

27

28 **1. Introduction**

29 Quantifying the rates and duration of deformation processes is key to understand how the
30 continental crust deforms. Quite a lot is known about rates and duration of ductile deformation in the
31 lower crust, for instance that shear zones can be active for 10s or 100s My (Schneider et al., 2013;
32 Mottram et al., 2015). However, less is known about the duration and rates of folding processes in the
33 upper crust. Short-term folding rates are usually captured by studying deformed terraces and alluvial fan
34 ridges associated with active folds, and the dating of the inception and lifetime of folds is based on the
35 extrapolation of these short-term rates back in time assuming a steady deformation rate.

36 The other classical mean to constrain the age and rate of upper crustal folding consists of dating
37 growth strata. In orogenic forelands, contractional deformation causes folding of the pre-deformational
38 sedimentary sequence and when sedimentation occurs continuously during deformation, growth strata
39 are deposited synchronously with folding. Growth strata often show a characteristic pattern, such as
40 decreasing dips up section toward the limbs of the fold, fan-like geometry and unconformities (Riba,
41 1976; Fig.1). Several factors control growth strata patterns, such as kink-band migration, fold uplift,
42 limb rotation and lengthening rates, as well as sedimentation and erosion rates (Suppe et al., 1992; Storti
43 and Poblet, 1997). Chronostratigraphic constraints are critical for defining the duration and rate of fold
44 growth (Butler and Lickorish, 1997). Dating the base of the growth strata defines the youngest initiation
45 age for the fold, while post-growth strata conceal the final geometry of the fold and mark the end of
46 folding (Fig.1).

47 However, preserved growth strata are not ubiquitous/are rare, and the folded multilayer typically
48 includes only pre-growth strata. Also, the fold growth may be highly discontinuous through time,
49 deformation being episodic at all timescales with tectonic uplift pulses of different duration and intensity
50 interrupted by periods of variable extent in which no fold growth occurred (Masferro et al., 2002;
51 Carrigan et al., 2016; Anastasio et al., 2018). Where available, the study of syntectonic unconformities
52 (Barnes, 1996) or terraces (Mueller and Suppe, 1997) otherwise suggest that the growth of some folds
53 may be caused by earthquake-related slip on active faults, which is by essence discontinuous. These
54 studies emphasize the difficulty to extrapolate fold growth rates back in time. The age of fold initiation

55 obtained by assuming steady shortening rate, deposition rate and fold growth rate is therefore at best
56 strongly biased, at worst false, so the duration of fold growth remains poorly constrained.

57 Folded sedimentary layers usually exhibit brittle mesostructures such as faults, joints and veins,
58 and stylolites (e.g. Tavani et al., 2015, and references therein). These mesostructures accommodate the
59 internal strain of strata during folding, but also before strata started to be tilted and after tilting, i.e.,
60 when shortening can no longer be accommodated by fold growth (Fig.1). Several deformation stages
61 can typically be identified in folded pre-compressional strata, starting with pre-shortening extension
62 related to foreland flexure and bulging, followed by layer-parallel shortening (LPS, horizontal
63 shortening of flat-lying strata) (Amrouch et al., 2010a; Callot et al., 2010; Lacombe et al., 2011; Tavani
64 et al., 2006, 2008, 2011, 2012; Rocher et al., 2000; Beaudoin et al., 2012, 2016; Branellec et al., 2015).
65 Continuing horizontal stress loading and shortening usually leads to folding, associated with strata tilting
66 and curvature which are accommodated by flexural slip in the fold limbs and tangential longitudinal
67 strain (outer arc extension and inner arc compression) at the fold hinge. The fold ‘locks’ when limb
68 rotation and/or kink-band migration cannot accommodate shortening anymore. At that stage, strata
69 tilting is over but continuous horizontal shortening leads to late stage fold tightening (LSFT),
70 accommodated by late mesostructures developing irrespective of bedding dip (Fig. 1) (Amrouch et al.,
71 2010a; Tavani et al., 2015).

72 Despite recent efforts (Wang et al., 2016; Grobe et al., 2019; Curzi et al., 2020; Cruset et al.,
73 2020, 2021), the dating of the early-, syn- and late-folding mesostructures has received poor attention,
74 although it is key to constrain not only the absolute timing of folding in the absence of growth strata,
75 but also the entire duration of the fold-related contractional stages and the associated stress evolution
76 from build-up to release. We explore hereinafter the possibility to define the age and duration of folding
77 by investigating how and for how long pre-folding strata have been accommodating shortening from the
78 onset to the end of the horizontal contraction from which the fold originated, an event we define as the
79 folding event (Fig. 1). This approach will help better constrain the duration of fold growth, by dating
80 directly the syn-folding mesostructures but also by bracketing the timing of fold growth through dating
81 of the mesostructures that immediately predate and postdate strata tilting. Doing so will also enable to

82 capture the duration of the LPS and LSFT. These two deformation stages have been overlooked since
83 they accommodate much less shortening than folding itself. However, they correspond to key periods
84 of time for large scale fluid flow and related ore deposition in fold-and-thrust belts and sedimentary
85 basins (e.g., Roure et al., 2005; Evans and Fischer, 2012; Beaudoin et al., 2014). For this purpose, we
86 consider four natural folds for which we either compile existing data or provide new estimates of the
87 age of LPS, fold growth and LSFT. Three of our examples are from fold-and-thrust belts (Apennines,
88 Pyrenees), and one from the Laramide basement-cored folding province (Rocky Mountains). We show
89 that mesostructures can be used to constrain the timing and duration of fold growth and/or of shortening
90 preceding and following folding. Our results not only provide new estimates of the duration of folding,
91 but also establish that the overall duration of the folding event may strongly vary as a function of the
92 tectonic style of deformation. Beyond regional implications, this study paves the way to a better
93 mechanical appraisal of contractional deformation and stress evolution in folded domains.

94

95 **2. Methods for dating the folding event using mesostructures**

96 In this paper, we focus on easily recognizable mesostructures that develop in the same
97 contractional stage and under the same regional trend of horizontal shortening than folding. We report
98 neither on microstructures such as calcite twins (Craddock et al., 1993; Lacombe et al., 2007, 2009;
99 Rocher et al., 1996; Hnat et al., 2011; see review by Lacombe, 2010) nor on rock physical properties
100 such as anisotropy of magnetic susceptibility (e.g, Aubourg et al., 2010; Amrouch et al., 2010b;
101 Branellec et al., 2015, Weil and Yonkee, 2012). The main reason is that even both of them have been
102 shown to be suitable recorders of the stress and strain history of folded strata (Lacombe et al., 2012),
103 their precise dating remains to date out of reach.

104 In the four folds that we investigated, the sequence and age of mesostructures were established
105 by various dating approaches, of which methodologies are briefly recalled below (Fig.2). Note that strata
106 from which mesostructures were dated are mainly pre-folding strata, and that there have been few (if
107 any) attempts at directly dating mesostructures that developed within growth strata. The reason is that
108 the often poorly indurated syn-folding formations are less prone to fracturing and calcite cementation at

109 the time of deformation compared to pre-folding, well-indurated formations, which is evidenced by the
110 paucity of fracture studies in syn-tectonic strata (e.g., Shackleton et al., 2011).

111 *2.1 Sequence of mesostructures related to the fold history*

112 The characterization of the sequence of deformation was based on field measurements of
113 stylolites, faults, joints and veins, and their grouping into sets according to their statistical orientation,
114 deformation mode and relative chronology established from abutting and crosscutting relationships
115 (Fig.2A). Their timing with respect to fold growth (i.e., early, syn-, and late folding mesostructures) was
116 further established by considering their current and unfolded attitude at fold hinge and limbs (eg.,
117 Beaudoin et al, 2012, 2016; Tavani et al., 2015) (Fig.1).

118 Field observations (eg., Bellahsen et al., 2006; Ahmadhadi et al., 2008; Tavani et al., 2015) and
119 numerical modelling (Guiton et al., 2003; Sassi et al., 2012) have emphasized the widespread
120 reactivation during folding of joints and veins formed during pre-folding stages. The role of reactivation
121 should not be, and has not been, overlooked in our study; however, for the sake of reliable absolute
122 dating we focused on faults and veins the characteristics of which support that they newly formed at
123 each deformation stage and show neither textural nor petrographic evidence of multiple opening or
124 shearing events, should it be at the meso-scale or at the micro-scale.

125

126 *2.2 Dating veins and faults*

127 Calcite-bearing veins and faults (Fig.2A) can be dated by combining the absolute precipitation
128 temperature of the fluids from which calcite cements formed as given by carbonate clumped isotope Δ_{47}
129 thermometry with the burial-time history of strata (Fig.2B,D). Provided that (1) cementation was nearly
130 coeval with fracturing, (2) the geotherm can be reliably estimated and (3) stable isotope geochemistry
131 points towards fluid precipitation at thermal equilibrium with the host rock, clumped isotope
132 thermometry of cements combined to strata burial history yields the absolute timing of the successive
133 vein sets, hence the timing of the related deformation stages (Fig.2D) (Labeur et al., 2021).

134 Calcite cements can also be directly dated by carbonate geochronology (Fig.2B). Laser ablation–
135 inductively coupled plasma–mass spectrometry (LA-ICP-MS) U-Pb dating of calcite consistently

136 reveals the age of brittle deformation events (Roberts and Walker, 2016; Nuriel et al., 2017; Hansman
137 et al., 2018; Beaudoin et al., 2018; Roberts et al., 2020)(Fig.2B,D), provided that cementation was coeval
138 with fracturing and that no later fluid infiltration and/or calcite recrystallization occurred (Roberts et al.,
139 2021).

140

141 *2.3 Combining sedimentary stylolite roughness inversion for paleodepth and burial history to* 142 *constrain the onset of LPS*

143

144 The onset of LPS corresponds to the time at which the maximum principal stress σ_1 switched
145 from a vertical attitude related to compaction and/or to foreland flexural extension to a horizontal
146 attitude in response to tectonic contraction (Beaudoin et al., 2020a). In order to constrain the timing of
147 this switch, our approach relies on the capability of bedding-parallel, sedimentary stylolite (Fig.2A) to
148 fossilize the magnitude of the vertical stress σ_1 at the time dissolution stopped. Indeed, signal analysis
149 (e.g. wavelets) of the final roughness of a sedimentary stylolite returns scale-dependent power laws, of
150 which the transition length (crossover length L_c) scales with the magnitude of the vertical stress σ_1
151 (Schmittbuhl et al, 2004; Toussaint et al., 2018) (Fig.2C). By analyzing a population of sedimentary
152 stylolites with this inversion technique which has been validated by numerous studies (Ebner et al.,
153 2009; Rolland et al., 2014; Bertotti et al., 2017; Beaudoin et al., 2016, 2019, 2020a,b), one can estimate
154 the maximum burial depth at which pressure solution was active, with 12% uncertainty (Rolland et al.,
155 2014). Combining this depth with the burial-time evolution of the strata as derived from well data and/or
156 exposed stratigraphic successions reveals the time at which compaction-driven pressure solution halted
157 in the rock because of the switch from a vertical to a horizontal σ_1 , and thus the age of the onset of LPS
158 (Fig. 2D). The validity of such an approach has been established on the basis of the comparison of the
159 age of the onset of LPS determined this way with the oldest U-Pb absolute age of LPS-related veins
160 (Beaudoin et al., 2020a).

161

162 **3. Dating natural folding events**

163 *3.1 Cingoli and San Vicino Anticlines (Apennines)*

164 The San Vicino and Cingoli anticlines belong to the Umbria-Marche Apennine Ridge (UMAR,
165 Fig. 3A). Apenninic deformation occurred by the Tortonian in the west of UMAR to the late Messinian-
166 early Pliocene in the east, reaching the Adriatic domain in the late Pliocene-Pleistocene (Calamita et al.,
167 1994). UMAR undergoes post-orogenic extension since ~3 Ma, being younger eastward and marked by
168 recent or active normal faults cutting through the nappe stack (Barchi, 2010). The San Vicino and the
169 Cingoli anticlines involve platform carbonates overlain by a hemipelagic succession detached above
170 Triassic evaporites. The folds formed in late Messinian-early Pliocene (~6-5 Ma) as indicated by growth
171 strata preserved in the nearby Aliforni syncline (Fig.3B), following a period of foreland flexure-related
172 extension marked by pre-contractual normal faults associated with turbidite deposition lasting until
173 early Messinian (~6.5 Ma) (Calamita et al., 1994; Mazzoli et al., 2002).

174 Field analysis in the Cingoli and San Vicino fault-bend anticlines (Fig.3B) has revealed three
175 main sets of mesostructures (Beaudoin et al., 2020b; Labeur et al., 2021). Set I consists of vertical veins
176 perpendicular to both bedding and fold axis and striking NE-SW, associated with bed-perpendicular
177 tectonic stylolites with peaks trending NE-SW and plunging parallel to bedding dip which, after
178 unfolding, indicates NE-SW-directed LPS. Set II veins are bed-perpendicular and strike NW-SE,
179 parallel to the fold axis; they abut or cut across set I veins and formed in response to outer-arc extension
180 at fold hinge. Set III comprises NE-SW striking veins closely associated with tectonic stylolites with
181 horizontal peaks trending NE-SW - both veins and tectonic stylolites being vertical regardless of the
182 bedding dip - and with conjugate vertical strike-slip faults which formed during a post-tilting horizontal
183 NE-SW contraction, i.e., LSFT (Fig.3C).

184 Labeur et al (2021) focused on the Cingoli anticline to reconstruct the burial history of the early
185 Cretaceous Maiolica Fm. and the Paleocene Scaglia Rossa Fm. The authors carried out an extensive
186 inversion of the roughness of sedimentary stylolites from these formations to constrain the maximum
187 depth at which compaction-related dissolution was active. The results are shown in Fig.3D, together
188 with the timing of veins from sets I and II as deduced from Δ_{47} thermometry (Labeur et al., 2021) by

189 considering a 23°C/km geotherm (Caricchi et al. 2015) and a 10°C surface temperature. The resulting
190 timing for LPS, fold growth and LSFT is shown in Fig.3F.

191 To extend the published dataset to the San Vicino Anticline, veins from sets I, II and III were
192 sampled in the Maiolica Fm. to perform U-Pb analyses for absolute dating. Selected veins display
193 antitaxial, elongated-blocky or blocky textures (Bons et al., 2012) ensuring that the cements precipitated
194 during, or soon after, vein opening. Cathodoluminescence observations further support the homogeneity
195 of the cements (Fig.4) as well as the absence of any vein re-opening and calcite recrystallization or fluid
196 infiltration that might cause anomalous younger (reset) ages (Roberts et al., 2021). U-Pb dating of calcite
197 cements was conducted using LA-ICP-MS at the Institut des Sciences Analytiques et de Physico-Chimie
198 pour l'Environnement et les Matériaux (IPREM) laboratory (Pau, France). Ages were determined from
199 the total-Pb/U-Th algorithm of Vermeesch (2020), are quoted at 95% confidence, and include
200 propagation of systematic uncertainties. Sample information, detailed methodology and results are
201 provided in the Supplemental Material. Three veins from the San Vicino anticline yielded reliable ages:
202 6.1 ± 2 Ma for the set I vein, 3.5 ± 1 Ma for the set II vein and 3.7 ± 0.3 Ma for the set III vein (Fig. 3E).
203 The large uncertainties on the U-Pb age from the set II vein lead to some overlap with the dates of set I
204 and set III veins (Fig.3F). However, these veins have distinctive orientations, consistent relative
205 chronology, and distinctive C and O stable isotopic signatures of their cements while being sampled in
206 the same parts of the fold (Beaudoin et al., 2020b). These observations support that these veins were not
207 cemented by the same fluid, hence were not cemented coevally. The absolute vein ages, combined with
208 existing time constraints (Fig.3F), indicate that LPS occurred from ~6.5 to 5.5 Ma for both anticlines,
209 followed by fold growth between ~5.5 and ~3.5 Ma, with a seemingly slightly longer duration in Cingoli
210 than in San Vicino. LSFT started ~5 Ma in the Camerino syncline (Beaudoin et al., 2020b), ~4.5 Ma in
211 San Vicino and ~3 Ma in Cingoli, and possibly lasted until the onset of post-orogenic extension in
212 eastern UMAR (~2.5-2 Ma, Fig.3F). The entire folding event was thus very short, having lasted 3-4 My
213 considering both anticlines as a whole (Fig.3F).

214 *3.2 Pico del Aguila Anticline (Pyrenees)*

215 The Pico del Aguila is a N160°E trending anticline in the southern Pyrenees (Fig. 5A), markedly
216 oblique to the south Pyrenean thrust front. It formed in response to Pyrenean thrusting and detachment
217 folding above Triassic evaporites (Poblet and Hardy, 1995; Vidal Royo et al., 2009, Fig. 5B). Growth
218 strata (Fig.5B) indicate that the fold developed by late Lutetian-Priabonian (~ 42-35 Ma, Hogan and
219 Burbank, 1996), before it was passively tilted and transported southward over the Guarga basement
220 thrust (Jolivet et al., 2007).

221 Beaudoin et al. (2015) investigated the fracturing history of the Pico del Aguila (Fig. 5C). Three
222 sets of bed-perpendicular joints/veins, oriented N080°E, N060°E and N045°E (from the oldest to the
223 youngest as established from abutting/cross cutting relationships), were recognized. These three sets
224 formed in progressively younging strata in response to a NE-SW-directed shortening while the area was
225 undergoing a vertical axis 30-40° clockwise rotation (Fig.5C). This rotation agrees with the Bartonian-
226 Priabonian clockwise rotation of 15-50° around a vertical axis identified from paleomagnetism (Pueyo
227 et al., 2002). The field study also revealed bed-perpendicular joints oriented N160°E and N-S trending
228 normal faults which formed during fold growth in response to outer-arc extension at fold hinge (Fig.5C).
229 The end of the fold-related fracturing history (LSFT) is marked by the formation of N-S trending reverse
230 faults and by the transpressional reactivation of earlier ENE striking joints under an E-W compression
231 resulting from the local rotation of the regional NE-SW compression (Beaudoin et al., 2015). Post-
232 folding, E-W trending reverse faults ultimately developed under the same N-S compression as the
233 Guarga thrust (Fig.5C).

234 U-Pb dating of calcite cements reveals that the veins related to NE-SW directed LPS formed as
235 early as $\sim 61 \pm 3$ Ma ago, while late oblique-slip reverse faults (LSFT) and post-folding E-W reverse
236 faults were dated 19 ± 5 Ma and $18-14 \pm 3$ Ma, respectively (Hoareau et al., 2021). LPS, folding and
237 LSFT therefore lasted ~ 19 My (61-42 Ma), ~ 7 My (42-35 Ma) and ~ 17 My (35-18 Ma), respectively
238 (Fig.5D).

239

240 3.3 Sheep Mountain Anticline (Rocky Mountains)

241 The Sheep Mountain anticline is a thrust-related, basement-cored NW-SE striking fold that
242 developed in the Bighorn basin (Figs. 6A and B) during the late Cretaceous-Paleogene Laramide
243 contraction. Three main joint/vein sets were recognized there (Fig. 6C, Bellahsen et al., 2006; Amrouch
244 et al., 2010; Barbier et al., 2012). Set I consists of bed-perpendicular, WNW-ESE oriented veins
245 associated with tectonic stylolites with ~WNW-ESE horizontal peaks (after unfolding) (Amrouch et al.,
246 2010a, 2011). This set formed prior to folding under a horizontal σ_1 trending WNW-ESE, likely
247 transmitted from the distant thin-skinned Sevier orogen at the time the Bighorn basin was still part of
248 the Sevier undeformed foreland. Set II comprises vertical, bed-perpendicular joints/veins striking NE-
249 SW, i.e., perpendicular to the fold axis. These veins are associated with tectonic stylolites with horizontal
250 peaks oriented NE-SW and witness a NE-SW directed LPS (Varga, 1993; Amrouch et al., 2010a; Weil
251 and Yonkee, 2012). The joints/veins of set III are bed-perpendicular and abut or cut across the veins of
252 the former sets. They strike NW-SE, i.e., parallel to the fold axis, and their distribution mainly at the
253 hinge zone of the fold support their development in response to outer-arc extension at the hinge of the
254 growing anticline (Fig.6C). Widespread reverse and strike-slip faults also formed during LPS and LSFT,
255 while bedding-parallel slip surfaces developed during fold growth (Amrouch et al., 2010a).

256 Veins from sets I, II and III were dated by means of U-Pb (Beaudoin et al., 2018). Set I veins
257 yielded ages between 81 and 72 Ma, supporting their pre-Laramide formation. The Laramide LPS-
258 related veins were dated 72–50 Ma. The age of set III veins constrains the timing of folding in the
259 absence of preserved growth strata to 50–35 Ma (Beaudoin et al., 2018). Laramide LPS and fold growth
260 therefore lasted ~20-25 My and ~15 My, respectively (Fig. 6D). The duration of the LSFT is poorly
261 constrained, being bracketed between 35 Ma and the onset of the Basin and Range extension and
262 Yellowstone hot-spot activity at ~17 Ma (Camp et al., 2015, Fig. 6D).

263 **4. Discussion and conclusion**

264 The absolute dating of mesostructures definitely confirms the sequence of deformation usually
265 deduced from orientation data and relative chronology with respect to bedding attitude, which includes
266 LPS, fold growth (e.g., strata tilting) and LSFT (Fig.1). This sequence is valid for the four folds studied,
267 despite the San Vicino, Cingoli and Pico del Aguila anticlines developed above a decollement in a fold-

268 and-thrust belt while the Sheep Mountain anticline formed as a basement-cored forced fold above a
269 basement thrust. The overall consistency between the ages of growth strata when preserved, the time
270 constraints derived from our multi-proxy analysis coupling isotopic geochemistry of cements and
271 stylolite paleopiezometry, and the U-Pb ages on early-, syn- and late-folding mesostructures
272 demonstrates the reliability of our approach. Minor age overlaps are observed only when the duration
273 of each deformation stage was shorter than age uncertainties, i.e., in the case of recent and rapid
274 deformation (San Vicino and Cingoli, Fig.3F). Note that age overlaps could also relate with the fact that
275 LPS and fold growth may slightly overlap, as documented in the Sibillini thrust anticline, i.e., the
276 southern continuation of the San Vicino anticline (Tavani et al., 2012).

277 In the four investigated anticlines, fold growth lasted between 1.5 Ma and 15 Ma, in accordance
278 with previous estimates of fold growth duration elsewhere using either syntectonic sedimentation (Holl
279 and Anastasio, 1993; Anastasio et al., 2018) or mechanical modeling (Yamato et al., 2011). Moreover,
280 our study quantifies for the first time the duration of the contraction before and after fold growth. The
281 results unexpectedly reveal that LPS and LSFT, which accommodate lower amounts of shortening than
282 fold growth but which are associated with substantial - if not most of - small-scale rock damage, may
283 have lasted much longer than fold growth itself. Such a trend could be key for the understanding of the
284 history of foreland basins, including mechanical evolution of strata and past fluid flow dynamics (Roure
285 et al., 2005; Beaudoin et al., 2014).

286 Dating precisely the onset of LPS, whatever the technique used (U-Pb geochronology or
287 absolute thermometry of calcite cements of mesostructures) is difficult because the entire range of vein
288 ages may not be captured with certainty due to limited sampling. However, the onset of LPS can be
289 further constrained either by the sedimentary record of the foreland flexure preceding contraction (San
290 Vicino) or by the estimate of the time at which compaction-related pressure solution along sedimentary
291 stylolites halted in the rocks in response to the switch of σ_1 axis from vertical to horizontal (Cingoli).
292 The end of LSFT is also difficult to constrain precisely, but an upper bound is given by the change from
293 fold-related shortening to a new regional state of stress. The latter is illustrated by the onset of post-

294 orogenic extension in eastern UMAR (Fig.3), by the late Pyrenean compression in the Pico del Aguila
295 area (Fig. 5) and by the Basin and Range extension in the Laramide province (Fig.6).

296 The four examples of folds also show that the overall duration of the folding event is variable
297 (Fig.7). Fold growth lasted longer in the case of forced folding above a high angle basement thrust
298 (Sheep Mountain) compared to fault-bend folding (San Vicino and Cingoli) along a flat-ramp
299 decollement and detachment folding (Pico del Aguila) above a weak detachment layer in the cover (Fig.
300 7). The rapid fold growth and the relatively short LSFT in San Vicino and Cingoli are in line with the
301 high rates of contraction and migration of deformation in the Apennines (Calamita et al., 1994, Fig .7).
302 In contrast, LSFT appears to last longer when folding is anchored to a high angle basement thrust or
303 when the fold is located at the front of the orogenic wedge, i.e., when the later propagation of
304 deformation is limited or slow or when it occurs in a complex sequence (Pico del Aguila and Sheep
305 Mountain, Fig.7). The duration of LPS reflects to some degree the duration of the stress/strain
306 accumulation in rocks required to generate folding, which can depend on the structural style (Beaudoin
307 et al., 2020c). Our results support that a longer LPS (and a higher level of differential stress as well) is
308 required to cause the inversion of a high angle basement normal fault and related forced folding of the
309 undetached sedimentary cover (Sheep Mountain) than to initiate folding of the cover above a weak
310 decollement (Pico del Aguila, Cingoli and San Vicino, Fig. 7). The longer LPS at Pico del Aguila with
311 respect to San Vicino and Cingoli (Fig.7) likely reflects the longer accumulation of displacement
312 required to initiate folding oblique to the regional compression rather than perpendicular to it. It is worth
313 to note that at first glance the fracture pattern (eg, Tavani et al., 2015) remains basically similar whatever
314 the overall duration of the folding event and related deformation stages.

315 In summary, beyond regional implications, this study demonstrates that pre-, syn- and post-
316 tilting mesostructures that formed under the same contraction as folding can be successfully dated. Our
317 results bring for the first time absolute time constraints on the age and duration on the entire folding
318 event for several upper crustal folds formed in different contractional settings. In particular, we not only
319 better constrain the age and duration of the fold growth stage, but also the onset and duration of the
320 layer-parallel shortening stage that predates folding, and the duration and end of the late stage fold

321 tightening. Because the duration of each deformation stage is found to depend on the structural style
322 and/or the regional sequence of deformation, our results emphasize the need to more carefully consider
323 the entire folding event for a better appraisal of folding processes and stress/strain evolution in orogenic
324 forelands, and for a more accurate prediction of host rock damage and fluid migrations in naturally
325 fractured reservoirs within folded domains.

326

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332

333 **Figure captions**

334 Fig.1. Concept of folding event and associated mesostructures and growth strata.

335 Fig.2. Principle of dating of mesostructures related to the folding event. A. Photograph of a bedding-
336 parallel sedimentary stylolite cut by a vertical vein related to layer-parallel shortening (LPS). B.
337 Principle of dating calcite veins using LA-ICP-MS, with laser ablation spots and final Tera-Wasserburg
338 diagram. C. Principle of inversion of the roughness of sedimentary stylolites for stress. σ_v is the vertical
339 stress, $\alpha = \frac{(1-2\nu)*(1+\nu)^2}{30\pi(1-\nu)^2}$, γ is the solid-fluid interfacial energy, ν is the Poisson ratio, E is the Young
340 modulus, ρ is the dry density, g is the gravitational field acceleration and z is the depth. D. Principle of
341 the combination of U-Pb dating and absolute Δ_{47} thermometry of calcite cements (here for LPS-related
342 veins) with maximum depth of burial-related dissolution inferred from roughness inversion of
343 sedimentary stylolites and burial-time evolution of strata to derive the timing of deformation stages
344 during the folding event. Regional data are from Mazzoli et al., 2002 (flexure), Calamita et al. 1994
345 (folding and thrusting), Beaudoin et al., 2020b (LSFT).

346

347 Fig.3. San Vicino and Cingoli anticlines: A: location (AS: Adriatic Sea; TS: Tyrrhenian Sea). B: Cross
348 section (after Mazzoli et al., 2002). C: Orientation of the main sets of mesostructures (relative
349 chronology, 1 to 3), reported in current or unfolded attitude on a lower hemisphere Schmidt stereonet,
350 and associated paleostress evolution. * denotes mesostructures dated using U-Pb. D: Burial model of
351 Cingoli constructed considering thickness from stratigraphic and well data corrected for chemical and
352 physical compaction (modified from Labeur et al., 2021). The range of depths reconstructed from
353 sedimentary stylolite roughness inversion (with uncertainty shaded in light grey) are reported for each
354 formation as grey levels. The results of clumped isotope analysis (i.e., temperatures of precipitation of
355 vein cements at thermal equilibrium with the host rock) are reported for LPS-related veins (blue) and
356 syn-folding veins (red). The deduced timing of the deformation stages is reported. E: Age dating results
357 for veins from San Vicino anticline: Tera-Wasserburg concordia plots for carbonate samples showing
358 $^{238}\text{U}/^{206}\text{Pb}$ vs $^{207}\text{Pb}/^{206}\text{Pb}$ for veins of sets I (LPS-related) and III (LSFT-related)(n—no. of spots).
359 MSWD—mean square of weighted deviates. F: Timing and duration of deformation stages. Color code
360 for C and F: dark blue: flexure-related extension. blue: layer-parallel shortening (LPS); red: fold growth;
361 green: late stage fold tightening (LSFT); yellow: post-folding extension.

362
363 Fig.4. 2D scans of veins dated by LA-ICP-MS U-Pb geochronology from San Vicino anticline, with
364 location of the ablation spots and diagenetic state observed under cathodoluminescence microscopy. A:
365 sample A16 (LPS-related vein). B: sample A19 (syn-folding vein). C: sample A20 (LSFT-related vein).
366

367 Fig.5. Pico del Aguila anticline: A: location (AB: Aquitaine Basin, JB: Jaca Basin, EB: Ebro Basin,
368 PAZ: Pyrenean Axial Zone; P: Paleozoic; M: Mesozoic; C: Cenozoic). B: Cross sections (north after
369 Poblet et al., 1997, south after Beaudoin et al., 2015). C: Orientation of the main sets of mesostructures
370 (relative chronology, 1 to 5), reported in current or unfolded attitude on a lower hemisphere Schmidt
371 stereonet (same key as Fig.3), and associated structural and paleostress evolution. Block diagrams
372 modified after Beaudoin et al. (2015). * denotes mesostructures dated using U-Pb. D: Timing and

373 duration of deformation stages. Color code for C and D : blue: layer-parallel shortening (LPS); red: fold
374 growth; green: late stage fold tightening (LSFT); yellow: post-folding compression.

375

376 Fig.6. Sheep Mountain anticline: A: location (BHB: Bighorn Basin; WRB: Wind River Basin; PRB:
377 Powder River Basin; GGB: Greater Green River Basin; DB: Denver Basin). B: Cross section (after
378 Amrouch et al., 2010); C: Orientation of the main sets of veins (relative chronology, 1 to 3), shown on
379 a field photograph and on a block-diagram of the final fold geometry, reported in unfolded attitude on a
380 lower hemisphere Schmidt stereonet (same key as Fig.3), and associated structural and paleostress
381 evolution. * denotes mesostructures dated using U-Pb. D: Timing and duration of the deformation
382 stages. Color code for C and D: grey: pre-folding layer-parallel shortening kinematically unrelated to
383 folding; blue: layer-parallel shortening (LPS); red: fold growth; green: late stage fold tightening (LSFT);
384 yellow: post-folding extension.

385 Fig.7. Compared durations of the deformation stages of the folding event, fold style (= final fold
386 geometry) and sequence of regional deformation for the four studied folds (circled numbers 1 to 6 :
387 order of structural development, i.e., sequence of folding/thrusting, with corresponding ages in Ma
388 (between parentheses), red : from this study; black : from the literature (Beaudoin et al., 2018 for
389 Wyoming, Jolivet et al., 2007 for the Pyrenees, Calamita et al., 1994 and Curzi et al., 2020 for the
390 Apennines). Color code: blue: layer-parallel shortening (LPS); red: fold growth; green: late stage fold
391 tightening (LSFT); yellow: post-folding extension/compression.

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616

617 **Dataset availability:** Data either are available as supplementary material or come from properly cited
618 literature.

619

620 **Author contribution:** Conceptualization : O. Lacombe, N. Beaudoin; Data acquisition : all authors;
621 Visualization : O. Lacombe, N. Beaudoin, G. Hoareau, A. Labeur; Funding acquisition : N. Beaudoin;
622 Writing – original draft preparation : O. Lacombe, N. Beaudoin; Writing – review and editing : O.
623 Lacombe, N. Beaudoin, G. Hoareau, J.P. Callot

624

625 **Competing interest:** “The authors declare that they have no conflict of interest”

626

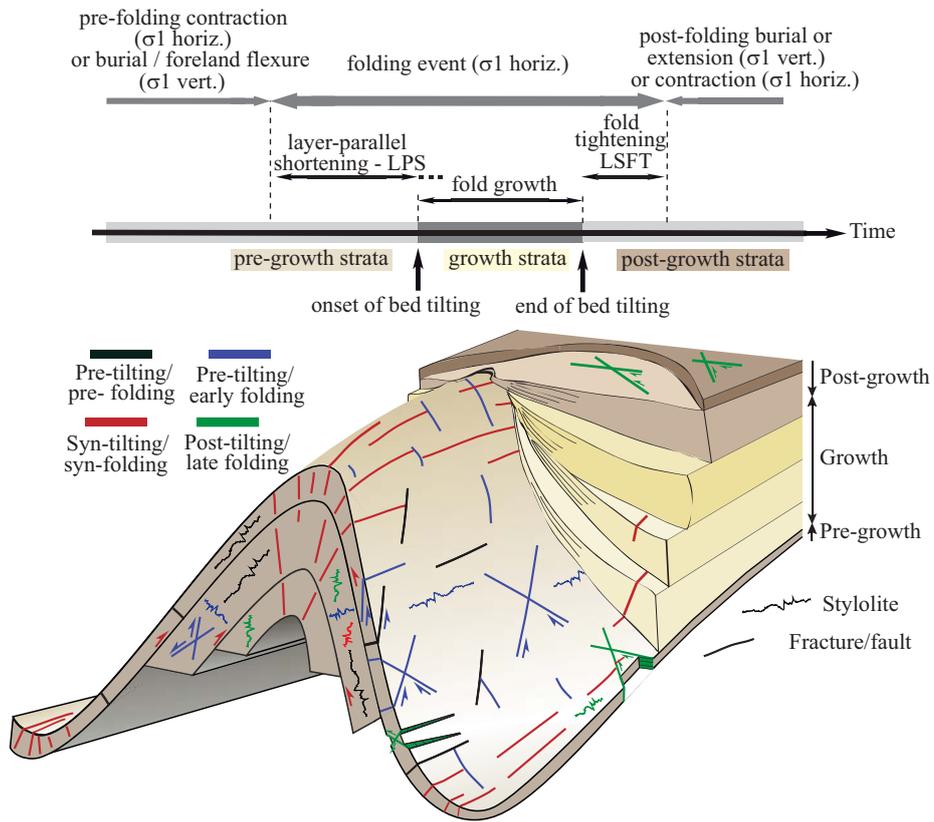


Fig.1. Concept of folding event and associated mesostructures and growth strata.

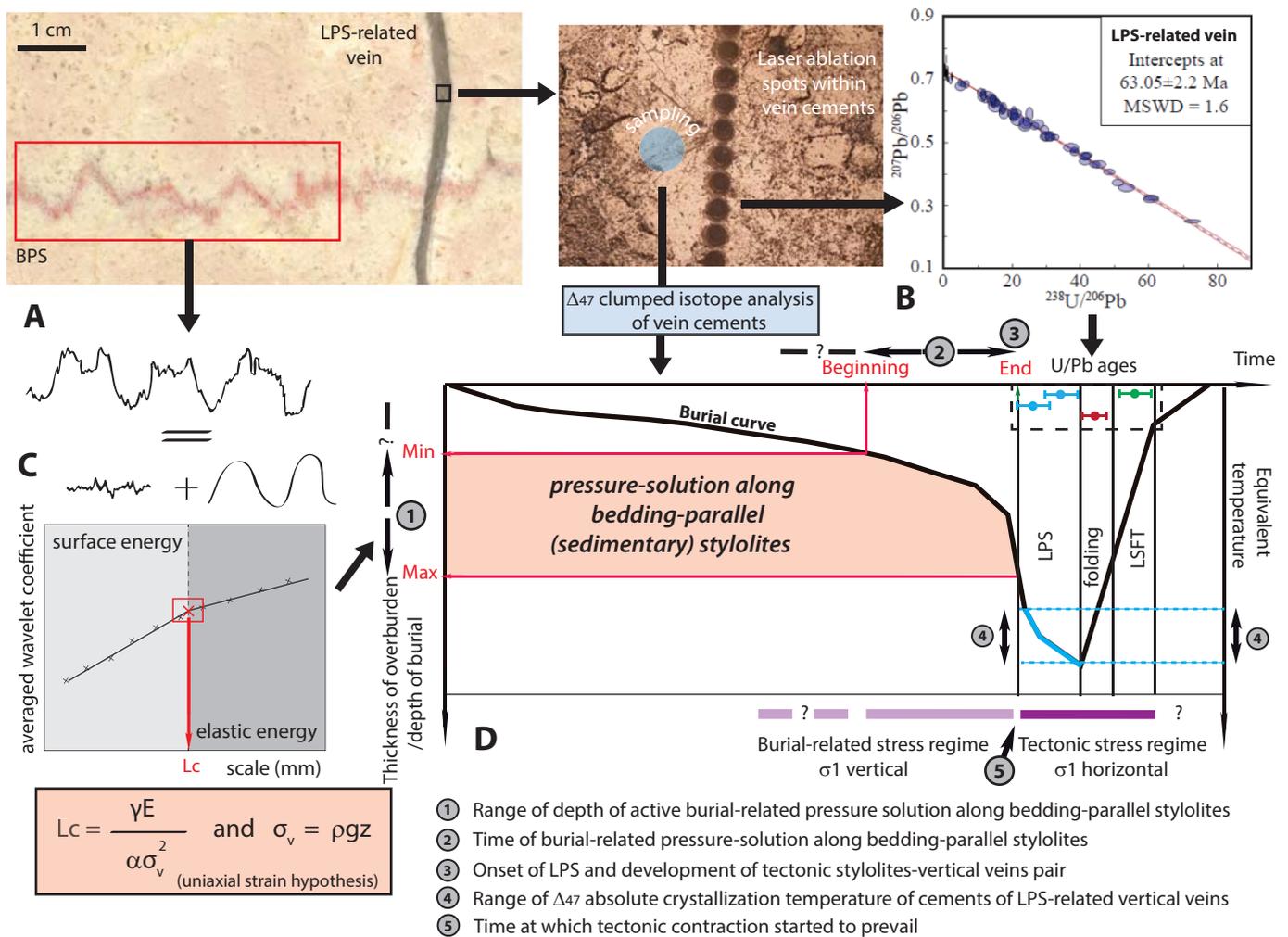


Fig.2. Principle of dating of mesostructures related to the folding event. A. Photograph of a sedimentary stylolite cut by a vertical vein related to layer-parallel shortening (LPS). B. Principle of dating calcite veins using LA-ICP-MS, with laser ablation spots and final Tera-Wasserburg diagram. C. Principle of inversion of the roughness of sedimentary stylolites for stress. σ_v is the vertical stress, $\alpha = \frac{(1-2\nu)(1+\nu)^2}{30\pi(1-\nu)^2}$, γ is the solid-fluid interfacial energy, ν is the Poisson ratio, E is the Young modulus, ρ is the dry density, g is the gravitational field acceleration and z is the depth. D. Principle of the combination of U-Pb dating and absolute $\Delta 47$ thermometry of calcite cements (here for LPS-related veins) with maximum depth of burial-related dissolution from sedimentary stylolites and burial-time evolution of strata to derive the timing of deformation stages during the folding event.

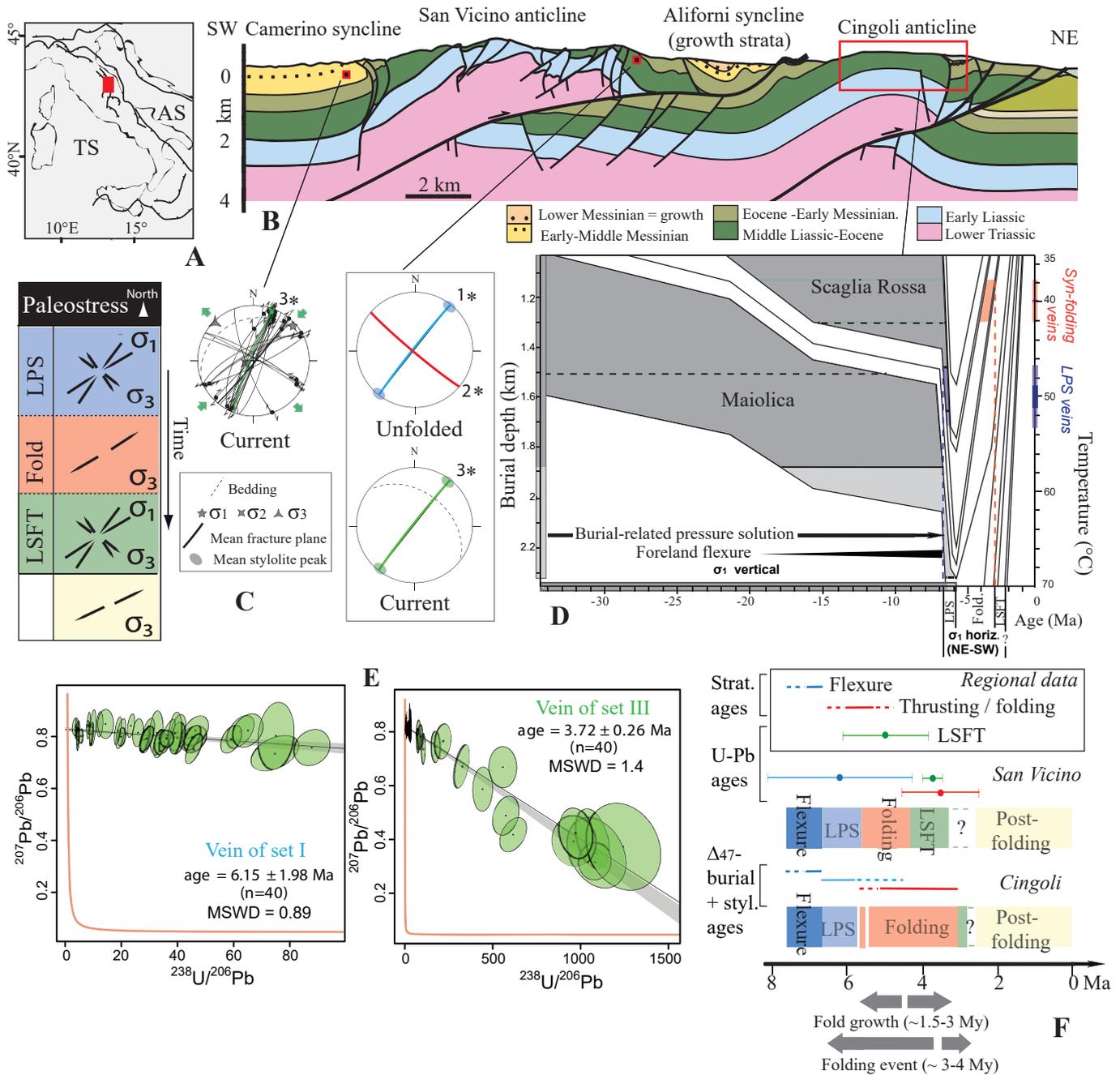


Fig.3. San Vicino and Cingoli anticlines: A: location (AS: Adriatic Sea; TS: Tyrrhenian Sea). B: Cross section (after Mazzoli et al., 2002). C: Orientation of the main sets of mesostructures (relative chronology, 1 to 3), reported in current or unfolded attitude on a lower hemisphere Schmidt stereonet, and associated paleostress evolution. * denotes mesostructures dated using U-Pb. D: Burial model of Cingoli constructed considering thickness from stratigraphic and well data corrected for chemical and physical compaction (modified from Labeur et al., 2021). The range of depths reconstructed from sedimentary stylolite roughness inversion (with uncertainty shaded in light grey) are reported for each formation as grey levels. The results of clumped isotope analysis (i.e., temperatures of precipitation of vein cements at thermal equilibrium with the host rock) are reported for LPS-related veins (blue) and syn-folding veins (red). The deduced timing of the deformation stages is reported. E: Age dating results for veins from San Vicino anticline: Tera-Wasserburg concordia plots for carbonate samples showing $^{238}\text{U}/^{206}\text{Pb}$ vs $^{207}\text{Pb}/^{206}\text{Pb}$ for veins of sets I (LPS-related) and III (LSFT-related) (n—no. of spots). MSWD—mean square of weighted deviates. F: Timing and duration of deformation stages. Regional data are from Mazzoli et al., 2002 (flexure), Calamita et al. 1994 (folding and thrusting), Beaudoin et al., 2020c (LSFT). Color code for C and F: dark blue: flexure-related extension. blue: layer-parallel shortening (LPS); red: fold growth; green: late stage fold tightening (LSFT); yellow: post-folding extension.

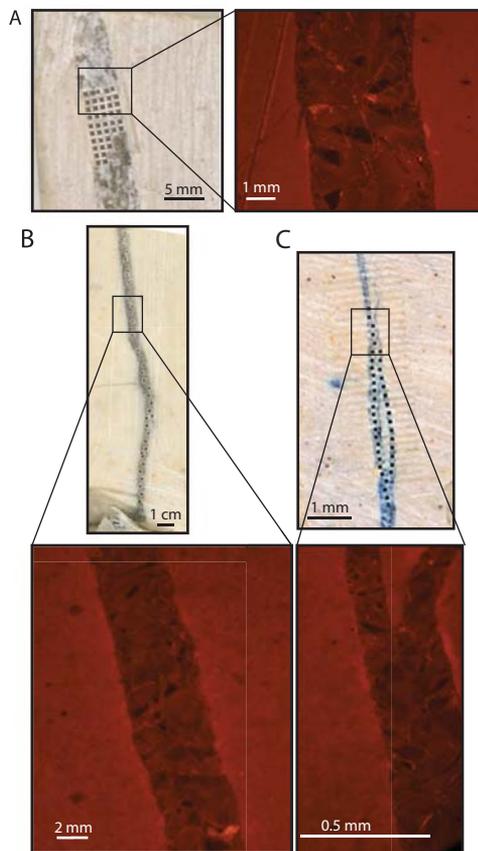


Fig.4. 2D scans of veins dated by LA-ICP-MS U-Pb geochronology from San Vicino anticline, with location of the ablation spots and diagenetic state observed under cathodoluminescence microscopy. A: sample A16 (LPS-related vein). B: sample A19 (syn-folding vein). C: sample A20 (LSFT-related vein).

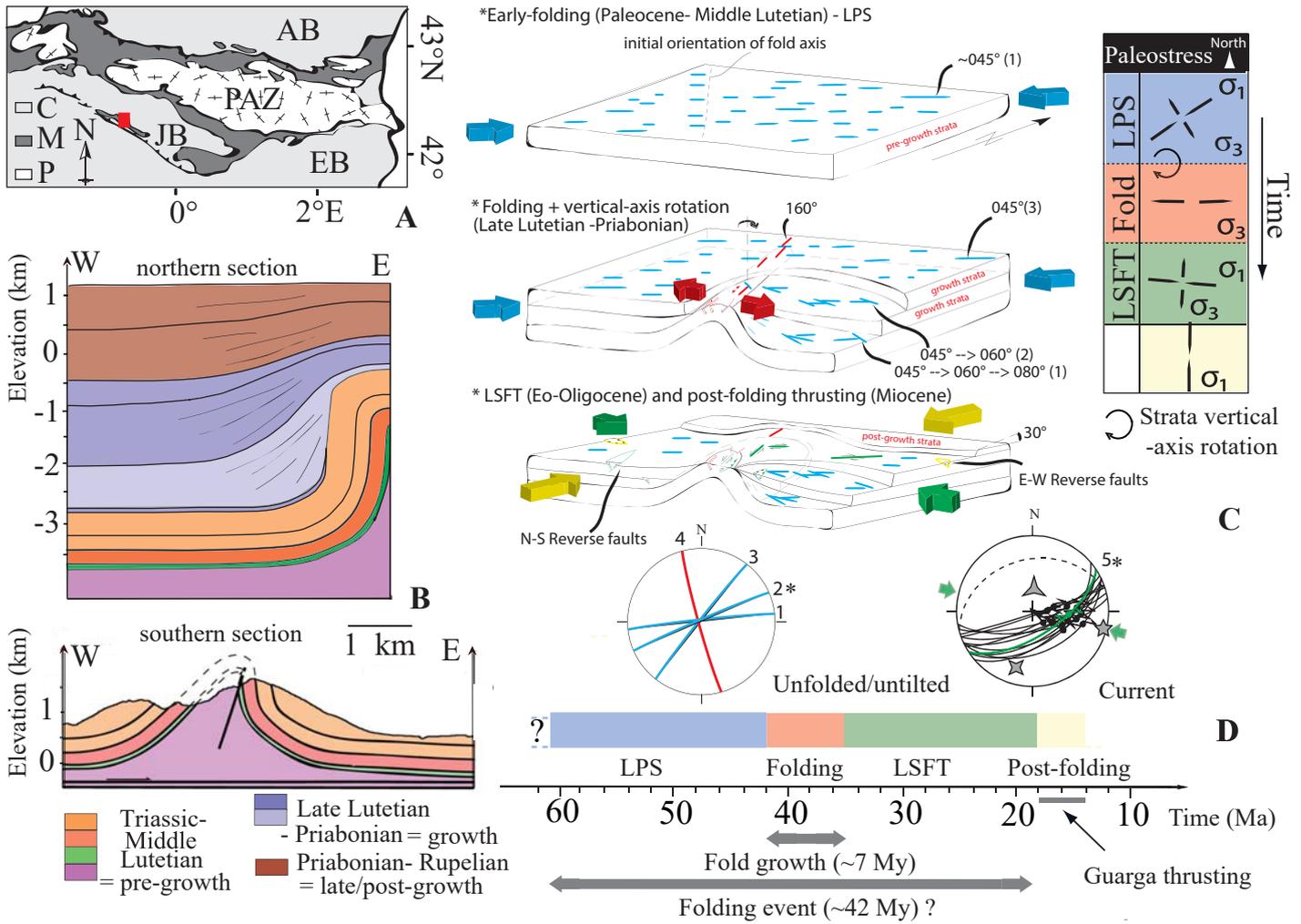


Fig.5. Pico del Aguila anticline: A: location (AB: Aquitaine Basin, JB: Jaca Basin, EB: Ebro Basin, PAZ: Pyrenean Axial Zone; P: Paleozoic; M: Mesozoic; C: Cenozoic). B: Cross sections (north after Poblet et al., 1997, south after Beaudoin et al., 2015). C: Orientation of the main sets of mesostructures (relative chronology, 1 to 5), reported in current or unfolded attitude on a lower hemisphere Schmidt stereonet (same key as Fig.3), and associated structural and paleostress evolution. Block diagrams modified after Beaudoin et al. (2015). * denotes mesostructures dated using U-Pb. D : Timing and duration of deformation stages. Color code for C and D : blue: layer-parallel shortening (LPS); red: fold growth; green: late stage fold tightening (LSFT); yellow: post-folding compression.

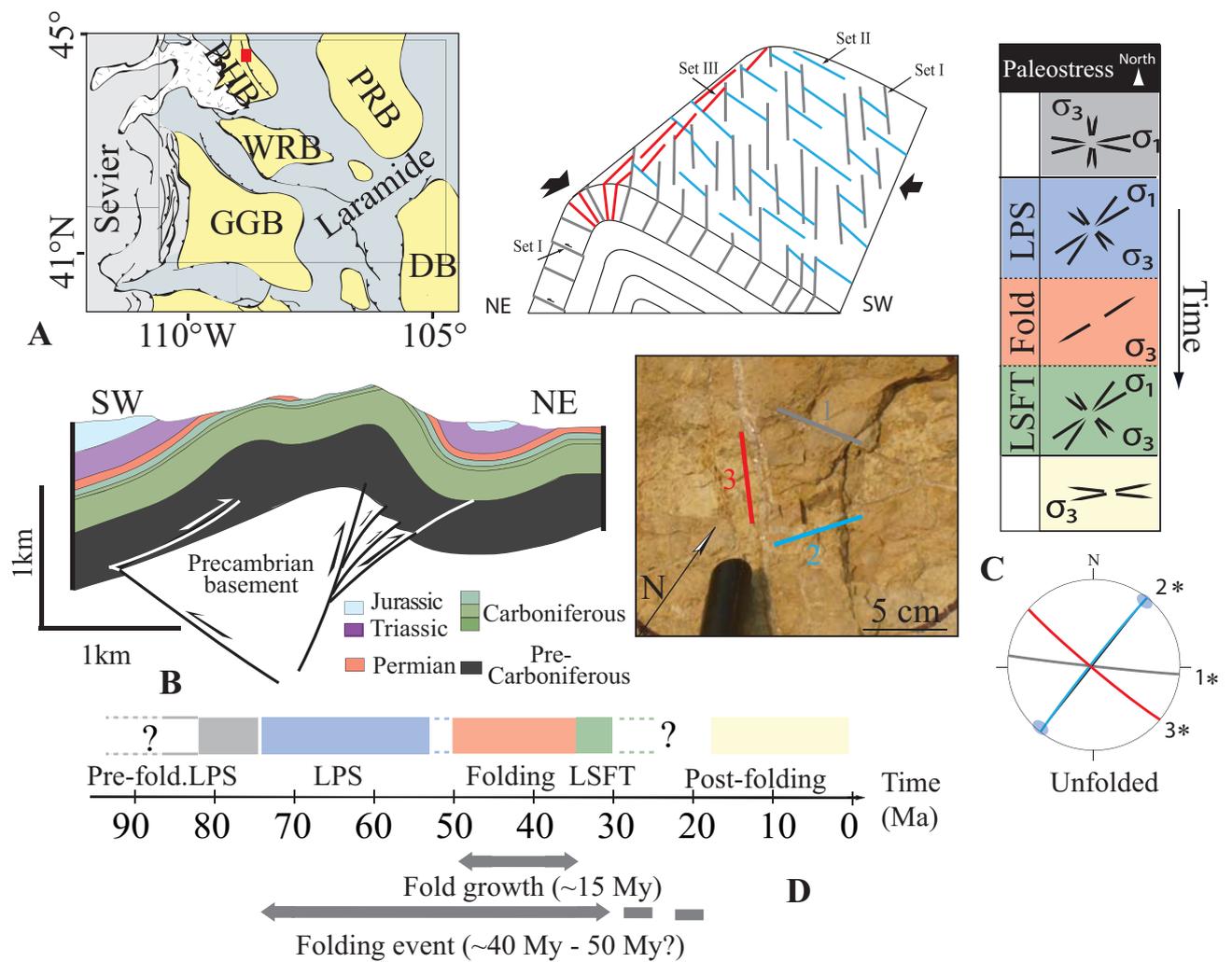


Fig.6. Sheep Mountain anticline: A: location (BHB: Bighorn Basin; WRB: Wind River Basin; PRB: Powder River Basin; GGB: Greater Green River Basin; DB: Denver Basin). B: Cross section (after Amrouch et al., 2010); C: Orientation of the main sets of veins (relative chronology, 1 to 3), shown on a field photograph and on a block-diagram of the final fold geometry, reported in unfolded attitude on a lower hemisphere Schmidt stereonet (same key as Fig.3), and associated structural and paleostress evolution. * denotes mesostructures dated using U-Pb. D: Timing and duration of the deformation stages. Color code for C and D: grey: pre-folding layer-parallel shortening kinematically unrelated to folding; blue: layer-parallel shortening (LPS); red: fold growth; green: late stage fold tightening (LSFT); yellow: post-folding extension.

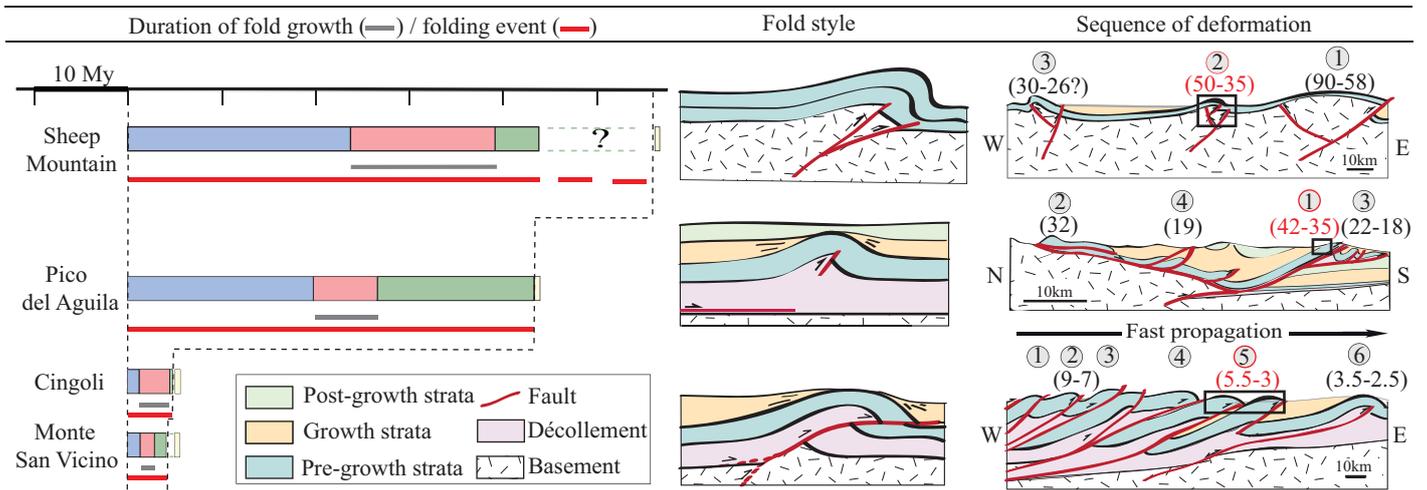


Fig.7. Compared durations of the stages of the folding event, fold style (= final fold geometry) and sequence of regional deformation for the four studied folds (circled numbers 1 to 6 : order of structural development, i.e., sequence of folding/thrusting, with corresponding ages in Ma (between parentheses), red : from this study; black : from the literature (Beaudoin et al., 2018 for Wyoming, Jolivet et al. 2007 for the Pyrenees, Calamita et al., 1994 and Curzi et al., 2020 for the Apennines). Color code: blue: layer-parallel shortening (LPS); red: fold growth; green: late stage fold tightening (LSFT); yellow: post-folding extension/compression.