



1    **Fracture attribute scaling and connectivity in the Devonian Orcadian**  
2            **Basin with implications for geologically equivalent sub-surface**  
3                    **fractured reservoirs**

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15



16 **Abstract:** Fracture attribute scaling and connectivity datasets from analogue systems are widely used  
17 to inform sub-surface fractured reservoir models in a range of geological settings. However,  
18 significant uncertainties are associated with the determination of reliable scaling parameters in  
19 surface exposures, particularly for fault widths and fracture aperture. This has limited our ability to  
20 upscale key parameters that control fluid-flow at reservoir to basin scales. In this study, we present  
21 nine 1D-transect (scanline) fault and fracture attribute datasets from Middle Devonian sandstones in  
22 Caithness (Scotland) that are widely used as an onshore analogue for nearby sub-surface reservoirs  
23 such as the Clair Field, West of Shetland. Our multiscale analysis confirms power-law behaviours for  
24 both length over 8 orders of magnitude ( $10^{-4}$  to  $10^4$ ) and fracture aperture and fault width (including  
25 fills) over 4 orders of magnitude ( $10^{-6}$  to  $10^{-2}$ ). We also present a 2D fault and fracture topology  
26 analysis which allows assessment of the heterogeneity of connectivity and self-similarity. This  
27 multiscale approach provides a new basis for upscaling micro- to meso-scale fracture attributes  
28 collected in outcrop analogues for use in static and dynamic reservoir models at reservoir to basin  
29 scales.

30

31 *Keywords:* fault, fracture attribute, multiscale, Clair Field, Devonian

32



## 33 1 Introduction

34 Fractures, used here as a general term to include faults, joints and veins, exist over a wide range of  
35 scales from microns to hundreds of kilometres and fundamentally control the fluid-flow and  
36 mechanical properties of crustal rocks, including many sub-surface reservoirs holding oil, gas or  
37 water (e.g. Sibson, 1996; Odling et al., 1999; Bonnet et al., 2001). The heterogeneous distribution of  
38 natural fracture systems and uncertainties associated with the determination of reliable scaling  
39 parameters in 3D over large-scale ranges remains a persistent problem in reservoir studies. Small  
40 faults (fractures with <1m displacement) and joints (fractures with no shear displacement) may occur  
41 in isolation, or as part of a damage zone of larger displacement (>10s m) faults (e.g. Shultz and  
42 Fossen, 2008). Fractures (*sensu lato*) can be described by their *geometrical* attributes such as  
43 orientation and size (displacement, length, aperture) and also by *spatial* attributes such as intensity  
44 (density), clustering, connectivity and continuity (Sanderson and Nixon, 2015).

45

46 In practice, fracture attribute distributions are typically constrained from drillholes and cores  
47 which provide high resolution ( $10^{-4}$  to  $10^0$  m), but highly censored (size limited by borehole diameter),  
48 spatially limited 1D samples of the reservoir. In contrast, 2D and 3D seismic reflection datasets  
49 provide continuous, but relatively low-resolution fracture network maps at 10 to  $10^5$  m scales.  
50 Consequently, since fluid-flow in a fractured reservoir is a volumetric (3D) summation of all small-  
51 (< 1m displacement) to large-scale fracture contributions, accurately characterizing 3D fracture  
52 network using just borehole-, cores- and seismic-derived datasets is particularly challenging.

53

54 Analogue datasets from outcrops are used to fill the gap between high-resolution but sparse  
55 borehole data and low-resolution seismic data and give access to fracture datasets across many scales  
56 ( $10^{-2}$  to  $10^6$  m scales) and in 1, 2 and 3 dimensions (e.g. Mäkel, 2007). Using one dimensional  
57 sampling methods (1D), fracture attributes in outcrop analogues have been investigated in different  
58 tectonic contexts and lithologies at given scales (e.g. Baecher, 1983; Gillespie et al., 1993; McCaffrey  
59 and Johnston, 1996; Knott et al., 1996; Odling et al., 1999; Bour et al., 2002; Manzocchi, 2002; Olson,  
60 2003; Kim and Sanderson, 2005; Gomez and Laubach, 2006; Schultz et al., 2008; Hooker et al., 2009;  
61 Torabi and Berg, 2011). However, results from *multi-scale* sampling of fracture attributes are less  
62 common (e.g. Walsh and Watterson, 1988; Guerriero et al., 2010; Torabi and Berg, 2011; Bertrand  
63 et al., 2015).

64



65 In this study, we use a multi-scale 1D sampling approach to describe fractures (including faults)  
66 formed in Devonian sandstones of the Orcadian Basin, North Scotland. These rocks are widely  
67 viewed as being a useful analogue for the fractured Devonian siliclastic reservoirs that form the giant  
68 Clair Field, West of Shetland (Allen and Mange-Rajetzky, 1992; Coney et al., 1993; Barr et al., 2007),  
69 one of the largest remaining oilfields in the UKCS (c. 7 billion barrels of Stock Tank oil initially in  
70 place, Robertson et al. 2020). We investigate here the size and spatial distributions of fracture trace  
71 length (multi-scale) and aperture (small-scale only), and their scaling properties. In addition, we use  
72 a multi-scale 2D sampling approach that allows us to quantify the connectivity of fracture networks  
73 following the fracture topology methodology used by Nixon (2013) and Sanderson and Nixon (2015).  
74 We use datasets derived from a high-resolution bathymetric map (sub-regional scale), aerial  
75 photographs, coastal exposure and a thin-section made from hand samples. We discuss how this  
76 integrated approach can be used to upscale analogue datasets - in particular the aperture/fracture width  
77 parameter - to reservoir or basin scales. Whilst, we do not aim here to revise the theoretical statistical  
78 background of fitting methods (extensively treated in Corral and González, 2019) we do show their  
79 potential when applied to a multiscale analysis. This work shows that the determination of multiscale  
80 fracture attributes scaling in 1D and 2D can form a useful input for building realistic static geological  
81 models at reservoir scale that serve as starting points for simulations of fluid storage, migration  
82 processes and production (e.g. Odling et al., 1999).

83

## 84 2 Methodology

### 85 2.1 Sampling of fractures and fracture network attributes

86 The most common data acquisition methodologies use: (i) scanlines (or transects); (ii) window  
87 sampling; (iii) circular scanline windows; and (iv) box counting (**Fig. 1a**), which collectively provide  
88 access to different attributes as shown in **Table 1**. Scanlines (1D method) allow a relatively simple  
89 characterization of individual fracture sizes and spacing (**Fig. 1b**), and act as a good proxy for the  
90 borehole data that typically serve as starting points for building reservoir models (Priest and Hudson,  
91 1981; Baecher, 1983; Gillespie et al., 1993; McCaffrey and Johnston, 1996; Knott et al., 1996; Ortega  
92 and Marrett, 2000; Ortega et al., 2006; Bonnet et al., 2001; Odling et al., 1999). Window sampling  
93 and circular scanline windows (both 2D methods) provide further information on the spatial  
94 relationships within the fractured system (Mauldon, 1994; Mauldon et al., 2001; Rohrbaugh et al.,  
95 2002; Manzocchi, 2002; Zeeb et al., 2013; Watkins et al., 2015; Sanderson and Nixon, 2015; Rizzo  
96 et al., 2017) and importantly provide access to connectivity estimates for the fracture array, which is  
97 a key input when modelling fluid-flow.



98 In this study, fracture orientations, trace lengths and apertures, together with composition and  
99 texture of fracture infills and fracture terminations on joints and faults were recorded. The start and  
100 end point of each transect was recorded using a hand-held GPS unit. Most fractures in the Orcadian  
101 Basin are filled with minerals (calcite or pyrite) or, locally, oil, and, following Ortega et al. (2006),  
102 the apertures measured in this study are the orthogonal distance between the fracture walls and include  
103 the fill, i.e. the '*kinematic aperture*'. When it was not possible to measure the transect orthogonally  
104 to the main fault because of outcrop exposure limitations (e.g. at the sub-regional scale), the measured  
105 attributes were adjusted using the Terzaghi's Correction (**Fig. 1c**). To more precisely measure the  
106 aperture attributes, an aperture size comparator ( $10^{-5}$  to  $10^{-4}$ m) was used in the field to in order to  
107 ensure a larger range of recorded apertures, thereby reducing censoring effects.

108 To extend the analysis to other scales, the above mentioned scanline method was adapted and  
109 applied to both aerial photographs (regional scale) to quantify trace length, and to thin-section  
110 (microscale) to quantify trace length and aperture.

111

#### 112 2.1.1 *Fracture intensity/frequency plots (1D)*

113 The fracture intensity/frequency distribution for 1D datasets can be visualised by plotting sorted  
114 attribute values (e.g. fracture length) versus cumulative frequency. This enables assessment of the  
115 distribution, spatial and scaling properties of the fracture sample (i.e. the ratio of short to long  
116 fractures for given sample line length). Fracture attribute distributions are thought to display three  
117 main types of statistical distribution (**Fig. 2**; Bonnet et al., 2001; Gillespie et al., 1993; Zeeb et al.,  
118 2013): (a) *Exponential, random or Poisson distributions* are characteristic of a system with one  
119 randomised variable (Gillespie et al., 1993); (b) *Log-normal distributions* are generally produced by  
120 systems with a characteristic length scale, due to mechanical stratigraphic boundaries controlling  
121 layer-bound jointing for example (Narr, 1991 and Olson, 2007); (c) *Power-law distributions* lack a  
122 characteristic length scale in the fracture growth process (Zeeb et al., 2013) and the data exhibit scale-  
123 invariant fractal geometries (**Fig. 2c** bottom). This means that the relative number of small versus  
124 large elements remains the same at all scales between the upper and lower fractal limits (Barton,  
125 1995). Limits to the fractal behaviour, although unknown (Corral and González, 2019), can be related  
126 to both spatial and temporal influence, e.g., lithological boundaries across which fracture  
127 characteristics change, and changes in stress orientation, respectively. Although some fracture  
128 populations are better described by scale-limited laws, such as log-normal or exponential  
129 distributions, it is generally accepted that for many systems power-law distributions and fractal



130 geometry provide a widely applicable descriptive tool for fracture system characterization (e.g.  
131 Bonnet et al., 2001). Ideally, the best-fit in a power-law distribution should be consistent over several  
132 orders of magnitude at a given scale (Walsh and Watterson, 1993; McCaffrey and Johnston, 1996).  
133

134 Fracture sampling issues (e.g. censoring and truncation in **Fig. 2c**) are commonly encountered  
135 and can result in difficulty in ascribing the best-fit distribution. For instance, when long fractures are  
136 incompletely sampled (e.g. censoring in **Fig. 2c**), it is difficult to determine between log-normal and  
137 power-law fits to distributions. These sampling issues (due to resolution effects) may mean that, while  
138 a log-normal distribution is the best-fit to a dataset, a power-law distribution can also show a good fit  
139 (Corral and González, 2019) and may be preferred because of its greater physical significance and  
140 practical applicability (Bonnet et al., 2001). These assumptions need to be examined closely in any  
141 analysis of scaling (see Clauset et al., 2009). The maximum likelihood estimator (MLE) is a statistical  
142 technique that determines which distribution model is most likely to describe the data and it returns  
143 governing parameters of the fitting equations (see Supplementary Data File). The Kolmogorov-  
144 Smirnov (KS) test is then used to evaluate the difference between the data and synthetic data  
145 generated using the governing parameter derived from the MLE (Clauset et al., 2009). We use these  
146 statistical methods and adapted the methodology proposed by Rizzo et al. (2017) and used by  
147 FracPaQ (Healy et al., 2017) to calculate the MLE on progressively truncated populations for power-  
148 law, exponential and log-normal distributions.

149

### 150 *2.1.2 2D topology analysis*

151 Whilst 1D analyses provide information about fractures as single entities and their distribution per  
152 unit length of sample, 2D analyses measure fracture network properties and provide estimates of  
153 fracture connectivity and self-similarity. The 2D analysis used here was carried out on fractures at  
154 mesoscale using outcrop pavement photographs and at a larger scale using an offshore bathymetric  
155 data. Circular scanline windows and box counting methods were performed using the Corel Draw  
156 Graphic Suite™, ArcGis™ and MATLAB™ to produce small-scale fracture density maps (**Fig. 2d**),  
157 self-similarity plots (**Fig. 2f**) and ternary plots (**Fig. 2e**). To understand fracture topology, we follow  
158 Sanderson and Nixon (2015) in considering that fracture arrays are typically composed of nodes and  
159 branches. Nodes are points where a fracture terminates (I-type), abuts against another fracture  
160 (Y-type) or intersects another fracture (X-type) and branches are the portions of a fracture confined  
161 between two nodes. These are defined as I-I type (isolated branch) if delimited by two I-nodes, I-C



162 type (singly connected) if delimited by and I-node and Y- or X-node and C-C type (multiply  
163 connected) if delimited by Y- and X-nodes.

164

165 The number of branches and nodes for a given fracture network is strictly related meaning that,  
166 by knowing one of the two elements for the fracture network, it is possible to quantify all its  
167 components.  $N_I$ ,  $N_Y$  and  $N_X$  can be defined as the number of I-, Y- and X-type nodes and  $P_I$ ,  $P_Y$  and  
168  $P_X$  their relative proportions. Once the number of nodes and/or branches making up a fracture array  
169 are known, the connectivity can be visualized using a ternary plot of the component proportions (see  
170 e.g. **Fig. 2e**) or can be quantified by calculating the number of connections existing in the 2D map.  
171 In general, X- and Y-type nodes provide respectively 4 and 3 times more connectivity than I-type  
172 nodes (Nixon, 2013). This forms the basis for creating 2D density maps (see **Fig. 2d**). An array  
173 dominated by I-nodes is isolated, while arrays dominated by Y- and X-type nodes are increasingly  
174 more connected. Connectivity can be quantified by measuring the number of connections per line  
175  $n_{C/L}$  and the number of connections per branch  $n_{C/B}$  (see Sanderson & Nixon 2015 for details).

176

### 177 3 Geological Setting

#### 178 3.1 Location and regional structure

179 The studied siliciclastic strata are Devonian Old Red Sandstone (ORS) of the Orcadian Basin exposed  
180 in the Caithness region, North Scotland. The Orcadian Basin covers a large area of onshore and  
181 offshore northern Scotland forming part of a regionally linked system of basins extending northwards  
182 into western Norway and East Greenland (Seranne, 1992; Duncan and Buxton, 1995) (**Fig. 3a**). The  
183 great majority of the onshore sedimentary rocks of the Orcadian Basin in Caithness belong to the  
184 Middle Devonian and sit unconformably on top of eroded Precambrian (Moine Supergroup)  
185 basement. These sedimentary rocks and the fractures they contain have long been used as an onshore  
186 analogue for parts of the Devonian to Carboniferous Clair Group sequence that hosts the Clair oilfield  
187 west of Shetland (**Fig. 3a**; Allan and Mange-Rajetzki, 1992, Duncan and Buxton, 1995). It should be  
188 noted that strictly speaking, the Clair Group formed in an adjacent basin, in a somewhat different  
189 tectonic setting (Dichiarante, 2017).

190 Recent fieldwork has shown that the onshore Devonian sedimentary rocks of the Orcadian  
191 basin in Caithness host significant localized zones of fracturing, faulting and some folding on all  
192 scales. Field and microstructural analyses reveal three regionally recognised groups of structures



193 based on orientation, kinematics and infill (Dichiarante et al. 2016; Dichiarante, 2017). In summary,  
194 these are as follows:

195 **Group 1 faults** trend mainly N-S and NW-SE and display predominantly sinistral strike-slip to dip-  
196 slip extensional movements. They form the dominant structures in the eastern regions of Caithness  
197 closest to the offshore trace of the Great Glen Fault (GGF) (**Fig. 3a-b**). Deformation bands, gouges  
198 and breccias associated with these faults display little or no mineralization or veining. It is suggested  
199 that these structures are related to Devonian ENE-WSW transtension associated with sinistral shear  
200 along the Great Glen Fault during formation of the Orcadian and proto-West Orkney basins (Wilson  
201 et al., 2010; Dichiarante, 2017).

202 **Group 2 structures** are closely associated systems of metre- to kilometre-scale N-S trending folds  
203 and thrusts related to a highly heterogeneous regional inversion event recognized locally throughout  
204 Caithness. Once again, fault rocks associated with these structures display little or no mineralization  
205 or veining. Group 2 features are likely due to late Carboniferous – early Permian E-W shortening  
206 related to dextral reactivation of the Great Glen Fault (Coward et al., 1989; Seranne, 1992;  
207 Dichiarante, 2017).

208 **Group 3 structures** are the dominant fracture sets seen in the main coastal section west of St. John's  
209 Point (SJ in **Fig. 3b**). They comprise dextral oblique NE-SW trending faults and sinistral E-W trending  
210 faults with widespread syn-deformational low temperature hydrothermal carbonate mineralisation ( $\pm$   
211 base metal sulphides and bitumen) both along faults and in associated mineral veins (Dichiarante et  
212 al., 2016). Hydrocarbons are widespread in fractures in small volumes and are locally sourced from  
213 organic-rich fish beds within the Devonian sequences of the Orcadian Basin (Parnell, 1985; Marshall  
214 et al, 1985). Re-Os model ages of syn-deformational fault-hosted pyrite in Caithness yield Permian  
215 ages (ca. 267 Ma; Dichiarante et al., 2016). This is consistent with the field observation that Group 3  
216 deformation fractures and mineralization are synchronous with the emplacement of ENE-trending  
217 lamprophyre dykes east of Thurso (ca. 268-249 based on K-Ar dating; Baxter and Mitchell, 1984).  
218 Stress inversion of fault slickenline data associated with the carbonate-pyrite-bitumen mineralization  
219 imply NW-SE regional rifting (Dichiarante et al., 2016), an episode also recognized farther west in  
220 the Caledonian basement of Sutherland (Wilson et al., 2010). Thus from St. John's Point to Cape  
221 Wrath (CW in **Fig. 3b**), Permian-age faults are the dominant brittle structures developed along the  
222 north coast of Scotland, forming part of a regional-scale North Coast Transfer Zone translating  
223 extension from the offshore West Orkney Basin westwards into the North Minch Basin (see  
224 Dichiarante et al., 2016).





225

226 In the present study, fracture attribute analyses were carried out in areas where Group 3 structures are  
227 dominant, or in locations where there is good field evidence that pre-existing Group 1 faults have  
228 undergone significant later reactivation synchronous with Group 3 age deformation. This approach is  
229 justified based on the fact that the Group 3 structures are the only set widely associated with syn-  
230 faulting mineralization and bitumen and have therefore clearly acted as fluid channelways in the  
231 geological past. There is also good evidence for the preservation of open fractures and vuggy cavities  
232 consistent with these fractures continuing to be good potential fluid-flow pathways at the present day.  
233 No such features are associated with Group 1 or Group 2 structures. Thus we argue that the Group 3  
234 structures are the best direct analogue for the oil-bearing fracture systems that occur in the Clair  
235 Group reservoir in the sub-surface.

236

#### 237 **4 Locations and orientation data from the 1D scanlines**

238 In the present study, 1D scanlines were performed at different scales in the Caithness area resulting  
239 in datasets from regional- (km scale, **Fig. 3b**) and sub-regional- ( $10^2$  m to dm scale, **Fig. 3c**),  
240 mesoscale (m to cm, **Fig. 3d**) and micro-scale ( $\mu\text{m}$ , **Fig. 3e**).

241

##### 242 **4.1 Regional- and sub-regional scale**

243 Scanline data have been collected at a regional scale (km-scale) using a tectonic lineament  
244 interpretation map created by Wilson et al. (2010). In their study, the lineament analysis was  
245 conducted at 1:100k scale extending from Lewisian basement outcrops in western Sutherland  
246 eastwards into the Devonian rocks of Caithness (**Fig. 3b**). We performed two scanlines (WTr1 and  
247 WTr2) trending orthogonally to the Brough-Risa Fault, the major N-S trending basin-scale fault in  
248 Caithness (**Fig. 3b**; Dichiarante et al. 2016). Scanline WTr1 intersects mainly NE-SW and NW-SE  
249 trending lineaments, while scanline WTr2 intersects mainly N-S and a few NE-SW trending  
250 lineaments (**Fig. 4a**). Although, datasets with few data points generally give poorly defined  
251 distributions on graphical presentations, it will be shown that the data from these two transects are of  
252 value in the multiscale approach adopted here.

253

254 At the sub-regional scale, scanlines have been performed on lineament maps produced from  
255 Google Earth satellite images at 1:1000 scale (pixel resolution c. 10 m). These datasets are limited to



256 well exposed wave-cut platforms on the coast because the flat topography and thick cover of drift has  
257 obscured the structures inland. The interpreted lineaments from the images were verified during  
258 fieldwork to be faults (large to mesoscale) and joints. The narrow width of the platform limits the  
259 analysis to only one scanline in each locality (DO at Dounreay, SJ at St. John's Point; see **Fig. 3c**).  
260 Fracture strikes and spacing measurements have been corrected using the Terzaghi's Correction (see  
261 dashed red and blue lines in the rose diagrams in **Fig. 4b-c**).

262

263 The scanline at Dounreay (DO) is NE-SW trending and intersected mainly NW-SE and NNE-  
264 SSW trending, with a subset of NE-SW lineaments (**Fig. 4b**). The scanline at St. John's Point (SJ)  
265 intercepts mainly ENE-WSW lineaments with subsets of N-S and NW-SE trending features (**Fig. 4c**).

266

#### 267 4.2 Mesoscale outcrops

268 Fracture data along six mesoscale scanlines were collected at three field localities: Brims Ness (BTr1,  
269 BTr2; **Fig. 4d, e**), Castletown (CTr1, CTr2; **Fig. 4f, g**) and Thurso (TTr1, TTr2; **Fig. 4h, i**) where  
270 there is very good exposure. In each outcrop, the position, direction and length of the scanlines were  
271 chosen with reference to the trend of the basin-scale master faults in each area (e.g. ENE-WSW at  
272 Castletown and NNE-SSW at Thurso and Brims Ness; **Fig. 4d-i**). At Castletown and Brims Ness, two  
273 scanlines were carried out to record the full range of fracture orientations: one parallel and one  
274 perpendicular to the master fault set. Scanlines at Thurso differ from the others because they are both  
275 measured parallel and next to a fault zone, resulting in higher values of fracture intensity (see TTr1  
276 and TTr2 in **Tab. 2**). These scanlines are also shorter (< 4m) and record exclusively thin veins. Each  
277 locality is characterized by one (e.g. Thurso) or more fracture sets (e.g. Castletown, Brims Ness).  
278 Where two sets of fractures are present, they generally intersect at high angles to one another and it  
279 was observed that they were active during the same geological event; hence they are analysed here  
280 as single population (Dichiarante, 2017).

281

282 Additionally, for each scanline, fracture termination type, kinematics and type of fractures  
283 were recorded (**Tab. 2**). Although fracture terminations are more usefully assessed in a 2D analysis,  
284 we recorded the nature of fracture branch terminations for each structure intersecting the transect line.  
285 These data are reported using a ternary plot (**Fig. 4j**) which shows there is no dominant fracture  
286 termination type. In general, the transects show intermediate to high connectivity, except for scanline  
287 TTr1, which shows a more isolated pattern.

288



289 4.3 Microscale scanlines

290 At microscales, one transect was performed on the oriented thin-section taken from sample SK04  
291 (inset in **Fig. 3e**, left). The fault rock was chosen after fieldwork analysis because of its large thickness  
292 of fault rock and micro-fractured appearance. Field observations also ensured that the age of this fault  
293 was the same as the other Group 3 structures analysed at different scales. The fault rock, from which  
294 the thin-section has been produced, is a typical example of a NE-trending fault with normal dextral  
295 oblique kinematics, filled with carbonate mineralization and red stained (hematite) sandstone-breccia  
296 of inferred Permian age (**Fig. 3e** left, see also **Fig. 5e**). The oriented thin-section was analysed under  
297 an optical microscope and spacing, aperture and the lengths of microfractures recorded. Photo-  
298 micrographs were merged and the scanline was measured orthogonally to the bounding NE-SW  
299 meso-fracture seen in **Fig. 3e**.

300

301 **5 1D fracture population results**

302 5.1 Fracture length - aperture data

303 MLE distribution fitting and KS tests were performed for all datasets and different types of  
304 distribution (exponential, log-normal, power-law). The recorded range values of trace length and  
305 aperture (or vein width) for each of datasets are shown in **Table 2**. In Table 3 and Table 4 in the  
306 Supplementary Data File, we report the MLE distribution fitting results for both non-truncated  
307 (exponential, log-normal and power-law distributions) and for truncated (power-law distribution)  
308 populations for trace length and aperture, respectively.

309 Length population datasets yielded values, rounded to the nearest order of magnitude, centred  
310 at ca.  $10^1$  m for the sub-regional scale,  $10^{-1}$  m at mesoscale and  $10^{-4}$  m at microscale (**Fig. 6a**). Aperture  
311 populations are centred between ca.  $10^{-3}$  m for the mesoscale dataset and ca.  $10^{-5}$  m for the microscale  
312 dataset (**Fig. 6b**).

313 The plots in **Fig. 6** give an insight into the relationship between cumulative  
314 frequency/intensity (inverse spacing), and length or aperture. For example, at the mesoscale (**Fig. 6b**  
315 centre), the intensity of fractures with  $> 25$  mm aperture is about  $0.03 \text{ m}^{-1}$  corresponding to a 34 m  
316 spacing. Similarly, the intensity of fractures with  $> 0.4$  mm aperture is between  $0.45 \text{ m}^{-1}$  and  $11.2 \text{ m}^{-1}$   
317  $^1$  corresponding to 8.9 cm to 2.2 m spacing, respectively. At microscales (**Fig. 6b** left), the intensity



318 of fractures with  $> 2.9 \cdot 10^{-5}$  m aperture is about  $155.51 \text{ m}^{-1}$  corresponding to 6 mm spacing whilst the  
319 intensity of fractures with  $> 3.9 \cdot 10^{-6}$  m aperture is about  $1555 \text{ m}^{-1}$  corresponding to a 0.64 mm spacing.

320 To examine the possible influence of mechanical stratigraphy on fracture scaling across the  
321 Orcadian Basin in Caithness, we indicate on the fracture size plots, selected sedimentary unit  
322 thickness values reported in previous studies (Fig. 8a). These include sedimentary laminae thickness  
323 (0.3 mm) at microscale, bedding-range thicknesses of the Lower Stromness Formation (20 cm to 5  
324 m) at mesoscale, and thicknesses of the Ham-Scarfskerry and Latheron Subgroups at sub-regional  
325 scales (data from the in Andrews et al., 2016). Also, the approximate boundary between faults that  
326 can be imagined in seismic reflection images and smaller-scale structures is shown in Fig. 8a (yellow  
327 arrows) based on well-known empirical displacement-length relationships (a 10m displacement  
328 corresponding to a length of ca 100m following Kim and Sanderson, 2005).

329

### 330 *5.1.1 Analysis of uncertainties: validity of data populations and reliability of best-fit distributions*

331 In any statistical analysis, the sampled population should be large enough to give a statistically  
332 acceptable representation of the population and to properly determine the distribution type and its  
333 parameters (Bonnet et al., 2001). The samples sets are statistically valid for most samples after the  
334 first 20 measurements (grey area in Fig. 7) because the cumulative fracture intensity of the population  
335 data and its standard deviation (black and green curves, respectively) become reasonably stable. The  
336 uncertainty in the cumulative fracture intensity reduces progressively towards the end of the scanline.  
337

## 338 **6 The scalability of fracture attributes**

### 339 6.1 Slope determination –MLE approach

340 The complete (non-truncated) populations show that a log-normal distribution best describes the data  
341 as they show consistently high percentage fitting values. However, the choice of the best-fit  
342 distribution should not be based on the complete population because the distribution tails  
343 (corresponding to the largest and smallest size fractures) are biased (see also Supplementary Data  
344 File). We therefore also investigated progressively truncated populations in order to validate the  
345 hypothesis. The fitting results for complete log-normal and truncated power-law datasets are  
346 generally similar (see Supplementary Data Files), suggesting that either type of distribution can  
347 successfully describe the size attribute data.



348

## 349 6.2 Multiscale analysis

350 Trace length distribution data from all transects have been normalised using the sample line length  
351 and are displayed together on a single population plot (**Fig. 8a**) which enables us to assess scaling  
352 over 8 orders of magnitudes ( $10^{-4}$  to  $10^4$ ). The grey region in **Fig. 8a** shows that the multiscale data  
353 can be described by a power-law distribution with overall scaling coefficient close to a slope of -1  
354 centred on a 1 m length fracture with a 1 metre spacing. This power-law distribution implies fractal  
355 or self-similar behaviour of the length parameter over 8 orders of magnitudes which effectively means  
356 that the fracture array maintains the same statistical properties of intensity and length at all scales  
357 assessed here.

358

359 The aperture datasets collected in the meso- and micro-scale transects are also shown on a  
360 single population plot (**Fig. 8b**) and show evidence for an overall power-law scaling over 4 orders of  
361 magnitude ( $10^{-6}$  to  $10^{-2}$ ) also with a coefficient slope of -1. However, the best-fit line is centred on a  
362 1 mm wide fracture with a 1 metre spacing. This overall slope is indicative of a fractal distribution or  
363 self-similar behaviour of the aperture parameter over 4 orders of magnitude which means that the  
364 fracture array maintains the same relationship between intensity and aperture at all scales assessed  
365 here.

366

367 Length attributes for regional faults extend over the estimated thickness of the Devonian rocks  
368 in Caithness by Donovan (1975) as shown in **Fig. 8a** (dashed red line). Although Andrews et al.  
369 (2016) did not report an exact estimate of thickness for the entire Devonian sequence, they suggested  
370 that the thickness reported in Donovan (1975) was overestimated.

371

## 372 6.3 Length-Aperture correlations

373 Trace length and aperture or vein width data are plotted side by side to illustrate the positive  
374 correlation between these attributes over 4 orders of magnitude (**Fig. 8c**). A linear scale length vs.  
375 aperture scatterplot in **Fig. 9a** shows that the data are clustered towards the origin, reflecting the  
376 greater frequency of smaller fractures expected for a power-law distribution (Vermilye and Scholz,  
377 1995). The plot of logarithmic length vs logarithmic aperture in **Fig. 9b** shows two clusters of data  
378 which correspond to the mesoscale population (larger datasets in the centre of the figure) and the  
379 microscale population (bottom left dataset). Small aperture mesoscale data are poorly resolved,



380 plotting at either 0.01 or 0.05 mm due to the effect of using the thickness comparator in the field. In  
381 the distribution plots, this artefact is removed conventionally by only plotting the highest cumulative  
382 frequency for each aperture value. In contrast, however, in the aperture vs. length plot each individual  
383 data point of the cloud is statistically equally important, although this results in increased uncertainty  
384 at lower aperture values. The logarithmic plot for veins only (triangles in Fig. 9b) shows a clear  
385 positive power-law correlation between aperture and length, has less pronounced artefacts and  
386 permits an appraisal of the relationship between these two parameters. Line fitting methods suggest  
387 a slope of 0.65 or larger with a  $R^2$  of 0.75 (red line in Fig. 9b) for all fracture data in this study. A  
388 comparison of veins (triangles) with other fractures including joints (grey dots in Fig. 9b) might  
389 further suggest that veins tend to be shorter for any given aperture.

390

## 391 7 2D population analysis

392 The 2D analysis was conducted at sub-regional scale on a bathymetric map from the near offshore  
393 (Fig. 10a) and on the mesoscale using a photograph of a large rock pavement outcrop (Fig. 10b) to  
394 provide quantitative assessments of fracture connectivity and self-similarity. The offshore data  
395 provides access to a much larger area compared to onshore, however, the nature of the fractures  
396 themselves can only be constrained by extrapolation from adjacent onshore exposures. We chose to  
397 perform 2D analysis on these areas for two main reasons. First, both contain large numbers of  
398 fractures spread over a large plan view area and therefore were most likely to provide a statistically  
399 meaningful analysis using different 2D methods (e.g. circular scanline windows and box counting).  
400 Second, the difference in size between the two areas gives an insight into to fracture scaling  
401 properties. The fracture interpretation of the bathymetric image enabled analysis of the fracture length  
402 distribution for comparison with the 1-D results, and a topological fracture network analysis of the  
403 fracture nodes.

404

### 405 7.1 2D sampling locations and fracture orientations

#### 406 7.1.1 Bathymetry map

407 The bathymetry map used for this study is a high-resolution multibeam dataset provided by MeyGen  
408 Ltd (IXsurvey Ltd, 2009) in the area between St. John's Point and Stroma Island where the Devonian  
409 rocks are exposed on the sea floor which has been washed clean by the action of strong water currents  
410 (Fig. 10a, raw images in Supplementary Data File). Interpreted faults from the bathymetric data show



411 ENE-WSW and NNW-SSE orientations. ENE-WSW trending faults dominate in this region (see SJ  
412 rose diagram in **Fig. 4a**) and show “corridor-like” arrays. The orientations of these faults are  
413 comparable to the two main fault sets seen onshore in locations such as St. John’s Point (**Fig. 4c**).  
414 NNW-SSE trending faults are regularly spaced (100 to 200 m) in the central part of the area, while  
415 the ENE-WSW trending faults are present across the entire survey. The latter set show two different  
416 spacing values: less than 100 m for the shorter structures and about 1000 m for larger structures.

417

#### 418 7.1.2 Brims Ness pavement photograph

419 A similar 2D analysis was carried out using a mesoscale photograph taken at Brims Ness (location in  
420 **Fig. 3b** and raw image in Supplementary Data File). Distortion effects were minimized by analysing  
421 a single photo taken orthogonally to the outcrop pavement and by conducting the analysis in a circular  
422 area to avoid edge distortions. The photo shows three different sets of fractures: N-S, NE-SW and  
423 WNW-ESE trending (**Fig. 10b**). The N-S and NE-SW trending structures form the majority of the  
424 fractures. Most fractures have straight traces and crosscut each other. Three larger WNW-ESE and  
425 NNE- to NE-trending faults were detected. A single curved WNW-ESE trending fault was also  
426 identified (**Fig. 10b**).

427

#### 428 7.2 Fracture topology results and fracture connectivity

429 The bathymetric topology is comprised of 698 I-, 123 Y- and 117 X-nodes, respectively (yellow, cyan  
430 and red squares in **Fig. 10a**) whilst the outcrop topology is composed of 916 I-, 240 Y- and 202 X-  
431 nodes, respectively (yellow, cyan and red squares in **Fig. 10b**).

432

433 I-type nodes are regularly distributed in the area while Y- and X-type nodes mainly occur in  
434 the central part of the bathymetry map, where longer ENE-WSW trending faults occur (**Fig. 10a**). X-  
435 and Y-type nodes, which contribute most to connectivity of the 2D system, are mainly localized where  
436 the ENE-WSW trending faults crosscut NNW-SSE trending structures.

437

438 The number of connections per line ( $n_{C/L}$ ) and number of connections per branches ( $n_{C/B}$ )  
439 are respectively 1.18 and 1.1 for the bathymetry image, and 1.53 and 1.22 for the outcrop analysis  
440 (on a scale value between 0 and  $\infty$  for  $n_{C/L}$  and between 0 and 2 for  $n_{C/B}$ ). This indicates low overall



441 connectivity for the fracture systems exposed in 2D. The  $n_{C/L}$  is also shown in a ternary I-Y-X plot  
442 (inset in the bottom left of **Fig. 10** a and b).

443

444 For the bathymetry dataset, the nodal density map shows that the large majority of nodes are  
445 aligned along a series of ENE-WSW trending faults (**Fig. 11a-b** top). The density map shows that Y  
446 and X-nodes are mainly associated with NNW-SSE trending faults and are responsible for producing  
447 most of the connectivity of the system (**Fig. 11a-b** bottom).

448

### 449 7.3 Assessing self-similarity on 2D maps

450 Circular scanlines were performed to investigate the connectivity of specific smaller areas of the  
451 fracture network on the bathymetry map and mesoscale outcrop photograph (44 and 22 circular  
452 scanlines carried out, respectively – see **Fig. 12**). Circular scanline windows of three different  
453 diameters were used. The numbers of X-, Y- and I-nodes for each scanline are plotted in the ternary  
454 diagrams: blue for small, orange for intermediate and green larger scanlines. The data generally  
455 spread out from the centre of the ternary plot (**Fig. 12a** right and **Fig. 12b** right) and the overall data-  
456 spread is clearly unrelated to the size of the performed scanlines.

457

458 Box counting methods were performed in the red-boxed areas shown in **Fig. 12** at the  
459 mesoscale and regional scale to assess whether the self-similarity in the length and intensity attributes  
460 observed in 1D transects are present in fracture patterns in 2D. (**Fig. 12a-b**). The normalized  
461 population plot shown in **Fig. 12c** shows a self-similarity over 1 order of magnitude for both the  
462 bathymetry dataset (**Fig. 12c**, red) and for the mesoscale dataset (**Fig. 12c**, blue). Best-fit exponent  
463 coefficients were obtained using the box counting method plots performed at the two different scales  
464 of analysis: -1.77 for the outcrop photograph and -1.81 for the bathymetry map (**Fig. c**). Both best-fit  
465 curves yielded  $R^2$  values of 0.99. The almost identical slopes of ca -1.8 show that the 2D spatial  
466 distribution of fractures sampled at the two different ranges of scale, almost three orders of magnitude  
467 apart, is the same within the resolution of the box-counting method.

468





## 469 8 Discussion

### 470 8.1 Self-similar fault and fracture scaling

471 Fracture attribute analyses are often conducted on field outcrop analogues because they can provide  
472 useful information to bridge the gap between faults imaged in geophysical datasets (e.g. seismic  
473 reflection profiles) and fractures observed in borehole data. Our findings show that although  
474 individual datasets - particularly at the mesoscale - are best described by a log-normal distribution,  
475 this may be the result of sampling bias (incomplete sampling, as discussed in Section 2.1.1). Analysis  
476 of truncated populations shows that a power-law distribution can provide an equally representative  
477 description of the data. Our results suggest that obtaining an unequivocal power-law fit at a given  
478 scale is difficult to achieve because the data may not range over more than 1-2 orders of magnitude.  
479 However, when our data were combined from microscale to regional scales, a self-similar (power-  
480 law) distribution of fracture aperture and trace length attributes emerges over 4 and 8 orders of  
481 magnitudes, respectively (**Fig. 8c**). We suggest that the slope variability observed in individual  
482 datasets could result from variation due to local factors such as the presence of damage zones, zones  
483 of intense strain or sampling bias. Thus this multi-scale approach can help to reduce the influence of  
484 any single dataset and the approach overall can help to reduce uncertainty in assessing the scaling of  
485 attributes over a large scale range. If we are correct, then it implies that, at different magnifications  
486 (or scales), the dataset structure remains much the same so that the statistical properties can be  
487 interpolated to other scales within that range. If present, mechanical stratigraphy at different scales is  
488 known to affect the aspect ratio of faults, limiting their vertical size and increasing layer-parallel  
489 growth; strata-bound fault distributions are log-normal (e.g. Olson, 2007, see Section 2). Known  
490 mechanical stratigraphic boundaries for Devonian rocks in Caithness relative to individual datasets  
491 are included in **Fig. 8a** (e.g. cm scale beds at mesoscale), but they do not seem to affect the distribution  
492 plots, suggesting that it is not unreasonable to use power-law distributions to describe these data. We  
493 note that whilst individual fracture datasets show considerable variability in their slopes (see e.g. **Fig.**  
494 **6**), over larger scale ranges, data align well along a slope of approximately -1 (see **Fig. 8**) with the  
495 same abscissa (intensity) intercept. Previous studies (Odling et al., 1999) on comparable Devonian  
496 basins have also demonstrated this type of self-similar scaling, although individual datasets show  
497 considerable variability. They investigated fracture length over many orders of magnitudes (1 cm to  
498 1 km) from the Devonian sandstones in the Hornelen Basin (Norway) and showed that, while  
499 individual datasets show log-normal distributions, the collective datasets are reasonably well  
500 described by a power-law distribution.



501

502 We recognise that caution should be applied when using datasets acquired at a given scale to  
503 estimate a fracture attribute on other scales. Censored data might bias the choice of distribution  
504 function that best-fit the data suggesting that log-normal may seem more appropriate even when this  
505 is not the case in reality. However, by extending the scale observation (i.e. by applying a multiscale  
506 approach), we reduce the potential effects of censoring, truncation and variability due to individual  
507 datasets on the overall result and also extend the estimation range for the size parameters such as  
508 length, aperture and intensity. The multiscale approach, together with the analysis of truncated  
509 populations, has enabled us to be more confident in concluding that both single- and multi-scale  
510 populations follow a power-law distribution.

511

512 Although, our result remains to be tested with more datasets, the positive correlation we observe  
513 between aperture and length (**Fig. 9**) can provide a basis for a good estimation of frequency and  
514 fracture attributes for large scale (regional) fractures (see next section). The scaling exponent (0.65)  
515 is consistent with recent work that suggests that sub-linear scaling (exponent <1) results when  
516 fractures have grown large enough to be segmented and fracture length increase becomes inhibited  
517 by interactions between segments (see Mayrhofer et al. 2019).

518

## 519 8.2 Applications to offshore fractured reservoirs

### 520 8.2.1 Fracture morphology, apertures and fills

521 Most of the fracture apertures measured during the onshore study in the Orcadian Basin in Caithness  
522 are partially to completely filled with either fault rocks, hydrothermal minerals or bitumen; a range  
523 of filling morphologies are preserved (**Fig. 5a-e**). It is reasonable to assume that wholly bitumen-  
524 filled fractures can be viewed as being equivalent to open fractures in a sub-surface reservoir (**Fig.**  
525 **5a, b**), whilst other veins may be completely filled with minerals/fault rock (lacking bitumen) or  
526 partially filled with hydrocarbon held either in vuggy cavities (**Fig. 5c**), fractured mineral fills (**Fig.**  
527 **d**) and/or porous sediment fills (**Fig. 5e**). There are many examples of partly or fully open fractures  
528 in the surface coastal exposures of the Orcadian Basin, but it is difficult to prove whether or not  
529 surface weathering and seawater washing of coastal outcrops has not removed pre-existing fracture  
530 fills. This is supported by the observation that fracture-hosted bitumen fills are most widely preserved  
531 in recently exposed quarry or excavation sites inland (e.g. see Dichiarante et al., 2016).



532 Dichiarante et al. (2016) presented textural evidence showing that fracture-hosted calcite,  
533 sulphides and oil fills are broadly contemporaneous. Open vugs and fractures are almost certainly  
534 only preserved due to hydrocarbon flooding which shuts down the further precipitation of carbonate  
535 and sulphide in open or partially open fractures/veins (e.g. **Fig. 5b-e**). Observations from the Clair  
536 Field cores by Holdsworth et al. (2019) reveal similar associations between fractures filled, or  
537 partially filled, with similar hydrothermal minerals, younger porous sediment and hydrocarbons. This  
538 suggests that despite differences in source rocks (local Devonian onshore vs. more distant Jurassic  
539 offshore), the Orcadian Basin fracture fills and apertures are a good analogue for the fractured rocks  
540 of the Clair Group.

541

542 It is also important to realise that fracture fills of the kind seen in Caithness are not always bad  
543 for the hydrocarbon potential of a fractured reservoir. Wall rock fragments (**Fig. 5b**), early fracture-  
544 hosted hydrothermal minerals (**Fig. 5c,d**), and fills of younger porous sediment all have the ability to  
545 act as natural proppants that hold fractures open in the long term and counteract the tendency for the  
546 present day stress field to close open fracture networks in sub-surface reservoirs (**Fig. 5a**; Holdsworth  
547 et al. 2019, 2020). These fracture fills will however reduce permeability dramatically from the ‘cubic  
548 law’ relationships of ideal parallel-sided open fractures (Nelson, 1985, Laubach, 2003).

549

### 550 8.2.2 1D prediction for reservoir volumetrics

551 Our approach allows us to provide an illustration of how the fracture scaling relationships established  
552 onshore can be applied as a calibration curve for off-shore reservoirs such as in the Clair Field (**Fig.**  
553 **13**). Published data from Coney et al. (1993) identified three systems of fractures spaced at 30 – 35 m,  
554 100 – 200 m and 1 - 1.5 km hosted in the Clair Group sequences. These scale-ranges are plotted on  
555 the analogue Caithness 1D scaling curves in **Fig. 13**, as a predictor of fracture sizes such as length or  
556 aperture (light grey regions) that might be encountered in a well. Predicted lengths for the spacing  
557 values (inverse of fracture intensity) obtained by Coney et al. (1993) fall in the range of regional to  
558 sub-regional fractures in Caithness, with values of 30 – 60 m length (for fractures with 30 – 35 m  
559 spacing), 100 – 150 m length (for fractures of 100 – 200 m spacing) and 1 – 2 km length (for fractures  
560 with 1 - 1.5 km spacing). Values of aperture can similarly be estimated. Values of 30 – 35 m spacing  
561 have been also measured in our field analogue permitting estimated apertures of about 3 to 3.5 cm.  
562 For larger spacing faults (more than 100 m), values of aperture or fault width can be extrapolated by



563 extending the slope obtained for smaller scales (light grey area in **Fig. 13**). For example, for faults  
564 spaced 100-200 m and 1-1.5 km, average aperture or fault width is estimated to be 10-20 cm and 1-  
565 1.5m, respectively (light yellow lines in **Fig. 13**). Despite the uncertainties (of 1 to 2 orders of  
566 magnitude) associated with the estimates made here, it is important to note that these larger faults are  
567 likely to only be partially open in the sub-surface (Laubach, 2003). Nevertheless, a 14 cm wide open  
568 fracture was recognized in the core well 208-8 from the Clair Field (Franklin, 2013).

569

### 570 8.2.3 2D prediction of permeability distribution

571 The analysis of 2D datasets using the nodal counting method has shown low connectivity for the  
572 overall systems due to the dominance of I-type nodes compared to Y- and X-type nodes (see ternary  
573 plot in **Fig. 10a** and **b**). Regions of relatively higher connectivity are localized at the intersection  
574 between larger and smaller structures or in “corridor”-like arrays (**Fig. 11a-5** and **Fig. 11b-5**).  
575 However, disconnected fractures in 2-D may be connected in 3D and the connectivity density maps  
576 (X- and Y-type nodes) therefore represent a *minimum* estimate of the real 3D connectivity of the  
577 system. A future development of the 2D methodology should be to combine the nodal analysis with  
578 aperture values to produce “weighted” density maps and ternary diagrams. This approach could  
579 provide more realistic values for connectivity flow characteristics of the fracture network.

580

581 The increase in connectedness is specific to certain areas of the fracture network (e.g. fracture  
582 “corridors” at sub-regional scale or longer structures at mesoscale). Our findings suggest that large  
583 fractures (faults) will form wide damage zones where there is interaction/intersection between  
584 structures. Correlated with this spatial clustering, we should expect large variability in fluid transport  
585 within the 2D network. If we consider that the spacing between adjacent fracture corridors is about  
586 1 km on the bathymetry map and that from our analogue data the width of similarly spaced corridors  
587 is approximately 10 m, we would predict focused fluid-flow along these structures.

588

589 An orientation analysis of fracture intersections has been carried out for onshore faults and  
590 fractures data at St. John’s Point (**Fig. 14a**, Dichiarante, 2017), based on its proximity and geological  
591 similarity to the area covered by the bathymetric map which lies immediately offshore (**Fig. 10a**). A  
592 similar plot is also shown for all the faults and fractures data collected in Caithness (**Fig. 14b**,  
593 Dichiarante, 2017). Both datasets show consistent best-fit intersections that are sub-vertical to steeply  
594 plunging to the east, 73/084 and 78/098, respectively (yellow diamonds in the stereonet in **Fig. 14a-  
595 b**). The combination of the connectivity information in plan-view derived from the bathymetry map



596 and the fracture dip information derived from fieldwork shows that fracture corridor structures and  
597 fracture intersections will be useful in constraining the main fluid-flow direction that should to be  
598 considered when developing the most effective drilling strategy. In general, the calculated steeply  
599 plunging fault/fracture intersections would seem to favour horizontal drilling as opposed to vertical  
600 drill orientations (**Fig. 14c**).

601

602 In the analogue bathymetric map dataset (**Fig. 10a**), we observed 1D spacing ranges similar  
603 to those observed by Coney et al. (1993) for the Clair Field. We recognize 100 – 200 m spacing for  
604 NNW-SSE trending faults and less than 100 m and 1 km for ENE-WSW trending faults. The  
605 spacing/intensity values seem to confirm that the Devonian in Caithness is a good analogue for the  
606 Clair Field. Connectivity results from the bathymetry data have shown that these fractures are locally  
607 well-connected in plan-view (**Fig. 11a-5**) and scanline analysis results have shown that these fractures  
608 are potentially permeable with (kinematic) apertures of about  $10^{-1}$  m to 10 m producing, in the latter  
609 case, “corridors of partially open fractures” where these are clustered. These localized regions are  
610 believed to provide most of the connectivity of the 2D system and fluid-flow, which is consistent with  
611 the distribution of mineralization observed in the field along corridor-type structures (e.g. the White  
612 Geos Fault locality described by Dichiarante et al., 2016).

613

614 Our study shows that a multiscale 1D and 2D data analysis of the Orcadian Basin is a useful  
615 analogue to aid understanding the fracture-dominated fluid-flow patterns in a sub-surface reservoir  
616 (Clair Field). The relationship between aperture and fracture size (e.g. length) is known to have a  
617 major impact on fracture rock permeability (Odling et al., 1999 and references therein). Our  
618 mesoscale description of this relationship together with the multiscale constraint on the 1D fracture  
619 sizes distributions enables us to estimate the kinematic aperture of the largest fractures in the analogue  
620 system even though we have not sampled them directly. The 1D fracture size analysis is extended by  
621 the 2D approach that captures fracture interaction, clustering and connectivity to describe map-scale  
622 spatial variability of the system. These relationships can be directly applied to the Clair Field and  
623 other equivalent sub-surface reservoirs by calibrating the fracture size populations from drill core and  
624 image log data, the spatial properties from seismic attribute data, and the fracture fills from core  
625 description.

626 A similar methodology may be applied in geological contexts ranging from hydrocarbon  
627 exploration, geothermal reservoir analyses, carbon capture and deep radioactive waste disposal  
628 facilities (e.g. see Pastoriza et al. in review). The straightforward multiscale approach allows direct



629 comparison between analogues and sub-surface targets and is easy to apply to different areas, dataset-  
630 types and scales to provide important constraints for reservoir modelling and prediction at regional  
631 scales.

632

## 633 9 Conclusions

634 The orientation of fluid conductive faults at basin scale, together with their spacing and connectivity  
635 is crucial to understanding the geometries and fluid-flow characteristics of a sub-surface reservoirs.  
636 Statistical analysis of fracture attributes from suitable outcrop analogues can provide reliable and  
637 robust qualitative (geological) and quantitative (attribute information and scaling) information which  
638 can be used in the design and conditioning of reservoir simulation models.

639

640 The Devonian rocks of the Orcadian Basin in Caithness provide a direct analogue for the main  
641 reservoir in the Clair Field and other equivalent offshore fractured reservoirs hosted in similar tight  
642 sandstone strata. The methodology used here represents an alternative to the use of single-scale  
643 datasets in fracture characterization. We advocate an extended approach that integrates datasets  
644 collected at different scales and combines 1D and 2D analysis. The statistical analysis provides a  
645 useful insight into the nature and scalability of the natural fracture networks. Specifically:

- 646 - Our 1D analysis has shown that the population distribution of length and aperture of the  
647 onshore datasets may be represented using a truncated power-law distribution.
- 648 - The multiscale approach shows scale-invariance. The scalability of single dataset can be  
649 extended from 1-2 orders of magnitude (single plots) to up to 4 and 8 orders of magnitudes  
650 (side by side plots) for aperture and trace length, respectively. This illustrates the effectiveness  
651 of the multiscale approach (**Fig. 8**).
- 652 - The positive correlation between vein aperture and length is well represented by a power-law  
653 distribution over 4 orders of magnitude. Although, this remains to be tested with more  
654 microscale datasets, we suggest that this methodology might provide a good estimation of  
655 frequency and fracture attributes for large scale (regional) fractures (**Fig. 9b**).
- 656 - A comparison with published datasets (Devonian Old Red Sandstones in the Hornelen Basin  
657 and seismic data from the North Sea) reveals similar power law -1 slope coefficients to the  
658 one obtained during the present study in Caithness.

659



660 An associated topological 2D analysis has provided the following additional insights:  
661 - The overall connectivity of the 2D system is low and very similar on the two scales of  
662 observation studied (ternary plots **Fig. 10a** and **b**).  
663 - However, connectivity is highly variable in the system and appears to be mainly associated  
664 with corridor-like structures (e.g. bathymetry map) at a large scale (**Fig. 11a-5**) and on longer  
665 structures at the mesoscopic outcrop scale (**Fig. 11b-5**). This is particularly important when  
666 considering the fluid transport properties of the system.  
667 - Box counting methods have shown the self-similarity of fracture analysis over about 1 order  
668 of magnitude for at bathymetry- and outcrop-scales. The datasets have almost identical slopes  
669 showing that the fracture arrays over different scale ranges have the same 2D spatial  
670 distribution (**Fig. 12c**).

671

672 Compilations of onshore fracture data show a regional predominance of sub-vertical fault  
673 intersections (3D). This suggest that a horizontal drilling strategy would be favoured were these rocks  
674 to be drilled as a reservoir. The combination of 2D connectivity density maps (plan view) with dip  
675 information derived from onshore structures helps constrain the likely optimal fluid-flow locations  
676 and directions.

677

678 Our study demonstrates how a comprehensive and multiscale approach to analogue outcrop  
679 studies may provide a better understanding of the 1D size distribution of fracture networks and map  
680 view variability of fracture networks in an analogue system and how it may be applied to a fractured  
681 reservoir in sub-surface locations.

682

### 683 **Data availability**

684 Fracture data and results of topological analysis are available at [doi:10.15128/r1cv43nw819](https://doi.org/10.15128/r1cv43nw819)

685

### 686 **Author Contributions**



687 AD designed and conducted the research, interpreted the data and prepared the manuscript. KM  
688 assisted with data analysis and manuscript preparation. RH designed the study and assisted with  
689 manuscript preparation. TB assisted with data analysis, ED assisted with data collection and analysis.

690

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695

#### 696 **Supplement**

697 A supplementary data file containing the statistical method and images used in the analysis is  
698 available at <http://xxxxxxxxxxxxx>.

699

#### 700 **Competing Interests**

701 The authors declare that they have no conflicts of interest.

702

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## 869 FIGURES

870 **Fig. 1:** (a) Synthesis of 1D and 2D methodologies to estimate fracture attributes: (i) scanline sampling  
871 (or transect), (ii) window sampling, (iii) circular scanline window and (iv) box counting method  
872 (modified after Zeeb et al., 2013).  $L$  = box counting size,  $l$  = box size grid. (b) Schematic illustration  
873 of fracture attributes measured along a scanline (or transect). Fractures are represented as straight  
874 lines differently orientated to the scanline AB. Termination types are defined as X for cross-cutting  
875 relationship, Y for abutment of a fracture and I for isolated fracture (or termination against a  
876 lithological boundary). (c) Graphical representation of the Terzaghi's Correction, consisting of  
877 multiplying the scanline spacing  $S_i$  by the sine of the angle  $\alpha$  between the main trend of the fractures  
878 and the scanline (after Mäkel, 2007).

879 **Fig. 2:** Population distribution plots for (a) exponential (linear-logarithmic axes), (b) log-normal  
880 (logarithmic-linear axes) and (c) power-law (logarithmic-logarithmic axes) distributions with relative  
881 best-fit equations (top) and sketch of physical meaning (bottom). In the distribution plots, datasets  
882 are shown as black diamonds and typical best-fits are shown as red dashed lines. (d) Examples of  
883 density maps showing higher connectivity where Y- and X-nodes occur, (e) ternary plots showing  
884 that the overall system shown in Fig. d is isolated and (f) self-similarity plot method from **Fig. 1a**  
885 (iv).

886 **Fig. 3:** (a) Location map of the North Sea with the outline of the Orcadian Basin (light blue area). (b)  
887 Schematic geological map of the North Scotland showing the interpreted fault lineaments by Wilson  
888 et al. (2010) and the trace of the regional scale transects (WTR1 and WTR2) and the location of the  
889 sub-regional transects (DO and SJ). (c) Example of Landsat aerial image showing the trace of the  
890 sub-regional scale transect at Dounreay (DO). (d) Oblique view of the platform at Castletown. The  
891 meter ruler shows the trace of the transect CTr1 (mesoscale). (e) Outcrop photograph of the NE-SW  
892 fault zone where the sample for the thin-section SK04 was collected (yellow star), thin-section  
893 photograph (top) with an example of one of the microphotographs showing one fracture (right). The  
894 trace of the scanline is shown by a continuous red line and a reference line is shown in blue. CW =  
895 Cape Wrath, GGF = Great Glen Fault, fr = fracture, SK = Scarfiskerry.

896 **Fig. 4:** Rose diagrams of fracture orientation data for the transects at (a) regional scale, (b,c) sub-  
897 regional scale and (d - i) mesoscale. Note that the transect strike is corrected for the transects at sub-  
898 regional scale (dashed blue lines in rose diagrams). (j) Ternary plot providing an estimation of the



899 different type of fracture branches intersecting each transect.  $N$  = number of fractures,  $MAX$  =  
900 maximum,  $CI$  = 95% confidence interval.

901 **Fig. 5:** (a) Diagram summarizing how the present day aperture of a fracture is related to its  
902 morphology, aperture and fill and the general influence of present day stress. (b-e) Different fracture  
903 aperture and fill types associated with oil in the Orcadian Basin. (b) Photomicrograph of open fissure  
904 with oil fill and wall rock fragments, Thurso Bay foreshore; (c) photomicrograph of partial calcite fill  
905 with vuggy oil fill, Dounreay; (d) photomicrograph of oil-filled brecciated calcite in dilational jog,  
906 Dounreay; (e) Outcrop photo of calcite and red sandstone fill of inferred Permian age, Scarfiskerry  
907 foreshore (see Fig 3). All thin sections are taken in plane polarized light, with scale bar = 1mm.

908 **Fig. 6:** Cumulative distribution plots of (a) fracture and fault trace length for transects at (left)  
909 microscale, (centre) mesoscale and (right) sub-regional scale and (b) aperture and vein width for  
910 transects at (left) microscale, (right) mesoscale. On the plots reported stratigraphic layer thicknesses  
911 are shown as grey boxes. The Ham-Skarfiskerry Subgroup (177m) and the Latheron Subgroup (114m)  
912 from Anders et al. (2016) are shown on the sub-regional scale plot, The Lower Stromness Flagstone  
913 (5m) on the sub-regional scale and mesoscale plots. At mesoscale plot the average thickness of beds  
914 (c. 20cm) is also plotted. On the microscale plot, the thickness of individual laminae (c. 0.3mm) is  
915 shown. Dashed lines and number refer to values discussed in text.

916 **Fig. 7:** Fracture intensity and standard deviation as function of fracture number for (a) sub-regional  
917 scale, (b) mesoscale and (c) microscale transects. Fracture intensity is unstable for a relatively small  
918 number ( $< 20$ ) of detected fractures (grey area).

919 **Fig. 8:** Cumulative frequency plots of (a) fracture length and (b) fracture aperture. (c) Side by side  
920 population distribution plots of length (right side of the plot) and aperture (left side of the plot). Note  
921 that the distance between the datasets in different localities (down to mesoscale) represents the  
922 relationship in terms of order magnitude between aperture and length.

923 **Fig. 9:** (a) Length vs. aperture scatter plot and (b) Log of length vs. log of aperture for veins (triangles)  
924 and other structures (circle). Linear regression for veins on logarithmic plot is shown (dashed red  
925 line).

926 **Fig. 10:** (a) 2D analysis of bathymetric data from the area between St. John's Point and Stroma Island  
927 with lineament interpretation and I-, Y- and X-nodes, rose diagrams of lineaments and ternary plot of



928 node-types proportions. b) 2D analysis of outcrop pavement photograph with lineament interpretation  
929 and I, Y and X nodes and ternary plot of node-types proportions. MAX = maximum density.

930 **Fig. 11:** Lineament and density maps of nodes for (a) the bathymetry fault network and (b) the fault  
931 network in pavement. All nodes density map (top) Y, X- type nodes density map allowing a  
932 qualitative assessment of connectivity (bottom).

933 **Fig. 12:** (a left) 2D topological map of bathymetric data and (b left) 2D topological map of outcrop  
934 pavement photograph showing box counting area and example of performed circular scanlines.  
935 Ternary plots of circular scanlines performed on (a right) bathymetric data and (b right) outcrop scale  
936 photograph. Note in the ternary plot from the bathymetry data the 22 circular scanlines resulted in 16  
937 distinct proportions of I-, Y- and X- nodes. Box counting method applied to (c) bathymetric data and  
938 (d) outcrop scale photograph. (e) Logarithmic-logarithmic scale plot showing the result obtained from  
939 the maps in d and e. Data are normalized by box size and number of fractures.

940 **Fig. 13:** Sketch of the side by side population distribution plots of fracture lengths and apertures from  
941 Fig. 6. The dark grey areas represent the region where all the aperture (left) and length (right) plots  
942 are localized. Coloured lines represent the distributions at each scale. Orange horizontal lines  
943 represent the reported spacing values for Clair (Coney et al., 1993) and yellow vertical lines represent  
944 the relative estimated aperture values using trends from this study. Note that we extrapolate the  
945 aperture (light grey area) with the slope derived from the microscale and mesoscale datasets.

946 **Fig. 14:** Lower hemisphere equal area projections of measured offshore data at (a) St. John's Point  
947 and (b) Caithness. (c) Schematic block diagram created by combining offshore 2D density map of  
948 connectivity and onshore dip values. Note that the best-fit of faults and fractures data collected  
949 onshore at St. John's Point (yellow diamond in the top stereonet) is consistent with the best-fit of  
950 fault and fractures data collected in Caithness (yellow diamond in the bottom stereonet, Dichiarante,  
951 2017). MAX = maximum density, MEAN = mean density.

952 **Table 1:** Basic parameters, definitions and equations provided by 1D and 2D methods (Zeeb et al.,  
953 2013 *modified*)

954 **Table 2:** Transect data. GPSs = GPS position of the starting point,  $N$ = total number of sampled  
955 fractures,  $J$ = joint,  $V$ = vein,  $FnI$ = Fracture without infill,  $T$ = tensile,  $Dx$ = dextral,  $Sn$ = sinistral,  $I-I$  =  
956 "isolated branch", delimited by two I-nodes.  $I-Y$  and  $I-X$  = "singly connected" branches, delimited by





957 one I-node and one Y or X-node.  $YY$ ,  $YX$  and  $XX$  = "multiply connected" branches, delimited by two  
958 Y or X-nodes or one Y and one X-node.  
959

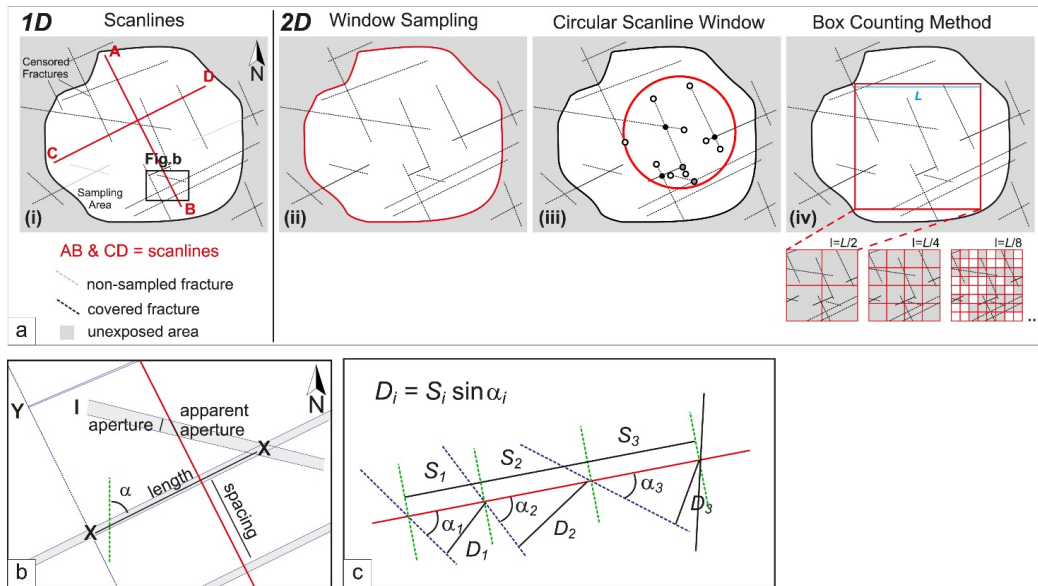


Fig. 1

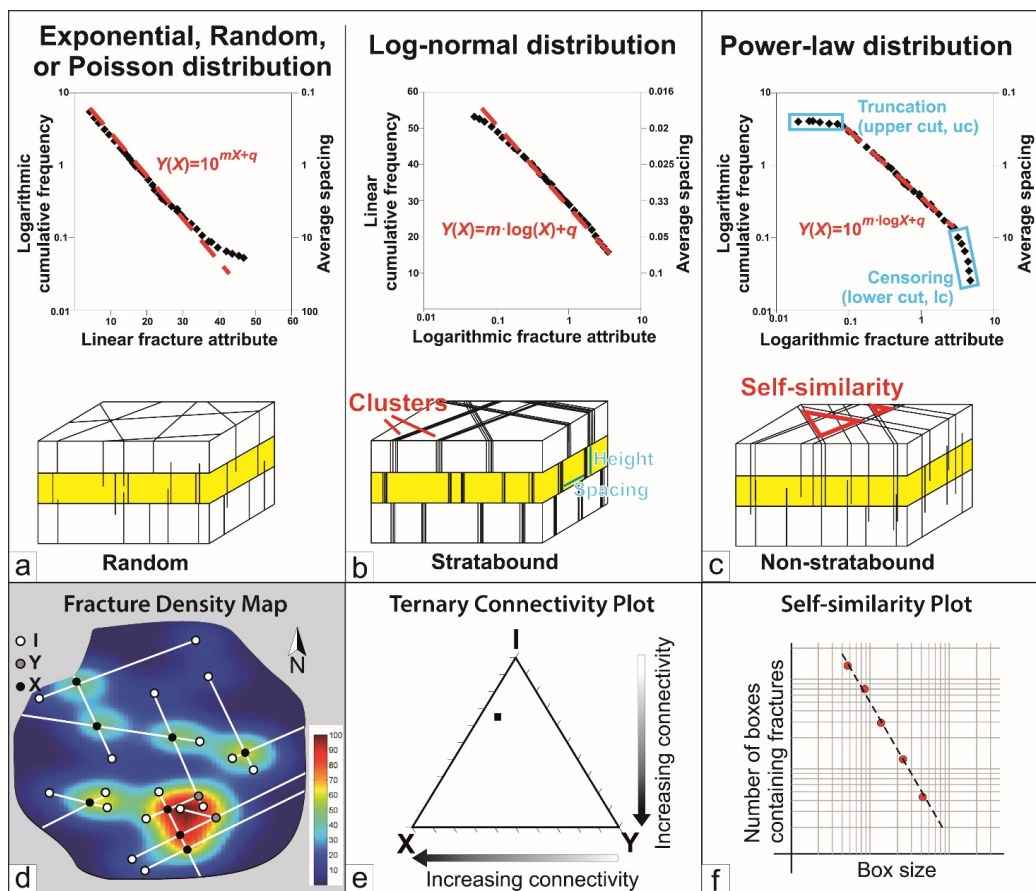


Fig. 2

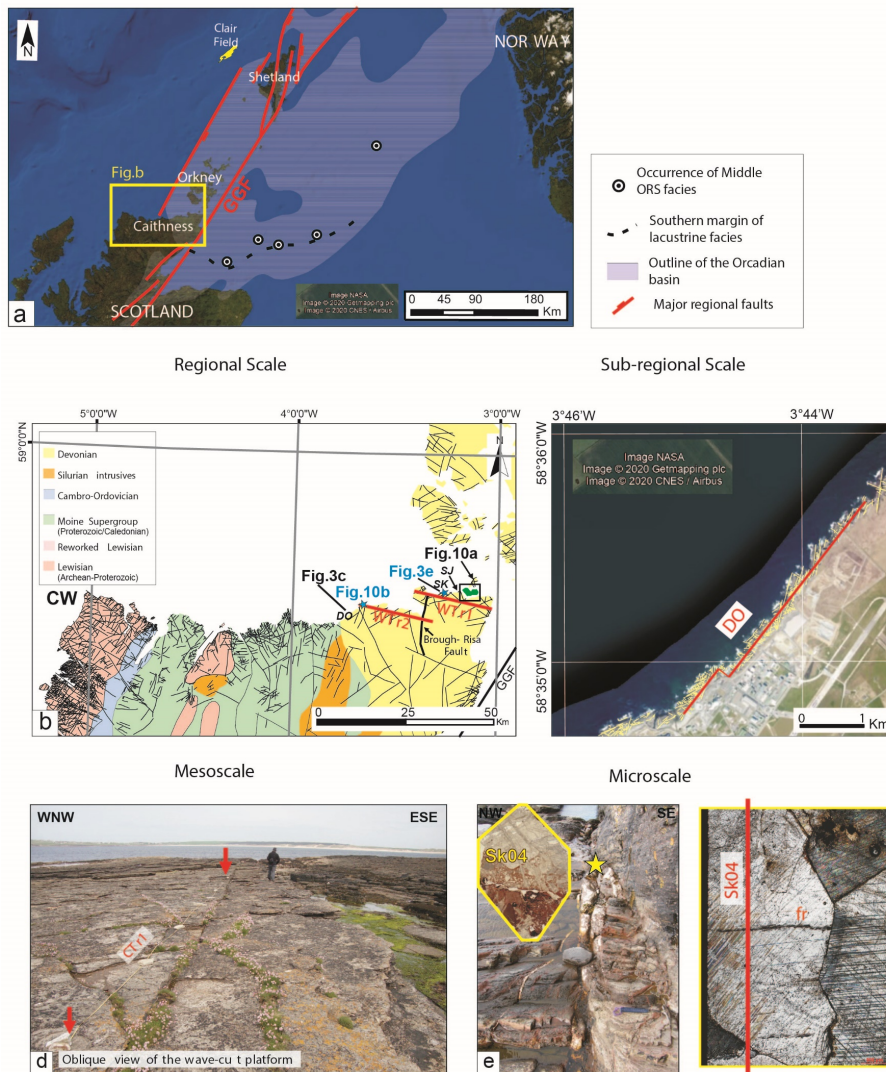


Fig. 3

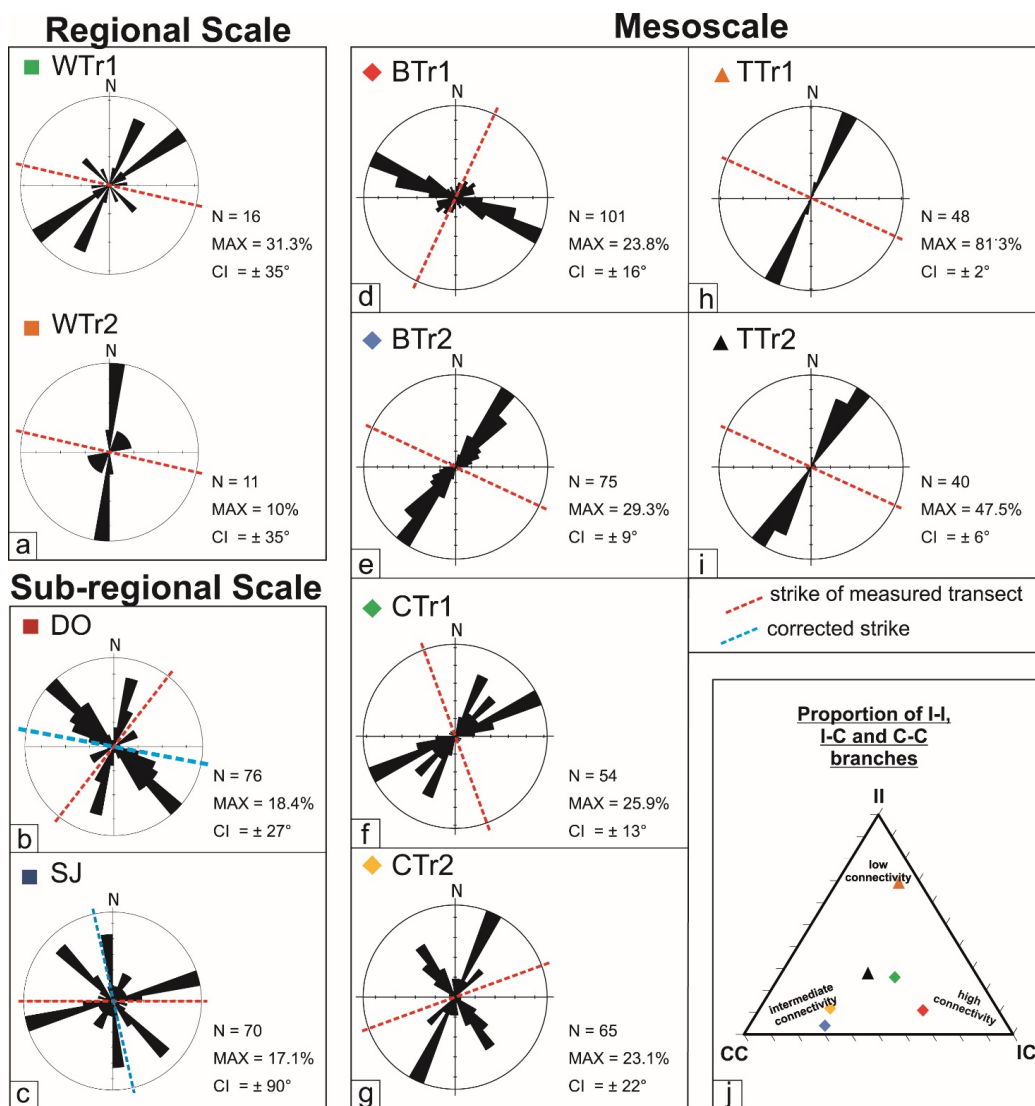


Fig. 4

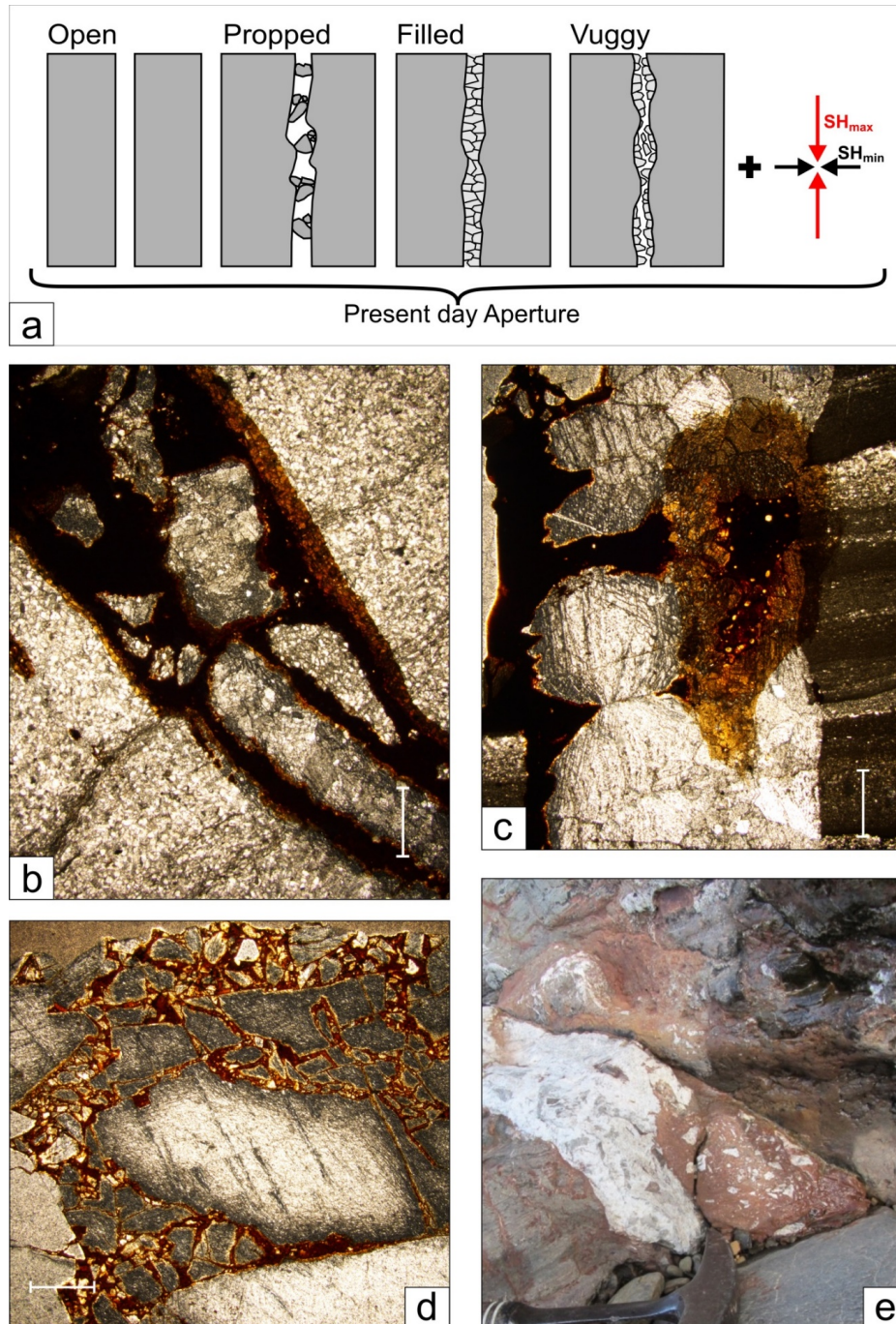


Fig. 5

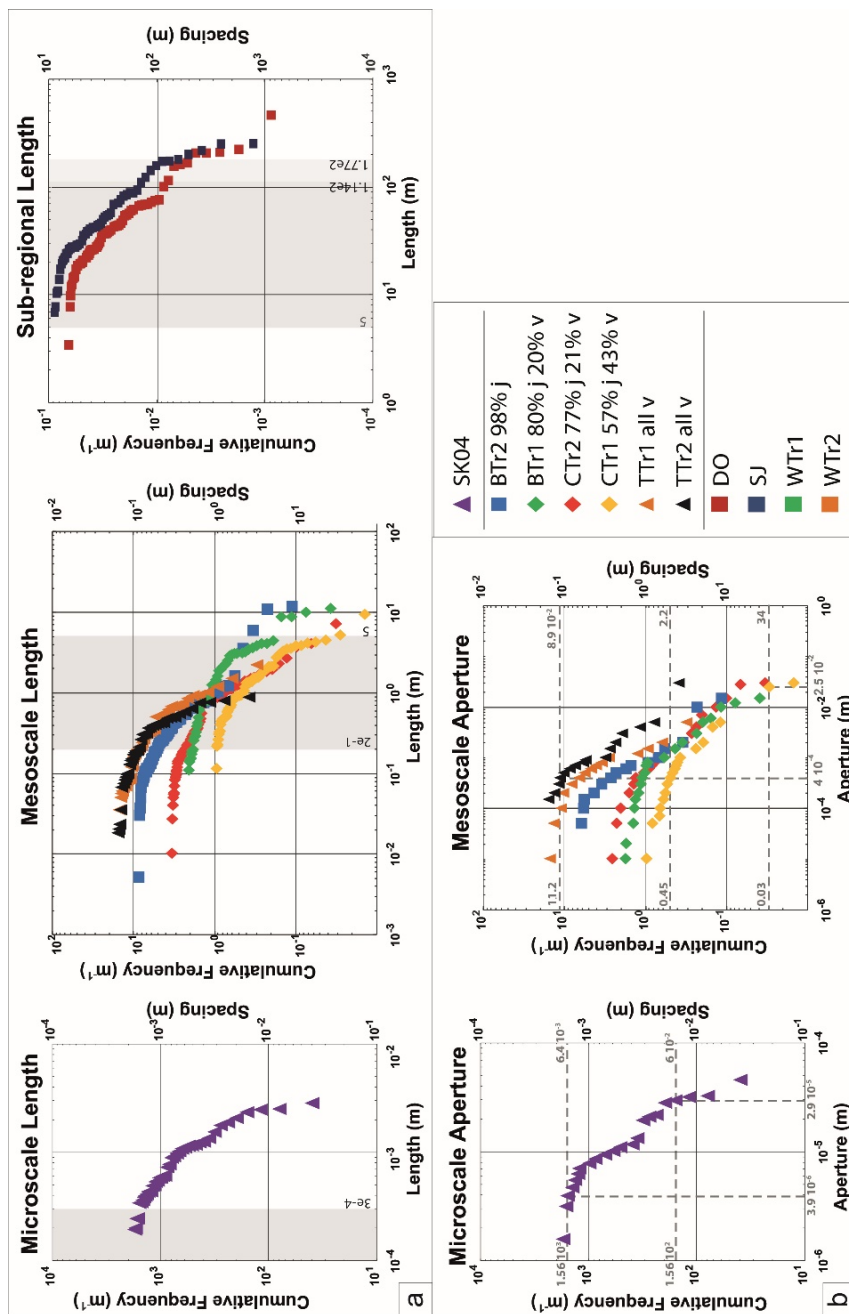


Fig. 6

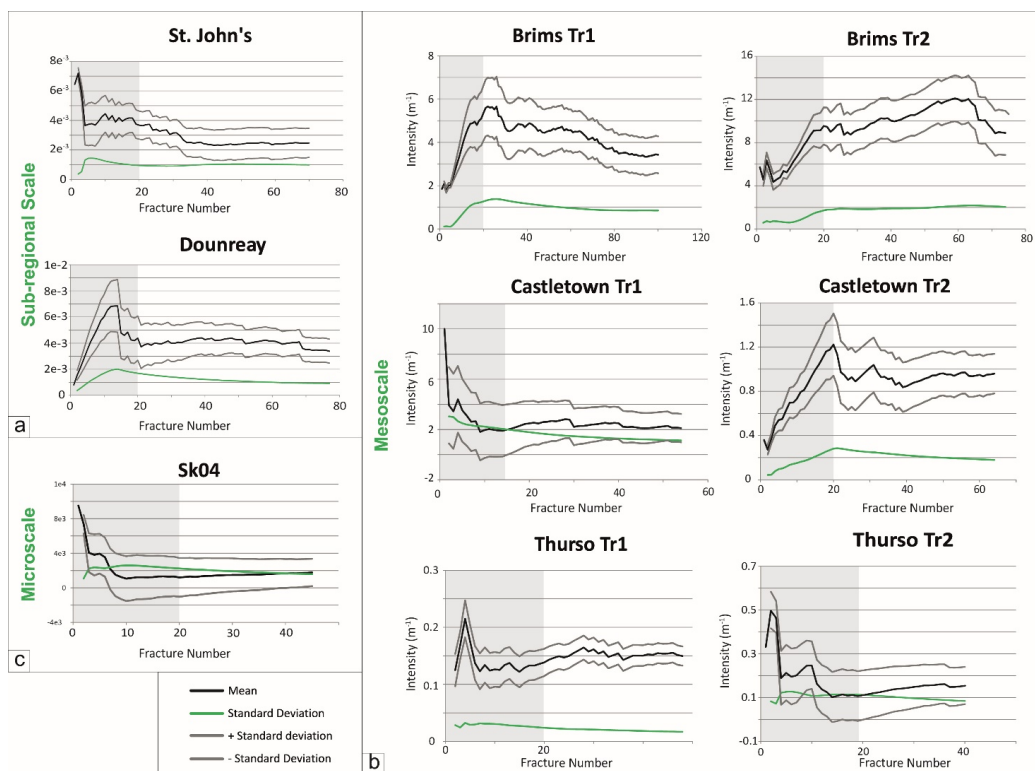


Fig. 7



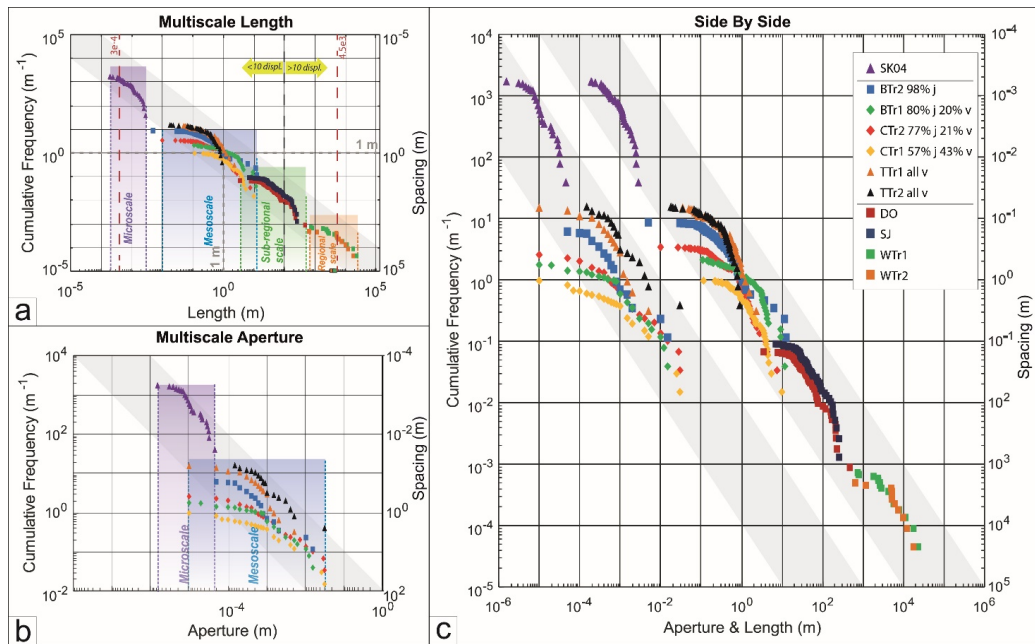


Fig. 8

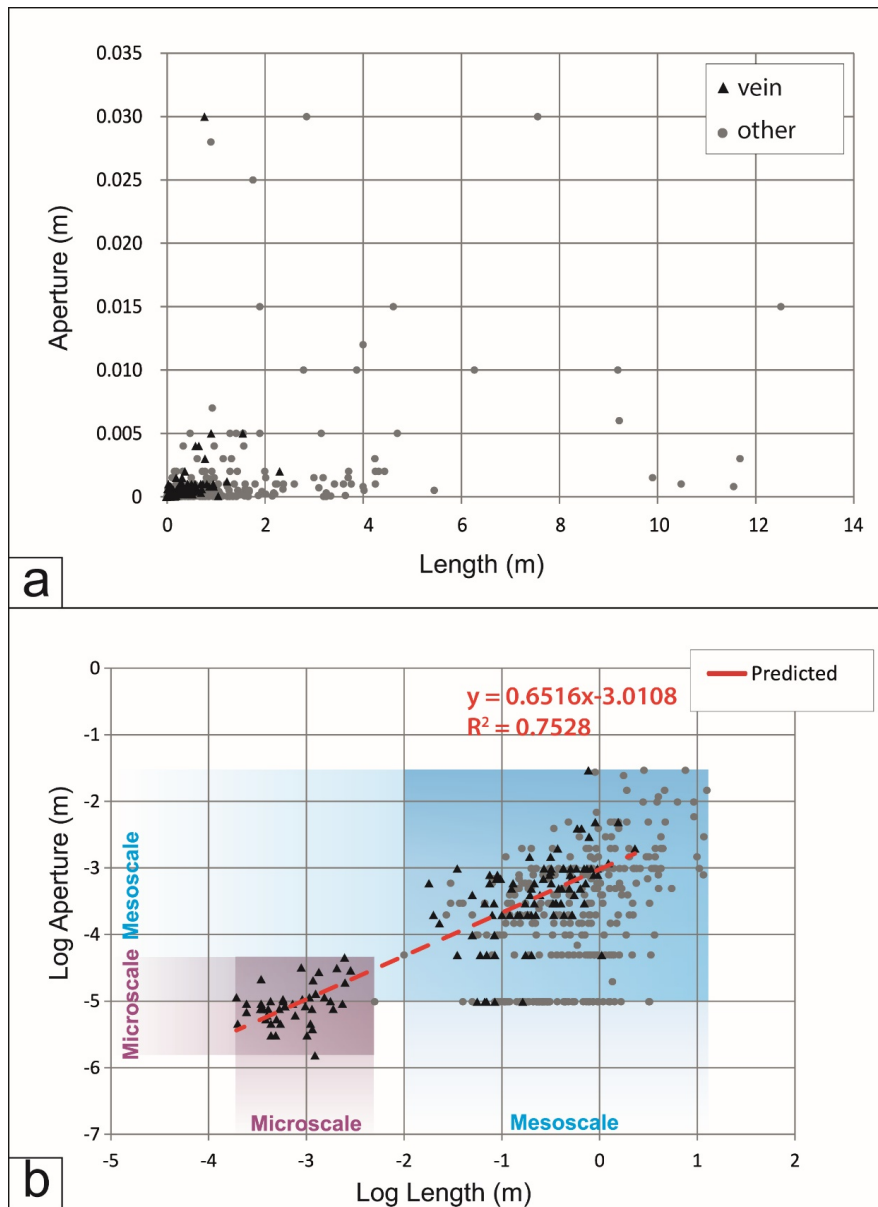


Fig. 9

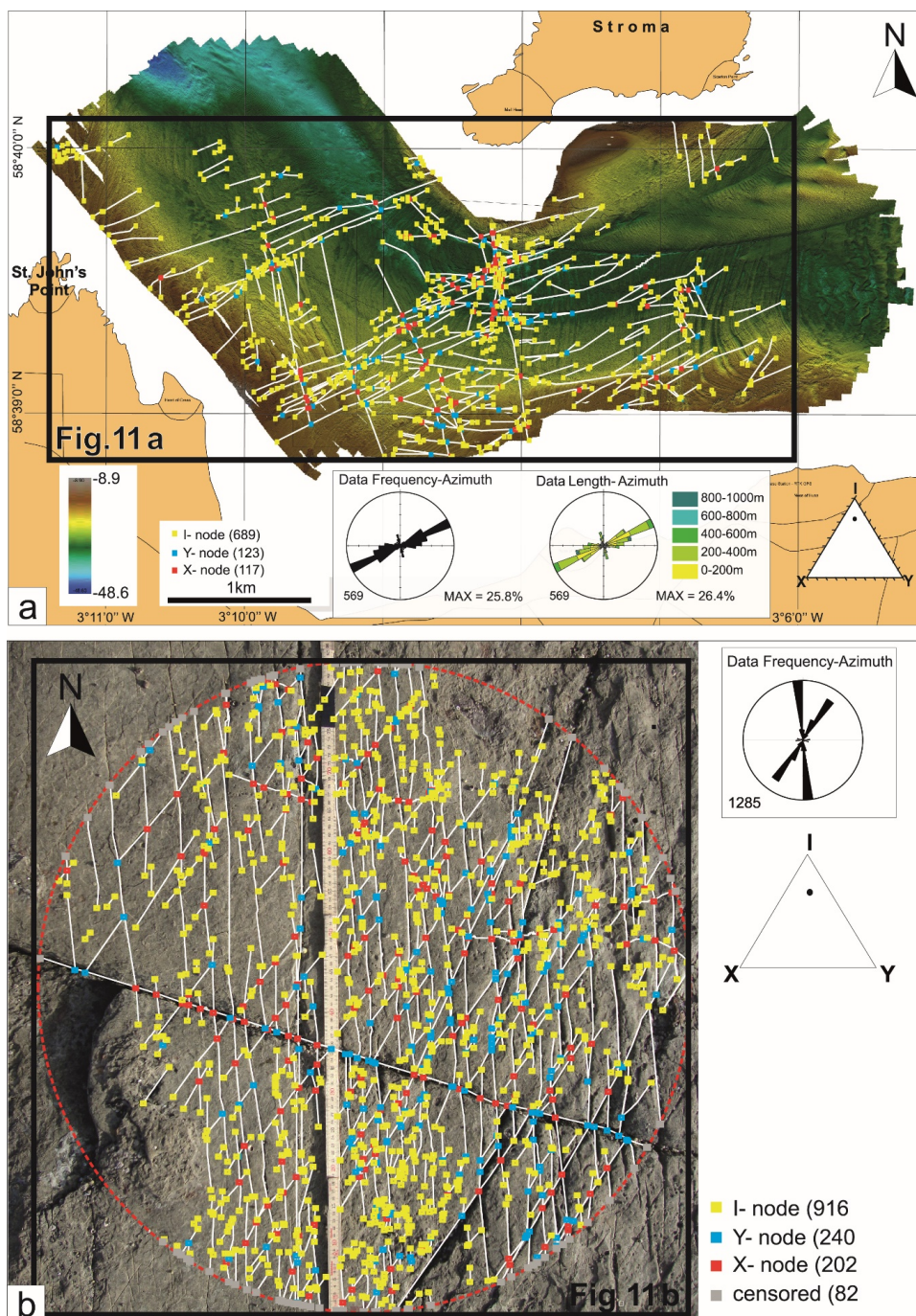


Fig. 10

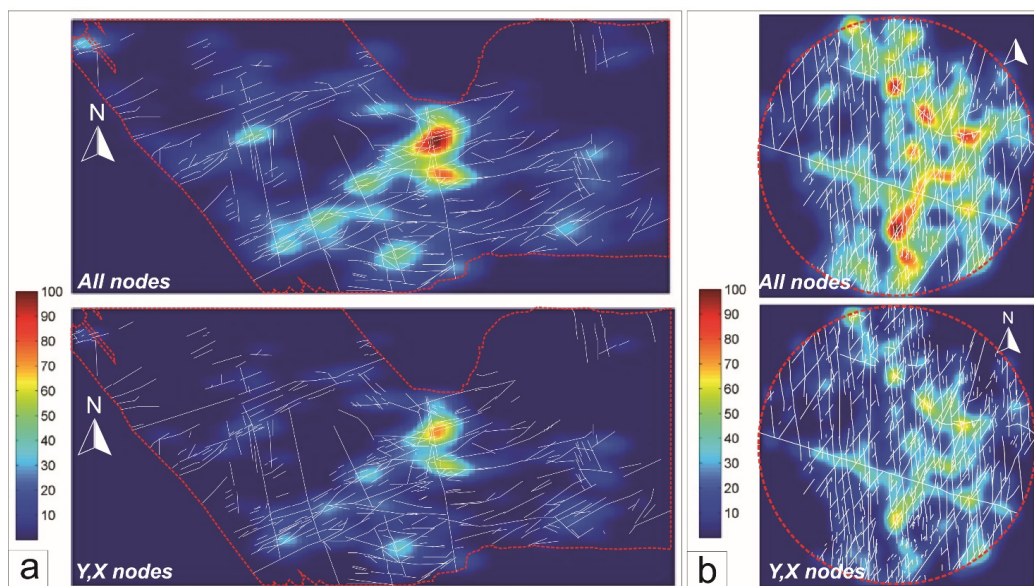


Fig. 11

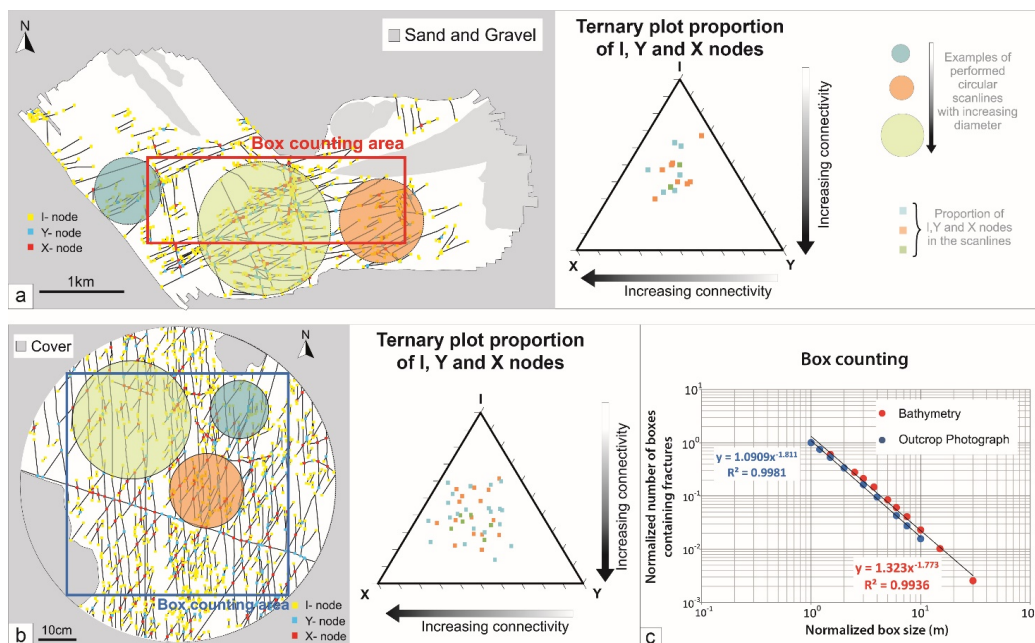


Fig. 12

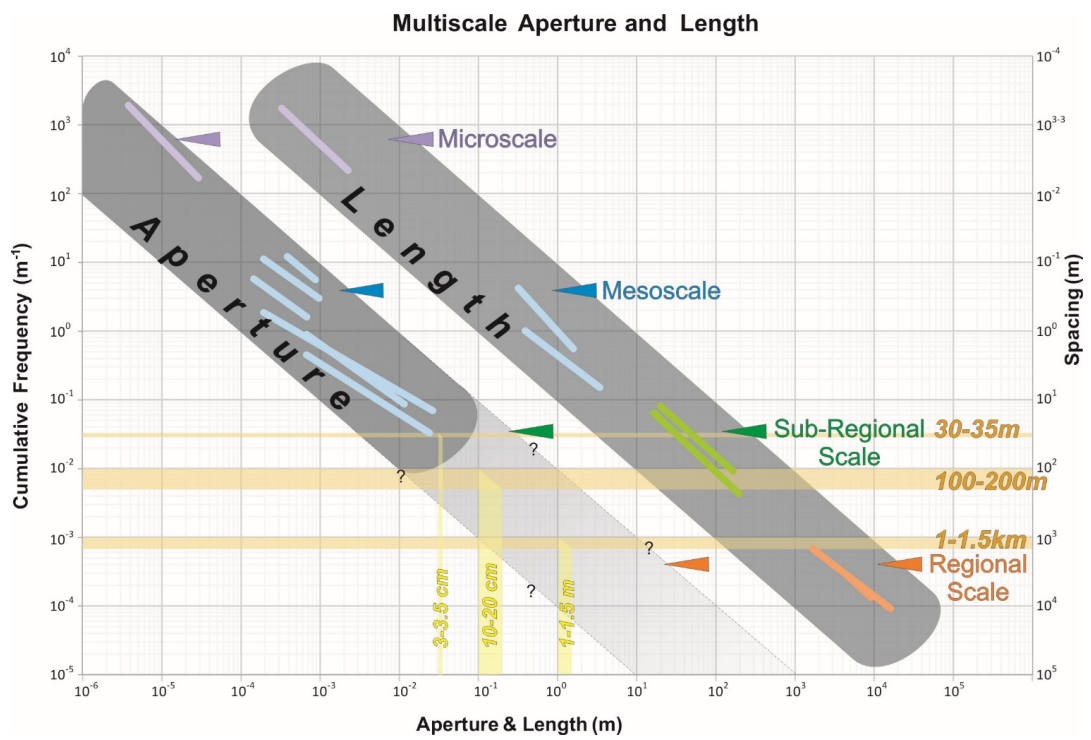


Fig. 13

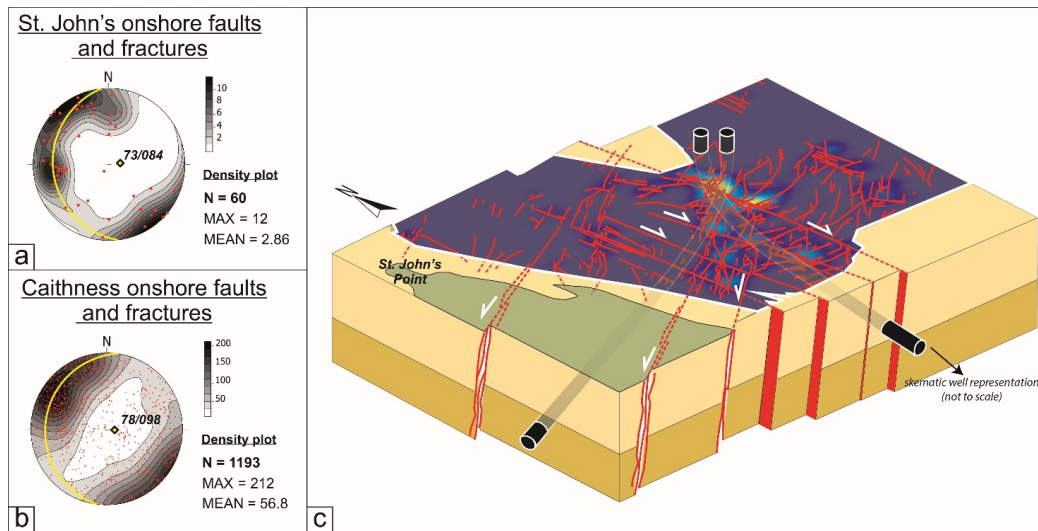


Fig. 14



Parameter	Definition	Scanline Sampling	Window Sampling	Circular Scanline	Box Counting Method
Orientation	Orientation of a fracture on a sampling plane (1D) or sampling volume (3D)	YES	YES	-	-
Spacing ( $s$ )	Spacing between consecutive fractures [m] (1D)	$S = l/l$	-	-	YES
Length ( $l$ )	Length of fracture intersecting the scanline (1D) or sampling area (2D)	YES	YES	-	YES
Aperture ( $a$ )	Aperture of fracture intersecting the scanline (1D)	YES	YES	-	-
Intensity or Frequency ( $I$ )	Number of fractures ( $N$ ) per unit length ( $L$ ) [ $m^{-1}$ ] (1D)	$I = N/L$	-	-	-
Density ( $D$ )	Number of fractures ( $N$ ) per unit area ( $A$ ) [ $m^{-2}$ ] (2D)	-	$D = N/A$	$D = m/2\pi r^2$	YES



Name	GPSs	N	Type			Kinematic			Termination					Spacing Range [m]		Length Range [m]		Aperture Range [m]		
			J	V	FnI	T	Dx	Sn	IY	IX	YY	YX	XX	From	to	From	to	From	to	
WTr1	ND18351 75022	16	-	-	-	-	-	-	-	-	-	-	-	-	3.7·10 <sup>3</sup>	3.4·10 <sup>2</sup>	2.3·10 <sup>4</sup>	7.4·10 <sup>2</sup>	-	-
WTr2	ND03054 71126	11	-	-	-	-	-	-	-	-	-	-	-	-	3.8·10 <sup>3</sup>	1.78·10 <sup>1</sup>	1.8·10 <sup>4</sup>	6.4·10 <sup>2</sup>	-	-
DO	NC98340 67080	76	-	-	-	-	-	-	-	-	-	-	-	-	2.6·10 <sup>2</sup>	0.8	4.8·10 <sup>2</sup>	3.5	-	-
SJ	ND29312 74823	70	-	-	-	-	-	-	-	-	-	-	-	-	1.5·10 <sup>2</sup>	1.2	2.6·10 <sup>2</sup>	7	-	-
BTr1	ND04322 71142	99	80	20	1	94	5	2	21	7	27	19	16	1.3	4·10 <sup>-3</sup>	7.6	10 <sup>-2</sup>	3·10 <sup>-2</sup>	1·10 <sup>-5</sup>	
BTr2	ND04360 71157	75	73	-	2	75	-	-	10	11	8	22	21	8·10 <sup>-1</sup>	2·10 <sup>-3</sup>	12	5·10 <sup>-3</sup>	1.5·10 <sup>-2</sup>	5·10 <sup>-5</sup>	
CTr1	ND18885 69104	54	31	23	-	14	-	-	10	4	9	4	0	3.2	5·10 <sup>-3</sup>	12	0.1	1.5·10 <sup>-2</sup>	1·10 <sup>-5</sup>	
CTr2	ND18922 69088	65	50	14	1	8	-	-	7	11	17	12	0	4.6	2·10 <sup>-2</sup>	9	0.11	3·10 <sup>-2</sup>	1·10 <sup>-5</sup>	
TTr1	ND10899 69071	48	-	48	-	48	-	-	11	0	3	1	0	2·10 <sup>-1</sup>	3·10 <sup>-3</sup>	2.3	3.5·10 <sup>-2</sup>	5·10 <sup>-3</sup>	1·10 <sup>-5</sup>	
TTr2	ND10914 69036	39	-	39	-	39	-	-	13	0	6	8	2	0.33	5·10 <sup>-3</sup>	0.9	1.8·10 <sup>-2</sup>	3·10 <sup>-2</sup>	1.5·10 <sup>-4</sup>	
SK04	ND26135 74584	45	-	-	-	-	-	-	-	-	-	-	-	-	2.2·10 <sup>-4</sup>	1.2·10 <sup>-6</sup>	2.8·10 <sup>-3</sup>	1.9·10 <sup>-4</sup>	4.6·10 <sup>-5</sup>	1.5·10 <sup>-6</sup>