M_1$ ,  $M_9$ ) with different compositional properties are shown. (b) Zoomed in profile at the depth range of present slab segments.

The difference in density distribution (density contrast) within the slab segments with a Tecton composition ( $M_1$ ,  $M_3$ ) to the reference model ( $M_0$ ) is in the order of  $5 \text{ kg/m}^3$  for the lithosphere and in the order of  $10 \text{ kg/m}^3$  for the sub lithospheric domain (Fig. 10a). The density variations within the lithospheric and sub lithospheric slab domain are less than  $1 \text{ kg/m}^3$  resulting from both depth dependent variations in pressure and temperature. Between lithosphere and sub lithosphere, a rapid increase in density contrast is observed (Fig. 10a). The density contrast of a lithospheric Proterozoic slab composition ( $M_9$ ) to the reference model ( $M_0$ ) is in the order of  $-30 \text{ kg/m}^3$  (Fig. 10b).

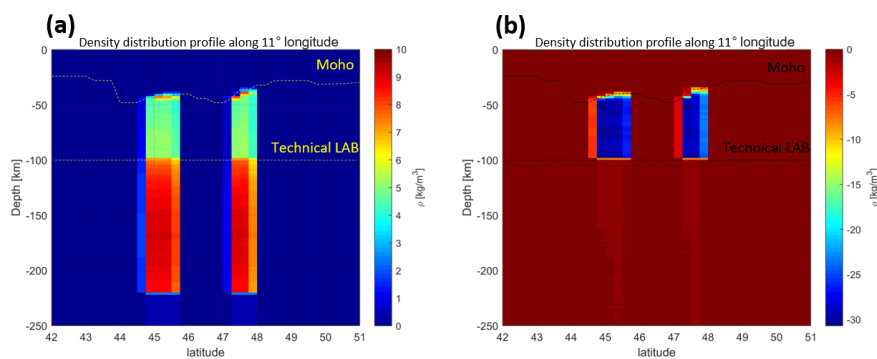
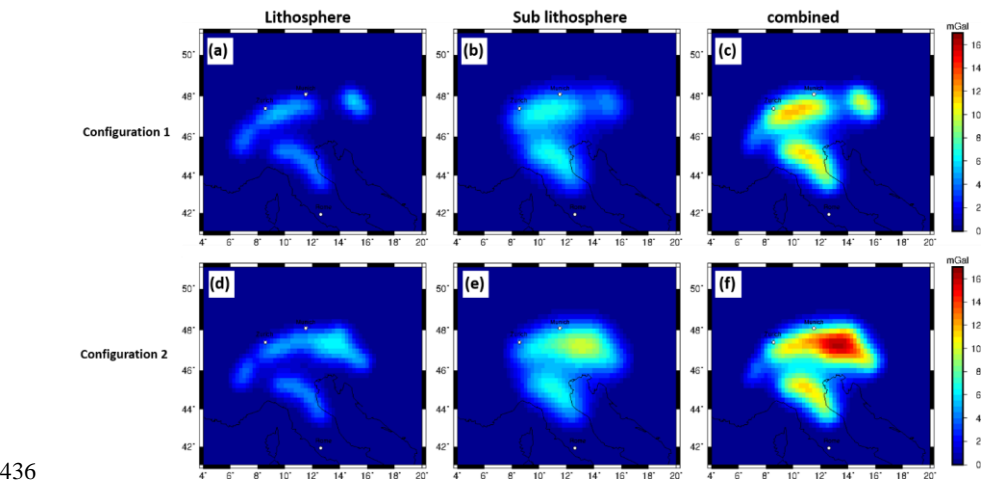


Figure 10a (a) residual density contrast for lithospheric and sub lithospheric slab segments of model ( $M_3$ ) with Tecton like composition within the lithosphere and PUM and DMM composition in the sub lithosphere with an additional thermal anomaly of  $-100^\circ \text{K}$  for the sub lithospheric slab segment to the background model ( $M_0$ ). (b) Residual lithospheric density contrast of a Proterozoic lithospheric slab segment ( $M_9$ ) to a Tecton compositional surrounding mantle ( $M_0$ ). Residual density contrast is limited to the technical LAB as the sub-lithospheric part is identical to the reference model (see also Fig. 9b)

429 The gravity signal caused by the proposed slab segment configurations is estimated for  
 430 lithosphere and sub lithosphere separately. The forward calculated gravity effect, at topographic  
 431 surface level, for the slab configuration 1 for the lithospheric part is in the order of 4 mGal  
 432 while the sub lithospheric gravity signal is in the range of 7 mGal (Fig. 12a, b). The combined  
 433 gravity signal is in the order of 12 mGal (Fig. 12c). The gravity signal in the Eastern Alps for  
 434 Configuration 2 is significantly larger in the order of 17 mGal for the combined model (Fig.  
 435 12f).



437 *Figure 12. Residual of the forward calculated  $g_z$  gravity signal of lithospheric slabs at surface station height based on LitMod*  
 438 *models with Tecton like compositions in the lithosphere and PUM and DMM compositions in the sub lithosphere ( $M_1$ ,  $M_2$ ,  $M_3$ ,*  
 439  *$M_4$ ) with an additional thermal anomaly of  $-100^\circ\text{K}$  for the sub lithospheric slab segment, for predefined slab Configuration to*  
 440 *the background model ( $M_0$ ). (a)-(c) Configuration 1. (d)-(f) Configuration 2. Crustal and topographic contribution are nullified.*

441 The calculated gravitational effect of a slab segment with Proterozoic composition and a Tecton  
 442 surrounding mantle composition is in the order of -40 mGal for the  $g_z$  component (Fig. 12 a).

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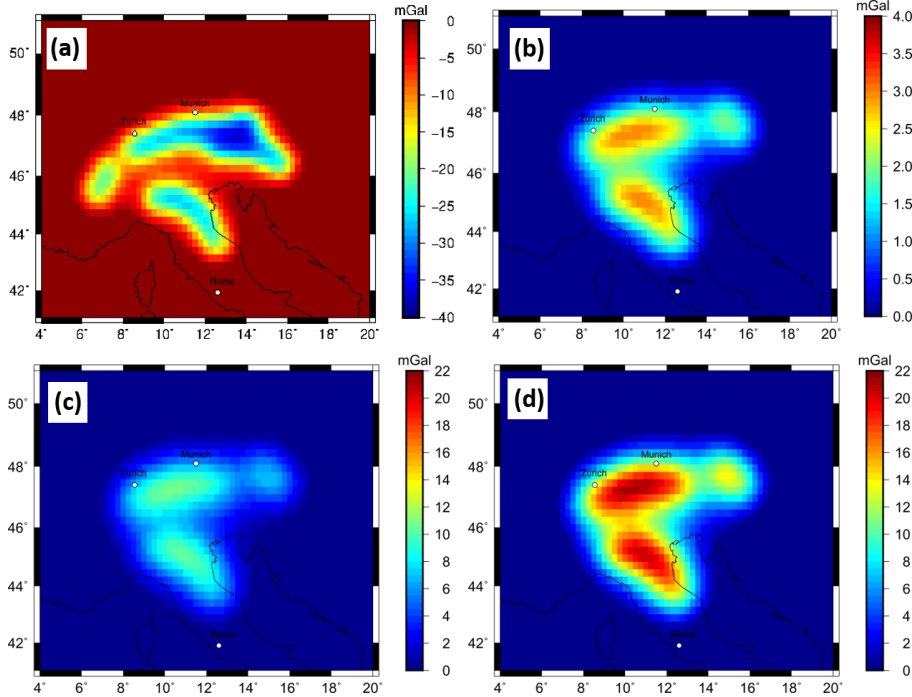


Figure 12: (a) Forward calculated gravity effect of a Proterozoic lithospheric slab segment to a Tecton compositional surrounding mantle for configuration 2, obtained by calculating the residual between  $M_8$  and  $M_0$ . (b) gravity signal produced by purely compositional effect in the sub lithosphere between a PUM and DMM composition, obtained by calculating the residual between  $M_5$  and  $M_6$ . (c) gravity signal produced by purely thermal anomaly of  $-100^\circ\text{K}$  for a sub lithospheric slab segment, obtain by calculating the residual between  $M_3$  and  $M_4$ . (d) gravity signal produced by purely thermal anomaly of  $-200^\circ\text{K}$  for a sub lithospheric slab segment obtained by calculating the residual between  $M_4$  and  $M_7$ .

The gravity response to a compositional variation within the sub lithosphere between the incorporated slab segment (DMM composition) and the surrounding mantle (PUM composition) is in the order of 4 mGal (Fig. 12b). The gravity response for a pure thermal anomaly of  $-100^\circ\text{K}$  within the sub lithospheric slab segment is in the order of 16 mGal (Fig. 12c), while a pure thermal anomaly of  $-200^\circ\text{K}$  within the sub lithospheric slab segment is in the order of 21 mGal.

## 5 Discussion

The imprint of the gravity response caused by the density distribution based on direct conversion of seismic velocities (approach 1) is visible, however, individual and independent slab segments cannot be identified (Fig. 4). The strength of this approach is that it is fast to

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459 implement and can provide a first order characterization of the gravity signal and slab  
 460 geometries of subducting lithosphere. However, a clear characterization of subducting slab  
 461 segments is not possible. First of all, the density model depends on the resolution and  
 462 regularization of the seismological model, which can lead to distortions in the gravity response  
 463 (e.g. Root, 2020). The method is dependent on the choice of the conversion factor and might  
 464 overestimate the density (see the large negative anomaly in the Ligurian Sea). The conversion  
 465 factor is a strong simplification of nature and for such a geodynamic complex area, a constant  
 466 conversion factor is not adequate.

467 The forward calculated gravity field with competing predefined slab geometries (approach 2)  
 468 shows a clear gravity signal, where the individual slab segments are distinguishable (Fig. 6).  
 469 A relative gravity low related to the slab gap in the Eastern Alps is a prominent feature in the  
 470 gravity signal of Configuration 1 (Fig. 6a). The eastern Alpine slab segment of Configuration  
 471 1, due to its relatively small volume, result in a lower signal compared to the Central Alpine  
 472 slab segment.

473 Configuration 2 shows a larger gravity signal in the Eastern Alps up to 100 mGal (Fig. 6b)  
 474 compared to Configuration 1. The increase of the gravity signal is attributed to the subduction  
 475 of both Eurasian and Adriatic lithosphere in the Eastern Alps. The gravity signal shows a  
 476 continuous transition from the Central Alps to the Eastern Alps, where the contribution of the  
 477 destined slab segment cannot be distinguished in the resulting gravity field (Fig. 6b). In the  
 478 Western Alps, Configuration 1 and 2 show a lower gravity signal compared to the Central Alps.  
 479 This is attributed to the much shallower Western Alpine slab segment that penetrate down to  
 480 100 km depth.

481 The gravity signal is influenced by both the assigned density contrast and thickness of the slab.  
 482 A trade of between both parameters is clearly observable as the same gravity response of the  
 483 slab configuration can be achieved with different values of density contrast and slab thickness.

Therefore, making it impossible to derive slab properties in form of density contrast and slab thickness from the gravity field (Fig. 7).

The calculated densities in LitMod 3-D models (approach 3) are estimated taking temperature and pressure variations into account based on an assigned composition. The composition has a strong influence on the resulting density contrast. In the case that the compositional contrast between slab segment and surrounding mantle is small, the density contrast is consequently small as well (Fig. 9 and 10a). With increasing compositional differences, the density contrast increases as well. A strong density contrast within the slab segment is recognizable between lithospheric and sub lithospheric domain (Fig. 10a and b), while the variations between the slab and surrounding mantle remain small.

The gravity signal shows in the Eastern Alps significant larger signal from the lithosphere and sub lithosphere domain for Configuration 2 (Fig. 11d, e, and f) compared to Configuration 1 (Fig. 11a- c). The different slab segments are distinguishable with the exception of the two slab segments in the Eastern Alps in Configuration 2 (Fig. 11). The contribution from the lithospheric domain to the gravity signal is smaller than from the sub lithospheric domain (Fig. 11b, and e). However, the slab gap and the eastern slab segment feature can be recognized in the lithospheric part in Configuration 1 but not in the gravity signal of the full model.

The Proterozoic slab segment has a larger gravity response compared to the Tecton-like composition. This gravitational signal is negative due to the less dense Proterozoic composition in comparison to the reference model ( $M_0$ ) (Fig. 12a).

Sub lithospheric composition has only a small influence on the gravity field, in the order of 4 mGal (Fig. 12b). However, a thermal anomaly within the sub lithospheric slab in the order of -100K result in a gravitational response of 16 mGal (Fig. 12c) and for a -200 K anomaly in the order of 21 mGal (Fig. 12d). Both the composition and the thermal variation influence the density and consequently the gravity response. However, the thermal component is a much larger contributor.

For the three approaches (section 3, 4.1 and 4.2) a measurable gravity effect of the subducting slab segments is observable. The independent slab segments are distinguishable to a certain degree with the exception of the bivergent slab configuration in the Eastern Alps (Fig. 6, and 11) and the model containing converted density from seismic velocities (Fig 4), while the slab configurations cannot be separated at satellite altitude (Appendix). Forward calculated gravity anomalies from converted density distribution suggest a gravitational signal of the slab segments in the order of 40 mGal which corresponds to a density contrast of 20 to 40 kg/m<sup>3</sup> in the models with predefined slab geometry. The models with a Tecton like composition suggest a gravity effect of the slab segments in the order of only 16 mGal, corresponding to a density contrast of 20 kg/m<sup>3</sup> in the simple model. Increasing the compositional difference with a Tecton composition suggests a gravity signal in order of 30 mGal and is in line with the converted density model.

All three methods show a positive gravity signal contribution, which can be related to sub-crustal density variations for approach 1 and to predefined sub-crustal slab segments for approach 2 & 3, up to 40 mGal to the Alpine gravity field. That is significant in comparison to the observed Bouguer Anomaly with a minimum of ~200 mGal. If this contribution is not considered, a significant part of the gravity signal is attributed to crustal thickness or intra-crustal sources. Due to the long-wavelength appearance of the gravity effect, that might not be relevant for small-scale or local studies, the effect is only seen as a shift. For gravity models of larger areas (e.g. Eastern Alps) or even the entire regions that should not be neglected. For one, estimates of crustal thickness or the mass distribution are significantly biased, and placing the Alps in the geodynamic context of the surrounding requires a careful and complete consideration of all sources in order to provide realistic density distribution required for geodynamic models (e.g. Reuber et al., 2019).

## 6 Conclusions



We have addressed the potential gravity effect of proposed slab segments in the Alpine region using three different modelling approaches.

- Converted density from seismic tomography: In the resulting gravity signal the imprint of slab segments is visible, however, distinguishing between the different and independent slab segments is not possible.
- Models with predefined slab segments are dependent on the assigned density contrast and volume as well as on the predefined positions of the slab segments. The gravity signal caused by the slab segments are sharp and can be separated for the different slab segments for the gravity field at the surface. Significant gravity contributions from slab segments below 200 – 250 km to the Alpine gravity are unlikely.
- Combined petrophysical-geophysical modelling results in the most complex models. The calculated density variation within the slab is rather small compared to the density contrast between lithosphere and sub lithosphere. The density distribution within the slabs, and consequently the gravity field, is highly influenced by the slab composition and thermal structure.

Sub-crustal density variation (approach 1) and predefined slab segments (approach 2 & 3) suggest a positive sub-crustal gravity contribution of up to 40 mGal. Even though this might be considered as a maximum gravity estimation of slabs~~an end of the envelope calculations~~, this value is significant, even compared to the observed Bouguer ~~A~~ anomaly low of -200 mGal along the Alps. ~~Previous studies compensated this effect by lithosphere thickness and/or intra-crustal sources.~~ The interpretation of density variation in the mantle in terms of subducting slab structures is a means to provide a meaningful representation of the geodynamic complex Alpine area. For future studies correct slab density structure are crucial~~should incorporate subducting slab structures in order~~ to provide a ~~meaningful~~ representation of the Alpine geodynamic ~~setting~~~~complex Alpine area~~. Precise estimations of the slab density structure require a correct crustal density and crustal thickness model. With the integration of further observables, it might

561 be possible to judge on the correct slab configuration beneath the Alps. Furthermore, future  
562 studies based on the AlpArray Network will be of high interest in better defining slab  
563 geometries as well as their properties.

564 **Competing interests**

565 The authors declare that they have no conflict of interest.

566 **Author contributions**

567 ML carried out the gravity modelling, visualized and interpreted the results and prepared the  
568 first manuscript draft. JE supervised the gravity modelling and interpretation, designed the  
569 original research project, acquisition of the financial support for the project leading to this  
570 publication and writing (reviewing and editing). TM defined the slab configurations based on  
571 tectonic and seismological knowledge and writing (reviewing and editing). AE created and  
572 provided the surface wave tomography model MeRE2020 and writing (reviewing and editing).

573 **Acknowledgment**

574 The authors thank the reviewers, Carla Braitenberg and an anonymous referee for their valuable  
575 suggestions, which helped to improve the manuscript significantly.

576 This study is part of the projects "Integrierte 3D Modellierung des Schwere- und  
577 Temperaturfelds zum Verständnis von Rheologie und Deformation der Alpen und ihrer  
578 Vorlandbecken - INTEGRATE" and "Surface Wavefield Tomography of the Alpine Region to  
579 Constrain Slab Geometries, Lithospheric Deformation and Asthenospheric Flow in the Alpine  
580 Region" funded by German Research Foundation (DFG) in the SPP Mountain Building  
581 Processes in 4D.

We thank the developer of open scientific Software which were utilized in this study: tesseroids (Uieda et al., 2016), LitMod 3D (Fullea et al., 2009 and Afonso et al., 2008) and Generic Mapping Tools (GMT) (Wessel et al., 2013; Wessel & Luis, 2017).

## References

- Afonso, J. C., Fernandez, M., Ranalli, G., Griffin, W. L., & Connolly, J. A. D. (2008). Integrated geophysical-petrological modeling of the lithosphere and sublithospheric upper mantle: Methodology and applications. *Geochemistry, Geophysics, Geosystems*, 9(5).
- Amante, C., & Eakins, B. W. (2009). ETOPO1 arc-minute global relief model: procedures, data sources and analysis.
- Artemieva, I. M. (2019). Lithosphere structure in Europe from thermal isostasy. *Earth-Science Reviews*, 188, 454-468.
- Babuška, V., Plomerova, J., & Granet, M. (1990). The deep lithosphere in the Alps: a model inferred from P residuals. *Tectonophysics*, 176(1-2), 137-165.
- Beller, S., Monteiller, V., Operto, S., Nolet, G., Paul, A., & Zhao, L. (2018). Lithospheric architecture of the South-Western Alps revealed by multiparameter teleseismic full-waveform inversion. *Geophysical Journal International*, 212(2), 1369-1388.
- Bouman, J., Ebbing, J., Fuchs, M., Sebera, J., Lieb, V., Szwillus, W., ... & Novak, P. (2016). Satellite gravity gradient grids for geophysics. *Scientific reports*, 6(1), 1-11.
- Braitenberg, C. (2015). Exploration of tectonic structures with GOCE in Africa and across-continentals. *International Journal of Applied Earth Observation and Geoinformation*, 35, 88-95.
- Channell, J. E. T., & Horvath, F. (1976). The African/Adriatic promontory as a palaeogeographical premise for Alpine orogeny and plate movements in the Carpatho-Balkan region. *Tectonophysics*, 35(1-3), 71-101.
- Connolly, J. A. D. (2009). The geodynamic equation of state: what and how. *Geochemistry, Geophysics, Geosystems*, 10(10).
- Dewey, J. F., Helman, M. L., Knott, S. D., Turco, E., & Hutton, D. H. W. (1989). Kinematics of the western Mediterranean. *Geological Society, London, Special Publications*, 45(1), 265-283.
- Ebbing, J., Braitenberg, C., & Götze, H. J. (2001). Forward and inverse modelling of gravity revealing insight into crustal structures of the Eastern Alps. *Tectonophysics*, 337(3-4), 191-208.
- Ebbing, J., Braitenberg, C., & Götze, H. J. (2006). The lithospheric density structure of the Eastern Alps. *Tectonophysics*, 414(1-4), 145-155.
- El-Sharkawy, A., Meier, T., Lebedev, S., Behrmann, J., Hamada, M., Cristiano, L., ... & Köhn, D. (2020). The Slab Puzzle of the Alpine - Mediterranean Region: Insights from a new, High -

Resolution, Shear - Wave Velocity Model of the Upper Mantle. *Geochemistry, Geophysics, Geosystems*, e2020GC008993.

Fichtner, A., van Herwaarden, D. P., Afanasiev, M., Simutè, S., Krischer, L., Çubuk-Sabuncu, Y., ... & Trampert, J. (2018). The collaborative seismic earth model: Generation 1. *Geophysical research letters*, 45(9), 4007-4016.

Frisch, W. (1979). Tectonic progradation and plate tectonic evolution of the Alps. *Tectonophysics*, 60(3-4), 121-139.

Fullea, J., Afonso, J. C., Connolly, J. A. D., Fernandez, M., García-Castellanos, D., & Zeyen, H. (2009). LitMod3D: An interactive 3-D software to model the thermal, compositional, density, seismological, and rheological structure of the lithosphere and sublithospheric upper mantle. *Geochemistry, Geophysics, Geosystems*, 10(8).

Fullea, J., Fernández, M., Afonso, J. C., Vergés, J., & Zeyen, H. (2010). The structure and evolution of the lithosphere–asthenosphere boundary beneath the Atlantic–Mediterranean Transition Region. *Lithos*, 120(1-2), 74-95.

Ganguly, J., Freed, A. M., & Saxena, S. K. (2009). Density profiles of oceanic slabs and surrounding mantle: Integrated thermodynamic and thermal modeling, and implications for the fate of slabs at the 660 km discontinuity. *Physics of the Earth and Planetary Interiors*, 172(3-4), 257-267.

Götze, H. J., Lahmeyer, B., Schmidt, S., & Strunk, S. (1994). The lithospheric structure of the Central Andes (20–26 S) as inferred from interpretation of regional gravity. In *Tectonics of the southern Central Andes* (pp. 7-21). Springer, Berlin, Heidelberg.

Götze, H. J., & Krause, S. (2002). The Central Andean gravity high, a relic of an old subduction complex?. *Journal of South American Earth Sciences*, 14(8), 799-811.

Götze, H. J., & Pail, R. (2018). Insights from recent gravity satellite missions in the density structure of continental margins—With focus on the passive margins of the South Atlantic. *Gondwana Research*, 53, 285-308.

Grad, M., Tiira, T., & ESC Working Group. (2009). The Moho depth map of the European Plate. *Geophysical Journal International*, 176(1), 279-292.

Griffin, W. L., O'reilly, S. Y., Afonso, J. C., & Begg, G. C. (2009). The composition and evolution of lithospheric mantle: a re-evaluation and its tectonic implications. *Journal of Petrology*, 50(7), 1185-1204.

Gutknecht, B. D., Götze, H. J., Jahr, T., Jentzsch, G., & Mahatsente, R. (2014). Structure and state of stress of the Chilean subduction zone from terrestrial and satellite-derived gravity and gravity gradient data. *Surveys in Geophysics*, 35(6), 1417-1440.

Handy, M. R., Schmid, S. M., Bousquet, R., Kissling, E., & Bernoulli, D. (2010). Reconciling plate-tectonic reconstructions of Alpine Tethys with the geological–geophysical record of spreading and subduction in the Alps. *Earth-Science Reviews*, 102(3-4), 121-158.

- Handy, M. R., Ustaszewski, K., & Kissling, E. (2015). Reconstructing the Alps–Carpathians–Dinarides as a key to understanding switches in subduction polarity, slab gaps and surface motion. *International Journal of Earth Sciences*, 104(1), 1-26.
- Hawkesworth, C. J., Waters, D. J., & Bickle, M. J. (1975). Plate tectonics in the Eastern Alps. *Earth and Planetary Science Letters*, 24(3), 405-413.
- Hetényi, G., Plomerová, J., Bianchi, I., Exnerová, H. K., Bokelmann, G., Handy, M. R., ... & AlpArray-EASI Working Group. (2018). From mountain summits to roots: Crustal structure of the Eastern Alps and Bohemian Massif along longitude 13.3 E. *Tectonophysics*, 744, 239-255.
- Holzrichter, N., & Ebbing, J. (2016). A regional background model for the Arabian Peninsula from modeling satellite gravity gradients and their invariants. *Tectonophysics*, 692, 86-94.
- Hua, Y., Zhao, D., & Xu, Y. (2017). P wave anisotropic tomography of the Alps. *Journal of Geophysical Research: Solid Earth*, 122(6), 4509-4528.
- Isaak, D. G., Anderson, O. L., Goto, T., & Suzuki, I. (1989). Elasticity of single-crystal forsterite measured to 1700 K. *Journal of Geophysical Research: Solid Earth*, 94(B5), 5895-5906.
- Isaak, D. G. (1992). High-temperature elasticity of iron-bearing olivines. *Journal of Geophysical Research: Solid Earth*, 97(B2), 1871-1885.
- Karato, S. I. (1993). Importance of anelasticity in the interpretation of seismic tomography. *Geophysical Research Letters*, 20(15), 1623-1626.
- Karousová, H., Plomerová, J., & Babuška, V. (2013). Upper-mantle structure beneath the southern Bohemian Massif and its surroundings imaged by high-resolution tomography. *Geophysical Journal International*, 194(2), 1203-1215.
- Kästle, E. D., El-Sharkawy, A., Boschi, L., Meier, T., Rosenberg, C., Bellahsen, N., ... & Weidle, C. (2018). Surface wave tomography of the alps using ambient-noise and earthquake phase velocity measurements. *Journal of Geophysical Research: Solid Earth*, 123(2), 1770-1792.
- Kästle, E. D., Rosenberg, C., Boschi, L., Bellahsen, N., Meier, T., & El-Sharkawy, A. (2020). Slab break-offs in the Alpine subduction zone. *International Journal of Earth Sciences*, 1-17.
- Kincaid, C., & Olson, P. (1987). An experimental study of subduction and slab migration. *Journal of Geophysical Research: Solid Earth*, 92(B13), 13832-13840.
- Kissling, E., Schmid, S. M., Lippitsch, R., Ansorge, J., & Fügenschuh, B. (2006). Lithosphere structure and tectonic evolution of the Alpine arc: new evidence from high-resolution teleseismic tomography. *Geological Society, London, Memoirs*, 32(1), 129-145.
- Kogan, M. G., & McNutt, M. K. (1993). Gravity field over northern Eurasia and variations in the strength of the upper mantle. *Science*, 259(5094), 473-479.

- Koulakov, I., Kaban, M. K., Tesauero, M., & Cloetingh, S. A. P. L. (2009). P-and S-velocity anomalies in the upper mantle beneath Europe from tomographic inversion of ISC data. *Geophysical Journal International*, 179(1), 345-366.
- Le Breton, E., Handy, M. R., Molli, G., & Ustaszewski, K. (2017). Post-20 Ma motion of the Adriatic Plate: New constraints from surrounding orogens and implications for crust-mantle decoupling. *Tectonics*, 36(12), 3135-3154.
- Lippitsch, R., Kissling, E., & Ansorge, J. (2003). Upper mantle structure beneath the Alpine orogen from high-resolution teleseismic tomography. *Journal of Geophysical Research: Solid Earth*, 108(B8).
- Lüschen, E., Lammerer, B., Gebrande, H., Millahn, K., Nicolich, R., & TRANSALP Working Group. (2004). Orogenic structure of the Eastern Alps, Europe, from TRANSALP deep seismic reflection profiling. *Tectonophysics*, 388(1-4), 85-102.
- Lüschen, E., Borrini, D., Gebrande, H., Lammerer, B., Millahn, K., Neubauer, F., ... & TRANSALP Working Group. (2006). TRANSALP—deep crustal Vibroseis and explosive seismic profiling in the Eastern Alps. *Tectonophysics*, 414(1-4), 9-38.
- Lyu, C., Pedersen, H. A., Paul, A., Zhao, L., & Solarino, S. (2017). Shear wave velocities in the upper mantle of the Western Alps: new constraints using array analysis of seismic surface waves. *Geophysical Journal International*, 210(1), 321-331.
- Mahatsente, R. (2019). Plate Coupling Mechanism of the Central Andes Subduction: Insight from Gravity Model. *Journal of Geodetic Science*, 9(1), 13-21.
- McDonough, W. F., & Sun, S. S. (1995). The composition of the Earth. *Chemical geology*, 120(3-4), 223-253.
- McKenzie, D., & Fairhead, D. (1997). Estimates of the effective elastic thickness of the continental lithosphere from Bouguer and free air gravity anomalies. *Journal of Geophysical Research: Solid Earth*, 102(B12), 27523-27552.
- Mitterbauer, U., Behm, M., Brückl, E., Lippitsch, R., Guterch, A., Keller, G. R., ... & Šumanovac, F. (2011). Shape and origin of the East-Alpine slab constrained by the ALPASS teleseismic model. *Tectonophysics*, 510(1-2), 195-206.
- Nocquet, J. M., & Calais, E. (2004). Geodetic measurements of crustal deformation in the Western Mediterranean and Europe. *Pure and applied geophysics*, 161(3), 661-681.
- Piomallo, C., & Morelli, A. (2003). P wave tomography of the mantle under the Alpine - Mediterranean area. *Journal of Geophysical Research: Solid Earth*, 108(B2).
- Reuber, G., Meier, T., Ebbing, J., El-Sharkawy, A., & Kaus, B. (2019, January). Constraining the dynamics of the present-day Alps with 3D geodynamic inverse models-model version 0.2. In *Geophysical Research Abstracts* (Vol. 21).
- Root, B. C. (2020). Comparing global tomography-derived and gravity-based upper mantle density models. *Geophysical Journal International*, 221(3), 1542-1554.

777 Schmid, S. M., Fügenschuh, B., Kissling, E., & Schuster, R. (2004). Tectonic map and overall  
778 architecture of the Alpine orogen. *Eclogae Geologicae Helvetiae*, 97(1), 93-117.  
779  
780 Serpelloni, E., Vannucci, G., Anderlini, L., & Bennett, R. A. (2016). Kinematics,  
781 seismotectonics and seismic potential of the eastern sector of the European Alps from GPS and  
782 seismic deformation data. *Tectonophysics*, 688, 157-181.  
783  
784 Spada, M., Bianchi, I., Kissling, E., Agostinetti, N. P., & Wiemer, S. (2013). Combining  
785 controlled-source seismology and receiver function information to derive 3-D Moho  
786 topography for Italy. *Geophysical Journal International*, 194(2), 1050-1068.  
787  
788 Spakman, W., & Wortel, R. (2004). A tomographic view on western Mediterranean  
789 geodynamics. In *The TRANSMED atlas. The Mediterranean region from crust to mantle* (pp.  
790 31-52). Springer, Berlin, Heidelberg.  
791  
792 Spooner, C., Scheck-Wenderoth, M., Götze, H. J., Ebbing, J., & Hetényi, G. (2019). Density  
793 distribution across the Alpine lithosphere constrained by 3-D gravity modelling and relation to  
794 seismicity and deformation. *Solid Earth*, 10(6), 2073-2088.  
795  
796 Stampfli, G. M., & Borel, G. D. (2002). A plate tectonic model for the Paleozoic and Mesozoic  
797 constrained by dynamic plate boundaries and restored synthetic oceanic isochrons. *Earth and*  
798 *Planetary Science Letters*, 196(1-2), 17-33.  
799  
800 Tadiello, D., & Braitenberg, C. (2021). Gravity modeling of the Alpine lithosphere affected by  
801 magmatism based on seismic tomography. *Solid Earth Discussions*, 1-31.  
802  
803 Tašárová, Z. A. (2007). Towards understanding the lithospheric structure of the southern  
804 Chilean subduction zone (36 S–42 S) and its role in the gravity field. *Geophysical Journal*  
805 *International*, 170(3), 995-1014.  
806  
807 Tiberi, C., Diamant, M., Lyon Caen, H., & King, T. (2001). Moho topography beneath the  
808 Corinth Rift area (Greece) from inversion of gravity data. *Geophysical Journal*  
809 *International*, 145(3), 797- 808.  
810  
811 Uieda, L., Barbosa, V. C., & Braitenberg, C. (2016). tesseroids: Forward-modeling  
812 gravitational fields in spherical coordinates. *Geophysics*, 81(5), F41-F48.  
813  
814 Vacher, P., Mocquet, A., & Sotin, C. (1998). Computation of seismic profiles from mineral  
815 physics: the importance of the non-olivine components for explaining the 660 km depth  
816 discontinuity. *Physics of the Earth and Planetary Interiors*, 106(3-4), 275-298.  
817  
818 Vrabec, M., & Fodor, L. (2006). Late Cenozoic tectonics of Slovenia: structural styles at the  
819 Northeastern corner of the Adriatic microplate. In *The Adria microplate: GPS geodesy,*  
820 *tectonics and hazards* (pp. 151-168). Springer, Dordrecht.  
821  
822 Wang, Y., He, Y., Lu, G., & Wen, L. (2020). Seismic, thermal and compositional structures of  
823 the stagnant slab in the mantle transition zone beneath southeastern China. *Tectonophysics*,  
824 775, 228208.  
825  
826 Webb, S. J. (2009). The use of potential field and seismological data to analyze the structure of  
827 the lithosphere beneath southern Africa (Doctoral dissertation).

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Wessel, P., Smith, W. H., Scharroo, R., Luis, J., & Wobbe, F. (2013). Generic mapping tools: improved version released. *Eos, Transactions American Geophysical Union*, 94(45), 409-410.

Wessel, P., & Luis, J. F. (2017). The GMT/MATLAB Toolbox. *Geochemistry, Geophysics, Geosystems*, 18(2), 811-823.

Workman, R. K., & Hart, S. R. (2005). Major and trace element composition of the depleted MORB mantle (DMM). *Earth and Planetary Science Letters*, 231(1-2), 53-72.

Zeyen, H., & Fernández, M. (1994). Integrated lithospheric modeling combining thermal, gravity, and local isostasy analysis: Application to the NE Spanish Geotranssect. *Journal of Geophysical Research: Solid Earth*, 99(B9), 18089-18102.

Zhao, L., Paul, A., Malusà, M. G., Xu, X., Zheng, T., Solarino, S., ... & Aubert, C. (2016). Continuity of the Alpine slab unraveled by high-resolution P wave tomography. *Journal of Geophysical Research: Solid Earth*, 121(12), 8720-8737.

Zingerle, P., Pail, R., Gruber, T., & Oikonomidou, X. (2020). The combined global gravity field model XGM2019e. *Journal of Geodesy*, 94(7), 1-12.

~~Zingerle, P., Pail, R., Gruber, T., & Oikonomidou, X. (2019). The experimental gravity field model XGM2019e.~~

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## Appendix A Gravity Gradients at satellite height

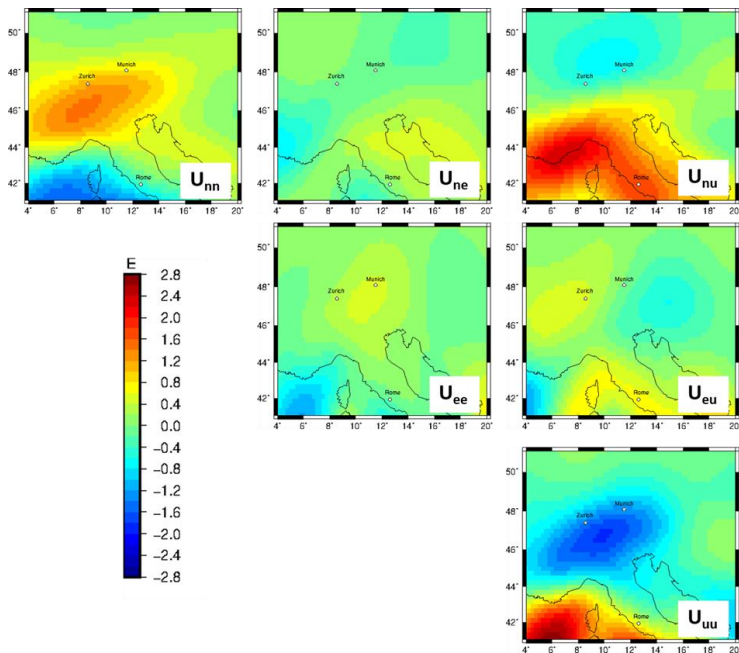
For all Alpine density models presented above (section 3, 4.1 and 4.2) we have also calculated gravity gradients at a station height of 225 km. This station height corresponds to the second mission phase of GOCE (Gravity field and steady-state ocean circulation explorer) carried out by ESA (European Space Agency).

We anticipated that gravity gradients measured by the GOCE satellite mission are sensitive to the slab segments in the Alpine region. Our result show, that the long wavelength signal of the different present slab segments contributes to a large-scale gravity response where the different contributor cannot be separated. Therefore, we conclude that against our anticipation gravity gradients at satellite height are in fact not sensitive to the Alpine slab configuration. We show here, the gravity gradients (mainly the gzz component) for completeness.

Measured gravity gradients from the GOCE mission (Bouman et al., 2016), which were corrected for topography and bathymetry ranges from 2.5 to -2.5 E at satellite altitude of 225



864 km height (Fig. 13). A negative gravity anomaly of -2.5 E in the gzz component is observed  
865 equivalent to the vertical gz component (Fig. 13). However, no clear sign for subducting  
866 lithosphere can be observed in any component of the gravity gradient tensor.



867  
868 **Figure 13** GOCE gradients at 225 km height after Bouman et al. (2016) corrected for topography and bathymetry with a 5°  
869 extension to remove far field effects. The gravity gradients are presented in a North-East-Up coordinate system.

870 The forward calculated gzz component at 225 km station height from a density model (section  
871 3) with converted densities ranges from -3.5 E to 0.7 E (Fig. 14). A positive gravity signal of  
872 about 0.5 E in the Apennine and Alpine region is observed which could be linked to subducting  
873 slab segments. However, it is impossible to separate specific slab segments.

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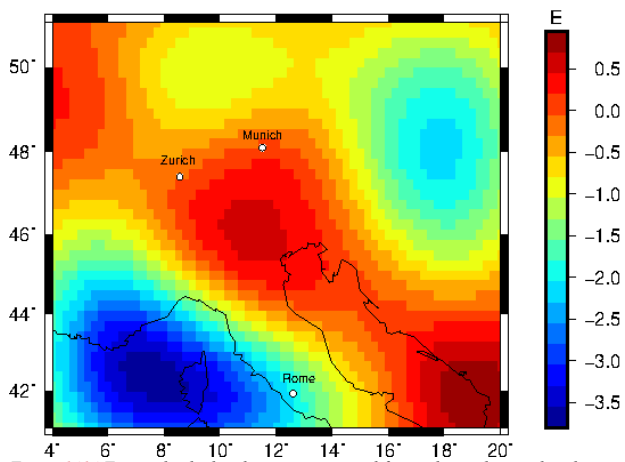


Figure 14.4 Forward calculated gzz gravity signal from relative density distribution converted from relative seismic velocities using a conversion factor of 0.3 for the at 225 km station height.

Forward calculated tesseroïd models (section 4.1) for slab configuration 1 and 2 with a constant density contrast of  $60 \text{ kg/m}^3$  and a constant thickness of 80 km result in a less sharp gravity signal for the gzz component at a station height of 225 km (Fig. 15) compared to the gz component at station height of 6040 m (Fig. 6). The gravity signal for the gzz component is in the range of 0.8 E to 1 E. At satellite altitude the gravity signal is observed as a large area with a positive gravity effect for Configuration 1 and 2. The contribution of the different slab segments to this positive gravity effect is not distinguishable. The only recognizable difference is the size of this positive gravity signal. Configuration 1 shows a smaller anomaly, due to a lower volume of subducting material in the Eastern Alps.

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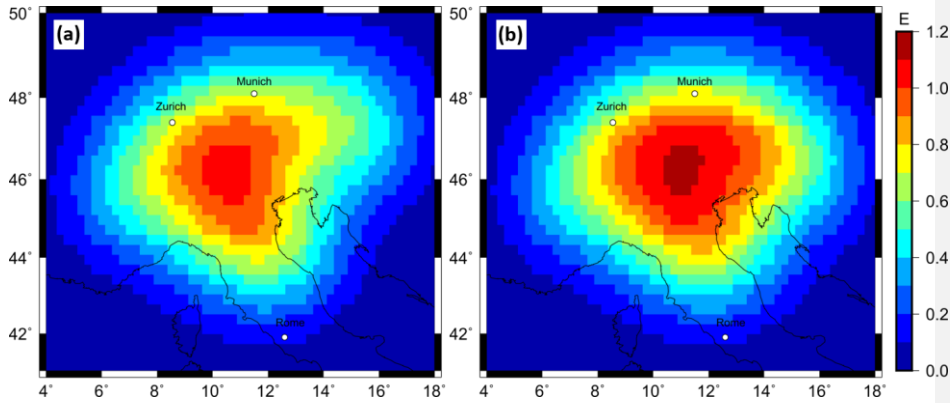


Figure 15.15 Forward calculated gzz gravity signal at a station height of 225 km from predefined sub-crustal slab geometries with a content density contrast of  $60 \text{ kg/m}^3$  and a constant thickness of 80 km. (a) slab configuration of hypothesis 1 (b) slab configuration of hypothesis 2.

In Addition, the signal strength for the forward calculated gzz component show the same dependency of signal strength to the density contrast and slab thickness (Fig. 16) as the gz component (Fig. 7). The signal strength of the gzz component ranges for the 12 different combinations from 0.3 E to 2 E (Fig. 16). The gravity signal cannot be separated and affiliated to a certain slab segment. The gzz gradient signal shows a large blurry gravity high over the Alps, which thins out to the edges.

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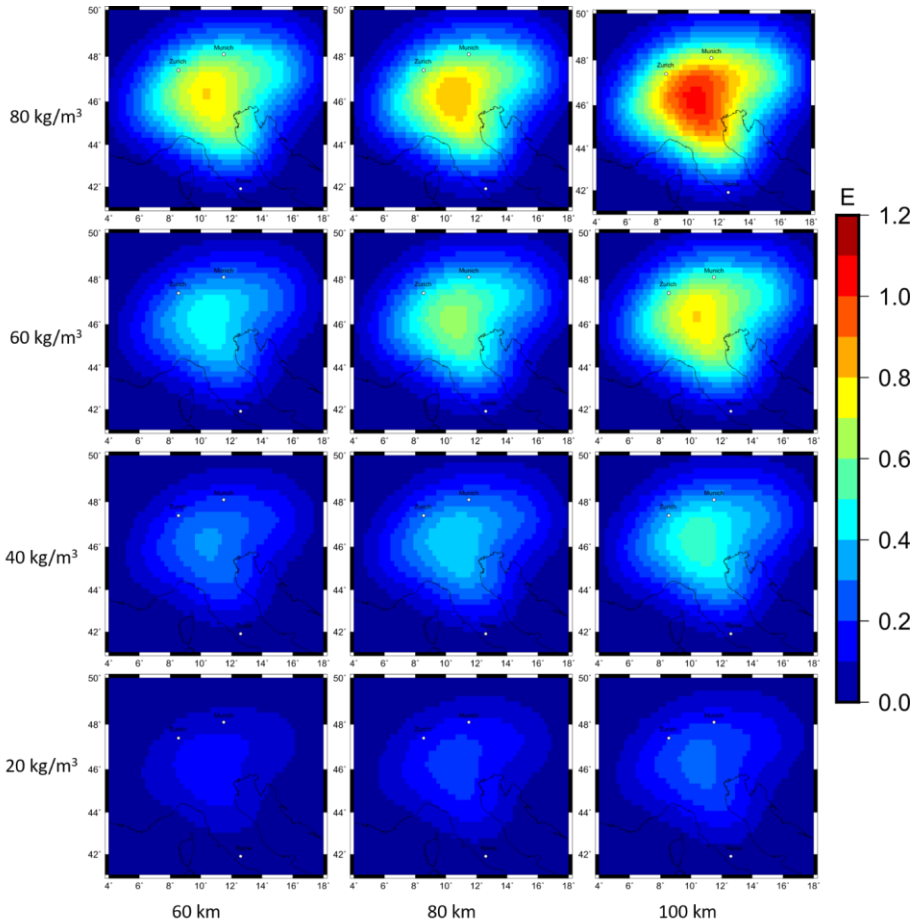


Figure 16+6. Forward calculated gzz gravity signal for 12 different combination of density contrast and slab thickness at a station height of 225 km for sub-crustal slab configuration 1.

The gravity effect for the LitMod models (section 4.2) with the slab Configuration 1 shows in the lithosphere domain a signal strength of about 0.05 E, while the sub lithospheric gravity signal is in the range of 0.1 E for the gzz component at satellite altitude of 225 km height. The combined gravity signal is in the order of 0.14 E (Fig. 17). A Proterozoic slab produces a larger amplitude in signal strength, however the different slab segments can again not be separated (Fig. 18).

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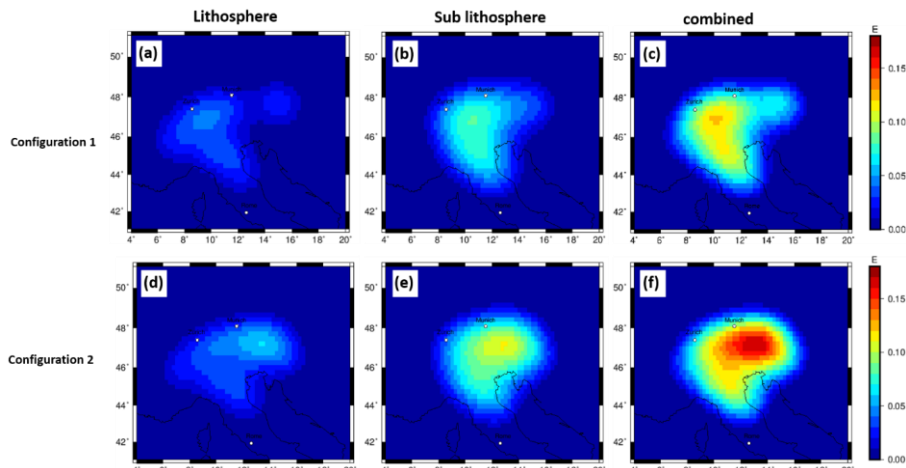


Figure 17-17, forward calculated gzz gravity signal at satellite altitude of 225 km based on LitMod models with tecton like compositions in the lithosphere and PUM and DMM compositions in the sub lithosphere ( $M_1$ ,  $M_2$ ,  $M_3$ ,  $M_4$ ) with an additional thermal anomaly of  $-100^\circ\text{K}$  for the sub-lithospheric slab segment, for predefined slab Configuration to the background model  $M_0$ . (a)-(c) for Configuration 1. (d)-(f) for Configuration 2. Topographic and crustal effects are nullified.

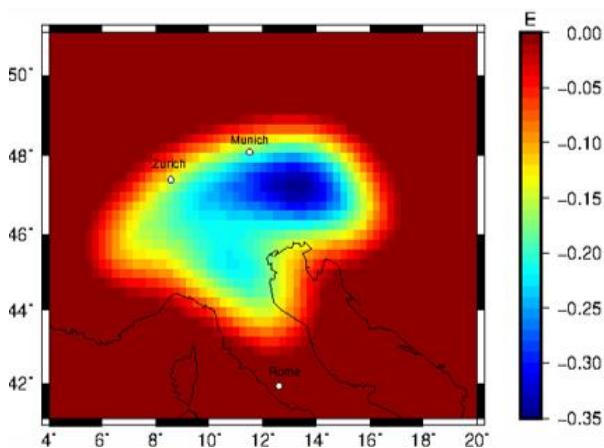


Figure 18-18, Forward calculated gravity effect for the gzz component at satellite height of a Proterozoic lithospheric slab segment to a Tecton compositional surrounding mantle for Configuration 2 obtained by calculating the residual between  $M_8$  and  $M_0$ .

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